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Problem Statement

Simulate the current and proposed harbor unloading systems to evaluate their efficiency in terms of average and maximum times per ship in the harbor, average and maximum waiting times per ship, the percentage of idle time for unloading facilities, and the length of the longest queue.

Introduction

The owners of a small harbor with ship unloading facilities are grappling with operational inefficiencies and service quality challenges. Originally, the harbor's management relied on straightforward scheduling and queuing models to manage ship arrivals and unloading times, assuming that the system could be effectively managed within the existing time intervals of 15 to 145 minutes for ship arrivals and 45 to 90 minutes for unloading.

However, new concerns have arisen indicating that the current operational model is not meeting service expectations. Long waiting times and idle unloading facilities are affecting the harbor's reputation and bottom line. This realization has significant implications for the harbor's overall operational strategy, rendering the existing models insufficient for their evolving needs.

Recognizing the complexities involved, the harbor's owners have commissioned a simulation model to more accurately capture the nuances of harbor operations. Specifically, tasked with simulating the current harbor system and a proposed system that aims to reduce offload times to between 35 and 75 minutes and adjust the time between successive ship arrivals to 10 to 120 minutes.

In this scenario, a discrete-event simulation is the preferred approach to evaluate the efficiency of the current and proposed harbor unloading systems. The harbor is facing operational inefficiencies and service quality challenges that necessitate a more sophisticated modeling technique. While initial attempts relied on simplistic scheduling and queuing models, these have proven inadequate in addressing the complexities of ship arrivals, unloading times, and resource allocation. To comprehensively assess the systems, a discrete-event simulation is employed to capture the dynamic nature of harbor operations. It allows for the realistic modeling of ship arrivals and unloading processes, incorporating variability and uncertainties. Through this simulation, key performance metrics such as average and maximum ship times in the harbor, waiting times, idle facility percentages, and queue lengths can be accurately measured. The simulation also enables a direct comparison between the current and proposed systems, providing valuable insights for optimizing service quality and operational efficiency in the harbor.

This comprehensive report will outline the methodology used to develop the simulation model, including the statistical tests and techniques employed. It will also present the findings from both the current and proposed harbor system simulations, explaining how they differ and what these differences signify. The report will conclude with an assessment of the proposed changes' effectiveness

and offer recommendations for their practical implementation in the harbor's ongoing efforts to improve service quality and efficiency.

Methodology

Algorithm Adaptation and Verification

The initial step involves adapting the Harbor System Simulation Algorithm for our specific research context. Given the critical nature of this foundational work, we place a high emphasis on verification. The algorithm is fine-tuned for the research environment, and verification runs are conducted to ensure it aligns with anticipated behaviors. During this verification process, we compare the outcomes generated by the model against benchmark data provided in Tables 5.15, 5.16, and 5.17 from the eText. Based on this analysis, the model is iteratively refined to enhance its accuracy and reliability. The significance of this step is to establish a validated, credible model that will serve as the cornerstone of the entire study.

The key aspects of the adapted algorithm include the following:

1. **Arrival Time**: Calculate the arrival time ($arrive_i$) for each ship, based on the generated $between_i$ value and the arrival time of the previous ship ($arrive_{i-1}$).

2. **Idle and Wait Time**: The algorithm calculates whether the dock facilities are idle ($idle_i$) or whether the ship has to wait ($wait_i$) before unloading commences. This is done by comparing $arrive_i$ with the finish time for unloading the previous ship ($finish_{i-1}$).

3. **Unloading Time**: We calculate the start ($start_i$) and finish ($finish_i$) times for unloading each ship.

4. **Total Time in Harbor**: Calculate the total time each ship spends in the harbor ($harbor_i$), which is the sum of its waiting and unloading times.

5. **Metric Update Algorithm**: After each simulation run, metrics are updated as follows:

   - If $harbor_i > MAXHAR$, then $MAXHAR$ is updated to be $harbor_i$.
   - $wait_i$ is summed into the total waiting time $WAITIME$ for averaging.
   - $idle_i$ is summed into the total idle time $IDLETIME$.
   - If $wait_i > MAXWAIT$, then $MAXWAIT$ is updated to be $wait_i$.
   - Finally, the average metrics are computed as $HARTIME = HARTIME/n$, $WAITIME = WAITIME/n$, and $IDLETIME = IDLETIME/finish_n$.

This adaptation allows for a more nuanced and detailed simulation, capturing all the relevant metrics: Average time of a ship in the harbor ($HARTIME$), Maximum time of a ship in the harbor ($MAXHAR$), Average waiting time of a ship ($WAITIME$), Maximum waiting time of a ship ($MAXWAIT$), and Percentage of time dock facilities are idle ($IDLETIME$).

Simulation Runs

Next, the execution of extensive simulation runs, intended to test the harbor system under a variety of conditions. The model will be verified by running multiple simulation scenarios. Each scenario will consist of 100 ships and will be executed 6 times. The simulation results will be compared with existing data from Tables 5.15, 5.16, and 5.17 to ensure accuracy and reliability. These are repeated multiple times to account for stochastic variability. Each run is examined for the range of key metrics like average waiting times, maximum waiting times, and idle times. This ensures that the data set generated is not only extensive but also statistically robust, lending further credibility to subsequent analyses. The simulation runs are vital for two primary reasons: they generate the comprehensive data set required for in-depth analysis and interpretation, and they act as a validation point to reaffirm that the model accurately represents real-world scenarios.

Operations for the Discrete Event Simulation

In the context of harbor operations, Discrete Event Simulation (DES) serves as an effective tool for modeling and analyzing the system dynamics. The method is particularly well-suited for capturing the stochastic nature of ship arrivals and unloading times.

will simulate the arrival and unloading of a single ship at the harbor.

Components of the Simulation

1. **State Variables:**
    - Last ship's arrival time ($LastArrival$)
    - Time it takes to finish unloading the last ship ($LastUnloadingTime$)
    - Metrics such as harbor time ($HarborTime$), waiting time ($WaitTime$), and idle time ($IdleTime$)
2. **Events:**
    - Arrival of a new ship
    - Completion of unloading a ship

Sequence of Operations

1. **Initialization:**
   - Set initial values for state variables and metrics.
2. **Ship Arrival:**
   - Generate a random arrival time for the new ship based on specified distributions.
   - Update state variables ($LastArrival$) based on the new arrival.
3. **Idle and Wait Time:**
   - Determine whether the dock facilities are idle or whether the ship has to wait before unloading based on the comparison between the ship's arrival time and the finish time for unloading the previous ship ($LastUnloadingTime$).
   - Update waiting time ($WaitTime$) and idle time ($IdleTime$) accordingly.
4. **Unloading Time:**
   - Calculate the start time ($StartTime$) and finish time ($FinishTime$) for unloading the ship based on specified distributions.
5. **Total Time in Harbor:**
   - Calculate the total time the ship spends in the harbor ($HarborTime$), which is the sum of its waiting and unloading times.
6. **Metric Updates:**
   - Update metrics after each simulation run:
     - If $HarborTime$ for the ship exceeds the maximum harbor time ($MAXHAR$), update $MAXHAR$.
     - Sum the ship's waiting time ($WaitTime$) into the total waiting time ($WAITIME$) for averaging.
     - Sum the ship's idle time ($IdleTime$) into the total idle time ($IDLETIME$).
     - If the ship's waiting time ($WaitTime$) exceeds the maximum waiting time ($MAXWAIT$), update $MAXWAIT$.
     - Finally, compute average metrics as $HARTIME = HARTIME/n$, $WAITIME = WAITIME/n$, and $IDLETIME = IDLETIME/FinishTime$.

This sequence of operations is repeated for each ship arrival, accumulating data on various metrics such as average waiting times, maximum waiting times, idle times, and harbor times. The simulation is run multiple times to ensure statistical robustness.

Application of Discrete-Event Simulation to Code and Validation

The described discrete-event simulation process will be implemented in code to simulate harbor operations. The code will capture the dynamics of ship arrivals, unloading times, waiting times, and other relevant metrics. It will be validated to ensure its accuracy and reliability in representing real-world scenarios.

The validation of the simulation code will be conducted as a critical step in the study. This validation will involve comparing the simulation outputs with benchmark data and conducting various statistical tests to assess its performance. The results of the validation will be included as an appendix at the end of this report, reaffirming the credibility of the simulation model.

The validation process is essential to ensure that the simulation accurately reflects the complexities of harbor operations and provides a solid foundation for the subsequent analyses and recommendations. Details of the validation, including the code used and the validation results, will be presented in the report's appendix.

Discrepancy Observation

Moreover, following the simulation runs, a thorough discrepancy analysis is conducted. This involves a line-by-line comparison between our simulation outputs and the benchmark data in Tables 5.15, 5.16, and 5.17. Possible sources of these discrepancies could be limitations in the model's ability to capture complex dynamics, random fluctuations in the data, or unaccounted external variables. Several statistical tests are utilized to compare the datasets, such as: qualitative assessment (through Data Visualizations), Root Mean Square Error (RMSE) and Confidence Intervals. The importance of this phase is paramount, as it directly impacts the reliability and credibility of the findings and recommendations.

Sensitivity Analysis

The final step of the methodology is the sensitivity analysis. This entails systematically altering key parameters such as arrival rates and offloading times within the simulation model to assess how sensitive the outcomes are to these changes. For each alteration, the entire simulation is rerun, and the new results are compared to the baseline scenario. This aids in determining which parameters have the most significant impact on the system's performance and efficiency. The sensitivity analysis is crucial for several reasons: it confirms the model's robustness across a range of conditions, identifies the most influential variables, and provides insights into how changes in these variables could affect the harbor's operations.

In summary, each step in this comprehensive methodology serves a crucial role in ensuring the study's scientific rigor and practical relevance. By adhering to this meticulously crafted approach, it helps to offer reliable, actionable

insights to the client.

Results

Simulation Runs

Presented are the outcomes of 6 simulation runs conducted to evaluate the harbor system's performance under various conditions. Each table represents a distinct set of operational parameters. The parameters for each simulation run are based on the values specified in Tables 5.15, 5.16, and 5.17 of the reference document. The metrics we focus on include the average and maximum time a ship spends in the harbor, the average and maximum waiting time for unloading, and the percentage of time the dock facilities remain idle. These simulation runs offer valuable insights into how changes in operational parameters could affect the harbor's efficiency and service quality.

Metrics	Run 1	Run 2	Run 3	Run 4	Run 5	Run 6
Average time of a ship in the harbor	117.48	100.26	138.79	78.95	118.93	92.24
Maximum time of a ship in the harbor	272	236	336	190	305	236
Average waiting time of a ship	48.29	33.56	70.21	13.68	53.09	24.89
Maximum waiting time of a ship	197	166	262	125	243	165
Percentage of time dock facilities are idle	0.1764	0.1790	0.0932	0.2757	0.1604	0.2181

Table 1: Simulation Results for Table 5.15

Metrics	Run 1	Run 2	Run 3	Run 4	Run 5	Run 6
Average time of a ship in the harbor	61.84	62.69	78.34	62.73	62.63	66.98
Maximum time of a ship in the harbor	119	135	235	124	126	141
Average waiting time of a ship	7.25	9.92	23.73	8.13	7.03	11.25
Maximum waiting time of a ship	51	97	175	76	54	89
Percentage of time dock facilities are idle	0.3630	0.3308	0.2499	0.3711	0.3609	0.3318

Table 2: Simulation Results for Table 5.16

Discrepancy Observation

After executing multiple simulation runs, a comprehensive assessment of the model's accuracy was performed by comparing the simulated metrics against their real-world counterparts from Tables 5.15, 5.16, and 5.17. These comparisons were systematically visualized through a series of bar charts, serving as an initial qualitative evaluation of the model's applicability and effectiveness.

Discrepancy Observation for Table 5.15

Discrepancy Observation for Table 5.15

The Root Mean Square Error (RMSE) and confidence intervals for each metric as follows:

- Average time of a ship in the harbor (HARTIME): $RMSE = 23.15$, 95% Confidence Interval = $[80.85, 131.15]$
- Maximum time of a ship in the harbor (MAXHAR): $RMSE = 68.18$, 95% Confidence Interval = $[218.82, 349.18]$
- Average waiting time of a ship (WAITIME): $RMSE = 22.04$, 95% Confidence Interval = $[16.96, 45.04]$
- Maximum waiting time of a ship (MAXWAIT): $RMSE = 61.75$, 95% Confidence Interval = $[89.25, 162.75]$
- Percentage of time dock facilities are idle (IDLETIME): $RMSE = 0.0399$, 95% Confidence Interval = $[0.1301, 0.2699]$

The RMSE values suggest varying degrees of model accuracy for different metrics. While the RMSE for IDLETIME is relatively low, suggesting a good fit for this specific metric, the RMSE values for HARTIME, MAXHAR, WAITIME, and MAXWAIT are relatively high. This indicates that the simulation model could benefit from further refinement to better align with real-world data for these metrics. The 95% confidence intervals further indicate the precision of our simulation model. Wider intervals suggest more variability and less reliability in the simulated data for the corresponding metrics.

Discrepancy Observation for Table 5.16

The Root Mean Square Error (RMSE) values and 95% confidence intervals for each metric are as follows:

- Average time of a ship in the harbor (HARTIME): $RMSE = 4.43$, 95% Confidence Interval = $[61.21, 70.53]$
- Maximum time of a ship in the harbor (MAXHAR): $RMSE = 17.66$, 95% Confidence Interval = $[114.53, 178.80]$

- Average waiting time of a ship (WAITIME): $RMSE = 2.35$, 95% Confidence Interval = $[6.59, 15.85]$
- Maximum waiting time of a ship (MAXWAIT): $RMSE = 19.09$, 95% Confidence Interval = $[57.20, 123.47]$
- Percentage of time dock facilities are idle (IDLETIME): $RMSE = 0.0189$, 95% Confidence Interval = $[30.19, 36.73]$

The RMSE values for each metric were relatively low, particularly for *HARTIME*, *WAITIME*, and *IDLETIME*, indicating that the model offers a good approximation of real-world behaviors. Furthermore, the 95% confidence intervals for these metrics were narrow, suggesting a high level of reliability for the model in these specific areas. However, *MAXHAR* and *MAXWAIT* had higher RMSE values and wider confidence intervals, possibly due to higher variability in these metrics. This could imply that while the model performs well in general, but it might require further calibration for predicting maximum times. Overall, the observations indicate that the simulation model is highly reliable and accurate for the given scenario.

Discrepancy Observation for Table 5.17

The Root Mean Square Error (RMSE) values and 95% confidence intervals for each metric are as follows:

- Average time of a ship in the harbor (*HARTIME*): $RMSE = 27.98$, 95% Confidence Interval = $[5.12, 39.94]$
- Maximum time of a ship in the harbor (*MAXHAR*): $RMSE = 92.35$, 95% Confidence Interval = $[12.08, 132.58]$
- Average waiting time of a ship (*WAITIME*): $RMSE = 27.72$, 95% Confidence Interval = $[4.97, 39.60]$
- Maximum waiting time of a ship (*MAXWAIT*): $RMSE = 88.37$, 95% Confidence Interval = $[-3.06, 128.06]$
- Percentage of time dock facilities are idle (*IDLETIME*): $RMSE = 12.31$, 95% Confidence Interval = $[7.80, 15.66]$

These metrics suggest that the simulation model generally aligns well with real-world data but could benefit from further calibration to improve its predictive accuracy, particularly for metrics like *MAXHAR* and *MAXWAIT*. The RMSE values are moderate for these metrics, indicating room for improvement. The confidence intervals for *MAXHAR* and *MAXWAIT* are also wider, suggesting that the model's predictions for these metrics may be less reliable. Overall, the model provides a good starting point for simulating harbor operations but could be refined further for more accurate predictions.

The observed discrepancies between the real-world and simulated data across Tables 5.15, 5.16, and 5.17 can be attributed to a range of factors. Firstly, it's important to note that real-world operations are often subject to a myriad of variables that a simulation model may not fully account for. While the simulation employs random variables to approximate factors like time between ship arrivals and unloading times, it may fall short of capturing real-world complexities. These complexities can include operational inefficiencies, unexpected delays, or even external influences like weather conditions and seasonal variations, which are often challenging to model accurately.

Secondly, the model's assumptions themselves may introduce bias. For instance, if the model assumes a uniform distribution for a particular variable when the real-world distribution is skewed, this can lead to significant disparities in the results. This is particularly noticeable in metrics with higher variability, such as the maximum time a ship spends in the harbor or the maximum waiting time.

Lastly, the simulation's performance can be influenced by the number of runs and the number of ships considered. In this case, a relatively low number of runs and ships were used, which might not be sufficient to approximate the long-term behavior of the system.

Overall, while the simulation provides a useful approximation that is generally reliable for most metrics, as indicated by the relatively low RMSE values and narrow confidence intervals, it may require further calibration or complexity to fully align with real-world data. This could involve adjusting the model's assumptions, incorporating more variables, or using a larger dataset for more robust results.

Sensitivity Analysis

The robustness of our simulation model for harbor operations has been exhaustively assessed in this sensitivity analysis. The study focuses on evaluating how changes in operational parameters could potentially affect key performance metrics.

The bar graph provides a comprehensive visual overview of the model's performance across four distinct scenarios: The baseline scenario serves as a control group (based on table 5.15 real-world data), increased ships to 100, increase of unloading times and increase of arrival times.

In the High Load Scenario, there is a significant uptick in *HARTIME*, *MAXHAR*, *WAITIME*, and *MAXWAIT*. This suggests that the harbor operation system could face bottlenecks and inefficiencies when handling an increased volume of ships. The idle time at the dock, however, decreases, indicating more efficient use of the dock but at the expense of longer waiting and harbor times for the ships.

The Expanded Unloading Interval scenario showcases the sensitivity of both *HARTIME* and *MAXHAR* to changes in unloading times. Extending the un-

loading time interval has a moderate but noticeable impact on these metrics, signaling that unloading operations are a critical component of overall harbor efficiency. Additionally, *WAITIME* and *MAXWAIT* are also affected, though not as significantly as *HARTIME* and *MAXHAR*.

In contrast, the Expanded Arrival Interval scenario shows a slight decrease in *HARTIME* and *MAXHAR*, indicating that spreading out the arrival times of ships can alleviate some of the congestion and result in better harbor management. However, this also results in increased dock idle times, suggesting that there is a trade-off between operational efficiency and resource utilization.

Overall, this sensitivity analysis reveals that the model is particularly sensitive to changes in ship volume, unloading intervals, and arrival intervals. The model performs robustly within specific operational parameters, but deviations from these can lead to either operational bottlenecks or efficiencies. Therefore, careful consideration and potential recalibration of these parameters are essential for optimizing harbor operations.

Recommendations

The current simulation model, while generally robust and reliable for most metrics, could be improved in several ways to better align it with real-world data and scenarios. First, one significant improvement could be the introduction of a weather component into the model. Weather conditions often have a substantial impact on harbor operations, affecting ship speeds, loading and unloading times, and even leading to unexpected delays. The model could incorporate a weather variable with a probabilistic distribution based on historical weather data. This addition would enable the model to account for weather-related disruptions, thereby enhancing its realism and predictive accuracy.

In addition, the current model's predictive capabilities, particularly for metrics that exhibit higher variability like 'Maximum time of a ship in the harbor' and 'Maximum waiting time of a ship,' could be strengthened by utilizing a more extensive and diverse dataset for calibration. Incorporating data from different seasons, weather conditions, and operational challenges could help in capturing the complete range of real-world scenarios. Machine learning techniques such as decision trees or neural networks could be employed to analyze this data. The insights gained could be used to adjust the model's parameters, making the simulation more dynamically responsive to various operational settings.

Finally, the model could benefit from the inclusion of real-world operational inefficiencies, such as equipment breakdowns or labor strikes, which are currently not considered. These inefficiencies can significantly affect harbor operations and should be modeled to capture the full complexity of the system. Algorithms can be designed to introduce these inefficiencies at random intervals based on historical frequency and impact data. By doing so, the model would not only offer a more accurate representation of real-world operations but also provide actionable insights into how these inefficiencies could be mitigated to improve overall harbor efficiency.

Conclusion

The study provides a comprehensive analysis of a harbor operation system through simulation modeling. Real-world data served as the baseline for multiple simulation runs conducted under varying operational parameters, as outlined in Tables 5.15, 5.16, and 5.17. Key metrics such as Average Time a Ship Spends in the Harbor (*HARTIME*), Maximum Time a Ship Spends in the Harbor (*MAXHAR*), Average Waiting Time (*WAITIME*), Maximum Waiting Time (*MAXWAIT*), and Dock Idle Time (*IDLETIME*) were the focus of this analysis.

The report included reliable statistical measures such as: Root Mean Square Error (RMSE) and 95% confidence intervals to evaluate the simulation model's accuracy. Low RMSE values and narrow confidence intervals were observed for most metrics, particularly in the scenario represented by Table 5.16. However, certain metrics like *MAXHAR* and *MAXWAIT* exhibited higher RMSE values and wider confidence intervals. This suggests that the model, while robust for most metrics, may require further calibration for specific variables with higher variability.

Discrepancies between the simulated and real-world data can be attributed to several factors. These include the complexity of real-world harbor operations, assumptions inherent in the model, and limitations in the number of simulation runs and ships. While the model offers valuable approximations and insights, these discrepancies signal the need for further refinements, which could involve adjusting model assumptions, adding more variables, or employing more advanced optimization techniques.

The sensitivity analysis highlighted the model's robustness and adaptability to changes in operational parameters, such as the number of ships, unloading intervals, and arrival intervals. The study identified potential operational bottlenecks and efficiencies under different scenarios, indicating specific areas where the model showed sensitivity.

In summary, the simulation model presents a valuable tool for understanding and optimizing harbor operations. Although the model demonstrates high reliability across several key metrics, areas for future research and calibration have been identified. These findings lay a robust foundation for subsequent studies aimed at achieving more accurate and comprehensive simulation models for harbor operations.

Simulation Code

Import Libraries

Import the necessary libraries.

```
import numpy as np
import pandas as pd
```

Initialize Metrics

Define a function to initialize metrics.

```
def initialize_metrics():
    return {
        'HARTIME': 0,
        'MAXHAR': 0,
        'WAITIME': 0,
        'MAXWAIT': 0,
        'IDLETIME': 0,
        'finish_last_ship': 0,
        'total_ships': 0
    }
```

Run Simulation for 5.15

Define a function to run a single simulation.

```
def run_simulation(n_ships, between_time_range, unload_time_range):
    metrics = initialize_metrics()
    arrive_last = 0
    finish_last = 0
     for i in range(1, n_ships + 1):
        # Step 5: Generate the random pair of integers betweeni and unloadi
        between_i = np.random.randint(between_time_range[0], between_time_range[1] + 1)
        unload_i = np.random.randint(unload_time_range[0], unload_time_range[1] + 1)

        # Step 6: Calculate the time of arrival for Ship i
        arrive_i = arrive_last + between_i

        # Step 7: Calculate the time difference between the arrival of Ship i and the fi
        time_diff = arrive_i - finish_last

        # Step 8 and 9: Calculate idle and wait time
        if time_diff >= 0:
            idle_i = time_diff
            wait_i = 0
        else:
```

```
            idle_i = 0
            wait_i = -time_diff

        # Step 10 and 11: Calculate the start and finish time for unloading Ship i
        start_i = arrive_i + wait_i
        finish_i = start_i + unload_i

        # Step 12: Calculate the time in harbor for Ship i
        harbor_i = wait_i + unload_i

        # Step 13 to 16: Update metrics
        metrics['HARTIME'] += harbor_i
        metrics['MAXHAR'] = max(metrics['MAXHAR'], harbor_i)
        metrics['WAITIME'] += wait_i
        metrics['MAXWAIT'] = max(metrics['MAXWAIT'], wait_i)
        metrics['IDLETIME'] += idle_i
        metrics['finish_last_ship'] = finish_i
        metrics['total_ships'] = i

        # Update last arrival and finish time for the next iteration
        arrive_last = arrive_i
        finish_last = finish_i

    # Step 17: Calculate average and percentage metrics
    metrics['HARTIME'] /= n_ships
    metrics['WAITIME'] /= n_ships
    metrics['IDLETIME'] = (metrics['IDLETIME'] / metrics['finish_last_ship']) * 100

    return metrics
```

Set Parameters and Run Simulation

Set the parameters for the simulation and run it.

```
n_ships = 100  # number of ships
between_time_range_515 = (15, 145)  # time between successive ships in minutes
unload_time_range_515 = (45, 90)  # unloading time per ship in minutes

metrics_list_515 = [run_simulation(n_ships, between_time_range_515, unload_time_range_515
```

Convert Results to DataFrame

Convert the simulation results to a DataFrame for easier viewing.

```
df_515 = pd.DataFrame(metrics_list_515)
df_515['IDLETIME'] = df_515['IDLETIME'] / 100  # Convert to percentage
```

```
f_515 = df_515.drop(columns=['finish_last_ship', 'total_ships'])  # Drop unnecessary colu
df_515.columns = ['Average time of a ship in the harbor (HARTIME)',
                  'Maximum time of a ship in the harbor (MAXHAR)',
                  'Average waiting time of a ship (WAITIME)',
                  'Maximum waiting time of a ship (MAXWAIT)',
                  'Percentage of time dock facilities are idle (IDLETIME)']
df_515.index = [f'Run {i+1}' for i in range(6)]
df_515 = df_515.T  # Transpose for better readability
df_515
```

Run Simulation for 5.16

Define a function to run a single simulation.

```
# Parameters for the second table (5.16)
# For 5.16, the time between successive ships is between 10 and 120 minutes, and the unlo
between_time_range_516 = (10, 120)  # time between successive ships in minutes
unload_time_range_516 = (35, 75)  # unloading time per ship in minutes

# The simulation function `run_simulation` remains the same, we just call it with differe
# Run the simulation 6 times for 5.16 and store the metrics
metrics_list_516 = [run_simulation(n_ships, between_time_range_516, unload_time_range_51
metrics_list_516

metrics_list_516 = simulated_metrics_516
# Create a DataFrame for Scenario 5.16
df_516 = pd.DataFrame(simulated_metrics_516)

# Rename columns for better understanding
df_516 = df_516.rename(columns={
    'HARTIME': 'Average time of a ship in the harbor (HARTIME)',
    'MAXHAR': 'Maximum time of a ship in the harbor (MAXHAR)',
    'WAITIME': 'Average waiting time of a ship (WAITIME)',
    'MAXWAIT': 'Maximum waiting time of a ship (MAXWAIT)',
    'IDLETIME': 'Percentage of time dock facilities are idle (IDLETIME)'
})

# Drop unnecessary columns
df_516 = df_516.drop(columns=['finish_last_ship', 'total_ships'])

# Transpose the DataFrame for better visualization
df_516_transposed = df_516.T

# Rename columns
df_516_transposed.columns = [f'Run {i+1}' for i in range(6)]
```

Metrics	Run 1	Run 2	Run 3	Run 4	Run 5	Run 6
Average time of a ship in the harbor	74.38	80.35	72.4	89.18	82.43	89.16
Maximum time of a ship in the harbor	143	192	176	241	189	239
Average waiting time of a ship	18.37	25.39	18.95	34.01	27.43	33.94
Maximum waiting time of a ship	82	143	122	175	124	171
Percentage of time dock facilities are idle	0.1758	0.173	0.2603	0.1474	0.1868	0.1331

Table 3: Simulation Results for Table 5.17

[width=1.2]ecd26393-b511-4a1c-bad2-ffaba81203d2.png

Figure 1: Comparison between Simulated and Real-World Data of Table 5.15

[width=1.2]d21d7d9f-6762-4599-bf08-bd22fa54431a.png

Figure 2: Comparison of Real-world and Simulated Data for Table 5.16

[width=1.2]124314c9-83e5-4c63-aa4e-29065016f0aa.png

Figure 3: Comparison of Real-world and Simulated Data for Table 5.17

[width=1.2]78cf142f-887f-4c30-b7c0-4e52b35a268f.png

Figure 4: Sensitivity Analysis

[width=1.2] Screenshot 2023-09-19 210343.png

Figure 5: Code Output

```
df_516_transposed
```

Run Simulation for 5.17

Define a function to run a single simulation.

```
# Parameters for the third table (5.17)
# For 5.17, the time between successive ships is between 10 and 120 minutes, and the unl
between_time_range_517 = (10, 120)  # time between successive ships in minutes
unload_time_range_517 = (35, 75)  # unloading time per ship in minutes

# The simulation function ‘run_simulation‘ remains the same, we just call it with differ
# Run the simulation 6 times for 5.17 and store the metrics
metrics_list_517 = [run_simulation(n_ships, between_time_range_517, unload_time_range_51
metrics_list_517

metrics_list_517

# Create a DataFrame
df_517 = pd.DataFrame(data_517)

# Rename the columns for better readability
df_517 = df_517.rename(columns={
    'HARTIME': 'Average time of a ship in the harbor (HARTIME)',
    'MAXHAR': 'Maximum time of a ship in the harbor (MAXHAR)',
    'WAITIME': 'Average waiting time of a ship (WAITIME)',
    'MAXWAIT': 'Maximum waiting time of a ship (MAXWAIT)',
    'IDLETIME': 'Percentage of time dock facilities are idle (IDLETIME)'
})

# Transpose the DataFrame for better visualization
df_517_transposed = df_517.T
df_517_transposed.columns = [f'Run {i+1}' for i in range(6)]  # Rename column
df_517_transposed
```

Statistics for 5.15, 5.16 and 5.17

```
import pandas as pd
import numpy as np
from scipy import stats
import math

# Sample simulated data for 5.15, 5.16, and 5.17 as lists of dictionaries
```

```
metrics_list_515 = [{'HARTIME': 96.53, 'MAXHAR': 213, 'WAITIME': 29.79, 'MAXWAIT': 131,
                     {'HARTIME': 86.55, 'MAXHAR': 169, 'WAITIME': 20.16, 'MAXWAIT': 98, '
                     {'HARTIME': 110.06, 'MAXHAR': 351, 'WAITIME': 42.95, 'MAXWAIT': 275,
                     {'HARTIME': 103.62, 'MAXHAR': 285, 'WAITIME': 36.31, 'MAXWAIT': 216,
                     {'HARTIME': 120.6, 'MAXHAR': 296, 'WAITIME': 52.57, 'MAXWAIT': 227,
                     {'HARTIME': 89.59, 'MAXHAR': 218, 'WAITIME': 23.78, 'MAXWAIT': 151,

metrics_list_516 = [{'HARTIME': 90, 'MAXHAR': 200, 'WAITIME': 25, 'MAXWAIT': 120, 'IDLETI
                     {'HARTIME': 85, 'MAXHAR': 175, 'WAITIME': 20, 'MAXWAIT': 115, 'IDLETI
                     {'HARTIME': 97, 'MAXHAR': 245, 'WAITIME': 29, 'MAXWAIT': 175, 'IDLETI
                     {'HARTIME': 92, 'MAXHAR': 215, 'WAITIME': 27, 'MAXWAIT': 145, 'IDLETI
                     {'HARTIME': 104, 'MAXHAR': 225, 'WAITIME': 34, 'MAXWAIT': 155, 'IDLE
                     {'HARTIME': 87, 'MAXHAR': 205, 'WAITIME': 25, 'MAXWAIT': 125, 'IDLETI

metrics_list_517 = [{'HARTIME': 84.24, 'MAXHAR': 161, 'WAITIME': 15.93, 'MAXWAIT': 78, '
                     {'HARTIME': 81.93, 'MAXHAR': 185, 'WAITIME': 15.42, 'MAXWAIT': 87, '
                     {'HARTIME': 79.86, 'MAXHAR': 200, 'WAITIME': 14.21, 'MAXWAIT': 84, '
                     {'HARTIME': 80.07, 'MAXHAR': 178, 'WAITIME': 14.51, 'MAXWAIT': 80, '
                     {'HARTIME': 88.32, 'MAXHAR': 176, 'WAITIME': 16.55, 'MAXWAIT': 88, '
                     {'HARTIME': 82.46, 'MAXHAR': 190, 'WAITIME': 15.51, 'MAXWAIT': 85, '

# Function to calculate 95% confidence interval and RMSE
def calculate_stats(metrics_list):
    stats_dict = {}
    for metric in ['HARTIME', 'MAXHAR', 'WAITIME', 'MAXWAIT', 'IDLETIME']:
        values = [x[metric] for x in metrics_list]
        mean_val = np.mean(values)
        stderr = stats.sem(values)
        confidence_interval = stats.t.interval(0.95, len(values)-1, loc=mean_val, scale=s
        rmse = math.sqrt(np.mean((np.array(values) - mean_val)**2))
        stats_dict[metric] = {'Lower_Bound_CI': confidence_interval[0], 'Upper_Bound_CI'
    return stats_dict

# Calculate stats for 5.15, 5.16, and 5.17
stats_515 = calculate_stats(metrics_list_515)
stats_516 = calculate_stats(metrics_list_516)
stats_517 = calculate_stats(metrics_list_517)

# Create a DataFrame for better visualization
df_stats_515 = pd.DataFrame(stats_515).T
df_stats_516 = pd.DataFrame(stats_516).T
df_stats_517 = pd.DataFrame(stats_517).T

df_stats_515.index.name = 'Metrics_515'
df_stats_516.index.name = 'Metrics_516'
df_stats_517.index.name = 'Metrics_517'
```

```
# Concatenate them into a single DataFrame
df_stats_all = pd.concat([df_stats_515, df_stats_516, df_stats_517])
df_stats_all



\subsection*{Plotting for Sensitivity Analysis}
# Base Code, same code applied to 5.16 and 5.17 and the output is the figures in the resu
import matplotlib.pyplot as plt
import numpy as np

# Simulated data
simulated_HARTIME = [96.53, 86.55, 110.06, 103.62, 120.6, 89.59]
simulated_MAXHAR = [213, 169, 351, 285, 296, 218]
simulated_WAITIME = [29.79, 20.16, 42.95, 36.31, 52.57, 23.78]
simulated_MAXWAIT = [131, 98, 275, 216, 227, 151]
simulated_IDLETIME = [16.79, 21.5, 19.21, 19.86, 17.5, 19.29]  # Multiplied by 100 for vi

# Real-world data for 5.15
real_HARTIME = [106, 85, 101, 116, 112, 94]
real_MAXHAR = [287, 180, 233, 280, 234, 264]
real_WAITIME = [39, 20, 35, 50, 44, 27]
real_MAXWAIT = [213, 118, 172, 203, 167, 184]
real_IDLETIME = [18, 17, 15, 20, 14, 21]  # Multiplied by 100 for visibility

# Data preparation
labels = ['Run 1', 'Run 2', 'Run 3', 'Run 4', 'Run 5', 'Run 6']
x = np.arange(len(labels))
width = 0.35

fig, axs = plt.subplots(2, 3, figsize=(18, 10))

# HARTIME comparison
axs[0, 0].bar(x - width/2, simulated_HARTIME, width, label='Simulated')
axs[0, 0].bar(x + width/2, real_HARTIME, width, label='Real-world')
axs[0, 0].set_title('HARTIME Comparison')
axs[0, 0].set_xticks(x)
axs[0, 0].set_xticklabels(labels)
axs[0, 0].legend()

# MAXHAR comparison
axs[0, 1].bar(x - width/2, simulated_MAXHAR, width, label='Simulated')
axs[0, 1].bar(x + width/2, real_MAXHAR, width, label='Real-world')
axs[0, 1].set_title('MAXHAR Comparison')
axs[0, 1].set_xticks(x)
```

```
axs[0, 1].set_xticklabels(labels)
axs[0, 1].legend()

# WAITIME comparison
axs[0, 2].bar(x - width/2, simulated_WAITIME, width, label='Simulated')
axs[0, 2].bar(x + width/2, real_WAITIME, width, label='Real-world')
axs[0, 2].set_title('WAITIME Comparison')
axs[0, 2].set_xticks(x)
axs[0, 2].set_xticklabels(labels)
axs[0, 2].legend()

# MAXWAIT comparison
axs[1, 0].bar(x - width/2, simulated_MAXWAIT, width, label='Simulated')
axs[1, 0].bar(x + width/2, real_MAXWAIT, width, label='Real-world')
axs[1, 0].set_title('MAXWAIT Comparison')
axs[1, 0].set_xticks(x)
axs[1, 0].set_xticklabels(labels)
axs[1, 0].legend()

# IDLETIME comparison
axs[1, 1].bar(x - width/2, simulated_IDLETIME, width, label='Simulated')
axs[1, 1].bar(x + width/2, real_IDLETIME, width, label='Real-world')
axs[1, 1].set_title('IDLETIME Comparison (multiplied by 100)')
axs[1, 1].set_xticks(x)
axs[1, 1].set_xticklabels(labels)
axs[1, 1].legend()

# Hide the last subplot for symmetry
axs[1, 2].axis('off')

plt.tight_layout()
plt.show()
```

[width=1.2] Screenshot 2023-09-19 214530.png

Figure 6: Code Output

[width=1.2] Screenshot 2023-09-19 212214.png

Figure 7: Code Output

[width=1.2] Screenshot 2023-09-19 225050.png

Figure 8: Code Output