

a) i) $FGPA = 2.442 + 0.063 SATV + e$

$b = 0.063$, $SE(b) = 0.028$, $p\text{-value} = 0.023$

ii) As $n = 609$ is large, $t(n-k) = t(609-2) = t(607)$ distribution is very close to standard normal dist.

95% conf. interval:

$$b \pm 2 \times SE(b) = 0.063 \pm 2 \times 0.028 = (0.007, 0.119)$$

\downarrow
1.96

b) i) $FGPA = 1.557 + 0.014 SATV + 0.173 SATM + 0.200 FEM + e$

$b = 0.014$, $SE(b) = 0.028$, $p\text{-value} = 0.612$

ii) $b \pm 2 \times SE(b) = 0.014 \pm 2 \times 0.028 = (-0.042, 0.070)$

includes zero
→ in line with

- c) Total effect of SATV on FGPA = significant
 ↳ ind. indirect effects due to SATM and gender
- partial effect of SATV on FGPA = not significant
 ↳ after correction for indirect effects of SATM and gender
- difference → suggests correlation between SATV, SATM, gender

	FGPA	SATV	SATM	FEM
FGPA	1	0.092	0.195	0.176
SATV		1	0.288	0.034
SATM			1	-0.163
FEM				1

- ↳ if exclude SATM from the model FGPA
 → effect SATM is absorbed by SATV

d) i) restricted model under H_0 is:

$$FGPA = \beta_1 + \beta_2 SATM + \beta_3 FEM + \varepsilon$$

OLS gives: $SSR_0 = e_0' e_0 = 118.151224$

$$R_0^2 = 0.082575$$

OLS unrestricted model part (b) gives:

$$SSR_1 = e_1' e_1 = 118.101025$$

$$R_1^2 = 0.082965$$

$$g=1$$

$$n=609$$

$$k=4$$

$$F(g, n-k) \Rightarrow F(1, 605) \quad 5\% \text{ C.V.} = 3.9$$

$$F = \frac{(e_0' e_0 - e_1' e_1) / g}{e_1' e_1 / (n-k)} = \frac{(118.151224 - 118.101025) / 1}{118.101025 / 605} = 0.257 < 3.9$$

$$F = \frac{(R_1^2 - R_0^2) / g}{(1 - R_1^2) / (n-k)} = \frac{(0.082965 - 0.082575) / 1}{(1 - 0.082965) / 605} = 0.257 < 3.9$$

$\rightarrow H_0$ not rejected

d) ii) t -value for SATV in (b-i) = $0.507105 (= b/SE(b))$

$$t^2 = 0.257 = F \text{ (d-i)}$$