General Physics II (152)

# Discussion Questions #3 Electric Force and Field

## 1. Varying $q_1$ while Keeping $q_1 + q_2$ Constant

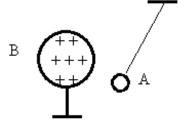
Case I: Distribute two positive charges  $q_1$  and  $q_2$ , with  $q_1 > q_2$ , on two identical conducting spheres. Each sphere has a radius R. The separation between centers of the two spheres is r, where r >> R. Denote the magnitude of the Case I repulsive force between the two spheres by  $F_1$ .

Case II: Now, let the same two charged spheres from Case I touch each other. While they are in contact, there is a charge flow. After an electric equilibrium is established, separate the two centers again by the same distance r. The magnitude of the force is now  $F_{\rm II}$ . How do  $F_{\rm I}$  and  $F_{\rm II}$  compare to each other?

Hint: Express the magnitude of the force between the two charges as  $F = \frac{kq_1(q_0 - q_1)}{r^2}$ , where  $q_0 = q_1 + q_2 = \text{constant}$ . Then, inspect how F varies as a function of  $q_1$ .

#### 2. Electrostatic Attraction

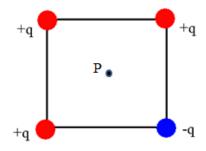
a) Two conducting spheres A and B are shown. Sphere B is positively charged. Sphere A, suspended by a string from above, is attracted to B. The setup is in equilibrium. What is the sign of the net charge on A?



b) Consider a new situation: where  $q_A$  is *negative* and  $q_B >> |q_A|$ . Now A swings upward and touches B. Do you expect that A will remain in contact with B?

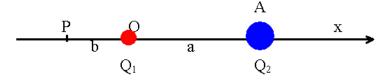
## 3. Electric Field at Square Center Due to Corner Charges

The diagram shows a square with charges as marked located at the vertices. What is the direction of the electric field at P, the center of the square? Assume magnitudes of all charges are the same.



#### 4. Electric Field Due to Two Unequal Point Charges

Consider the setup below, where  $Q_1 = 1 \mu C$  and  $Q_2 = 4 \mu C$  are located at O and A respectively, with OA = a = 1 m. Consider an arbitrary point P, to the left of O where OP = b. Denote the magnitudes of fields at P contributed by  $Q_1$  and  $Q_2$  as  $E_1$  and  $E_2$  respectively. Which is greater between  $E_1$  and  $E_2$ ? Could they be equal?



## 5. Electric Field Due to Point Charges in a Square

- a) What is the direction of the electric field at A due to the positive charges at the three corners? Assume the magnitudes of all charges are *q*.
- b) Show the magnitude of the electric field at A due to the three positive charges is  $E = \left(\sqrt{2} + \frac{1}{2}\right) \frac{kq}{c^2}$ , where c is the side of the square.

