Homework Assignment 3 Dynamics Of Non Linear Robotic Systems

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Task 1:

Derive FK equations for the robot depicted in figure 1. Use θ_1 , θ_2 , d_3 as joint space variables, p_x , p_y , p_z as operational space variables. Parameters d_1 , d_2 are known (assign them some positive values for succeeding tasks).

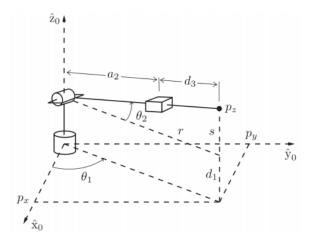


Figure 1: RRP robot.

Task 2

Derive IK equations.

Task 3:

Compute the manipulator Jacobian for representation of linear and angular velocity of point \mathbf{p} .

- Use classical approach (partial derivatives).
- Use geometric approach (cross products).

Task 4:

Analyze the Jacobian for singularities. Characterize each singular configuration if any.

Task 5:

Compute the velocity of the tool frame when joint variables are changing with time as follows:

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\theta_1(t) = sin(t), \ \theta_2(t) = cos(2t), \ d_3(t) = sin(3t).
Add some fancy graphs showing evolution of all variables
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Task 6:

Let tool coordinates changing with time as follows: $p_x(t) = 2a_2 sin(t), p_y(t) = 2a_2 cos(2t), p_z(t) = d_1 sin(3t)$ Determine a feasible joint trajectory for this tool trajectory.

- Use IK solution.
- Use inverse differential kinematics approach. Consider only linear velocity part of Jacobian.