# **A5**

subset	type	chamber?	free?	orbit condition?
{}		CHAMBER	(FREE)	(???)
$\{1\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{2\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{3\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{4\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{5\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 2\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{2, 3\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3,4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{4,5\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{1, 2, 3\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{3, 4, 5\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{2, 3, 4, 5\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4, 5\}$	$A_5$	CHAMBER	(FREE)	(???)
$\{1, 3\}$	$A_1 \times A_1$	no	FREE	`??? <sup>´</sup>
$\{1, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{1,5\}$	$A_1 \times A_1$	no	FREE	???
$\{2,4\}$	$A_1 \times A_1$	no	FREE	???
$\{2,5\}$	$A_1 \times A_1$	no	FREE	???
$\{3,5\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 2, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 4, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{2, 3, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{2, 4, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 5\}$	$A_1 \times A_3$	no	no	(???)
$\{1, 3, 4, 5\}$	$A_1 \times A_3$	no	no	(???)
$\{1, 2, 4, 5\}$	$A_2 \times A_2$	no	FREE	???
$\{1, 3, 5\}$	$A_1 \times A_1 \times A_1$	no	no	(???)

# $\mathbf{B5}$

subset	type	chamber?	free?	orbit condition?
{}		CHAMBER	(FREE)	(???)
$\{1\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{2\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{3\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{4\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{5\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 2\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{2, 3\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3,4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{1, 2, 3\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{4, 5\}$	$B_2$	CHAMBER	(FREE)	(???)
$\{3, 4, 5\}$	$B_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4, 5\}$	$B_4$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4, 5\}$	$B_5$	CHAMBER	(FREE)	(???)
$\{1, 3\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{2, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{2, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{3, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 2, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{2, 3, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 5\}$	$A_1 \times A_3$	no	no	(???)
$\{1, 4, 5\}$	$A_1 \times B_2$	no	FREE	???
$\{2, 4, 5\}$	$A_1 \times B_2$	no	FREE	???
$\{1, 3, 4, 5\}$	$A_1 \times B_3$	no	no	(???)
$\{1, 2, 4, 5\}$	$A_2 \times B_2$	no	FREE	???
$\{1, 3, 5\}$	$A_1 \times A_1 \times A_1$	no	no	(???)

# C5

subset	type	chamber?	free?	orbit condition?
{}		CHAMBER	(FREE)	(???)
{1}	$A_1$	CHAMBER	(FREE)	(???)
$\{2\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{3\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{4\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{5\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 2\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{2,3\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3,4\}$	$\overline{A_2}$	CHAMBER	(FREE)	(???)
$\{1, 2, 3\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{4, 5\}$	$B_2$	CHAMBER	(FREE)	(???)
$\{3, 4, 5\}$	$C_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4, 5\}$	$C_4$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4, 5\}$	$C_5$	CHAMBER	(FREE)	(???)
$\{1, 3\}$	$A_1 \times A_1$	no	FREE	????
$\{1, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{2, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{2, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{3, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 2, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{2, 3, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 5\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 4, 5\}$	$A_1 \times B_2$	no	FREE	???
$\{2, 4, 5\}$	$A_1 \times B_2$	no	FREE	???
$\{1, 3, 4, 5\}$	$A_1 \times C_3$	no	FREE	???
$\{1, 2, 4, 5\}$	$A_2 \times B_2$	no	FREE	???
$\{1, 3, 5\}$	$A_1 \times A_1 \times A_1$	no	FREE	???

## D5

subset	type	chamber?	free?	orbit condition?
{}		CHAMBER	(FREE)	(???)
{1}	$A_1$	CHAMBER	(FREE)	(???)
$\{2\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{3\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{4\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{5\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 2\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{2, 3\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3,4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3, 5\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{1, 2, 3\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 5\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{3, 4, 5\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 5\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{2, 3, 4, 5\}$	$D_4$	no	no	(???)
$\{1, 2, 3, 4, 5\}$	$D_5$	CHAMBER	(FREE)	(???)
$\{1, 3\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{2,4\}$	$A_1 \times A_1$	no	FREE	???
$\{2, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{4, 5\}$	$A_1 \times A_1$	no	no	(???)
$\{1, 2, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 4, 5\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 4, 5\}$	$A_1 \times A_1 \times A_1$	no	no	(???)
$\{2, 4, 5\}$	$A_1 \times A_1 \times A_1$	no	no	(???)
$\{1, 2, 4, 5\}$	$A_1 \times A_1 \times A_2$	no	no	(???)

# G2

subset	type	chamber?	free?	orbit condition?
{}		CHAMBER	(FREE)	(???)
{1}	$A_1$	CHAMBER	(FREE)	(???)
{2}	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 2\}$	$G_2$	CHAMBER	(FREE)	(???)

## $\mathbf{F4}$

subset	type	chamber?	free?	orbit condition?
{}		CHAMBER	(FREE)	(???)
{1}	$A_1$	CHAMBER	(FREE)	(???)
$\{2\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{3\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{4\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 2\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3, 4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{2, 3\}$	$B_2$	CHAMBER	(FREE)	(???)
$\{1, 2, 3\}$	$B_3$	no	FREE	???
$\{2, 3, 4\}$	$C_3$	no	no	(???)
$\{1, 2, 3, 4\}$	$F_4$	CHAMBER	(FREE)	(???)
$\{1, 3\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{2, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 2, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 4\}$	$A_1 \times A_2$	no	FREE	???

**E7** 

subset	type	chamber?	free?	orbit condition?
{}		CHAMBER	(FREE)	(???)
{1}	$A_1$	CHAMBER	(FREE)	(???)
$\{2\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{3\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{4\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{5\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{6\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{7\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 3\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{2,4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3,4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{4, 5\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{5,6\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{6, 7\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{1, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 4, 5\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{3, 4, 5\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{4, 5, 6\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{5, 6, 7\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{1, 3, 4, 5\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{2,4,5,6\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{3, 4, 5, 6\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{4, 5, 6, 7\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{1, 3, 4, 5, 6\}$	$A_5$	no	FREE	???
$\{2,4,5,6,7\}$	$A_5$	CHAMBER	(FREE)	(???)
$\{3,4,5,6,7\}$	$A_5$	no	FREE	???
$\{1, 3, 4, 5, 6, 7\}$	$A_6$	no	FREE	???
$\{2, 3, 4, 5\}$	$D_4$	no	no	(???)
$\{1, 2, 3, 4, 5\}$	$D_5$	no	no	(???)
$\{2, 3, 4, 5, 6\}$	$D_5$	no	no	(???)
$\{2, 3, 4, 5, 6, 7\}$	$D_6$	no	no	(???)
$\{1, 2, 3, 4, 5, 6\}$	$E_6$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4, 5, 6, 7\}$	$E_7$	CHAMBER	(FREE)	(???)
$\{1, 2\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 4\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 6\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 7\}$	$A_1 \times A_1$	no	FREE	???
$\{2, 3\}$	$A_1 \times A_1$	no	FREE	???

$\{2, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{2,6\}$	$A_1 \times A_1$	no	FREE	???
$\{2,7\}$	$A_1 \times A_1$	no	FREE	???
$\{3, 5\}$	$A_1 \times A_1$	no	FREE	???
$\{3,6\}$	$A_1 \times A_1$	no	FREE	???
$\{3,7\}$	$A_1 \times A_1$	no	FREE	???
$\{4, 6\}$	$A_1 \times A_1$	no	FREE	???
$\{4,7\}$	$A_1 \times A_1$	no	FREE	???
$\{5,7\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 2, 3\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 6\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 7\}$	$A_1 \times A_2$	no	FREE	???
$\{1,4,5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 5, 6\}$	$A_1 \times A_2$	no	FREE	???
$\{1,6,7\}$	$A_1 \times A_2$	no	FREE	???
$\{2,4,6\}$	$A_1 \times A_2$	no	FREE	???
$\{2,4,7\}$	$A_1 \times A_2$	no	FREE	???
$\{2, 5, 6\}$	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
$\{2,6,7\}$	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
$\{3,4,6\}$	$A_1 \times A_2$	no	FREE	???
$\{3,4,7\}$	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
$\{3, 5, 6\}$	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
$\{3,6,7\}$	$A_1 \times A_2$ $A_1 \times A_2$		FREE	???
	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
$\{4,5,7\}$		no	FREE	???
$\{4,6,7\}$	$A_1 \times A_2$	no		???
$\{1, 2, 4, 5\}$	$A_1 \times A_3$	no	FREE	
$\{1, 3, 4, 6\}$	$A_1 \times A_3$	no	FREE	??? ???
$\{1, 3, 4, 7\}$	$A_1 \times A_3$	no	FREE	???
$\{1,4,5,6\}$	$A_1 \times A_3$	no	FREE	
$\{1, 5, 6, 7\}$	$A_1 \times A_3$	no	FREE	???
$\{2, 3, 4, 6\}$	$A_1 \times A_3$	no	FREE	???
$\{2, 3, 4, 7\}$	$A_1 \times A_3$	no	FREE	???
$\{2,4,5,7\}$	$A_1 \times A_3$	no	no	(???)
$\{2, 5, 6, 7\}$	$A_1 \times A_3$	no	no	(???)
$\{3,4,5,7\}$	$A_1 \times A_3$	no	FREE	???
$\{3, 5, 6, 7\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 2, 3, 4, 6\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 2, 3, 4, 7\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 2, 4, 5, 6\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 3, 4, 5, 7\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 4, 5, 6, 7\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 2, 4, 5, 6, 7\}$	$A_1 \times A_5$	no	FREE	???
$\{2, 3, 4, 5, 7\}$	$A_1 \times D_4$	no	no	(???)
$\{1, 2, 3, 4, 5, 7\}$	$A_1 \times D_5$	no	no	(???)

6				222
$\{1, 3, 5, 6\}$	$A_2 \times A_2$	no	FREE	???
$\{1, 3, 6, 7\}$	$A_2 \times A_2$	no	FREE	???
$\{2,4,6,7\}$	$A_2 \times A_2$	no	FREE	???
$\{3,4,6,7\}$	$A_2 \times A_2$	no	FREE	???
$\{1, 3, 4, 6, 7\}$	$A_2 \times A_3$	no	FREE	???
$\{1, 3, 5, 6, 7\}$	$A_2 \times A_3$	no	FREE	???
$\{2, 3, 4, 6, 7\}$	$A_2 \times A_3$	no	FREE	???
$\{1, 2, 3, 4, 6, 7\}$	$A_2 \times A_4$	no	FREE	???
$\{1, 2, 5\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 6\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1,4,6\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 4, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 5, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 5\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 6\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 5, 7\}$	$A_1 \times A_1 \times A_1$	no	no	(???)
$\{3, 5, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	`???
$\{1, 2, 3, 5\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 6\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 6\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 5, 6\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 6, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 3, 5, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 4, 5, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 4, 6, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 3, 5, 6\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 3, 6, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 5, 7\}$	$A_1 \times A_1 \times A_3$	no	no	(???)
$\{1, 2, 5, 6, 7\}$	$A_1 \times A_1 \times A_3$	no	no	(???)
$\{2, 3, 5, 6, 7\}$	$A_1 \times A_1 \times A_3$	no	no	(???)
$\{1, 2, 3, 5, 6\}$	$A_1 \times A_2 \times A_2$	no	FREE	`???
$\{1, 2, 3, 6, 7\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 4, 6, 7\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 3, 5, 6, 7\}$	$A_1 \times A_2 \times A_3$	no	no	(???)
$\{1, 2, 5, 7\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	no	(???)
$\{2, 3, 5, 7\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	no	(???)
$\{1, 2, 3, 5, 7\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	no	(???)

 $\mathbf{E8}$ 

subset	type	chamber?	free?	orbit
				condition?
{}		CHAMBER	(FREE)	(???)
{1}	$A_1$	CHAMBER	(FREE)	(???)
$\{2\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{3\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{4\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{5\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{6\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{7\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{8\}$	$A_1$	CHAMBER	(FREE)	(???)
$\{1, 3\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{2,4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{3,4\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{4, 5\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{5,6\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{6, 7\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{7, 8\}$	$A_2$	CHAMBER	(FREE)	(???)
$\{1, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 3, 4\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{2, 4, 5\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{3, 4, 5\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{4, 5, 6\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{5, 6, 7\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{6, 7, 8\}$	$A_3$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{1, 3, 4, 5\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{2,4,5,6\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{3,4,5,6\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{4, 5, 6, 7\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{5, 6, 7, 8\}$	$A_4$	CHAMBER	(FREE)	(???)
$\{1, 3, 4, 5, 6\}$	$A_5$	no	FREE	???
$\{2,4,5,6,7\}$	$A_5$	no	FREE	???
$\{3,4,5,6,7\}$	$A_5$	no	FREE	???
$\{4, 5, 6, 7, 8\}$	$A_5$	no	FREE	???
$\{1, 3, 4, 5, 6, 7\}$	$A_6$	no	FREE	???
$\{2,4,5,6,7,8\}$	$A_6$	no	FREE	???
$\{3,4,5,6,7,8\}$	$A_6$	no	FREE	???
$\{1, 3, 4, 5, 6, 7, 8\}$	$A_7$	no	FREE	???
$\{2, 3, 4, 5\}$	$D_4$	no	no	(???)
$\{1, 2, 3, 4, 5\}$	$D_5$	no	no	(???)
$\{2, 3, 4, 5, 6\}$	$D_5$	no	no	(???)
$\{2, 3, 4, 5, 6, 7\}$	$D_6$	no	no	(???)

$\{2, 3, 4, 5, 6, 7, 8\}$	$D_7$	no	no	(???)
$\{1, 2, 3, 4, 5, 6\}$	$E_6$	no CHAMBER	no (FREE)	(???)
$\{1, 2, 3, 4, 5, 6, 7\}$	$E_6$	no	no	(???)
$\{1, 2, 3, 4, 5, 6, 7, 8\}$	$E_8$	CHAMBER	(FREE)	(???)
$\{1, 2, 3, 4, 5, 6, 7, 6\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 4\}$	$A_1 \times A_1$ $A_1 \times A_1$		FREE	???
		no	FREE	???
$\{1,5\}$	$A_1 \times A_1$	no	$\frac{FREE}{FREE}$	???
$\{1,6\}$	$A_1 \times A_1$	no	FREE	???
$\{1,7\}$	$A_1 \times A_1$	no		???
$\{1,8\}$	$A_1 \times A_1$	no	${f FREE} {f FREE}$	???
$\{2,3\}$	$A_1 \times A_1$	no		???
$\{2,5\}$	$A_1 \times A_1$	no	FREE	
$\{2,6\}$	$A_1 \times A_1$	no	FREE	???
$\{2,7\}$	$A_1 \times A_1$	no	FREE	???
$\{2,8\}$	$A_1 \times A_1$	no	FREE	???
$\{3,5\}$	$A_1 \times A_1$	no	FREE	???
$\{3,6\}$	$A_1 \times A_1$	no	FREE	???
$\{3,7\}$	$A_1 \times A_1$	no	FREE	???
${3,8}$	$A_1 \times A_1$	no	FREE	???
$\{4,6\}$	$A_1 \times A_1$	no	FREE	???
$\{4,7\}$	$A_1 \times A_1$	no	FREE	???
$\{4, 8\}$	$A_1 \times A_1$	no	FREE	???
$\{5,7\}$	$A_1 \times A_1$	no	FREE	???
$\{5, 8\}$	$A_1 \times A_1$	no	FREE	???
$\{6, 8\}$	$A_1 \times A_1$	no	FREE	???
$\{1, 2, 3\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 4\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 6\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 7\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 3, 8\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 4, 5\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 5, 6\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 6, 7\}$	$A_1 \times A_2$	no	FREE	???
$\{1,7,8\}$	$A_1 \times A_2$	no	FREE	???
$\{2,4,6\}$	$A_1 \times A_2$	no	FREE	???
$\{2,4,7\}$	$A_1 \times A_2$	no	FREE	???
$\{2,4,8\}$	$A_1 \times A_2$	no	FREE	???
$\{2, 5, 6\}$	$A_1 \times A_2$	no	FREE	???
$\{2,6,7\}$	$A_1 \times A_2$	no	FREE	???
$\{2,7,8\}$	$A_1 \times A_2$	no	FREE	???
$\{3,4,6\}$	$A_1 \times A_2$	no	FREE	???
$\{3,4,7\}$	$A_1 \times A_2$	no	FREE	???
$\{3,4,8\}$	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
$\{3, 5, 6\}$	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
$\{3,6,7\}$	$A_1 \times A_2$ $A_1 \times A_2$	no	FREE	???
[0,0,1]	$n_1 \wedge n_2$	110	1:1(1212	

${3,7,8}$	$A_1 \times A_2$	no	FREE	???
$\{4, 5, 7\}$	$A_1 \times A_2$	no	FREE	???
$\{4, 5, 8\}$	$A_1 \times A_2$	no	FREE	???
$\{4, 6, 7\}$	$A_1 \times A_2$	no	FREE	???
$\{4, 7, 8\}$	$A_1 \times A_2$	no	FREE	???
$\{5,6,8\}$	$A_1 \times A_2$	no	FREE	???
$\{5, 7, 8\}$	$A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 5\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 3, 4, 6\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 3, 4, 7\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 3, 4, 8\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 4, 5, 6\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 5, 6, 7\}$	$A_1 \times A_3$	no	FREE	???
$\{1,6,7,8\}$	$A_1 \times A_3$	no	FREE	???
$\{2, 3, 4, 6\}$	$A_1 \times A_3$	no	FREE	???
$\{2,3,4,7\}$	$A_1 \times A_3$	no	FREE	???
$\{2,3,4,8\}$	$A_1 \times A_3$ $A_1 \times A_3$	no	FREE	???
$\{2, 4, 5, 7\}$	$A_1 \times A_3$ $A_1 \times A_3$	no	FREE	???
$\{2,4,5,7\}$ $\{2,4,5,8\}$	$A_1 \times A_3$ $A_1 \times A_3$	no	FREE	???
$\{2, 5, 6, 7\}$	$A_1 \times A_3$ $A_1 \times A_3$		FREE	???
$\{2, 6, 7, 8\}$		no	FREE	???
	$A_1 \times A_3$ $A_1 \times A_3$	no	FREE	???
$\{3,4,5,7\}$		no		???
$\{3,4,5,8\}$	$A_1 \times A_3$	no	FREE	
$\{3, 5, 6, 7\}$	$A_1 \times A_3$	no	FREE	???
$\{3, 6, 7, 8\}$	$A_1 \times A_3$	no	FREE	???
$\{4, 5, 6, 8\}$	$A_1 \times A_3$	no	FREE	???
$\{4, 6, 7, 8\}$	$A_1 \times A_3$	no	FREE	???
$\{1, 2, 3, 4, 6\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 2, 3, 4, 7\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 2, 3, 4, 8\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 2, 4, 5, 6\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 3, 4, 5, 7\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 3, 4, 5, 8\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 4, 5, 6, 7\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 5, 6, 7, 8\}$	$A_1 \times A_4$	no	FREE	???
$\{2, 4, 5, 6, 8\}$	$A_1 \times A_4$	no	FREE	???
$\{2, 5, 6, 7, 8\}$	$A_1 \times A_4$	no	FREE	???
$\{3,4,5,6,8\}$	$A_1 \times A_4$	no	FREE	???
$\{3, 5, 6, 7, 8\}$	$A_1 \times A_4$	no	FREE	???
$\{1, 2, 4, 5, 6, 7\}$	$A_1 \times A_5$	no	FREE	???
$\{1, 3, 4, 5, 6, 8\}$	$A_1 \times A_5$	no	FREE	???
$\{1, 4, 5, 6, 7, 8\}$	$A_1 \times A_5$	no	FREE	???
$\{1, 2, 4, 5, 6, 7, 8\}$	$A_1 \times A_6$	no	FREE	???
$\{2, 3, 4, 5, 7\}$	$A_1 \times D_4$	no	no	(???)
$\{2, 3, 4, 5, 8\}$	$A_1 \times D_4$ $A_1 \times D_4$	no	no	(???)
$\{1, 2, 3, 4, 5, 7\}$	$A_1 \times D_4$ $A_1 \times D_5$	no	no	(???)
[1, 4, 0, 4, 0, 1]	$n_1 \wedge \nu_5$	110	110	()

$\{1, 2, 3, 4, 5, 8\}$	$A_1 \times D_5$	no	no	(???)
$\{2, 3, 4, 5, 6, 8\}$	$A_1 \times D_5$ $A_1 \times D_5$	no	no	(???)
$\{1, 2, 3, 4, 5, 6, 8\}$	$A_1 \times E_6$	no	FREE	???
$\{1, 3, 5, 6\}$	$A_1 \times B_6$ $A_2 \times A_2$	no	FREE	???
$\{1, 3, 6, 7\}$	$A_2 \times A_2$	no	FREE	???
$\{1, 3, 7, 8\}$	$A_2 \times A_2$ $A_2 \times A_2$		FREE	???
		no	FREE	???
$\{2,4,6,7\}$	$A_2 \times A_2$	no	$\overline{FREE}$	???
$\{2,4,7,8\}$	$A_2 \times A_2$	no		???
$\{3,4,6,7\}$	$A_2 \times A_2$	no	FREE	???
$\{3,4,7,8\}$	$A_2 \times A_2$	no	FREE	???
$\{4,5,7,8\}$	$A_2 \times A_2$	no	FREE	
$\{1, 3, 4, 6, 7\}$	$A_2 \times A_3$	no	FREE	???
$\{1, 3, 4, 7, 8\}$	$A_2 \times A_3$	no	FREE	???
$\{1, 3, 5, 6, 7\}$	$A_2 \times A_3$	no	FREE	???
$\{1, 3, 6, 7, 8\}$	$A_2 \times A_3$	no	FREE	???
$\{2, 3, 4, 6, 7\}$	$A_2 \times A_3$	no	FREE	???
$\{2, 3, 4, 7, 8\}$	$A_2 \times A_3$	no	FREE	???
$\{2,4,5,7,8\}$	$A_2 \times A_3$	no	FREE	???
$\{2, 4, 6, 7, 8\}$	$A_2 \times A_3$	no	FREE	???
$\{3, 4, 5, 7, 8\}$	$A_2 \times A_3$	no	FREE	???
${3,4,6,7,8}$	$A_2 \times A_3$	no	FREE	???
$\{1, 2, 3, 4, 6, 7\}$	$A_2 \times A_4$	no	FREE	???
$\{1, 2, 3, 4, 7, 8\}$	$A_2 \times A_4$	no	FREE	???
$\{1, 3, 4, 5, 7, 8\}$	$A_2 \times A_4$	no	FREE	???
$\{1, 3, 5, 6, 7, 8\}$	$A_2 \times A_4$	no	FREE	???
$\{2, 3, 4, 5, 7, 8\}$	$A_2 \times D_4$	no	no	(???)
$\{1, 2, 3, 4, 5, 7, 8\}$	$A_2 \times D_5$	no	no	(???)
$\{1, 3, 4, 6, 7, 8\}$	$A_3 \times A_3$	no	FREE	???
$\{2, 3, 4, 6, 7, 8\}$	$A_3 \times A_3$	no	FREE	???
$\{1, 2, 3, 4, 6, 7, 8\}$	$A_3 \times A_4$	no	FREE	???
$\{1, 2, 5\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 6\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 4, 6\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 4, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1,4,8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 5, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 5, 8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 6, 8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 5\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 6\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 5, 7\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 5, 8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
( / / <b>)</b>		-		

$\{2, 6, 8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
${3,5,7}$	$A_1 \times A_1 \times A_1$	no	FREE	???
${3,5,8}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{3,6,8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{4,6,8\}$	$A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 3, 5\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 6\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 6\}$	$A_1 \times A_1 \times A_2$ $A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 7\}$	$A_1 \times A_1 \times A_2$ $A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 7\}$	$A_1 \times A_1 \times A_2$ $A_1 \times A_1 \times A_2$		FREE	???
		no		???
$\{1, 2, 5, 6\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 6, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	
$\{1, 2, 7, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 3, 5, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 3, 5, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 3, 6, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 4, 5, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 4, 5, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 4, 6, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 4, 7, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 5, 6, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 5, 7, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 3, 5, 6\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 3, 6, 7\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 3, 7, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2,4,6,8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 5, 6, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 5, 7, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{3,4,6,8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{3, 5, 6, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{3, 5, 7, 8\}$	$A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 5, 7\}$	$A_1 \times A_1 \times A_3$	no	FREE	???
$\{1, 2, 4, 5, 8\}$	$A_1 \times A_1 \times A_3$	no	FREE	???
$\{1, 2, 5, 6, 7\}$	$A_1 \times A_1 \times A_3$	no	FREE	???
$\{1, 2, 6, 7, 8\}$	$A_1 \times A_1 \times A_3$	no	FREE	???
$\{1, 3, 4, 6, 8\}$	$A_1 \times A_1 \times A_3$	no	FREE	???
$\{1, 4, 5, 6, 8\}$	$A_1 \times A_1 \times A_3$ $A_1 \times A_1 \times A_3$		FREE	???
$\{1, 4, 6, 7, 8\}$	$A_1 \times A_1 \times A_3$ $A_1 \times A_1 \times A_3$	no	FREE	???
$\{2, 3, 4, 6, 8\}$	$A_1 \times A_1 \times A_3$ $A_1 \times A_1 \times A_3$	no	FREE	???
		no		???
$\{2, 3, 5, 6, 7\}$	$A_1 \times A_1 \times A_3$	no	FREE	???
$\{2,3,6,7,8\}$	$A_1 \times A_1 \times A_3$	no	FREE	
$\{1, 2, 3, 4, 6, 8\}$	$A_1 \times A_1 \times A_4$	no	FREE	???
$\{1, 2, 4, 5, 6, 8\}$	$A_1 \times A_1 \times A_4$	no	FREE	???
$\{1, 2, 5, 6, 7, 8\}$	$A_1 \times A_1 \times A_4$	no	FREE	???

$\{2, 3, 5, 6, 7, 8\}$	$A_1 \times A_1 \times A_4$	no	FREE	???
$\{1, 2, 3, 5, 6\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 3, 6, 7\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 3, 7, 8\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 4, 6, 7\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 4, 7, 8\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 3, 5, 6, 8\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 3, 5, 7, 8\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 4, 5, 7, 8\}$	$A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 3, 5, 6, 7\}$	$A_1 \times A_2 \times A_3$	no	FREE	???
$\{1, 2, 3, 6, 7, 8\}$	$A_1 \times A_2 \times A_3$	no	FREE	???
$\{1, 2, 4, 5, 7, 8\}$	$A_1 \times A_2 \times A_3$	no	FREE	???
$\{1, 2, 4, 6, 7, 8\}$	$A_1 \times A_2 \times A_3$	no	FREE	???
$\{1, 2, 3, 5, 6, 7, 8\}$	$A_1 \times A_2 \times A_4$	no	FREE	???
$\{1, 2, 5, 7\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 5, 8\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 6, 8\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 4, 6, 8\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 5, 7\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 5, 8\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	FREE	???
$\{2, 3, 6, 8\}$	$A_1 \times A_1 \times A_1 \times A_1$	no	FREE	???
$\{1, 2, 3, 5, 7\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 5, 8\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 6, 8\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 4, 6, 8\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 5, 6, 8\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 5, 7, 8\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 3, 5, 6, 8\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{2, 3, 5, 7, 8\}$	$A_1 \times A_1 \times A_1 \times A_2$	no	FREE	???
$\{1, 2, 3, 5, 6, 8\}$	$A_1 \times A_1 \times A_2 \times A_2$	no	FREE	???
$\{1, 2, 3, 5, 7, 8\}$	$A_1 \times A_1 \times A_2 \times A_2$	no	FREE	???