



THE UNIVERSITY OF  
**SYDNEY**

## **THESIS TOPIC PROPOSAL**

BY TERA NYI (490067334)

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# NOMANCLATURE

$H$	set of time slot $h$
$N$	set of prosumers $n$
$\tau_h$	Time of tariff at time slot $h$
$p_{h,n}^{inf}$	Load demand of prosumer $n$ at time slot $h$
$p_{h,n}^{ev}$	EV (flexible) demand of prosumer $n$ at time slot $h$
$e_n^{ev}$	EV battery state of charge of prosumer $n$
$E_{min}^{ev}$	EV minimum state of charge
$P^{max}$	Transformer Thermal Limit
$p_{h,n}^{max}$	Power limit for prosumer $n$ at time slot $h$

# ABSTRACT

This is the abstract.

# **CHAPTER 1    INTRODUCTION**

## **1.1   IDJKSF**

### **1.1.1   LSDNF**

sldfn

## **1.2 SJDNF**



# CHAPTER 2 FORMULATION

## 2.1 LOWER LEVEL

$$\begin{aligned}
 & \underset{p_h^{ev}}{\text{MIN}} \quad \sum_{h \in H} \tau_h (p_h^{inf} + p_h^{ev}) \\
 & \text{subject to} \\
 & \quad E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \leq 0 \\
 & \quad p_h^{inf} + p_h^{ev} - p_h^{max} \leq 0 \quad \forall h \in H
 \end{aligned}$$

Lagrange:

$$\begin{aligned}
 \mathcal{L}(p_h^{ev}, \lambda) = & \sum_{h \in H} \tau_h (p_h^{inf} + p_h^{ev}) \\
 & + \lambda^1 \left( E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \right) \\
 & + \sum_{h \in H} \lambda_h^2 (p_h^{inf} + p_h^{ev} - p_h^{max})
 \end{aligned}$$

$$\text{Stationarity: } \frac{\partial \mathcal{L}}{\partial p_h^{ev}} = \tau_h - \lambda^1 + \lambda_h^2 = 0 \quad \forall h \in H$$

$$\begin{aligned}
 \text{Primal feasibility: } & E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \leq 0 \\
 & p_h^{inf} + p_h^{ev} - p_h^{max} \leq 0 \quad \forall h \in H
 \end{aligned}$$

$$\begin{aligned}
 \text{Dual feasibility: } & \lambda^1 \geq 0 \\
 & \lambda_h^2 \geq 0 \quad \forall h \in H
 \end{aligned}$$

$$\begin{aligned}
 \text{Complementary slackness: } & \lambda^1 \left( E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \right) = 0 \\
 & \lambda_h^2 (p_h^{inf} + p_h^{ev} - p_h^{max}) = 0 \quad \forall h \in H
 \end{aligned}$$

## 2.2 BI-LEVEL REFORMULATION WITH KKT

$$\max_{p_{h,n}^{max}} p_{h,n}^{max}$$

subject to

$$\sum_{n \in N} p_{h,n}^{max} - P^{max} \leq 0 \quad \forall h \in H$$

**(Stationarity)**

$$\tau_h - \lambda_n^1 + \lambda_{h,n}^2 = 0 \quad \forall h \in H, \forall n \in N$$

**(Primal Feasibility)**

$$E_{min}^{ev} - e_n^{ev} - \sum_{h \in H} p_{h,n}^{ev} \leq 0 \quad \forall n \in N$$

$$p_{h,n}^{inf} + p_{h,n}^{ev} - p_{h,n}^{max} \leq 0 \quad \forall h \in H, \forall n \in N$$

**(Dual Feasibility)**

$$\lambda_n^1 \geq 0 \quad \forall n \in N$$

$$\lambda_{h,n}^2 \geq 0 \quad \forall h \in H, \forall n \in N$$

**(Complementary Slackness)**

$$\lambda_n^1 \left( E_{min}^{ev} - e_n^{ev} - \sum_{h \in H} p_{h,n}^{ev} \right) = 0 \quad \forall n \in N$$

$$\lambda_{h,n}^2 (p_{h,n}^{inf} + p_{h,n}^{ev} - p_{h,n}^{max}) = 0 \quad \forall h \in H, \forall n \in N$$

**(Big M reformulation for Complementary Slackness)**

$$\lambda_n^1 \leq M z_n^1 \quad \forall n \in N$$

$$E_{min}^{ev} - e_n^{ev} - \sum_{h \in H} p_{h,n}^{ev} \leq M(1 - z_n^1) \quad \forall n \in N$$

$$\lambda_{h,n}^2 \leq M z_{h,n}^2 \quad \forall h \in H, \forall n \in N$$

$$p_{h,n}^{inf} + p_{h,n}^{ev} - p_{h,n}^{max} \leq M(1 - z_{h,n}^2) \quad \forall h \in H, \forall n \in N$$

$$z_n^1 \in \{0, 1\}, \quad z_{h,n}^2 \in \{0, 1\} \quad \forall h \in H, \forall n \in N$$