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General Physics I (151)

**Discussion Questions #1**  
**Measurement and Motion**

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**1. Dimensional Analysis & Similarity**

- a) One end of a spring is attached to a sturdy block, and a mass  $m$  is attached to the other end of the spring. Let  $\Delta x$  = the displacement of the mass from its rest position.

If the mass is displaced, the spring exerts a force on the mass, which makes it oscillate back and forth. The acceleration of the mass is given by the formula

$$a = \frac{k}{m} \Delta x$$

where  $k$  is called the spring constant. What are the dimensions of  $k$ ?

- b) Two masses  $M$  and  $m$  are separated by a distance  $r$ . The magnitude of the gravitational force between them is given by

$$F_{\text{grav}} = G \frac{Mm}{r^2}$$

where  $G$  is Newton's constant. Suppose  $M$  is changed by a factor  $A$  and  $r$  is changed by a factor  $B$ , that is,  $M \rightarrow AM$ ,  $r \rightarrow Br$ . Then the gravitational force between the masses changes,  $F_{\text{grav}} \rightarrow CF_{\text{grav}}$ . Find  $C$  in terms of  $A$  and  $B$ .

**2. Colliding Particles with Constant Velocities in One Dimension**

Initially, at time  $t = 0$ , two marbles A and B are separated by a distance  $L$  and are moving towards each other at constant speeds  $v_{A0}$  and  $v_{B0}$  respectively. Let's take A moving to the right, B to the left. You can take the position of A to be  $x_A = 0$  at  $t = 0$ .

- a) In this part of the problem, assume that you are given  $L$ ,  $v_{A0}$  and  $v_{B0}$  (initial data).
- i) By  $x_A(t)$ , we mean the position of A as a function of time. Write out an expression for  $x_A(t)$  in terms of the initial data.

ii) Write out an expression for  $x_B(t)$  in terms of initial data.

iii) Let  $t_{\text{hit}}$  = the amount of time until the marbles collide. Find  $t_{\text{hit}}$  in terms of the initial data.

iv) How far has A traveled?

b) In this part of the problem, assume that you know  $v_{A0}$ ,  $v_{B0}$  and  $t_{\text{hit}}$ .

Find the initial separation  $L$ .

### 3. Estimation

Estimate the number of drops of water in the ocean. Here “drop” is a precise volume measure, where there would be a fixed number of metric drops in a milliliter. Since this is an estimate, you can make fairly drastic approximations about the shape of the ocean bed, for example, that the ocean has a constant depth  $D$ .

Suggestion: First give your answer in terms of  $D$ , and other parameters you use in making the estimate. Then substitute in numbers as a last step. State your approximations clearly!