

scanner = <sup>stream of character</sup> ตัด input ที่สั้นเข้ามาเป็นคำๆ <sup>tokens</sup> → output คือ stream of tokens  
 write Regular Expression to cover set of words

grammar

given sample of sentences in a language, write its grammar

parsing

parse tree

recursive descent

LL(1)

compute First and Follow set

construct parsing table

given a grammar, compute First, Follow, draw parsing table

paser = ตัวที่เรียก scanner ให้ scanner ส่ง token มาทีละตัวๆ  
 → = ใช้ input กลายเป็น sequence of token แล้วใส่ใน + input ถูกต้องตามไวยากรณ์ grammar

code generation

interpreter

code generator

## ① Scanner

### ● Regular Expression

a character or symbol in the alphabet

$\lambda$ : an empty string → คือ e หรือ empty

$\phi$ : an empty set

if  $r$  and  $s$  are regular expressions

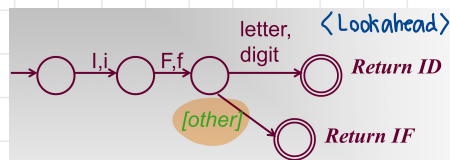
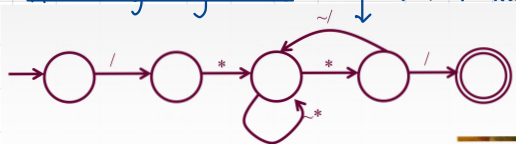
- $r | s$  → เลือก r หรือ s
- $rs$
- $r^*$  → เลือก r ซ้ำเรื่อยๆ
- $(r)$

- $[a-z]$ 
  - any character in a range from a to z
- $.$ 
  - any character
- $r^+$  → เลือก r อย่างน้อย 1 ครั้ง
  - one or more repetition
- $r?$  → เลือก a หรือ a ไม่เอา ตัว
  - optional subexpression
- $\sim(a | b | c), [^abc]$ 
  - any single character NOT in the set

## Examples of Patterns

- $(a | A)$  = the set  $\{a, A\}$
- $[0-9]^+ = (0 | 1 | \dots | 9) (0 | 1 | \dots | 9)^*$
- $(0-9)? = (0 | 1 | \dots | 9 | \lambda)$
- $[A-Za-z] = (A | B | \dots | Z | a | b | \dots | z)$
- $A.$  = the string with A following by any one symbol
- $\sim[0-9] = [^0123456789]$  = any character which is not 0, 1, ..., 9

## FA Recognizing Tokens (ใช้แผนภาพสถานะ)



**Production Rules:** $S \rightarrow aBDh$  $B \rightarrow cC$  $C \rightarrow bC \mid \epsilon$  $D \rightarrow EF$  $E \rightarrow g \mid \epsilon$  $F \rightarrow f \mid \epsilon$ **FIRST set** $\text{FIRST}(S) = \{ a \}$  $\text{FIRST}(B) = \{ c \}$  $\text{FIRST}(C) = \{ b, \epsilon \}$  $\text{FIRST}(D) = \text{FIRST}(E) \cup \text{FIRST}(F) = \{ g, f, \epsilon \}$  $\text{FIRST}(E) = \{ g, \epsilon \}$  $\text{FIRST}(F) = \{ f, \epsilon \}$ **FOLLOW Set** $\text{FOLLOW}(S) = \{ \$ \}$  $\text{FOLLOW}(B) = \{ \text{FIRST}(D) - \epsilon \} \cup \text{FIRST}(h) = \{ g, f, h \}$  $\text{FOLLOW}(C) = \text{FOLLOW}(B) = \{ g, f, h \}$  $\text{FOLLOW}(D) = \text{FIRST}(h) = \{ h \}$  $\text{FOLLOW}(E) = \{ \text{FIRST}(F) - \epsilon \} \cup \text{FOLLOW}(D) = \{ f, h \}$  $\text{FOLLOW}(F) = \text{FOLLOW}(D) = \{ h \}$ **Production Rules:** $S \rightarrow ACB \mid Cbb \mid Ba$  $A \rightarrow da \mid BC$  $B \rightarrow g \mid \epsilon$  $C \rightarrow h \mid \epsilon$ *From First(S)***FIRST set** $\text{FIRST}(S) = \text{FIRST}(A) \cup \text{FIRST}(B) \cup \text{FIRST}(C) = \{ d, g, h, \epsilon, b, a \}$  $\text{FIRST}(A) = \{ d \} \cup \{ \text{FIRST}(B) - \epsilon \} \cup \text{FIRST}(C) = \{ d, g, h, \epsilon \}$  $\text{FIRST}(B) = \{ g, \epsilon \}$  $\text{FIRST}(C) = \{ h, \epsilon \}$ **FOLLOW Set** $\text{FOLLOW}(S) = \{ \$ \}$  $\text{FOLLOW}(A) = \{ h, g, \$ \}$  $\text{FOLLOW}(B) = \{ a, \$, h, g \}$  $\text{FOLLOW}(C) = \{ b, g, \$, h \}$

## Production Rules:

$S \rightarrow aBDh$

$B \rightarrow cC$

$C \rightarrow bC \mid \epsilon$

$D \rightarrow EF$

$E \rightarrow g \mid \epsilon$

$F \rightarrow f \mid \epsilon$

## FIRST set

$FIRST(S) = \{ a \}$

$FIRST(B) = \{ c \}$

$FIRST(C) = \{ b, \epsilon \}$

$FIRST(D) = FIRST(E) \cup FIRST(F) = \{ g, f, \epsilon \}$

$FIRST(E) = \{ g, \epsilon \}$

$FIRST(F) = \{ f, \epsilon \}$

## FOLLOW Set

$FOLLOW(S) = \{ \$ \}$

$FOLLOW(B) = \{ FIRST(D) - \epsilon \} \cup FIRST(h) = \{ g, f, h \}$

$FOLLOW(C) = FOLLOW(B) = \{ g, f, h \}$

$FOLLOW(D) = FIRST(h) = \{ h \}$

$FOLLOW(E) = \{ FIRST(F) - \epsilon \} \cup FOLLOW(D) = \{ f, h \}$

$FOLLOW(F) = FOLLOW(D) = \{ h \}$

## Production Rules:

$S \rightarrow ACB|Cbb|Ba$

$A \rightarrow da|BC$

$B \rightarrow g|\epsilon$

$C \rightarrow h|\epsilon$

## FIRST set

$FIRST(S) = FIRST(A) \cup FIRST(B) \cup FIRST(C) = \{ d, g, h, \epsilon, b, a \}$

$FIRST(A) = \{ d \} \cup \{ FIRST(B) - \epsilon \} \cup FIRST(C) = \{ d, g, h, \epsilon \}$

$FIRST(B) = \{ g, \epsilon \}$

$FIRST(C) = \{ h, \epsilon \}$

## FOLLOW Set

$FOLLOW(S) = \{ \$ \}$

$FOLLOW(A) = \{ h, g, \$ \}$

$FOLLOW(B) = \{ a, \$, h, g \}$

$FOLLOW(C) = \{ b, g, \$, h \}$

## Computing Follow

1. If A is start symbol, put \$ in FOLLOW(A)

2. Productions of the form  $B \rightarrow \alpha A \beta$ ,

$FOLLOW(A) = FIRST(\beta)$

3. Productions of the form  $B \rightarrow \alpha A$  or

$B \rightarrow \alpha A \beta$  where  $\beta \Rightarrow^+ \epsilon$

Add  $FOLLOW(A) = FOLLOW(B)$

$S \rightarrow aBDh$

\*\*\* insertion  $\epsilon$

\*\* insertion 1)  $\epsilon$   $FOLLOW(h)$

$S \rightarrow \alpha A \beta$   
 $\therefore FOLLOW(A) = FIRST(c) \cup FIRST(B) \cup FOLLOW(S)$

$S \rightarrow \alpha A \beta$   
 $\therefore FOLLOW(C) = FIRST(B) \cup FOLLOW(S)$

$A \rightarrow \alpha A \beta$   
 $\therefore FOLLOW(C) = FOLLOW(A)$

$A \rightarrow \alpha A \beta$   
 $\therefore FOLLOW(B) = FIRST(c) \cup FOLLOW(A)$

## Production Rules:

$S \rightarrow ACB|CDB|Ba$

$A \rightarrow da|BC$

$B \rightarrow g|\epsilon$

$C \rightarrow h|\epsilon$

## EXAMPLE

Consider the expression grammar (4.11), repeated below:

$$\begin{aligned} E &\rightarrow T E' \\ E' &\rightarrow + T E' \mid \varepsilon \\ T &\rightarrow F T' \\ T' &\rightarrow * F T' \mid \varepsilon \\ F &\rightarrow ( E ) \mid \text{id} \end{aligned}$$

Then:

$$\text{FIRST}(E) = \text{FIRST}(T) = \text{FIRST}(F) = \{ (, \text{id} \}$$
$$\text{FIRST}(E') = \{ +, \varepsilon \}$$
$$\text{FIRST}(T') = \{ *, \varepsilon \}$$
$$\text{FOLLOW}(E) = \text{FOLLOW}(E') = \{ ), \$ \}$$
$$\text{FOLLOW}(T) = \text{FOLLOW}(T') = \{ +, ), \$ \}$$
$$\text{FOLLOW}(F) = \{ +, *, ), \$ \}$$

Examples of Quiz in compiler (old questions from yesteryear) (only two examples)

1) This is an input source for our scanner

```
fac(n)
  if( n == 0 ) return 1
  else return n * fac(n-1)
```

the kind of "words" in this program are:

reserve word : if else return

symbol: ( ) == \* -

constant: 0 1

identifier: fac n

write regular expression to capture all "words" in this program  
(there may be several REs)

2 ) Given this grammar, compute First, Follow set and draw Parsing Table

```
dc1 = ID dc12
dc12 = ( formal ) STMT | [ NUMBER ]
formal = ID formals | nil
formals = , formal | nil
```

## EXAMPLE

Consider the expression grammar (4.11), repeated below:

$E \rightarrow T E'$   
 $E' \rightarrow + T E' \mid \epsilon$   
 $T \rightarrow F T'$   
 $T' \rightarrow * F T' \mid \epsilon$   
 $F \rightarrow ( E ) \mid id$

Computing Follow

- If A is start symbol, put \$ in FOLLOW(A)
- Productions of the form  $B \rightarrow \alpha A \beta$ ,  
 $FOLLOW(A) = FOLLOW(A) \cup FIRST(\beta)$  (if  $\beta \neq \epsilon$ )
- Productions of the form  $B \rightarrow \alpha A$  or  
 $B \rightarrow \alpha A \beta$  where  $\beta \Rightarrow^+ \epsilon$   
Add  $FOLLOW(A) = FOLLOW(B)$

Then:

$FIRST(E) = FIRST(T) = FIRST(F) = \{ (, id \}$   
 $FIRST(E') = \{ +, \epsilon \}$   
 $FIRST(T') = \{ *, \epsilon \}$

$FOLLOW(E) = FOLLOW(E') = \{ \}, \$ \}$   
 $FOLLOW(T) = FOLLOW(T') = \{ +, ), \$ \}$   
 $FOLLOW(F) = \{ +, *, ), \$ \}$

Examples of Quiz in compiler (old questions from yesteryear) (only two examples)

1) This is an input source for our scanner

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 symbol: ( ) == \* -  
 constant: 0 1  
 identifier: fac n

write regular expression to capture all "words" in this program  
(there may be several REs)

2) Given this grammar, compute First, Follow set and draw Parsing Table

$dc1 = ID \ dc12$   
 $*dc12 = ( \ formal ) \ STMT \mid [ \ NUMBER ]$   
 $formal = ID \ formals \mid nil$   
 $formals = , \ formal \mid nil$

Computing Follow

- If A is start symbol, put \$ in FOLLOW(A)
- Productions of the form  $B \rightarrow \alpha A \beta$ ,  
 $FOLLOW(A) = FOLLOW(A) \cup FIRST(\beta)$  (if  $\beta \neq \epsilon$ )
- Productions of the form  $B \rightarrow \alpha A$  or  
 $B \rightarrow \alpha A \beta$  where  $\beta \Rightarrow^+ \epsilon$   
Add  $FOLLOW(A) = FOLLOW(B)$

reserve word = (if | else | return)  
 symbol = ( ) | == | \* | -  
 constants = 0 | 1  
 identifier = (fac | n)

```
reserve_word = (if | else | return)
symbols = ([()])|([==])|([*])|([-])
constants = [0-9]+
identifier = [A-Za-z][A-Za-z0-9]*
```

จากตัวอักษร

$First(dc1) = \{ ID \}$   
 $First(dc12) = \{ (, [ \}$   
 $First(formal) = \{ ID, nil \}$   
 $First(formals) = \{ , , nil \}$   
 $Follow(dc1) = \{ \$ \}$   
 $Follow(dc12) = Follow(dc1) = \{ \$ \}$   
 $Follow(formal) = \{ \} \cup Follow(formals) = \{ \}$   
 $Follow(formals) = Follow(formal) = \{ \}$

|         | ID | ( | ) | [ | ] | NUMBER | , | STMT |
|---------|----|---|---|---|---|--------|---|------|
| dc1     | ①  |   |   |   |   |        |   |      |
| dc12    |    | ② |   | ③ |   |        |   |      |
| formal  | ④  |   |   |   |   |        |   |      |
| formals |    |   |   |   |   |        | ⑥ |      |

\* มี nil อยู่ follow set

จากตัวอักษร

first set  
 : {ID}  
 : {(, [  
 : {ID, nil}  
 : {, nil}  
 follow set  
 : {\$}  
 : {\$}  
 : {}  
 : {}  
 parsing table  
 ID ( ) [  
 dc1 | dc1 -> ID dc12 | | |  
 dc12 | | dc12 -> (formal) STMT | | dc12 -> (formal) STMT |  
 formal | formal -> ID formals | | formal -> nil |  
 formals | | formals -> nil |  
 formals -> , formal |



## Parser (LL1)

Here is the grammar for a subset of BASIC language. Computer First and Follow set and construct a parsing table. (You can submit photo of your parsing table). Example of a parsing table is in slide page 25 of parsing. You can also find it here

<https://www.cp.eng.chula.ac.th/~prabhas/teaching/prolang/2022/write-parser-from-parsing-table.htm>

```

pgm := line | EOF
line := LNUM stmt line | empty
stmt := asgmt | goto
asgmt := ID = exp
exp := ID exps
exps := + exp | empty
goto := GOTO LNUM
    
```

Example of the program is:

```

10 A = B
30 B = A + A + A
40 GOTO 10
    
```

Note: the only variable name is "A". EOF is end of file (or end of input).  
You can read more about BASIC here: (It was a project of this class many years ago).

<https://www.cp.eng.chula.ac.th/~prabhas/teaching/prolang/2018/retro-basic.htm>

### Computing Follow

- If A is start symbol, put \$ in FOLLOW(A)
- Productions of the form  $B \rightarrow \alpha A \beta$   
 $\text{FOLLOW}(A) = \text{FIRST}(\beta)$
- Productions of the form  $B \rightarrow \alpha A$  or  $B \rightarrow \alpha A \beta$  where  $\beta \Rightarrow^* \epsilon$   
Add  $\text{FOLLOW}(A) = \text{FOLLOW}(B)$

- pgm  $\rightarrow$  line
- pgm  $\rightarrow$  EOF
- line  $\rightarrow$  LNUM  $\overset{\alpha}{\text{stmt}}$   $\overset{\beta}{\text{line}}$
- line  $\rightarrow$  empty
- stmt  $\rightarrow$  asgmt
- stmt  $\rightarrow$  goto
- asgmt  $\rightarrow$  ID = exp  $\rightarrow$  asgmt  $\rightarrow$  ID = exp tmp
- exp  $\rightarrow$  ID  $\overset{\alpha}{\text{exps}}$   $\overset{\beta}{\text{exps}}$
- exps  $\rightarrow$  + exp
- exps  $\rightarrow$  empty
- goto  $\rightarrow$  GOTO LNUM

- First (pgm) = {LNUM, empty, EOF}  
First (line) = {LNUM, empty}  
First (stmt) = {ID, GOTO}  
First (asgmt) = {ID}  
First (exp) = {ID}  
First (exps) = {+, empty}  
First (goto) = {GOTO}

- Follow (pgm) = {EOF}  $\rightarrow$  \$  
Follow (line) = {EOF}  $\rightarrow$  M  
Follow (stmt) = First (line)  $\cup$  Follow (line) = {LNUM, EOF}  
Follow (asgmt) = Follow (stmt) = {LNUM, EOF}  
\*\*\* Follow (exp) = Follow (exps) = {LNUM, EOF} = Follow (asgmt)  
Follow (exps) = Follow (exp) = {LNUM, EOF}  
Follow (goto) = Follow (stmt) = {LNUM, EOF}

M  
\* M E in EOF

### Parsing Table

|       | LNUM | ID | = | + | GOTO | EOF |
|-------|------|----|---|---|------|-----|
| pgm   | ①    |    |   |   |      | ②   |
| line  | ③    |    |   |   |      | ④   |
| stmt  |      | ⑤  |   |   | ⑥    |     |
| asgmt |      | ⑦  |   |   |      |     |
| exp   |      | ⑧  |   |   |      |     |
| exps  | ⑩    |    |   | ⑨ |      | ⑩   |
| goto  |      |    |   |   | ⑪    |     |

- pgm  $\rightarrow$  line
- pgm  $\rightarrow$  EOF
- line  $\rightarrow$  LNUM  $\overset{\alpha}{\text{stmt}}$   $\overset{\beta}{\text{line}}$
- line  $\rightarrow$  empty
- stmt  $\rightarrow$  asgmt
- stmt  $\rightarrow$  goto
- asgmt  $\rightarrow$  ID = exp
- exp  $\rightarrow$  ID  $\overset{\alpha}{\text{exps}}$   $\overset{\beta}{\text{exps}}$
- exps  $\rightarrow$  + exp
- exps  $\rightarrow$  empty
- goto  $\rightarrow$  GOTO LNUM

- pgm  $\rightarrow$  line First row line ①
- pgm  $\rightarrow$  EOF
- line  $\rightarrow$  LNUM stmt line
- line  $\rightarrow$  empty
- stmt  $\rightarrow$  asgmt First row asgmt
- stmt  $\rightarrow$  goto
- asgmt  $\rightarrow$  ID = exp
- exp  $\rightarrow$  ID exps
- exps  $\rightarrow$  + exp
- exps  $\rightarrow$  empty  $\rightarrow$  M empty in Follow (exps)
- goto  $\rightarrow$  GOTO LNUM

```

pgm := line pgm | EOF
line := lnum stmt line | empty
stmt := asgmt | goto
asgmt := id = exp
exp := id exps
exps := + exp | empty
goto := GOTO lnum
id := A | B

```

|       | First set          | Follow set  |
|-------|--------------------|---|
| pgm   | {lnum, empty, EOF} | {EOF}   |
| line  | {lnum, empty}      | First(pgm) = {EOF, lnum}                                      |
| stmt  | {A, B, GOTO}       | First(line) $\cup$ Follow(line) = {lnum, EOF}                 |
| asgmt | {A, B}             | Follow(stmt) = {lnum, EOF}                                    |
| exp   | {A, B}             | Follow(asgmt) $\cup$ Follow(exps) = {lnum, EOF}               |
| exps  | {+, empty}         | Follow(exp) = {lnum, EOF}                                     |
| goto  | {GOTO}             | Follow(stmt) = {lnum, EOF}                                    |
| id    | {A, B}             | {=} $\cup$ First(exps) $\cup$ Follow(exp) = {=, +, lnum, EOF} |

```

pgm := line pgm
pgm := EOF
line := lnum stmt line
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stmt := asgmt
stmt := goto
asgmt := id = exp
exp := id exps
exps := + exp
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goto := GOTO lnum
id := A
id := B

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```

return 0-error, 1-ok

pgm()

## Grammar of ASM

```

asm = op oprnd asm | EOF
op = CLRA | MOV | ADD | MOVA
oprnd = reg , num | reg | empty
reg = R[0..31]

```

## Parser

return 0 - error 1 - OK

```

reg()
  match('R')
  ret num()

```

```

op()
  switch tokentype()
  mov: match('MOV')
  ...
  default: ret 0

```

```

oprnd()
  if reg() != 0
    if token == ',' // lookahead
      match(',')
      ret num()
    else
      ret 1
  ret 1

```

```

asm()
  if token == EOF ret 1
  if op() != 0
    oprnd()
    asm()
  ret 0

```

Quiz compiler (section 1) 21 March 2022, time 1:30 hour  
Only one question, I think it will probably takes one hour.

Parser (LL1)

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Example of the program is:

```

10 A = B
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Note: the only variable name is "A". EOF is end of file (or end of input).  
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exp := id exps
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goto := GOTO lnum
id := A | B

```