

CMOS (P/N)MOS logic units. (delay/static power)

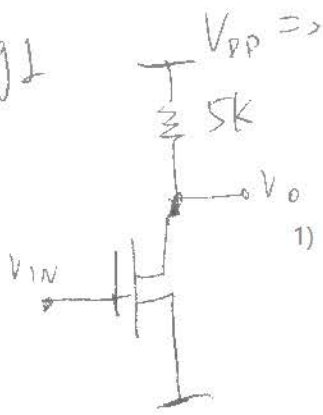
No RLC circuits

MOS + and/OR diode circuits

+ And/OR OpAmp.

+ And/OR $\begin{cases} RL \Rightarrow \text{HW11 Problem 4} \\ RC \Rightarrow \text{Lecture 3.5 (12-04) Eq. 2} \end{cases}$ see examples

e.g1



SR model $R_{on} = 500\Omega$ $V_t = 1V$

$V_{in} = 0$ and $3V$. find V_o and power

1) $V_{in} = 0$

$V_{GS} = 0$



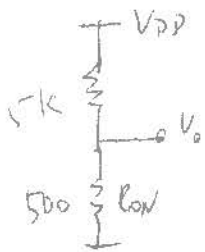
$$V_o = V_{DD} = 3V$$

I

$$P = 0$$

2) $V_{in} = 3V$

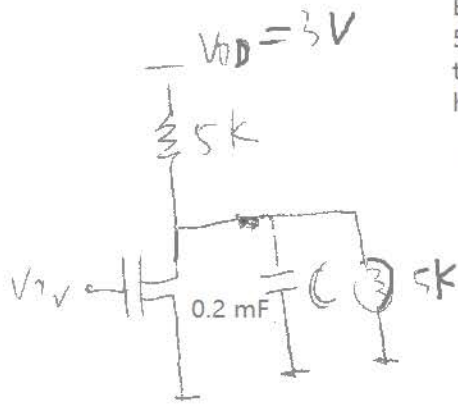
$$V_{GS} = V_{in} - 0 = 3V = V_{th}$$



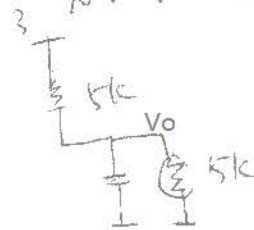
$$V_i = \frac{500}{5k + 500} \cdot 3 = \frac{1}{11} \cdot 3 = 0.273 (V)$$

$$P = \frac{V_{DD}^2}{5k + 500} = \frac{9}{5.5k} = 1.64 mW$$

Extension: A capacitor and lamp are connected. The lamp has internal resistance of $5K$ and requires a voltage $> 1V$ to light up. Calculate how long it takes for the lamp to change state when the V_{in} changes from $0V$ to $3V$. (Suppose before $t = 0$, V_{in} has been $0V$ for a long time).

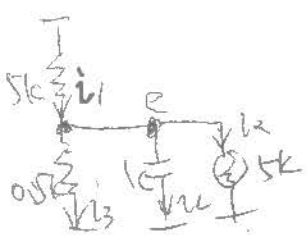


1) At $t < 0$: $V_{in} = 0$; $V_{GS} = 0$; transistor "OFF"



$$V_{(0+)} = \frac{5}{5+5} \times 3 = 1.5 (V)$$

2) At $t > 0$, $V_{in} = 3V$; $V_{GS} = 3V$; transistor "ON" -- $R_{on} = 0.5K$



$$i_1 - i_2 - i_c - i_3 = 0$$

$$\frac{3-e}{5k} - \frac{e}{5k} - 0.2m \frac{de}{dt} - \frac{e}{0.5k} = 0 \quad e = \frac{1}{4} + 1.25e^{-12t}$$

$$3 - e - e - \frac{de}{dt} - 10e = 0$$

$$\frac{de}{dt} + 12e = 3$$

$$e = \frac{1}{4} + k e^{-12t}$$

Since $V(0+) = 1.5$, we get $K = 1.25$

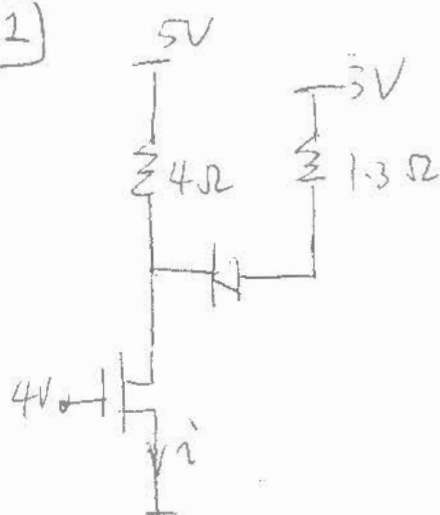
The boundary for lamp state change is $e = 1$

$$e = \frac{1}{4} + 1.25e^{-12t} = 1$$

$$e^{-12t} = \frac{1.75}{1.25} \quad 12t = 0.51$$

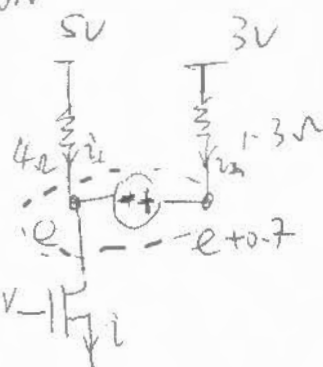
$$t = 0.043s$$

(eg 1)



$V_T = 1V$, $k = \frac{1}{8} A/V^2$, $V_D = 0.7V$
find i .

Assume $D_1 = \text{"ON"}$



MOS: $V_{GS} = 4 - v = 4 - 0V$

Assume MOS = saturation

$$i = i_{DS} = \frac{k}{2} (V_{GS} - V_T)^2 = \frac{1}{2} \times \frac{1}{8} \times (4 - 1)^2 = \frac{3}{4} (A)$$

Supernode $i_1 + i_2 - i = 0$

$$\frac{5 - e}{4} + \frac{3 - (e + 0.7)}{1.3} - \frac{3}{4} = 0$$

$$6.5 - 1.25e + [12 - 4e - 2.8] - 3 = 0 \Rightarrow 11.8 = 5.3e$$

$$\Rightarrow e = 2.23$$

check: $V_{DS} = e - 0 = 2.23V < V_{GS} - V_T = 4 - 1 = 3V$ X

Assume MOS = Triode: $k_{on} = \frac{1}{(V_{GS} - V_T)} = \frac{1}{8(4 - 1)} = \frac{1}{24}$

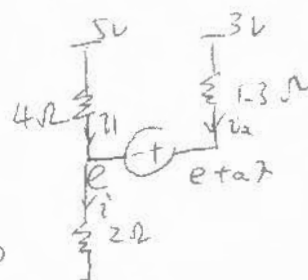
Supernode: $cl. \frac{5 - e}{4} + \frac{3 - (e + 0.7)}{1.3} - \frac{e}{2} = 0$

$$1.3(5 - e) + 4(3 - e - 0.7) - 2.6e = 0$$

$$6.5 - 1.3e + 12 - 4e - 2.8 - 2.6e = 0$$

$$15.7 - 7.9e = 0 \Rightarrow e = 1.99(V)$$

check: $V_{DS} = 1.99 < V_{GS} - V_T = 3(V)$ ✓



Check: current passing through the diode $i_D = i_2 > 0$;
assumption of diode being "ON" correct