

1d Kitaev chain

$$H = \sum_i -t c_i^\dagger c_{i+1} + \Delta c_i^\dagger c_{i+1}^\dagger + h.c. - \sum_i \mu c_i^\dagger c_i$$

考虑到OBC，可以将哈密顿量写为实空间BdG的形式，并且由于是Fermion可以直接对其进行对角化求得能谱。我们取 $t=1$; $\Delta=0.5$; $N=50$; 我们利用matlab进行程序编写：

```
clear;
N = 50;
t = 1;
delta = 0.5;

for mu = 0:0.1:5

    mulist = -mu*ones(1,N);
    Hmu = diag(mulist,0);

    Ht = diag(ones(1,N-1)*(-t),-1)+diag(ones(1,N-1)*(-t),1);

    Hmt = Ht + Hmu;

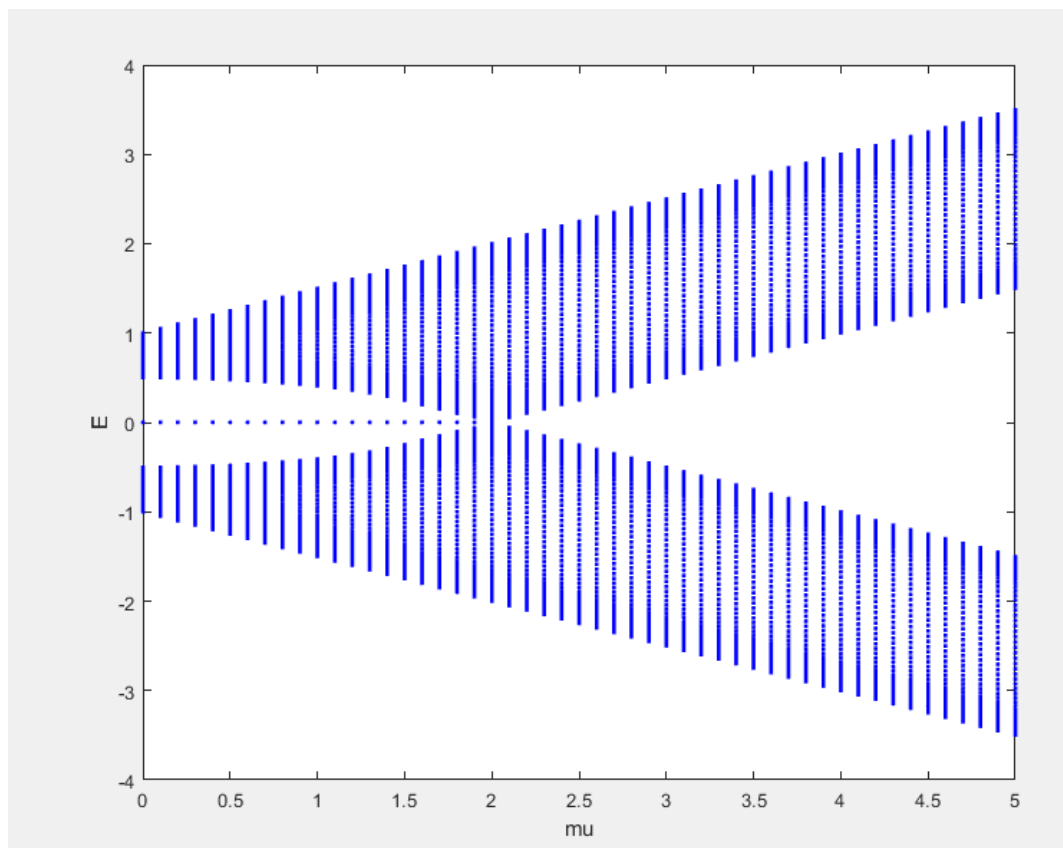
    Hd = diag(ones(1,N-1)*(-delta),-1)+diag(ones(1,N-1)*(delta),1);

    H = [Hmt,Hd;Hd',-Hmt]/2;

    E=eig(H);

    plot(mu*ones(length(E)),E,'b. ');
    xlabel('mu');
    ylabel('E');
    hold on;
end
```

调整化学势 μ ，从0到5，间隔为0.1得到下图：



之后加入disorder项，从而哈密顿量写为：

$$H = \sum_i -t c_i^\dagger c_{i+1} + \Delta c_i^\dagger c_{i+1}^\dagger + h.c. + \sum_i \lambda \cos(2\pi\alpha i) c_i^\dagger c_i$$

利用相同的思路，可以编写如下的matlab程序：

```

clear;
N = 50;
t = 1;
delta = 0.5;
alpha = (sqrt(5)-1)/2;

for lamda = 0:0.1:5

mulist = zeros(1,N);
for i = 1:N
mulist(i) = lamda*cos(2*pi*alpha*i);
end
Hmu = diag(mulist,0);

Ht = diag(ones(1,N-1)*(-t),-1)+diag(ones(1,N-1)*(-t),1);

Hmt = Ht + Hmu;

Hd = diag(ones(1,N-1)*(-delta),-1)+diag(ones(1,N-1)*(delta),1);

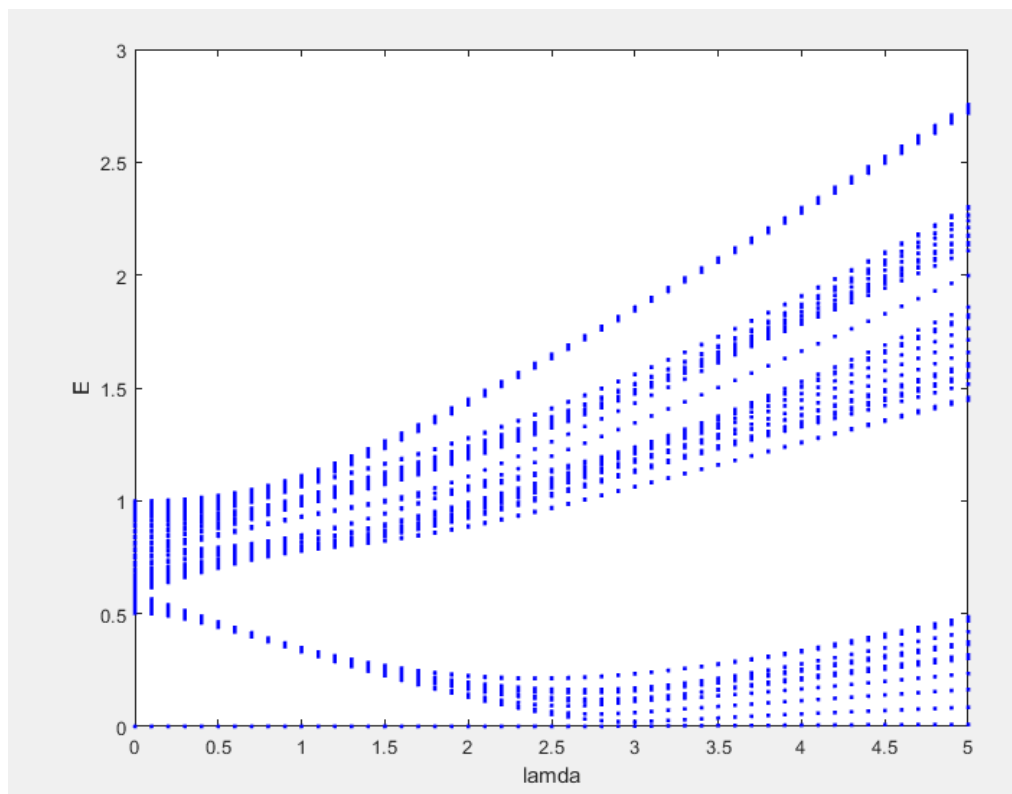
H = [Hmt,Hd;Hd',-Hmt]/2;

E=abs(eig(H));

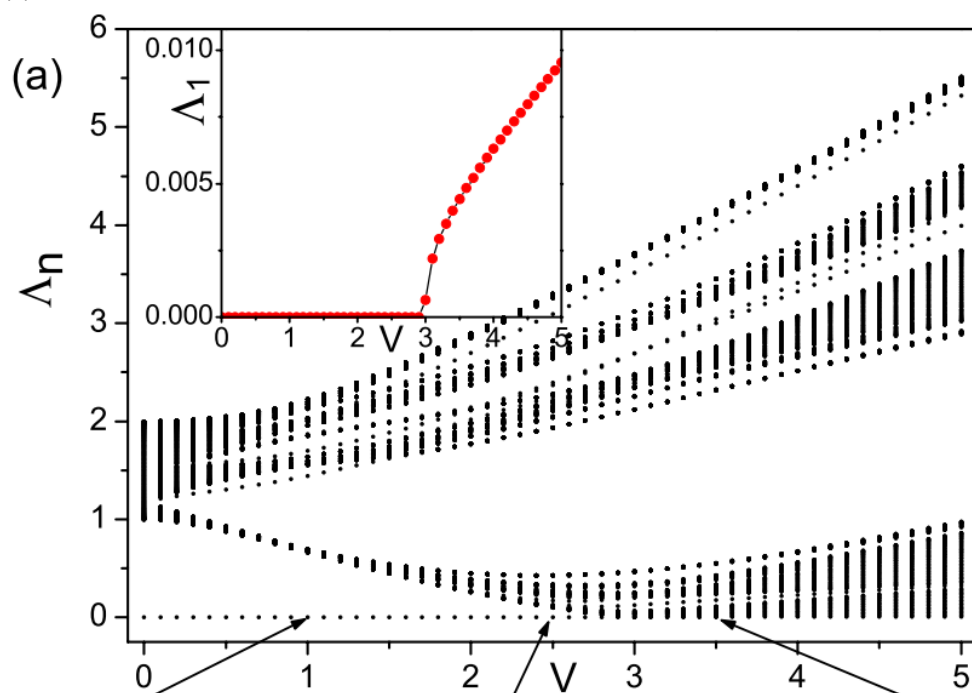
plot(lamda*ones(length(E)),E,'b. ');
xlabel('lamda');
ylabel('E');
hold on;
end

```

计算结果如下：



这一结果与论文当中的结果相吻合：



1d bose gas

对于bose气体的哈密顿量：

$$H = \sum_i -tb_i^\dagger b_{i+1} + \frac{1}{2}gn_0 b_i^\dagger b_i^\dagger + h.c. + \sum_i (-\mu + gn_0)b_i^\dagger b_i$$

由于要保持玻色子的对易关系，因此我们需要在对角化之前给矩阵乘以对角的方块z方向的泡利矩阵，具体的matlab代码如下：

```
clear;
N = 500;
t = 1;
g = 1.000;
n0 = 1;
mu = 5;

for mu = 0:0.5:5

    mulist = (-mu+g*n0)*ones(1,N);
    Hmu = diag(mulist,0);

    Ht = diag(ones(1,N-1)*(-t),-1)+diag(ones(1,N-1)*(-t),1);
    Hmt = Ht + Hmu;

    Hd = diag(0.5*g*n0*ones(1,N),0);

    H = [Hmt,Hd;Hd',Hmt]/2;
    H = [diag(ones(1,N)),zeros(N,N);zeros(N,N),-diag(ones(1,N))]*H;

    E=(eig(H));

    plot(mu*ones(length(E)),E,'b. ');
    xlabel('mu');
    ylabel('E');
    hold on
end
```

其求解出来的能谱为：

