#### \*\*You may detach this page from the test booklet\*\*

#### PLEASE READ THESE INSTRUCTIONS CAREFULLY

- Allowed: Calculator and an 8.5"×11" reference sheet with handwritten notes on both sides
- **Not Allowed:** phones, laptops, tablets, headphones, music players, cameras, anything with internet connectivity. Put these away while the exam is in progress.

#### • PRINT YOUR NAME AND SPIRE ID ON THE EXAM BOOKLET AND ANSWER SHEET

### •>>> USE #2 PENCIL TO FILL IN THE CIRCLES ON ANSWER SHEET WITH YOUR NAME

#### (last name first) and SPIRE ID. <<<

- Please go to the restroom before the midterm starts.
- Unless friction or air resistance are mentioned, you can assume that they are negligible.
- Use #2 Pencil to fill the circles with your answers in spaces 1 through 27. Each question is worth 1 point. Only bubble in one circle per answer, or you may not receive credit. Erase pencil marks cleanly.
- When done, hand in ANSWER SHEET, EXAM BOOKLET, and show your UMass ID.
- There are 27 questions but the exam will be graded out of 25. This means you can get one question incorrect and still get a perfect score.

#### Math

# $\frac{d}{dx}(x^n) = nx^{n-1}$ $\int x^n dx = \frac{x^{n+1}}{n+1} + C$ $ax^2 + bx + c = 0$ $\Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

#### Angular Motion

$$a = v^{2}/r = \omega^{2}r$$

$$v = \omega r$$

$$\omega = 2\pi/T$$

$$L = r\theta; v = r\omega; a = r\alpha$$

$$\theta(t) = \theta_{0} + \omega_{0}t + \frac{1}{2}\alpha t^{2}$$

$$\omega(t) = \omega_{0} + \alpha t$$

$$\omega^{2} = \omega_{0}^{2} + 2\alpha\Delta\theta$$

#### 1D Kinematics

$$x(t) = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$v(t) = v_0 + a t$$

$$\Delta x = \frac{v_1^2 - v_0^2}{2a}$$

#### Projectile Motion

Range: 
$$D = \frac{v_0^2 \sin(2\theta)}{g}$$
  
[Same initial/final height only]

#### Dynamics

$$\sum_{\vec{F}_{AB}} \vec{F}_{ext} = m\vec{a}$$

$$\vec{F}_{AB} = -\vec{F}_{BA}$$

$$\vec{F}_{c} = \frac{mv^{2}}{r}(toward - \hat{r})$$

$$\vec{F}_{spring} = -k\Delta \vec{x}$$

#### Friction

$$\begin{aligned} f_k &= \mu_k N \\ f_s &\leq \mu_S N \end{aligned}$$

#### Rotational Dynamics

$$\vec{x}_{CM} = \sum m_i \vec{r_i} / \sum m_i$$

$$I = \sum m_i r_i^2$$

$$I_{parallel} = I_{CM} + Md^2$$

$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$|\vec{\tau}| = |\vec{r}| |\vec{F}| \sin \phi$$

$$\sum \vec{\tau} = I\alpha$$

$$v_{CM} = R\omega \text{ (rolling without slipping)}$$

$$\vec{L} = \vec{r} \times \vec{p}$$

## $\vec{L} = I\omega$ (fixed axis)

# **Conversion Factors and Constants**

1 minute = 60s 1 hour = 3600s 1 mile = 1.60934 km 1 mile = 5280 feet 1 foot = 0.3048 meters 1 foot = 12 inches 1 inch = 2.54 cm  $q = 9.8 \text{ m/s}^2$ 

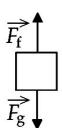
$$\begin{array}{c} \text{Hypotenuse} \\ \theta \\ \text{Adjacent} \\ \end{array} \text{Opposite} \quad \begin{array}{c} \sin \theta = \frac{\text{opposite}}{\text{hypotenuse}} \\ \cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}} \\ \tan \theta = \frac{\text{opposite}}{\text{adjacent}} \end{array}$$

Page 1 not included because it contained types of questions that won't be on this test.

(Circular kinematics was covered in MT1)

5) Which one of the following free-body diagrams best represents the free-body diagram, with correct relative force magnitudes, of a person in an elevator that is traveling upward but is gradually slowing down at a rate of 9 m/s<sup>2</sup>?  $\vec{F}_f$  is the force of the floor on the person and  $\vec{F}_g$  is the force of gravity on the person.

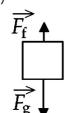
A)



B)



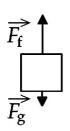
C)



D)



E)



acceleration of particle A is 8.5 time	orm circular motion about a common center. The less that of particle B. The period of particle B is 2.0 ratio of the radius of the motion of particle A to that  Circular kinematics questionwon't be on the test	6)
,	ve at a constant speed.	7)
	forces. One of the forces is 10.0 N acting toward the s is the other force if the acceleration of the object is	8)

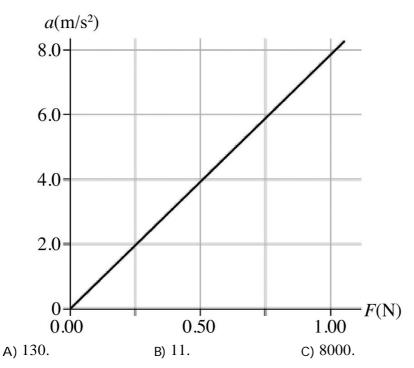
D) 3.0 N west E) 9.0 N west 9) The figure shows two forces, each of magnitude 4.6 N, acting on an object. The angle between these forces is 40°, and they make equal angles above and below the horizontal. What third force will cause the object to be in equilibrium (acceleration equals zero)?



- A) 8.6 N pointing to the right
- C) 3.5 N pointing to the right

- B) 7.0 N pointing to the right
- D) 4.3 N pointing to the right
- 10) The figure shows a graph of the acceleration of an object as a function of the net force acting on it. The mass of this object, in grams, is closest to





D) 89.

11) Two forces act on a 55-kg object. One force has magnitude 65 N directed 59° clockwise from the positive <i>x</i> -axis, and the other has a magnitude 35 N at 32° clockwise from the positive <i>y</i> -axis. What is the magnitude of this object's acceleration?					11)
A) 1.3 m/s <sup>2</sup>	B) 1.7 m/s <sup>2</sup>	=	m/s <sup>2</sup>	D) 1.5 m/s <sup>2</sup>	
	zontal force is applie	ed to it. The block	k and table are	then set up on the	12)
	cceleration due to g	•			
A) $1.8 \text{ m/s}^2$	B) $2.0 \text{ m/s}^2$	C) $2.2 \text{ m/s}^2$	D) 2.3 m/s <sup>2</sup>	E) $1.6 \text{ m/s}^2$	
13) A 10,000-kg rocke	et blasts off from ea	rth with a unifor	m unward acce	leration of 2 00	13)
	air resistance. The u				13)
A) 20,000 N.	в) 118,000 1	N. C) 98	0,000 N.	D) 78,000 N.	
14) A 60.0-kg person downward but slo	rides in elevator wh wing down at a rate	_		_	14)

A) 708 N. B) 349 N. C) 589 N. D) 120 N. E) 469 N.

15) You push downward on a box at an angle 25° below the horizontal with a force of 750 N. If the box is on a flat horizontal surface for which the coefficient of static friction with the box is 0.76, what is the mass of the heaviest box you will be able to move?

- A) 68 kg
- B) 54 kg
- c) 82 kg
- D) 59 kg
- 16) A 6.0 kg box slides down an inclined plane that makes an angle of 39° with the horizontal. If the coefficient of kinetic friction is 0.19, at what rate does the box accelerate down the slope?

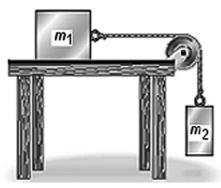
16)

- A)  $5.5 \text{ m/s}^2$
- B)  $6.2 \text{ m/s}^2$
- c)  $5.2 \text{ m/s}^2$
- D)  $4.7 \text{ m/s}^2$
- 17) An object weighing 4.00 N falls from rest subject to a frictional drag force given by  $F_{\text{drag}} = bv^2$ , where v is the speed of the object and  $b = 3.00 \text{ N} \cdot \text{s}^2/\text{m}^2$ . What terminal speed will this object approach?

17)

- A) 2.25 m/s
- B) 0.75 m/s
- C) 1.15 m/s
- D) 1.78 m/s
- E) 3.42 m/s
- 18) Two objects having masses  $m_1$  and  $m_2$  are connected to each other as shown in the figure and are released from rest. There is no friction on the table surface or in the pulley. The masses of the pulley and the string connecting the objects are completely negligible. What must be true about the tension T in the string just after the objects are released?

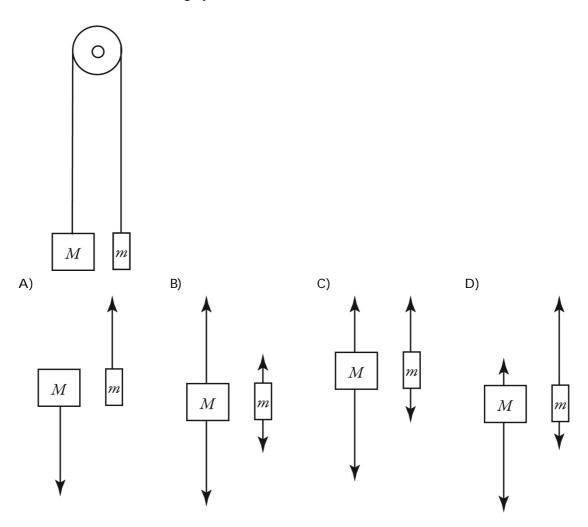
18)



- A) T > m2g
- B)  $T = m_1 g$
- C) T < m2g
- D)  $T > m_1 g$  E)  $T = m_2 g$

pulley of negligible mass, as shown in the figure. When released, the system accelerates. Friction is negligible. Which figure below gives the correct free-body force diagrams for

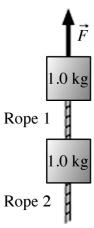
the two masses in the moving system?



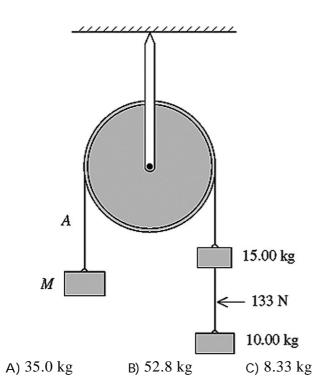
21)

- 20) The International Space Station has a mass of  $1.8 \times 10^5$  kg. A 70.0-kg astronaut inside the station pushes off one wall of the station so she accelerates at 1.50 m/s<sup>2</sup>. What is the magnitude of the acceleration of the space station as the astronaut is pushing off the wall? Give your answer relative to an observer who is space walking and therefore does not accelerate with the space station due to the push.
  - A) zero
  - B)  $4.7 \times 10^{-4} \text{ m/s}^2$
  - c)  $3.9 \times 10^{-3} \text{ m/s}^2$
  - D)  $5.8 \times 10^{-4} \text{ m/s}^2$
  - E) 1.50 m/s<sup>2</sup>

21) The figure shows two 1.0 kg-blocks connected by a rope. A second rope hangs beneath the lower block. Both ropes have a mass of 250 g. The entire assembly is accelerated upward at 2.3 m/s<sup>2</sup> by force  $\vec{F}$ . What is the tension at the top end of rope 1?

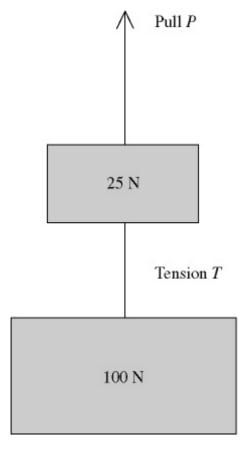


- A) 15 N
- B) 3.5 N
- c) 18 N
- D) 2.9 N



D) 95.0 kg

E) 33.9 kg



- A) 125 N.
- B) 1225 N.
- c) 245 N.
- D) 25 N.
- E) 187.5 N.

24)

- 24) A string is attached to the rear-view mirror of a car. A ball is hanging at the other end of the string. The car is driving around in a circle, at a constant speed. Which of the following lists gives all of the forces directly acting on the ball?
  - A) tension
  - B) tension, gravity, the centripetal force, and friction
  - C) tension and gravity
  - D) tension, gravity, and the centripetal force

25) A 23 kg mass is connected to a nail on a frictionless table by a massless string 1.3 m long. There is no appreciable friction between the nail and the string. If the tension in the string is 51 N while the mass moves in a uniform circle on the table, how long does it take for the mass to make one complete revolution?					25)	
	A) 4.5 s	B) 5.2 s		4.8 s	D) 3.8 s	
26)	A car travels at a stead minimum coefficient of the car to travel at this	of static friction b	oetween the roa			26)
		3) 1.23	c) 0.952	D) 0.736	E) 0.662	
	,	,		-,	<del>-</del> ,	
27)	A new roller coaster coupside down. If the rattraverse the loop so the	dius of the loop	is 13.2 m, with	what minimum sp	eed must the car	27)

c) 11.4 m/s

D) 14.9 m/s

Assume the rider is not strapped to the car.

A) 12.5 m/s

B) 10.1 m/s