

# Software Development and Abstract Data Types

Chapters 2, 4, 10

# Phases of Software Development

1. Problem statement
2. Specification of the task
3. Design of a solution for each task
4. Implementation of a solution
5. Testing and Debugging
6. Documentation and Maintenance

# Specification of a Method

- Short introduction/summary
- Description of parameters
- Preconditions
- Postconditions or Returns
- Exceptions thrown
- Special notes on usage

# Example

area

public static double area(double radius)

Parameters:

radius – radius of a circle in inches

Preconditions:

radius > 0

Returns:

Returns the area of the circle with the given radius.

Throws: `IllegalArgumentException`

Indicates that the radius is non positive.

# Efficiency

- What's the best way to program an algorithm?
- Efficiency in terms of
  - Time (running time)
  - Space (memory requirements)
  - Resources (Input/Output such as disk I/O)
- Most analysis focuses on time efficiency

# Order of Complexity

- Measuring running time(Benchmark, Analysis)
- Count the number of “operations”
- What is an “operation”?
- Example:  
 $C = A + B;$
- 1 operation?
- 4 operations?  
(LOAD A, LOAD B, ADD, STORE C)

# Order of Complexity (cont'd)

```
for (x=1; x<=n; x++)  
    c = a + b;
```

# of ops:                       $n$        $4n$        $3n+2$  ?

```
for (x=1; x<=n; x++)  
{  
    c = a + b;  
    d = e + f;  
}
```

# of ops:                       $2n$        $8n$        $4n+2$  ?

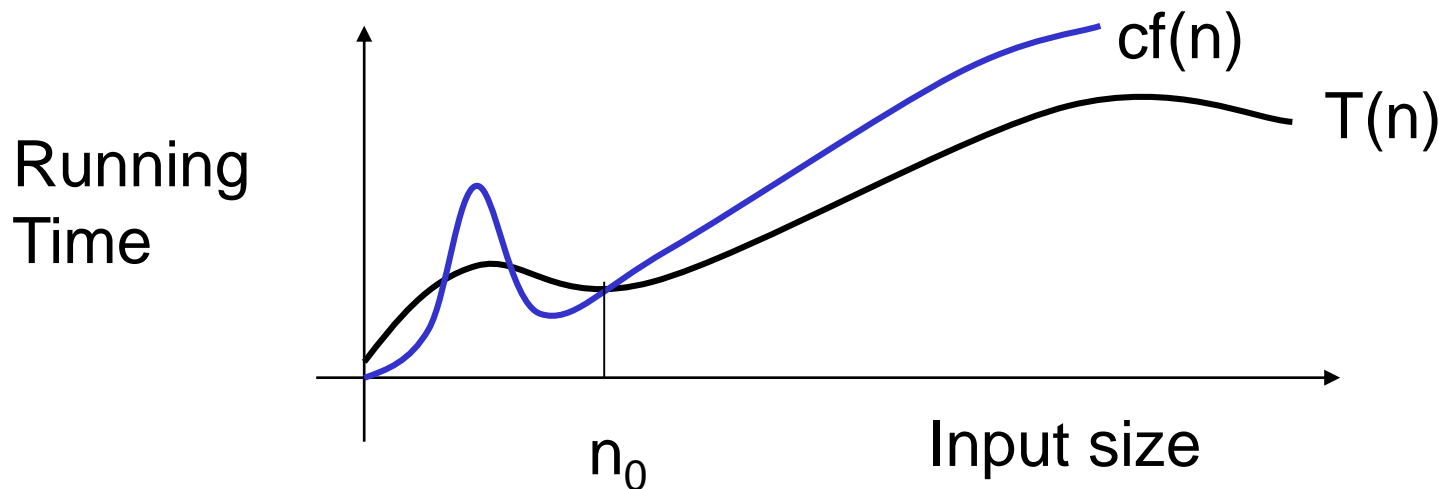
# Big O Notation (upper bound)

- Given an algorithm/routine processing  $n$  inputs, what is the number of operations as a function of  $n$ ?
- Big O expresses this function as a simplified function of  $n$  (input size)
- $O(n)$  – a function of  $n$
- $O(n^2)$  – a function of  $n^2$



# Big O Notation (cont'd)

- Let  $T(n)$  and  $f(n)$  be functions mapping nonnegative integers to real numbers.
- We say that  $T(n)$  is  $O(f(n))$  if there is a real constant  $c > 0$  and an integer constant  $n_0 \geq 1$  such that  $T(n) \leq cf(n)$  for every integer  $n \geq n_0$ .



# Big O Examples

```
for (x=1; x<=n; x++)  
    c = a + b;
```

n operations  
 $O(n)$

```
for (x=1; x<=n; x++)  
{  
    c = a + b;  
    d = e + f;  
}
```

2n operations  
 $O(2n) = O(n)$

# Big O Examples (cont'd)

```
for (x=1; x<=n; x++)
```

```
    c = a + b;
```

```
c = c + d;
```

n+1 operations

$$O(n+1) = O(n)$$

```
for (x=1; x<=n; x=x*2)
```

```
    c = a + b;
```

***Assume  $n$  is a power of 2 for simplicity.***

$\log_2 n + 1$  operations

$$O(\log_2 n + 1) = O(\log n)$$

# Big O Examples (cont'd)

```
for (x=1; x<=n; x++) {  
    d = e + f;  
    for (y=n; y>0; y--) {  
        c = a + b;  
        c = c * 2;  
        d = c + d;  
    }  
}
```

$3n^2+n$  operations  
 $O(3n^2+n) = O(n^2)$

# Worst-, Average-, Best-Case

- Many algorithms give their worst-case performance in terms of big-O.
- Other measures include average-case or best-case analysis.
- Example: Sequential Search on  $n$  elements  
*This time, an operation is a “comparison”.*
  - Worst Case:  $O(n)$
  - Average Case:  $O(n/2) = O(n)$
  - Best Case:  $O(1)$

# One more example

- Consider an algorithm that processes  $n$  data items in one minute. How long will it take to process 32 times as many items on the same computer using the same algorithm?

$$\text{original\_time} * \text{new\_number\_of\_ops} / \text{original\_number\_of\_ops}$$

- | # of operations  | APPROX TIME |
|------------------|-------------|
| – $n = O(n)$     |             |
| – $n^2 = O(n^2)$ |             |
| – $2^n = O(2^n)$ |             |

# Another view

- What is the maximum number of inputs that can be processed by an algorithm in one hour if one operation takes 1 microsecond?
- Number of Ops                      Max. Problem Size
  - $400n = O(n)$                        $n =$
  - $2n^2 = O(n^2)$                        $n =$
  - $2^n = O(2^n)$                        $n =$

# Misuse of the Big O!

- Number of Operations:  $10^{10}n$   
Is this  $O(n)$ ? (probably not)
- What's considered an efficient measure for an algorithm?  
Yes:  $O(\log n)$ ,  $O(n)$ ,  $O(n \log n)$ ,  
even  $O(n^2)$  sometimes  
No:  $O(n^{100})$ ,  $O(2^n)$
- Is  $O(1) + O(1) + \dots + O(1) = O(1)$  ?



# Tale of Two Algorithms

- Given an array  $X$  storing  $n$  numbers, we want to compute an array  $A$  such that  $A[i]$  is the average of elements  $X[0], \dots, X[i]$ , for  $i=0, \dots, n-1$ .
- Calculating “prefix averages”
- Used in economics: Given year-by-year returns on a mutual fund, an investor will want to know the average return over the past 3 years, 5 years, 10 years, etc.

# First Attempt

prefixAverages1(X)

Let  $A[ ]$  be an array of  $n$  numbers

for  $i \leftarrow 0$  to  $n-1$  do

$\text{sum} \leftarrow 0$

    for  $j \leftarrow 0$  to  $i$  do

$\text{sum} \leftarrow \text{sum} + X[j]$

$A[i] \leftarrow \text{sum}/(i + 1)$

return array  $A$

**CAREFUL!**

Order of Complexity?

# An Observation

- In the original algorithm, a lot of computations are recomputed over and over again.
- $A[i-1] = (X[0] + X[1] + \dots + X[i-1]) / i$
- $A[i] = (X[0] + X[1] + \dots + X[i-1] + X[i]) / (i+1)$
- Let the prefix sum  
 $S_i = X[0] + X[1] + \dots + X[i-1] + X[i]$
- $A[i-1] = (S_{i-1}) / i$
- $A[i] = (S_{i-1} + X[i]) / (i+1)$

# Second Attempt

prefixAverages2(X)

Let  $A[ ]$  be an array of  $n$  numbers

$\text{sum} \leftarrow 0$

for  $i \leftarrow 0$  to  $n-1$  do

$\text{sum} \leftarrow \text{sum} + X[i]$

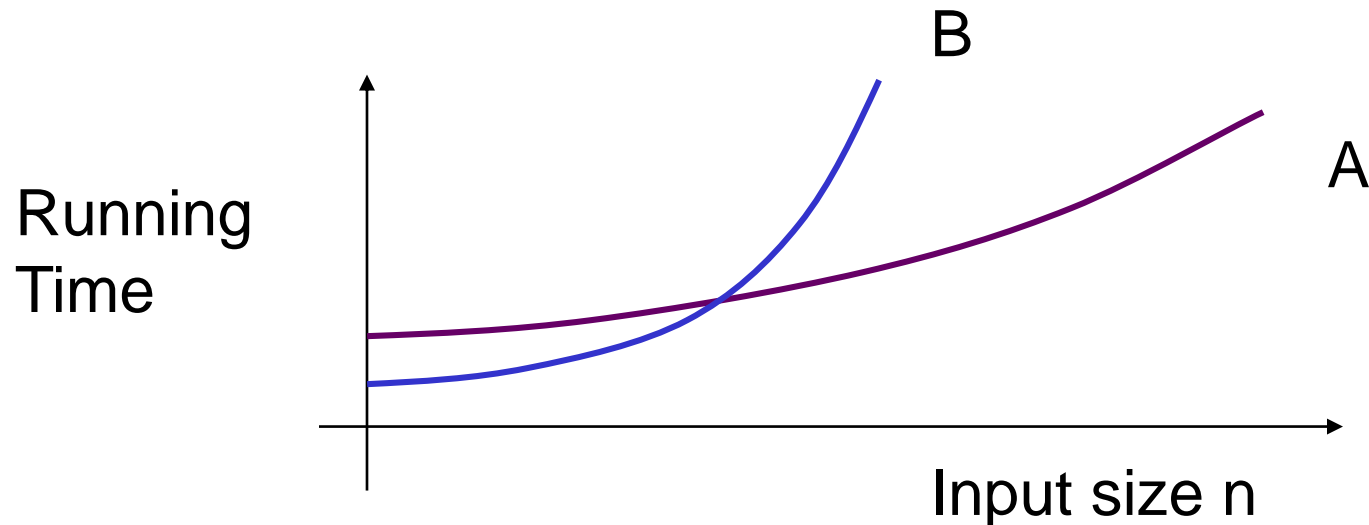
$A[i] \leftarrow \text{sum}/(i + 1)$

return array  $A$

Order of Complexity?

# Competing Algorithms

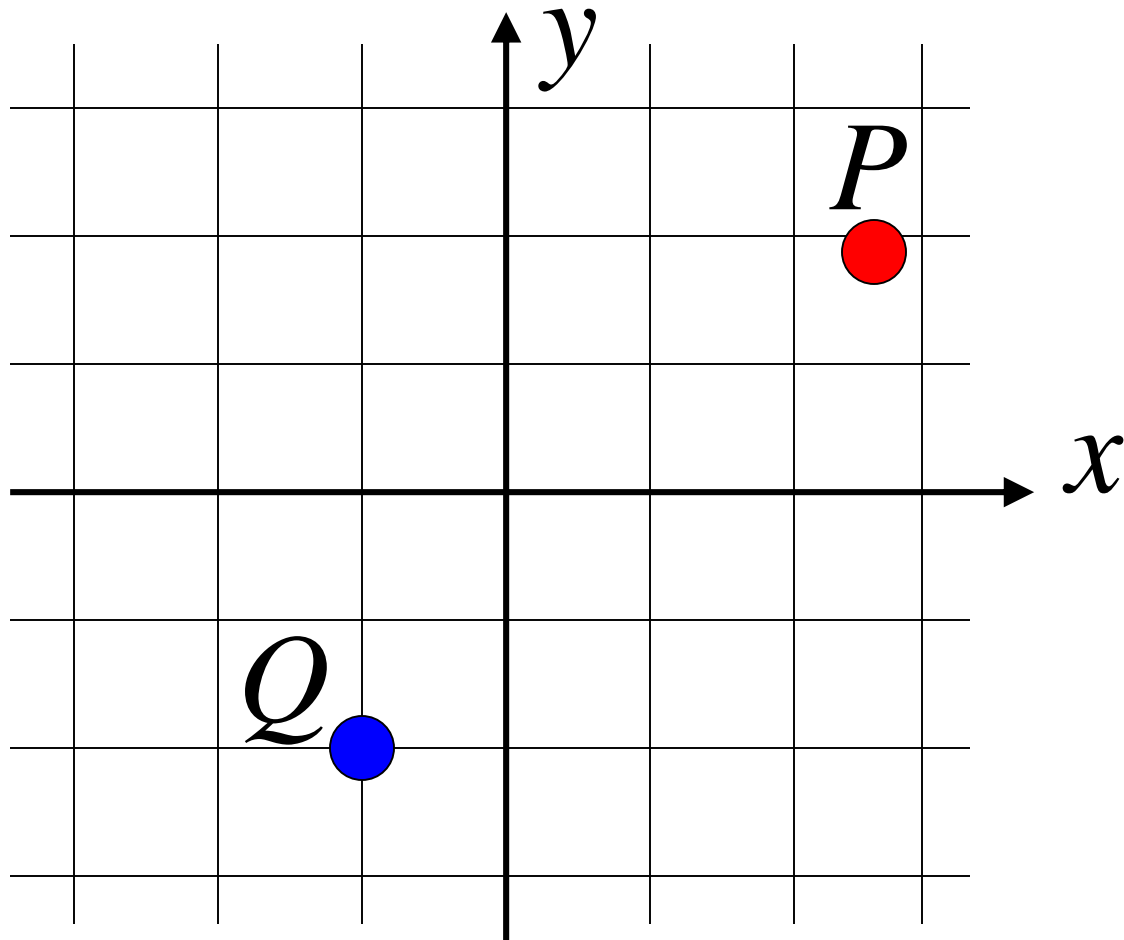
- Algorithm A:  $O(n \log n)$
- Algorithm B:  $O(n^2)$
- Which is more efficient?



# Abstract Data Types

- Information hiding – separation of specification from implementation
- Abstract Data Type –  
A mathematical specification of a data structure that specifies:
  - the type of data stored
  - the operations supported on that data
  - the types of parameters of the operations
- An ADT specifies what, but not how

# Example 1: Location ADT



# Specification – p.63

Constructor

```
public Location(double xInitial,  
                double yInitial)
```

Construct a location with specified coordinates.

Parameters:

xInitial – the initial x coordinate of this Location

yInitial – the initial y coordinate of this Location

Postcondition:

This Location has been initialized at the given coordinates.



# Specification (cont'd)

clone

```
public Object clone()
```

Generate a copy of this Location.

Returns:

The return value is a copy of this Location.

Special note:

The return value must be **typecast** to a Location before it can be used.

# Specification (cont'd)

distance

```
public static double distance  
    (Location p1, Location p2)
```

Compute the distance between two Locations.

Parameters:

p1 – the first Location

p2 – the second Location

Returns: The distance between p1 and p2.

Special Note: Returns Double.NaN if either Location is null.

# Specification (cont'd)

equals

**public boolean equals** (**Object** obj)

Compare this Location to another for equality.

Parameters:

obj – an object with which this Location is compared

Returns: True if obj refers to the same Location as this Location object. False otherwise.

Special Note: Returns false if obj is null or not a Location object.

# Specification (cont'd)

getX (and getY)

```
public double getX( ) ( or getY() )
```

Get the x (or y) coordinate of this Location

Returns: the x (or y) coordinate of this location

# Specification (cont'd)

midpoint

```
public static Location midpoint  
    (Location p1, Location p2)
```

Generates and returns a Location halfway between two Locations

Parameters:

p1 – the first Location

p2 – the second Location

Returns: a Location halfway between p1 and p2

Special note: Returns null if either p1 or p2 is null.

# Specification (cont'd)

rotate90

**public void rotate90 ()**

Rotate this Location 90 degrees in a clockwise fashion around the origin

Postcondition: This Location has been rotated clockwise 90 degrees around the origin

# Specification (cont'd)

shift

```
public void shift(double xAmount,  
double yAmount)
```

Move this location by given amounts along the x and y axes.

Postcondition: This location has been moved by the given amounts along the two axes.

Special note: (see text)

# Specification (cont'd)

toString

**public String toString()**

Generate a string representation of this Location object.

Returns: a string representation of this Location



# Method Types

- Accessor method – returns information about the state of an object without altering the state of the object [getX, getY]
- Modification (mutator) method – may change the state of an object through its invocation [rotate90, shift]
- Static method – returns information about a set of one or more objects [distance, midpoint]
- Support method – provides common support for objects [the constructor, clone, equals, toString]

# Implementation – p. 65

```
public class Location implements Cloneable
{
    private double x;    // state variables
    private double y;

    public Location (double xInitial,
                    double yInitial) // constructor
    {
        x = xInitial;
        y = yInitial;
    }
}
```

# Implementation (cont'd)

```
public Object clone()  
{  
    Location answer;  
    try {  
        answer = (Location)super.clone();  
    }  
    catch (CloneNotSupportedException e) {  
        throw new RuntimeException("...");  
    }  
    return answer;  
}
```

# Implementation (cont'd)

```
public static double distance
(Location p1, Location p2) {
    double a, b, c_squared;
    if ((p1==null) || (p2==null))
        return Double.NaN;

    a = p1.x - p2.x;
    b = p1.y - p2.y;
    c_squared = a*a + b*b;
    return Math.sqrt(c_squared) ;
}
```

# Implementation (cont'd)

```
public boolean equals(Object obj)
{
    if (obj instanceof Location)
    {
        Location candidate =
            (Location) obj;
        return (candidate.x == x) &&
            (candidate.y == y);
    }
    else
        return false;
}
```

# Implementation (cont'd)

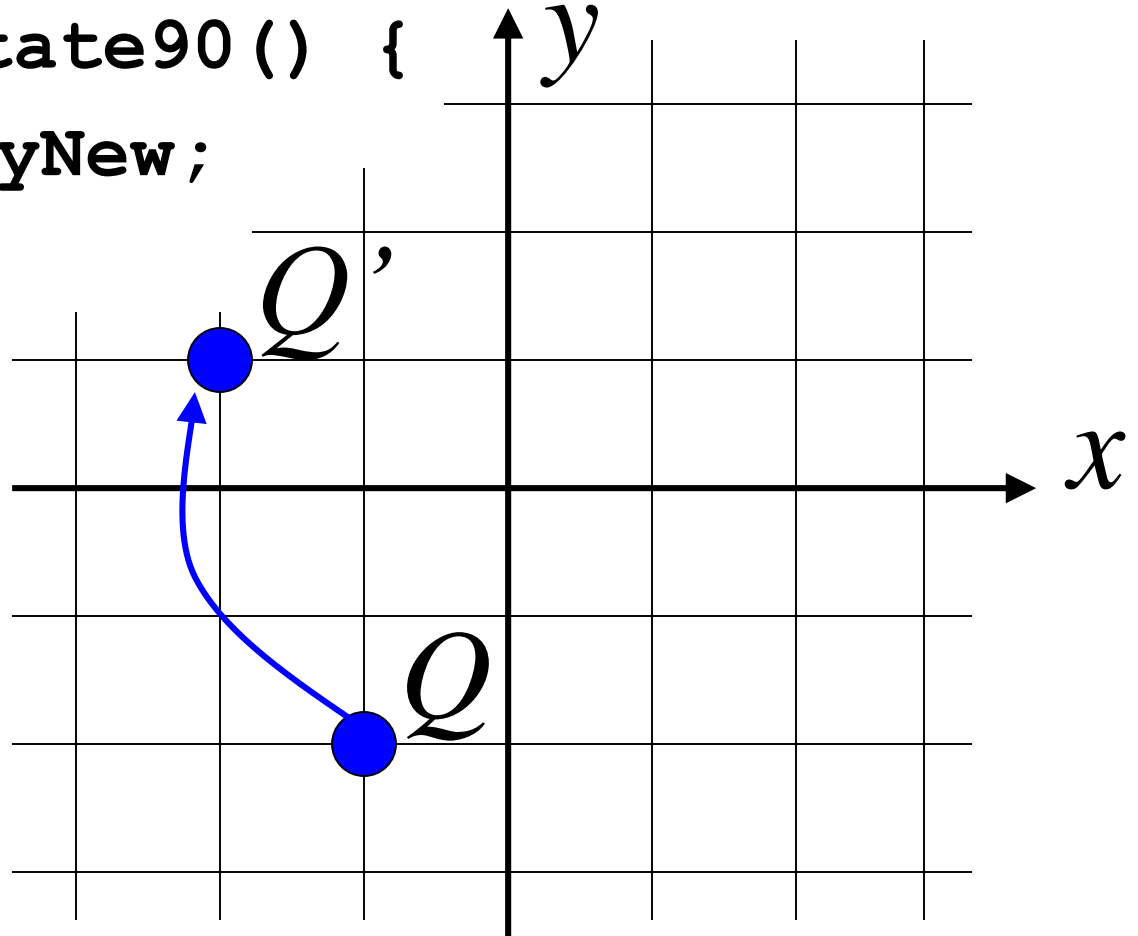
```
public double getX()  
{  
    return x;  
}  
public double getY()  
{  
    return y;  
}
```

# Implementation (cont'd)

```
public static Location midpoint
(Location p1, Location p2) {
    double xMid, yMid;
    if ((p1==null) || (p2==null))
        return null;
    xMid = (p1.x/2)+(p2.x/2);
    yMid = (p1.y/2)+(p2.y/2);
    Location answer =
        new Location(xMid, yMid);
    return answer;
}
```

# Implementation (cont'd)

```
public void rotate90 () {  
    double xNew, yNew;  
    xNew = y;  
    yNew = -x;  
    x = xNew;  
    y = yNew;  
}
```





# Implementation (cont'd)

```
public void shift(double xAmount,  
    double yAmount) {  
    x += xAmount;  
    y += yAmount;  
}  
  
public String toString()  
{  
    return "(x=" + x + "    y=" + y + ")";  
}  
  
} // end class Location
```

# Use of Location ADT

```
class LocationTester {  
    public static void main(String[] args)  
    {  
        Location server = new Location(2.0,4.5);  
        Location mobile = (Location) server.clone();  
        mobile.shift(-3.0, -3.0);  
        System.out.println("The devices are " +  
            Location.distance(server, mobile) +  
            " blocks away from each other.");  
    }  
}
```

etc.

## Example 2: Bag ADT

- Bag: A collection of items of the same type.
- A specific item may appear any number of times in a bag.
- A bag is not a set.
- A bag is not ordered.
- The items of a bag will be stored in an **array (for now)**.
- A bag may have **limited size** due to memory constraints.

# Specification – p.107

## Constructors

```
public IntArrayBag( )
```

```
public IntArrayBag(int initialCapacity)
```

Construct a bag of integers with capacity 10 (default) or initialCapacity.

Precondition:  $\text{initialCapacity} \geq 0$

Postcondition: This bag is empty and has an initial capacity.

Throws: `IllegalArgumentException`, `OutOfMemoryError`

# Specification (cont'd)

getCapacity

```
public int getCapacity()
```

Determines the current capacity of this bag.

Returns: the current capacity of this bag.

size

```
public int size()
```

Determines the number of elements in this bag.

Returns: the number of elements in this bag.

# Specification (cont'd)

ensureCapacity

```
public void ensureCapacity  
    (int minimumCapacity)
```

Change the current capacity of this bag.

Parameters: minimumCapacity – the new capacity for this bag

Postcondition: This bag's capacity has been changed to minimumCapacity, if this is greater than its current capacity.

Throws: OutOfMemoryException

# Specification (cont'd)

add

```
public void add(int element)
```

Add a new element to this bag.

Parameters:

element – the new element being added to the bag

Postcondition: A new copy of the element has been added to this bag.

Special Note: If the new element cannot be stored in the bag at its current capacity, the bag's **capacity is increased**.

Throws: OutOfMemoryError

# Specification (cont'd)

addAll

**public void addAll(IntArrayBag addend)**

Add the contents of another bag to this bag.

Parameters:

addend – a bag whose contents will be added to this bag

Postcondition: This bag will contain its original contents and the contents of the other bag.

Throws: NullPointerException, OutOfMemoryError



# Specification (cont'd)

union

```
public static IntArrayBag union  
    (IntArrayBag b1, IntArrayBag b2)
```

Create a new bag that contains all the elements from two other bags.

Parameters:

b1 – the first of two bags

b2 – the second of two bags

Precondition: neither b1 nor b2 is null

Returns: A new bag that is the union of b1 and b2

Throws: NullPointerException, OutOfMemoryError

# Specification (cont'd)

countOccurrences

```
public int countOccurrences(int target)
```

Count the number of occurrences of a particular value in this bag.

Parameters:

target – the element that needs to be counted

Returns: The number of times the target is in this bag.

# Specification (cont'd)

remove

**public boolean remove(int target)**

Remove **one** copy of a specified element from this bag.

Parameter:

target – the element search for in this bag for removal

Postcondition: If the target was found in this bag, then one copy is removed and the method returns true. Otherwise, this bag remains unchanged and the method returns false.

# Specification (cont'd)

trimToSize

**public void trimToSize()**

Reduce the current capacity of this bag to its actual size.

Postcondition: This bag's capacity has been changed to its current size.

Throws: **OutOfMemoryError**

# Specification (cont'd)

clone

```
public Object clone()
```

Generate a copy of this bag.

Returns:

The return value is a copy of this bag.

Special note:

The return value must be **typecast** to an IntArrayBag before it can be used.

Throws: OutOfMemoryError

# Invariant of the ADT

- An invariant is a condition that remains true before and after some operation is performed (i.e. precondition = postcondition)
- All the methods of an ADT (except the constructors) must ensure that the invariant of the ADT is valid before and after execution.

# Invariant of the Bag ADT

- Let `data` = the array that holds the bag items
- Let `data.length` = the capacity of the array
- Let `manyItems` = the number of items in the bag (i.e. its size)
- INVARIANTS:
  - The elements of a bag are stored in `data[0..manyItems-1]`.
  - $\text{manyItems} \leq \text{data.length}$

# Implementation – p. 113

```
public class IntArrayBag
    implements Cloneable
{
    private int[] data;
    private int manyItems;
```



# Implementation (cont'd)

```
public IntArrayBag(int initialCapacity) {  
    if (initialCapacity < 0)  
        throw new IllegalArgumentException();  
    manyItems = 0;  
    data = new int[initialCapacity];  
}  
  
public IntArrayBag() {  
    manyItems = 0;  
    data = new int[10];  
}
```

# Implementation (cont'd)

```
public int getCapacity() {  
    return data.length;  
}
```

```
public int size() {  
    return manyItems;  
}
```

Order of Complexity?

# Sidenote: `System.arraycopy`

`System.arraycopy(src, si, dest, di, n) ;`

**src** = reference of array to copy FROM

**si** = starting position to copy FROM

**dest** = reference of array to copy TO

**di** = starting position to copy TO

**n** = how many elements to copy

# Implementation (cont'd)

```
public void ensureCapacity(int
    minimumCapacity) {
    int biggerArray[];
    if (data.length < minimumCapacity) {
        biggerArray = new
            int[minimumCapacity];
        System.arraycopy(data, 0,
            biggerArray, 0, manyItems);
        data = biggerArray; // previous data?
    }
} // Order of Complexity?
```

# Implementation (cont'd)

```
public void add(int element) {  
    if (manyItems == data.length)  
        ensureCapacity(manyItems*2+1);  
    data[manyItems] = element;  
    manyItems++;  
}
```

Order of Complexity?

# Implementation (cont'd)

```
public void addAll(IntArrayBag addend) {  
    ensureCapacity(manyItems +  
        addend.manyItems);  
    System.arraycopy(addend.data, 0, data,  
        manyItems, addend.manyItems);  
    manyItems += addend.manyItems;  
}
```

Order of Complexity?

# Implementation (cont'd)

```
public static IntArrayBag union
(IntArrayBag b1, IntArrayBag b2) {
    IntArrayBag answer = new IntArrayBag
        (b1.getCapacity()+ b2.getCapacity());
    System.arraycopy(b1.data,0,answer.data,
        0,b1.manyItems);
    System.arraycopy(b2.data,0,answer.data,
        b1.manyItems, b2.manyItems);
    answer.manyItems =
        b1.manyItems + b2.manyItems;
    return answer;
} Order of Complexity?
```

# Implementation (cont'd)

```
public int countOccurrences(int target)
{
    int answer = 0;
    int index;
    for (index = 0; index < manyItems;
        index++)
    {
        if (target == data[index])
            answer++;
    }
    return answer;
} Order of Complexity?
```



# Implementation (cont'd)

```
public boolean remove(int target) {  
    int index = 0;  
    while ((index < manyItems) &&  
           (target != data[index]))  
        index++;  
    if (index == manyItems)  
        return false;  
    else {  
        manyItems--;  
        data[index] = data[manyItems];  
        return true;  
    }  
}
```

Order of Complexity?

# Implementation (cont'd)

```
public void trimToSize() {  
    int trimmedArray[];  
    if (data.length != manyItems) {  
        trimmedArray = new int[manyItems];  
        System.arraycopy(data, 0,  
            trimmedArray, 0, manyItems);  
        data = trimmedArray; // previous data?  
    }  
}
```

Order of Complexity?

# Implementation (cont'd)

```
public Object clone() {
    IntArrayBag answer;
    try {
        answer = (IntArrayBag) super.clone();
    }
    catch (CloneNotSupportedException e) {
        throw new RuntimeException("...");
    }
    answer.data = (int []) data.clone();
    return answer;
}
} // end class IntArrayBag
```

Order of Complexity?

# Order of Complexity

- **Given a bag with  $n$  items and capacity  $c$ .**
- **add**
  - Without a capacity increase:  $O(1)$
  - With a capacity increase:  $O(n)$
- **countOccurrences**  $O(n)$
- **getCapacity**  $O(1)$
- **remove**  $O(n)$
- **clone**  $O(c)$