A5

| subset | type | chamber? | free? | orbit |
|---------------------|-----------------------------|----------|--------|------------|
| | | | | condition? |
| {} | | CHAMBER | (FREE) | (YES) |
| $\{1\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{2\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{3\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{4\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{5\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{1, 2\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{2, 3\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{3,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{4, 5\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{3, 4, 5\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4, 5\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4, 5\}$ | A_5 | CHAMBER | (FREE) | (YES) |
| $\{1, 3\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{3, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 4, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{2, 3, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{2, 4, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 3, 5\}$ | $A_1 \times A_3$ | no | no | (no) |
| $\{1, 3, 4, 5\}$ | $A_1 \times A_3$ | no | no | (no) |
| $\{1, 2, 4, 5\}$ | $A_2 \times A_2$ | no | FREE | no |
| $\{1, 3, 5\}$ | $A_1 \times A_1 \times A_1$ | no | no | (no) |

$\mathbf{B5}$

| subset | type | chamber? | free? | orbit |
|---------------------|-----------------------------|----------|--------|------------|
| | | | | condition? |
| {} | | CHAMBER | (FREE) | (YES) |
| $\{1\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{2\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{3\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{4\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{5\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{1, 2\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{2, 3\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{3,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{4, 5\}$ | B_2 | CHAMBER | (FREE) | (YES) |
| $\{3, 4, 5\}$ | B_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4, 5\}$ | B_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4, 5\}$ | B_5 | CHAMBER | (FREE) | (YES) |
| $\{1, 3\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 5\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{2, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 5\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{3, 5\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 5\}$ | $A_1 \times A_2$ | no | FREE | YES |
| $\{1, 3, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{2, 3, 5\}$ | $A_1 \times A_2$ | no | FREE | YES |
| $\{1, 2, 3, 5\}$ | $A_1 \times A_3$ | no | no | (YES) |
| $\{1, 4, 5\}$ | $A_1 \times B_2$ | no | FREE | no |
| $\{2, 4, 5\}$ | $A_1 \times B_2$ | no | FREE | no |
| $\{1, 3, 4, 5\}$ | $A_1 \times B_3$ | no | no | (no) |
| $\{1, 2, 4, 5\}$ | $A_2 \times B_2$ | no | FREE | no |
| $\{1, 3, 5\}$ | $A_1 \times A_1 \times A_1$ | no | no | (no) |

C5

| subset | type | chamber? | free? | orbit |
|---------------------|-----------------------------|-----------------|--------|------------|
| | 5 <i>y</i> p 5 | 0110111120 01 1 | 22.007 | condition? |
| {} | | CHAMBER | (FREE) | (YES) |
| $\{1\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{2\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{3\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{4\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{5\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{1, 2\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{2, 3\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{3,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{4, 5\}$ | B_2 | CHAMBER | (FREE) | (YES) |
| ${3,4,5}$ | C_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4, 5\}$ | C_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4, 5\}$ | C_5 | CHAMBER | (FREE) | (YES) |
| $\{1, 3\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 5\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{2, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 5\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{3, 5\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 5\}$ | $A_1 \times A_2$ | no | FREE | YES |
| $\{1, 3, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{2, 3, 5\}$ | $A_1 \times A_2$ | no | FREE | YES |
| $\{1, 2, 3, 5\}$ | $A_1 \times A_3$ | no | FREE | YES |
| $\{1, 4, 5\}$ | $A_1 \times B_2$ | no | FREE | no |
| $\{2, 4, 5\}$ | $A_1 \times B_2$ | no | FREE | no |
| $\{1, 3, 4, 5\}$ | $A_1 \times C_3$ | no | FREE | no |
| $\{1, 2, 4, 5\}$ | $A_2 \times B_2$ | no | FREE | no |
| $\{1, 3, 5\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |

D5

| subset | type | chamber? | free? | orbit |
|---------------------|-----------------------------|----------|--------|------------|
| | <i>v</i> 1 | | | condition? |
| {} | | CHAMBER | (FREE) | (YES) |
| $\{1\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{2\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{3\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{4\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{5\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{1, 2\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{2, 3\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{3,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| ${3,5}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 5\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{3, 4, 5\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 5\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4, 5\}$ | D_4 | no | no | (no) |
| $\{1, 2, 3, 4, 5\}$ | D_5 | CHAMBER | (FREE) | (YES) |
| $\{1, 3\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{4,5\}$ | $A_1 \times A_1$ | no | no | (no) |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 4, 5\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 4, 5\}$ | $A_1 \times A_1 \times A_1$ | no | no | (no) |
| $\{2, 4, 5\}$ | $A_1 \times A_1 \times A_1$ | no | no | (no) |
| $\{1, 2, 4, 5\}$ | $A_1 \times A_1 \times A_2$ | no | no | (no) |

G2

| subset | type | chamber? | free? | orbit condition? |
|---------------------------|--|--|----------------------------|----------------------------------|
| {} {1} {2} {1,2} | $egin{array}{c} A_1 \ A_1 \ G_2 \end{array}$ | CHAMBER CHAMBER CHAMBER CHAMBER | (FREE) (FREE) (FREE) | (YES) (YES) (YES) (YES) |

$\mathbf{F4}$

| subset | type | chamber? | free? | orbit condition? |
|------------------|------------------|----------|--------|------------------|
| {} | | CHAMBER | (FREE) | (YES) |
| {1} | A_1 | CHAMBER | (FREE) | (YES) |
| $\{2\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{3\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{4\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{1, 2\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{3, 4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{2, 3\}$ | B_2 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3\}$ | B_3 | no | FREE | YES |
| $\{2, 3, 4\}$ | C_3 | no | no | (YES) |
| $\{1, 2, 3, 4\}$ | F_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 3\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{1, 4\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{2, 4\}$ | $A_1 \times A_1$ | no | FREE | YES |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | YES |
| $\{1, 3, 4\}$ | $A_1 \times A_2$ | no | FREE | YES |

| subset | type | chamber? | free? | orbit |
|------------------------|------------------|----------|--------|------------|
| | 71 | | | condition? |
| {} | | CHAMBER | (FREE) | (YES) |
| $\{1\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{2\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{3\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{4\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{5\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{6\}$ | A_1 | CHAMBER | (FREE) | (YES) |
| $\{1, 3\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{2,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{3,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{4, 5\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{5, 6\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{1, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2, 4, 5\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{3, 4, 5\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{4, 5, 6\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 3, 4, 5\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{2, 4, 5, 6\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{3, 4, 5, 6\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 3, 4, 5, 6\}$ | A_5 | no | FREE | YES |
| $\{2, 3, 4, 5\}$ | D_4 | no | no | (no) |
| $\{1, 2, 3, 4, 5\}$ | D_5 | no | no | (no) |
| $\{2, 3, 4, 5, 6\}$ | D_5 | no | no | (no) |
| $\{1, 2, 3, 4, 5, 6\}$ | E_6 | CHAMBER | (FREE) | (YES) |
| $\{1, 2\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 3\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{3, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{3, 6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{4, 6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 3\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 4, 5\}$ | $A_1 \times A_2$ | no | FREE | no |

| $\{1, 5, 6\}$ | $A_1 \times A_2$ | no | FREE | no |
|---------------------|-----------------------------|----|------|----|
| $\{2, 4, 6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{2, 5, 6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{3, 4, 6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{3, 5, 6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4, 5\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 3, 4, 6\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 4, 5, 6\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{2, 3, 4, 6\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 2, 3, 4, 6\}$ | $A_1 \times A_4$ | no | FREE | no |
| $\{1, 2, 4, 5, 6\}$ | $A_1 \times A_4$ | no | FREE | no |
| $\{1, 3, 5, 6\}$ | $A_2 \times A_2$ | no | FREE | no |
| $\{1, 2, 5\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 4, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{2, 3, 5\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{2, 3, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 3, 5\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 3, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 5, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{2, 3, 5, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 3, 5, 6\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | no |

E7

| subset | type | chamber? | free? | orbit |
|---------------------------|------------------|----------|--------|------------|
| | og P c | | 11001 | condition? |
| {} | | CHAMBER | (FREE) | (YES) |
| {1} | A_1 | CHAMBER | (FREE) | (YES) |
| {2} | A_1 | CHAMBER | (FREE) | (YES) |
| {3} | A_1 | CHAMBER | (FREE) | (YES) |
| {4} | A_1 | CHAMBER | (FREE) | (YES) |
| {5} | A_1 | CHAMBER | (FREE) | (YES) |
| {6} | A_1 | CHAMBER | (FREE) | (YES) |
| {7} | A_1 | CHAMBER | (FREE) | (YES) |
| $\{1,3\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{2,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{3,4\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{4,5\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{5, 6\}$ | A_2 | CHAMBER | (FREE) | (YES) |
| $\{6,7\}$ | $\overline{A_2}$ | CHAMBER | (FREE) | (YES) |
| $\{1, 3, 4\}$ | $\overline{A_3}$ | CHAMBER | (FREE) | (YES) |
| $\{2, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{2,4,5\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{3,4,5\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{4, 5, 6\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{5, 6, 7\}$ | A_3 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 3, 4, 5\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{2,4,5,6\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{3,4,5,6\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{4, 5, 6, 7\}$ | A_4 | CHAMBER | (FREE) | (YES) |
| $\{1, 3, 4, 5, 6\}$ | A_5 | no | FREE | YES |
| $\{2,4,5,6,7\}$ | A_5 | CHAMBER | (FREE) | (YES) |
| $\{3,4,5,6,7\}$ | A_5 | no | FREE | YES |
| $\{1, 3, 4, 5, 6, 7\}$ | A_6 | no | FREE | YES |
| $\{2, 3, 4, 5\}$ | D_4 | no | no | (no) |
| $\{1, 2, 3, 4, 5\}$ | D_5 | no | no | (no) |
| $\{2, 3, 4, 5, 6\}$ | D_5 | no | no | (no) |
| $\{2, 3, 4, 5, 6, 7\}$ | D_6 | no | no | (no) |
| $\{1, 2, 3, 4, 5, 6\}$ | E_6 | CHAMBER | (FREE) | (YES) |
| $\{1, 2, 3, 4, 5, 6, 7\}$ | E_7 | CHAMBER | (FREE) | (YES) |
| $\{1, 2\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 4\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 7\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2, 3\}$ | $A_1 \times A_1$ | no | FREE | no |

| $\{2, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
|-------------------------|--------------------------------------|-----|------|-------|
| $\{2, 6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{2,7\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{3, 5\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{3,6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{3,7\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{4,6\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{4,7\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{5,7\}$ | $A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 3\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1,3,6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1,3,7\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1,4,5\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 5, 6\}$ | $A_1 \times A_2$ $A_1 \times A_2$ | no | FREE | no |
| $\{1, 6, 7\}$ | $A_1 \times A_2$ $A_1 \times A_2$ | | FREE | no |
| $\{2,4,6\}$ | $A_1 \times A_2$ $A_1 \times A_2$ | no | FREE | |
| $\{2,4,0\}$ $\{2,4,7\}$ | $A_1 \times A_2$ $A_1 \times A_2$ | no | FREE | no |
| | | no | FREE | no |
| $\{2,5,6\}$ | $A_1 \times A_2$ | no | | no |
| $\{2,6,7\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{3,4,6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{3,4,7\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{3, 5, 6\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{3,6,7\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{4, 5, 7\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{4, 6, 7\}$ | $A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4, 5\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 3, 4, 6\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 3, 4, 7\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 4, 5, 6\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 5, 6, 7\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{2, 3, 4, 6\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{2, 3, 4, 7\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{2, 4, 5, 7\}$ | $A_1 \times A_3$ | no | no | (no) |
| $\{2, 5, 6, 7\}$ | $A_1 \times A_3$ | no | no | (no) |
| ${3,4,5,7}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{3, 5, 6, 7\}$ | $A_1 \times A_3$ | no | FREE | no |
| $\{1, 2, 3, 4, 6\}$ | $A_1 \times A_4$ | no | FREE | no |
| $\{1, 2, 3, 4, 7\}$ | $A_1 \times A_4$ | no | FREE | no |
| $\{1, 2, 4, 5, 6\}$ | $A_1 \times A_4$ | no | FREE | no |
| $\{1, 3, 4, 5, 7\}$ | $A_1 \times A_4$ | no | FREE | no |
| $\{1, 4, 5, 6, 7\}$ | $A_1 \times A_4$ | no | FREE | no |
| $\{1, 2, 4, 5, 6, 7\}$ | $A_1 \times A_5$ | no | FREE | no |
| $\{2, 3, 4, 5, 7\}$ | $A_1 \times D_4$ | no | no | (no) |
| $\{1, 2, 3, 4, 5, 7\}$ | $A_1 \times D_5$ | no | no | (no) |
| (-, -, 0, 1, 0, 1) | 11 ₁ \(\(\mu\)\D_0 | 110 | 110 | (110) |

| $\{1, 3, 5, 6\}$ | $A_2 \times A_2$ | no | FREE | no |
|------------------------|--|----|------|------|
| $\{1, 3, 6, 7\}$ | $A_2 \times A_2$ | no | FREE | no |
| $\{2,4,6,7\}$ | $A_2 \times A_2$ | no | FREE | no |
| $\{3,4,6,7\}$ | $A_2 \times A_2$ | no | FREE | no |
| $\{1, 3, 4, 6, 7\}$ | $A_2 \times A_3$ | no | FREE | no |
| $\{1, 3, 5, 6, 7\}$ | $A_2 \times A_3$ | no | FREE | no |
| $\{2, 3, 4, 6, 7\}$ | $A_2 \times A_3$ | no | FREE | no |
| $\{1, 2, 3, 4, 6, 7\}$ | $A_2 \times A_4$ | no | FREE | no |
| $\{1, 2, 5\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1,4,6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 4, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 5, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{2, 3, 5\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{2, 3, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{2, 3, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{2, 5, 7\}$ | $A_1 \times A_1 \times A_1$ | no | no | (no) |
| $\{3, 5, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | no |
| $\{1, 2, 3, 5\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 3, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 3, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 5, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 6, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 3, 5, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 4, 5, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 4, 6, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{2, 3, 5, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{2, 3, 6, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | no |
| $\{1, 2, 4, 5, 7\}$ | $A_1 \times A_1 \times A_3$ | no | no | (no) |
| $\{1, 2, 5, 6, 7\}$ | $A_1 \times A_1 \times A_3$ | no | no | (no) |
| $\{2, 3, 5, 6, 7\}$ | $A_1 \times A_1 \times A_3$ | no | no | (no) |
| $\{1, 2, 3, 5, 6\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | no |
| $\{1, 2, 3, 6, 7\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | no |
| $\{1, 2, 4, 6, 7\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | no |
| $\{1, 2, 3, 5, 6, 7\}$ | $A_1 \times A_2 \times A_3$ | no | no | (no) |
| $\{1, 2, 5, 7\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | no | (no) |
| $\{2, 3, 5, 7\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | no | (no) |
| $\{1, 2, 3, 5, 7\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | no | (no) |

E8

| subset | type | chamber? | free? | orbit |
|---------------------------|------------|----------|--------|------------|
| | <i>v</i> 1 | | | condition? |
| {} | | CHAMBER | (FREE) | (???) |
| {1} | A_1 | CHAMBER | (FREE) | (???) |
| $\{2\}$ | A_1 | CHAMBER | (FREE) | (???) |
| $\{3\}$ | A_1 | CHAMBER | (FREE) | (???) |
| $\{4\}$ | A_1 | CHAMBER | (FREE) | (???) |
| $\{5\}$ | A_1 | CHAMBER | (FREE) | (???) |
| $\{6\}$ | A_1 | CHAMBER | (FREE) | (???) |
| $\{7\}$ | A_1 | CHAMBER | (FREE) | (???) |
| $\{8\}$ | A_1 | CHAMBER | (FREE) | (???) |
| $\{1,3\}$ | A_2 | CHAMBER | (FREE) | (???) |
| $\{2,4\}$ | A_2 | CHAMBER | (FREE) | (???) |
| $\{3,4\}$ | A_2 | CHAMBER | (FREE) | (???) |
| $\{4, 5\}$ | A_2 | CHAMBER | (FREE) | (???) |
| $\{5,6\}$ | A_2 | CHAMBER | (FREE) | (???) |
| $\{6, 7\}$ | A_2 | CHAMBER | (FREE) | (???) |
| $\{7, 8\}$ | A_2 | CHAMBER | (FREE) | (???) |
| $\{1, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (???) |
| $\{2, 3, 4\}$ | A_3 | CHAMBER | (FREE) | (???) |
| $\{2, 4, 5\}$ | A_3 | CHAMBER | (FREE) | (???) |
| $\{3, 4, 5\}$ | A_3 | CHAMBER | (FREE) | (???) |
| $\{4, 5, 6\}$ | A_3 | CHAMBER | (FREE) | (???) |
| $\{5, 6, 7\}$ | A_3 | CHAMBER | (FREE) | (???) |
| $\{6, 7, 8\}$ | A_3 | CHAMBER | (FREE) | (???) |
| $\{1, 2, 3, 4\}$ | A_4 | CHAMBER | (FREE) | (???) |
| $\{1, 3, 4, 5\}$ | A_4 | CHAMBER | (FREE) | (???) |
| $\{2,4,5,6\}$ | A_4 | CHAMBER | (FREE) | (???) |
| $\{3,4,5,6\}$ | A_4 | CHAMBER | (FREE) | (???) |
| $\{4, 5, 6, 7\}$ | A_4 | CHAMBER | (FREE) | (???) |
| $\{5, 6, 7, 8\}$ | A_4 | CHAMBER | (FREE) | (???) |
| $\{1, 3, 4, 5, 6\}$ | A_5 | no | FREE | ??? |
| $\{2,4,5,6,7\}$ | A_5 | no | FREE | ??? |
| $\{3, 4, 5, 6, 7\}$ | A_5 | no | FREE | ??? |
| $\{4, 5, 6, 7, 8\}$ | A_5 | no | FREE | ??? |
| $\{1, 3, 4, 5, 6, 7\}$ | A_6 | no | FREE | ??? |
| $\{2, 4, 5, 6, 7, 8\}$ | A_6 | no | FREE | ??? |
| $\{3,4,5,6,7,8\}$ | A_6 | no | FREE | ??? |
| $\{1, 3, 4, 5, 6, 7, 8\}$ | A_7 | no | FREE | ??? |
| $\{2, 3, 4, 5\}$ | D_4 | no | no | (???) |
| $\{1, 2, 3, 4, 5\}$ | D_5 | no | no | (???) |
| $\{2, 3, 4, 5, 6\}$ | D_5 | no | no | (???) |
| $\{2, 3, 4, 5, 6, 7\}$ | D_6 | no | no | (???) |

| $\{2, 3, 4, 5, 6, 7, 8\}$ | D_7 | no | no | (???) |
|------------------------------|--------------------------------------|---------------|---------------------|-------|
| $\{1, 2, 3, 4, 5, 6\}$ | E_6 | no CHAMBER | no (FREE) | (???) |
| $\{1, 2, 3, 4, 5, 6, 7\}$ | E_6 | no | no | (???) |
| $\{1, 2, 3, 4, 5, 6, 7, 8\}$ | E_8 | CHAMBER | (FREE) | (???) |
| $\{1, 2, 3, 4, 5, 6, 7, 6\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 4\}$ | $A_1 \times A_1$ $A_1 \times A_1$ | | FREE | ??? |
| $\{1,4\}$ $\{1,5\}$ | $A_1 \times A_1$ $A_1 \times A_1$ | no | FREE | ??? |
| | | no | FREE | ??? |
| $\{1,6\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{1,7\}$ | $A_1 \times A_1$ | no | | ??? |
| $\{1,8\}$ | $A_1 \times A_1$ | no | ${f FREE} {f FREE}$ | ??? |
| $\{2,3\}$ | $A_1 \times A_1$ | no | | ??? |
| $\{2,5\}$ | $A_1 \times A_1$ | no | FREE | |
| $\{2,6\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{2,7\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{2,8\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{3,5\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{3,6\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{3,7\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| ${3,8}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{4,6\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{4,7\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{4, 8\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{5,7\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{5, 8\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{6, 8\}$ | $A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 3\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 5\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 6\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 7\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 4, 5\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 5, 6\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 6, 7\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 7, 8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{2,4,6\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{2,4,7\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{2,4,8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 5, 6\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{2,6,7\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{2,7,8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{3,4,6\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{3,4,7\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{3,4,8\}$ | $A_1 \times A_2$ $A_1 \times A_2$ | no | FREE | ??? |
| $\{3, 5, 6\}$ | $A_1 \times A_2$ $A_1 \times A_2$ | no | FREE | ??? |
| $\{3,6,7\}$ | $A_1 \times A_2$ $A_1 \times A_2$ | no | FREE | ??? |
| [0,0,1] | $n_1 \wedge n_2$ | 110 | 1:1(1212 | |

| ${3,7,8}$ | $A_1 \times A_2$ | no | FREE | ??? |
|------------------------|--------------------------------------|----|------|-------|
| $\{4, 5, 7\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{4, 5, 8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{4, 6, 7\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{4, 7, 8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{5, 6, 8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{5, 7, 8\}$ | $A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 5\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 3, 4, 6\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 3, 4, 7\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 3, 4, 8\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{1,4,5,6\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 5, 6, 7\}$ | $A_1 \times A_3$ $A_1 \times A_3$ | no | FREE | ??? |
| $\{1,6,7,8\}$ | $A_1 \times A_3$ $A_1 \times A_3$ | no | FREE | ??? |
| $\{2, 3, 4, 6\}$ | $A_1 \times A_3$ $A_1 \times A_3$ | | FREE | ??? |
| | | no | FREE | ??? |
| $\{2, 3, 4, 7\}$ | $A_1 \times A_3$ | no | | ??? |
| $\{2, 3, 4, 8\}$ | $A_1 \times A_3$ | no | FREE | |
| $\{2,4,5,7\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{2,4,5,8\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{2, 5, 6, 7\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{2, 6, 7, 8\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{3,4,5,7\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| ${3,4,5,8}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{3, 5, 6, 7\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{3, 6, 7, 8\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{4, 5, 6, 8\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{4, 6, 7, 8\}$ | $A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 3, 4, 6\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 3, 4, 7\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 3, 4, 8\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 4, 5, 6\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 3, 4, 5, 7\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 3, 4, 5, 8\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 4, 5, 6, 7\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 5, 6, 7, 8\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{2, 4, 5, 6, 8\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{2, 5, 6, 7, 8\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{3,4,5,6,8\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{3, 5, 6, 7, 8\}$ | $A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 4, 5, 6, 7\}$ | $A_1 \times A_5$ | no | FREE | ??? |
| $\{1, 3, 4, 5, 6, 8\}$ | $A_1 \times A_5$ $A_1 \times A_5$ | no | FREE | ??? |
| $\{1, 4, 5, 6, 7, 8\}$ | $A_1 \times A_5$ $A_1 \times A_5$ | | FREE | ??? |
| $\{1, 4, 5, 6, 7, 8\}$ | $A_1 \times A_5$ $A_1 \times A_6$ | no | FREE | ??? |
| | | no | | |
| $\{2,3,4,5,7\}$ | $A_1 \times D_4$ | no | no | (???) |
| $\{2,3,4,5,8\}$ | $A_1 \times D_4$ | no | no | (???) |
| $\{1, 2, 3, 4, 5, 7\}$ | $A_1 \times D_5$ | no | no | (???) |

| $\{1, 2, 3, 4, 5, 8\}$ | $A_1 \times D_5$ | no | no | (???) |
|---------------------------|-----------------------------|----|------|-------|
| $\{2, 3, 4, 5, 6, 8\}$ | $A_1 \times D_5$ | no | no | (???) |
| $\{1, 2, 3, 4, 5, 6, 8\}$ | $A_1 \times E_6$ | no | FREE | ??? |
| $\{1, 3, 5, 6\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 6, 7\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 7, 8\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{2,4,6,7\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{2, 4, 7, 8\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{3,4,6,7\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{3,4,7,8\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{4, 5, 7, 8\}$ | $A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 4, 6, 7\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{1, 3, 4, 7, 8\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{1, 3, 5, 6, 7\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{1,3,6,7,8\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{2, 3, 4, 6, 7\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{2,3,4,7,8\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{2,4,5,7,8\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{2, 4, 6, 7, 8\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{3,4,5,7,8\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{3,4,6,7,8\}$ | $A_2 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 3, 4, 6, 7\}$ | $A_2 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 3, 4, 7, 8\}$ | $A_2 \times A_4$ | no | FREE | ??? |
| $\{1, 3, 4, 5, 7, 8\}$ | $A_2 \times A_4$ | no | FREE | ??? |
| $\{1, 3, 5, 6, 7, 8\}$ | $A_2 \times A_4$ | no | FREE | ??? |
| $\{2, 3, 4, 5, 7, 8\}$ | $A_2 \times D_4$ | no | no | (???) |
| $\{1, 2, 3, 4, 5, 7, 8\}$ | $A_2 \times D_5$ | no | no | (???) |
| $\{1, 3, 4, 6, 7, 8\}$ | $A_3 \times A_3$ | no | FREE | `???′ |
| $\{2, 3, 4, 6, 7, 8\}$ | $A_3 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 3, 4, 6, 7, 8\}$ | $A_3 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 5\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 4, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 4, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 4, 8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 5, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 5, 8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 6, 8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 3, 5\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 3, 6\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 3, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 3, 8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 5, 7\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 5, 8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| | | | | |

| $\{2, 6, 8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
|------------------------|--|----|------|-----|
| ${3,5,7}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| ${3,5,8}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{3,6,8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{4,6,8\}$ | $A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 3, 5\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 6\}$ | $A_1 \times A_1 \times A_2$ $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 7\}$ | $A_1 \times A_1 \times A_2$ $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 7\}$ | $A_1 \times A_1 \times A_2$ $A_1 \times A_1 \times A_2$ | | FREE | ??? |
| | | no | | ??? |
| $\{1, 2, 5, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 6, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | |
| $\{1, 2, 7, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 5, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 5, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 6, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 4, 5, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 4, 5, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 4, 6, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 4, 7, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 5, 6, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 5, 7, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 3, 5, 6\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 3, 6, 7\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 3, 7, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2,4,6,8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 5, 6, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 5, 7, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{3,4,6,8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{3, 5, 6, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{3, 5, 7, 8\}$ | $A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 5, 7\}$ | $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 4, 5, 8\}$ | $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 5, 6, 7\}$ | $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 6, 7, 8\}$ | $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 3, 4, 6, 8\}$ | $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| $\{1, 4, 5, 6, 8\}$ | $A_1 \times A_1 \times A_3$ $A_1 \times A_1 \times A_3$ | | FREE | ??? |
| $\{1, 4, 6, 7, 8\}$ | $A_1 \times A_1 \times A_3$ $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| $\{2, 3, 4, 6, 8\}$ | $A_1 \times A_1 \times A_3$ $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| | | no | | ??? |
| $\{2, 3, 5, 6, 7\}$ | $A_1 \times A_1 \times A_3$ | no | FREE | ??? |
| $\{2,3,6,7,8\}$ | $A_1 \times A_1 \times A_3$ | no | FREE | |
| $\{1, 2, 3, 4, 6, 8\}$ | $A_1 \times A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 4, 5, 6, 8\}$ | $A_1 \times A_1 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 5, 6, 7, 8\}$ | $A_1 \times A_1 \times A_4$ | no | FREE | ??? |

| $\{2, 3, 5, 6, 7, 8\}$ | $A_1 \times A_1 \times A_4$ | no | FREE | ??? |
|---------------------------|--|----|------|-----|
| $\{1, 2, 3, 5, 6\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 6, 7\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 7, 8\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 6, 7\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 7, 8\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 5, 6, 8\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 3, 5, 7, 8\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 4, 5, 7, 8\}$ | $A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 5, 6, 7\}$ | $A_1 \times A_2 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 3, 6, 7, 8\}$ | $A_1 \times A_2 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 4, 5, 7, 8\}$ | $A_1 \times A_2 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 4, 6, 7, 8\}$ | $A_1 \times A_2 \times A_3$ | no | FREE | ??? |
| $\{1, 2, 3, 5, 6, 7, 8\}$ | $A_1 \times A_2 \times A_4$ | no | FREE | ??? |
| $\{1, 2, 5, 7\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 5, 8\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 6, 8\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 4, 6, 8\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 3, 5, 7\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 3, 5, 8\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{2, 3, 6, 8\}$ | $A_1 \times A_1 \times A_1 \times A_1$ | no | FREE | ??? |
| $\{1, 2, 3, 5, 7\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 5, 8\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 6, 8\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 4, 6, 8\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 5, 6, 8\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 5, 7, 8\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 3, 5, 6, 8\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{2, 3, 5, 7, 8\}$ | $A_1 \times A_1 \times A_1 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 5, 6, 8\}$ | $A_1 \times A_1 \times A_2 \times A_2$ | no | FREE | ??? |
| $\{1, 2, 3, 5, 7, 8\}$ | $A_1 \times A_1 \times A_2 \times A_2$ | no | FREE | ??? |