



THE UNIVERSITY OF
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THESIS TOPIC PROPOSAL

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CONTENTS

| | | |
|----------|---|----------|
| 1 | Introduction | 1 |
| 1.1 | idjksf | 1 |
| 1.1.1 | lsdnf | 1 |
| 1.2 | sjdnf | 2 |
| 2 | Formulation | 3 |
| 2.1 | Lower Level | 3 |
| 2.2 | Bi-level Reformulation with KKT | 4 |

LIST OF TABLES

LIST OF FIGURES

NOMANCLATURE

| | |
|-----------------|---|
| H | set of time slot h |
| N | set of prosumers n |
| τ_h | Time of tariff at time slot h |
| $p_{h,n}^{inf}$ | Load demand of prosumer n at time slot h |
| $p_{h,n}^{ev}$ | EV (flexible) demand of prosumer n at time slot h |
| e_n^{ev} | EV battery state of charge of prosumer n |
| E_{min}^{ev} | EV minimum state of charge |
| P^{max} | Transformer Thermal Limit |
| $p_{h,n}^{max}$ | Power limit for prosumer n at time slot h |

ABSTRACT

This is the abstract.

CHAPTER 1 INTRODUCTION

1.1 IDJKSF

1.1.1 LSDNF

sldfn

1.2 SJDNF

CHAPTER 2 FORMULATION

2.1 LOWER LEVEL

$$\begin{aligned}
 & \underset{p_h^{ev}}{\text{MIN}} \quad \sum_{h \in H} \tau_h (p_h^{inf} + p_h^{ev}) \\
 & \text{subject to} \\
 & \quad E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \leq 0 \\
 & \quad p_h^{inf} + p_h^{ev} - p_h^{max} \leq 0 \quad \forall h \in H
 \end{aligned}$$

Lagrange:

$$\begin{aligned}
 \mathcal{L}(p_h^{ev}, \lambda) = & \sum_{h \in H} \tau_h (p_h^{inf} + p_h^{ev}) \\
 & + \lambda^1 \left(E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \right) \\
 & + \sum_{h \in H} \lambda_h^2 (p_h^{inf} + p_h^{ev} - p_h^{max})
 \end{aligned}$$

$$\text{Stationarity: } \frac{\partial \mathcal{L}}{\partial p_h^{ev}} = \tau_h - \lambda^1 + \lambda_h^2 = 0 \quad \forall h \in H$$

$$\begin{aligned}
 \text{Primal feasibility: } & E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \leq 0 \\
 & p_h^{inf} + p_h^{ev} - p_h^{max} \leq 0 \quad \forall h \in H
 \end{aligned}$$

$$\begin{aligned}
 \text{Dual feasibility: } & \lambda^1 \geq 0 \\
 & \lambda_h^2 \geq 0 \quad \forall h \in H
 \end{aligned}$$

$$\begin{aligned}
 \text{Complementary slackness: } & \lambda^1 \left(E_{min}^{ev} - e^{ev} - \sum_{h \in H} p_h^{ev} \right) = 0 \\
 & \lambda_h^2 (p_h^{inf} + p_h^{ev} - p_h^{max}) = 0 \quad \forall h \in H
 \end{aligned}$$

2.2 BI-LEVEL REFORMULATION WITH KKT

$$\max_{p_{h,n}^{max}} p_{h,n}^{max}$$

subject to

$$\sum_{n \in N} p_{h,n}^{max} - P^{max} \leq 0 \quad \forall h \in H$$

(Stationarity)

$$\tau_h - \lambda_n^1 + \lambda_{h,n}^2 = 0 \quad \forall h \in H, \forall n \in N$$

(Primal Feasibility)

$$E_{min}^{ev} - e_n^{ev} - \sum_{h \in H} p_{h,n}^{ev} \leq 0 \quad \forall n \in N$$

$$p_{h,n}^{inf} + p_{h,n}^{ev} - p_{h,n}^{max} \leq 0 \quad \forall h \in H, \forall n \in N$$

(Dual Feasibility)

$$\lambda_n^1 \geq 0 \quad \forall n \in N$$

$$\lambda_{h,n}^2 \geq 0 \quad \forall h \in H, \forall n \in N$$

(Complementary Slackness)

$$\lambda_n^1 \left(E_{min}^{ev} - e_n^{ev} - \sum_{h \in H} p_{h,n}^{ev} \right) = 0 \quad \forall n \in N$$

$$\lambda_{h,n}^2 (p_{h,n}^{inf} + p_{h,n}^{ev} - p_{h,n}^{max}) = 0 \quad \forall h \in H, \forall n \in N$$

(Big M reformulation for Complementary Slackness)

$$\lambda_n^1 \leq M z_n^1 \quad \forall n \in N$$

$$E_{min}^{ev} - e_n^{ev} - \sum_{h \in H} p_{h,n}^{ev} \leq M(1 - z_n^1) \quad \forall n \in N$$

$$\lambda_{h,n}^2 \leq M z_{h,n}^2 \quad \forall h \in H, \forall n \in N$$

$$p_{h,n}^{inf} + p_{h,n}^{ev} - p_{h,n}^{max} \leq M(1 - z_{h,n}^2) \quad \forall h \in H, \forall n \in N$$

$$z_n^1 \in \{0, 1\}, \quad z_{h,n}^2 \in \{0, 1\} \quad \forall h \in H, \forall n \in N$$