

Test Exercise 2 – GPA

(a)

```
# import packages for the analysis
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
%matplotlib inline

import statsmodels.formula.api as smf
```

```
GPA = pd.read_table('TestExer2-GPA.txt')
```

```
# create a fitted model
lm = smf.ols(formula='FGPA ~ SATV', data=GPA).fit()

lm.summary()
```

OLS Regression Results

| | | | |
|--------------------------|------------------|----------------------------|---------|
| Dep. Variable: | FGPA | R-squared: | 0.008 |
| Model: | OLS | Adj. R-squared: | 0.007 |
| Method: | Least Squares | F-statistic: | 5.201 |
| Date: | Sun, 22 Sep 2019 | Prob (F-statistic): | 0.0229 |
| Time: | 10:57:44 | Log-Likelihood: | -388.44 |
| No. Observations: | 609 | AIC: | 780.9 |
| Df Residuals: | 607 | BIC: | 789.7 |
| Df Model: | 1 | | |
| Covariance Type: | nonrobust | | |

| | coef | std err | t | P> t | [0.025 | 0.975] |
|------------------|--------|---------|--------|-------|--------|--------|
| Intercept | 2.4417 | 0.155 | 15.747 | 0.000 | 2.137 | 2.746 |
| SATV | 0.0631 | 0.028 | 2.280 | 0.023 | 0.009 | 0.117 |

- (i) So for the model $FGPA = a + b \cdot SATV$,
 $b = 0.063$, standard error of b is 0.028 , P-value is 0.023
- (ii) 95% CI of SATV's increasing by 1 on FGPA is $[0.009, 0.117]$

(b)

```
# create a fitted model
mlm = smf.ols(formula='FGPA ~ SATM+SATV+FEM', data=GPA).fit()

# print the coefficients
mlm.summary()
```

| OLS Regression Results | | | | | | |
|------------------------|------------------|---------------------|----------|-------|--------|--------|
| Dep. Variable: | FGPA | R-squared: | 0.083 | | | |
| Model: | OLS | Adj. R-squared: | 0.078 | | | |
| Method: | Least Squares | F-statistic: | 18.24 | | | |
| Date: | Sun, 22 Sep 2019 | Prob (F-statistic): | 2.41e-11 | | | |
| Time: | 12:04:45 | Log-Likelihood: | -364.67 | | | |
| No. Observations: | 609 | AIC: | 737.3 | | | |
| Df Residuals: | 605 | BIC: | 755.0 | | | |
| Df Model: | 3 | | | | | |
| Covariance Type: | nonrobust | | | | | |
| | coef | std err | t | P> t | [0.025 | 0.975] |
| Intercept | 1.5570 | 0.216 | 7.205 | 0.000 | 1.133 | 1.981 |
| SATM | 0.1727 | 0.032 | 5.410 | 0.000 | 0.110 | 0.235 |
| SATV | 0.0142 | 0.028 | 0.507 | 0.612 | -0.041 | 0.069 |
| FEM | 0.2003 | 0.037 | 5.358 | 0.000 | 0.127 | 0.274 |

(i) So for the model $FGPA = a + b_1 \cdot SATM + b_2 \cdot SATV + b_3 \cdot FEM$,

$b_2 = 0.014$, standard error of b_2 is 0.028, P-value is 0.612

(ii) 95% CI of SATV's increasing by 1 on FGPA is $[-0.041, 0.069]$

(c) The correlation Matrix:

```
GPA.iloc[:,1:].corr()
```

| | FGPA | SATM | SATV | FEM |
|------|----------|-----------|----------|-----------|
| FGPA | 1.000000 | 0.195040 | 0.092167 | 0.176491 |
| SATM | 0.195040 | 1.000000 | 0.287801 | -0.162680 |
| SATV | 0.092167 | 0.287801 | 1.000000 | 0.033577 |
| FEM | 0.176491 | -0.162680 | 0.033577 | 1.000000 |

It shows that the correlation between SATV and FGPA is less than 10% and much smaller than the other two pairs. So when stronger predictors introduced into the model, the influence of SATV will become insignificant.

(d)

$H_0: b_2 = 0$

$H_1: b_2 \neq 0$

Analyze the restricted model:

```
# create a restricted fitted model without SATV
rmlm = smf.ols(formula='FGPA ~ SATM+FEM', data=GPA).fit()

R0_2 = rmlm.rsquared
R1_2 = mlm.rsquared
F = (R1_2 - R0_2) * 605 / (1 - R1_2)
F
```

0.25715514284401925

We get $F = 0.257155 < 3.9$. So, the effect of SATV on FGPA is insignificant.

As we know from (b) that t^2 of b_2 is $0.507105^2 = 0.257155$

Clearly, $F = t^2$