# E344 Assignment 2

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Design (E) 344 for the degree Baccalaureus in Engineering in the Department of Electrical
and Electronic Engineering at Stellenbosch University.

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# Nomenclature

**Variables and functions**

| | |
|---|---|
| $p(x)$ | Probability density function with respect to variable $x$. |
| $P(A)$ | Probability of event $A$ occurring. |
| $\varepsilon$ | The Bayes error. |
| $\varepsilon_u$ | The Bhattacharyya bound. |
| $B$ | The Bhattacharyya distance. |
| $s$ | An HMM state. A subscript is used to refer to a particular state, e.g. $s_i$ refers to the $i^{\text{th}}$ state of an HMM. |
| $\mathbf{S}$ | A set of HMM states. |
| $\mathbf{F}$ | A set of frames. |
| $\mathbf{o}_f$ | Observation (feature) vector associated with frame $f$. |
| $\gamma_s(\mathbf{o}_f)$ | A posteriori probability of the observation vector $\mathbf{o}_f$ being generated by HMM state $s$. |
| $\mu$ | Statistical mean vector. |
| $\Sigma$ | Statistical covariance matrix. |
| $L(\mathbf{S})$ | Log likelihood of the set of HMM states $\mathbf{S}$ generating the training set observation vectors assigned to the states in that set. |
| $\mathcal{N}(\mathbf{x}|\mu, \Sigma)$ | Multivariate Gaussian PDF with mean $\mu$ and covariance matrix $\Sigma$. |
| $a_{ij}$ | The probability of a transition from HMM state $s_i$ to state $s_j$. |
| $N$ | Total number of frames or number of tokens, depending on the context. |
| $D$ | Number of deletion errors. |
| $I$ | Number of insertion errors. |
| $S$ | Number of substitution errors. |

## Acronyms and abbreviations

| | |
|---|---|
| AE | Afrikaans English |
| AID | accent identification |
| ASR | automatic speech recognition |
| AST | African Speech Technology |
| CE | Cape Flats English |
| DCD | dialect-context-dependent |
| DNN | deep neural network |
| G2P | grapheme-to-phoneme |
| GMM | Gaussian mixture model |
| HMM | hidden Markov model |
| HTK | Hidden Markov Model Toolkit |
| IE | Indian South African English |
| IPA | International Phonetic Alphabet |
| LM | language model |
| LMS | language model scaling factor |
| MFCC | Mel-frequency cepstral coefficient |
| MLLR | maximum likelihood linear regression |
| OOV | out-of-vocabulary |
| PD | pronunciation dictionary |
| PDF | probability density function |
| SAE | South African English |
| SAMPA | Speech Assessment Methods Phonetic Alphabet |

# Chapter 1

# System design

## 1.1. System overview
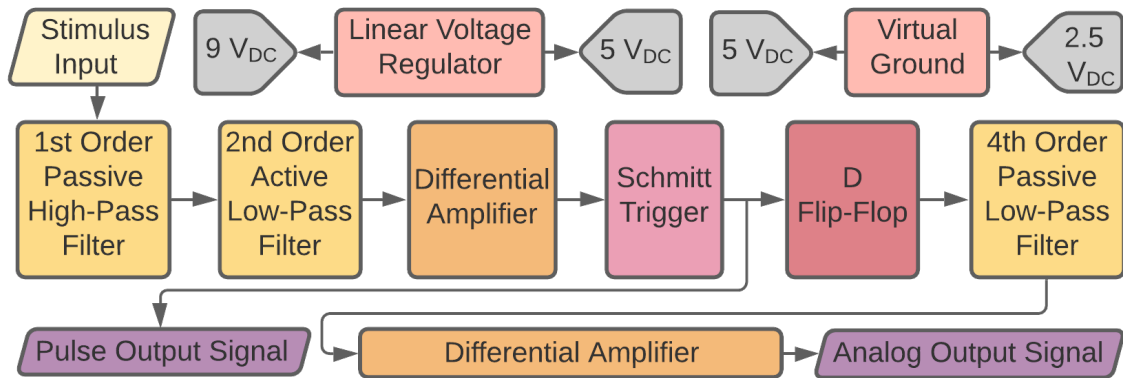


**Figure 1.1:** System Diagram

A heart-rate sensor is designed to receive an input signal from which pulses and analogue values are generated, corresponding to heart-beats and the heart-rate respectively. The aforementioned is achieved by voltage regulation, signal conditioning, pulse generation and conversion to analogue, as shown in figure 1.1. The circuit is powered by a voltage regulator [1] which can supply $100\,\text{mA}$, of which $12.8\,\text{mA}$ is used for the temperature sensor - see E344 Assigment 1 [1] - leaving $87.2\,\text{mA}$ at $5\,\text{V}$, mandating conservative current use. The input signal has an amplitude of insufficient magnitude for conversion, and is subject to noise, necessitating signal conditioning: a first order passive high-pass filter and a second order active low-pass filter attenuate both high- and low-frequencies. Chosen with maximal simplicity in mind to reduce cost and complexity, the filters still performing adequately. Thereafter, a differential amplifier produces a signal with a large amplitude and little noise. A Schmitt Trigger then outputs a pulse signal with a frequency corresponding to the heart-rate. The Schmitt Trigger was chosen as it provides a noise margin via hysteresis. An analogue voltage output is required for the microcontroller - filtering and peak detection using diodes was considered but discarded, as non-linear diodes result in extremely slow simulation. Rather, the pulse output signal was converted to a pulse-width modulated signal, where the frequency of the former determines the duty cycle of the latter. This was done as PWM signals lend themselves to conversion-to-analogue by simple filtering. The PWM signal was obtained by using a D Flip-Flop and a RC-circuit (see section **??**). A third order passive RC filter is then used - passive components reduce current usage and simulation time. The filter is of high order as to minimize noise, while meeting the settling time requirement. Finally, the signal was amplified to achieve the required range.

# Chapter 2

# Heart rate sensor

## 2.1. Introduction

Circuits pertaining to signal conditioning, pulse signal and analogue output generation will be discussed. Conditioning is done via filtering and amplification; active filters provide high input and low output impedance, and a large Q-factor [2]. A differential amplifier is suitable for amplification, as the gain is referenced against a customizable voltage [3]. A Schmitt Trigger is well-suited for pulse generation, as it provides a noise margin [4]. PWM signals can be converted to analogue using filtering [5]. **check template at end to make sure everything is included**
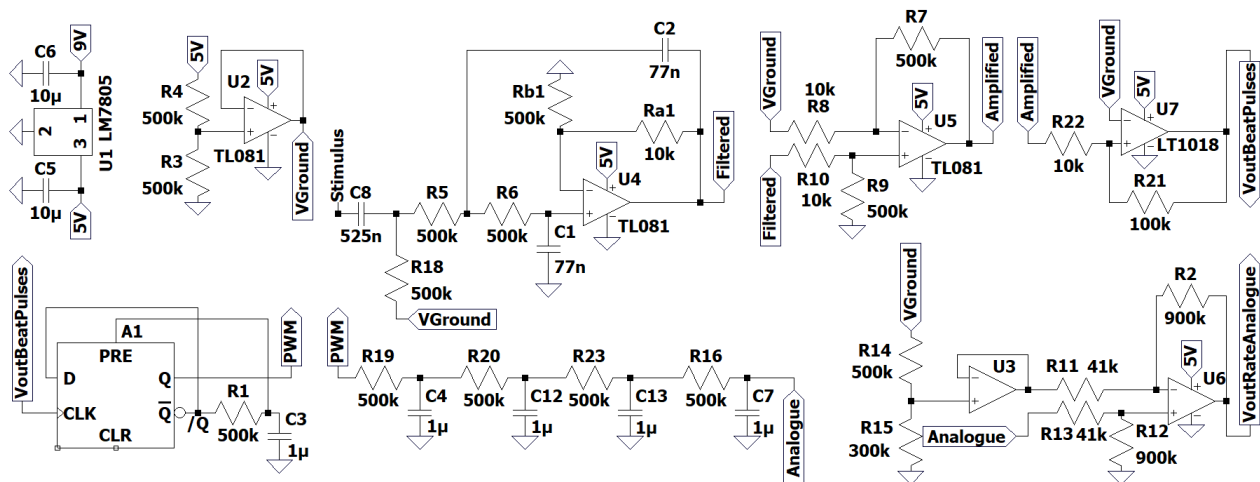
## 2.2. Design

**Figure 2.1:** Complete Circuit **enlarge this**

The complete circuit is shown upfront in figure 2.1 to aid with explanation. The largest resistor in sub-circuits is always chosen to be $500\,\mathrm{k\Omega}$, as to reduce current usage. The design process now follows. The FFT of the stimulus input in figure 2.2 has information residing between 0.8 to 2.5 Hz, corresponding to 50 and 150 BPM respectively. The other peaks represent noise
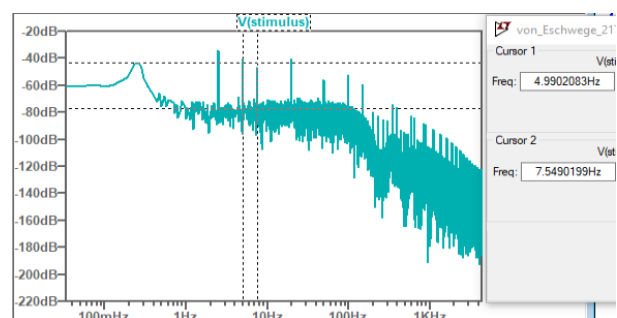
**Figure 2.2:** Fast fourier transform of stimulus

at 0.25 Hz, as well as at twice and three times the message signal, and higher. Noise distorts square wave output, necessitating filtering. A first order passive high-pass filter, cutoff frequency 0.606 Hz, attenuates the low frequency noise. R18 = 500 kΩ, thus C8 = 525 nF according to $f_c = \frac{1}{2\pi RC}$. The capacitor is connected to a virtual ground of 2.5 V, centering the signal around 2.5 V. A second order active low-pass filter, cutoff frequency 4.1 Hz, filters out high frequency noise. R5 = R6 = 500 kΩ, C1 = C2 = 77 nF - see aforementioned formula. Cutoff frequencies were selected to remove noise maximally while minimally affecting heart-rate data. The signal should reside slightly above 2.5 V to facilitate amplification (to be discussed). Thus, Rb1 = 500 kΩ and Ra1 = 10 kΩ since $A_v = 1 + \frac{R_A}{R_B}$ [?]. The TL081 op-amp is used, as it is less expensive than the TLC2272 [?]. A filter output with DC offset slightly above 2.5 V allows for the use of a differential amplifier with the existing virtual ground connected to the negative input, thus removing the need for additional circuitry otherwise required. The signal is amplified according to $V_{OUT} = \frac{R_a}{R_b}(V_2 - V_1)$ [3], where $R_a$ corresponds to R7 and R9, and $R_b$ to R8 and R10. The gain of 50 was selected to again provide a DC offset of 2.5 V, as it facilitates implementation of the comparator (to be discussed). Since the amplified signal has an amplitude of only 1.66 V, the inexpensive TL081 was chosen despite having a smaller output range. Next, the signal is fed into a Schmitt Trigger comparator, which produces 5 V if the input exceeds the upper trip point (UTP) and 0 V if the input falls below the lower trip point (LTP) [4]. The range between the UTP and LTP is referred to as the hysteresis width and serves as a noise margin [4] around the reference voltage, $V_{REF_{comparator}}$. The hysteresis width was chosen as 0.5 V as to be an order of magnitude larger than the highest levels of noise present on the comparator input signal. As mentioned previously, the amplified signal has a DC offset of 2.5 V, which was chosen as to require $V_{REF_{comparator}} = 2.5$ V, once again allowing for the use of the existing virtual ground (instead of additional circuitry) at the negative input of the LT1018 comparator, which was chosen as it allows for output very close to 0 and 5V, and has a high gain. Now, UTP = 2.75 V, LTP = 2.25 V, UTP = $V_{REF} + \beta Vcc$ and LTP = $V_{REF} - \beta Vcc$, thus $\beta = 0.05$ [4]. Further, $\beta = \frac{R_{22}}{R_{22}+R_{21}}$. Thus R21 = 190 kΩ and R22 = 10 kΩ. (R21 was later adjusted to 100 kΩ to account for loading effects). The design specifications require a pulse width of at least 150 ms. A one-shot was considered to extend the pulses, but was omitted as the requirement could be met without it. A square wave is thus produced, where the frequency of the pulses represent the heart-rate.

Obtaining an output suitable for a microcontroller presents itself as a problem of converting frequency to analogue. The decision was made to obtain a PWM signal from the FM pulse signal, as PWM signals lend themselves more readily to conversion-to-analogue using a simple low-pass RC filter. Pulse-width modulation was achieved by means of a D flip-flop. The essence of the design is to firstly keep the output high continually, but to then drive the output low for a fixed time, once per period. Since the period of the clock signal varies against BPM, driving low for a fixed amount of time results in a different ratio of the pulse being low

at different frequencies, producing a varying duty cycle. Specifically, the previously generated pulse signal is used as a clock signal for the D flip-flop, and the not-Q output is fed back into the data line. This would normally drive the output high for all time $t$; thus a RC circuit is added of which the capacitor is charged by the not-Q output, and connected to the SET-line of the flip-flop. Once the capacitor charges to 2.5 V, Q is pulled high and not-Q low until the next rising edge of the clock input inverts Q and not-Q. The result is a slightly delayed PWM signal, with a large duty cycle at high frequencies, and vice-versa. This configuration was preferred above the standard one-shot setup, as it results in a consistent PWM output as long as the capacitor charge time is selected to be shorter than the narrowest pulse of the clock signal. See section 2.3, figure 2.6 for output graphs. calculations follow. Selecting R1 = 500 kΩ gives $C = 1\mu$, according to the capacitor charge/discharge exponential equations, of which the extended solution (using a Matlab script) is given in Appendix C for the sake of brevity. Having obtained a PWM signal, a fourth order passive low-pass filter produces analogue values in the range of 0.95 to 1.2 V. A cutoff frequency of 0.5 Hz ensures maximal attenuation of noise while maintaining a 5% settling time of 10 seconds. Therefore resistor values are 500 kΩ and capacitor values are $1\,\mu$. Finally, the analogue output is amplified by means of a differential amplifier with a negative input at 0.938 V. A gain of 20 produces a sufficient output range. Resistor values were chosen to be larger as to minimize loading effects. Thus, R2 = R12 = 900 kΩ and R11 = R13 = 45 kΩ according to $V_{OUT} = \frac{R_a}{R_b}(V_2 - V_1)$ [3]. Loading effects still had a slight effect, and required adapting R11 and R13 to 41 kΩ. An analogue transducer is thus designed, and can be connected to a microcontroller.

## 2.3. Results

The frequency response of both the high- and low-pass filters are $-3dB$ at 0.606 Hz and $-6dB$ at 4.3 Hz respectively, as shown in figures 2.3a and 2.3b, thus matching the design calculations almost perfectly. **current!!!!!!!**



(a) High-pass filter



(b) Second-order low-pass filter
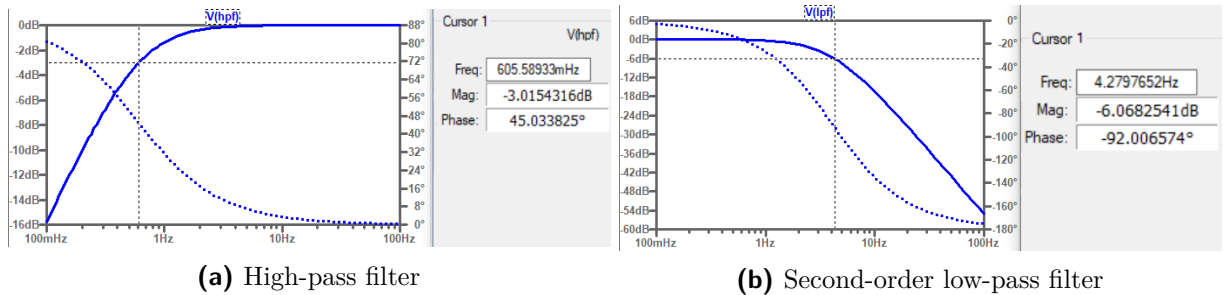
**Figure 2.3:** Frequency response of filters
.

The filtered signal is passed through a differential amplifier; the input is shown in blue and the output in red in figure 2.4. The filtered signal has a 50 mV amplitude (peak-to-peak), and the output 1.747 V. Therefore $A_v \approx 35$, which, although smaller than calculated, is to be expected due to non-linear behaviour for high amplification factors.

Following amplification, the signal is passed into a LT1018 comparator. Input and output thereof is shown in figure 2.5. Measurements
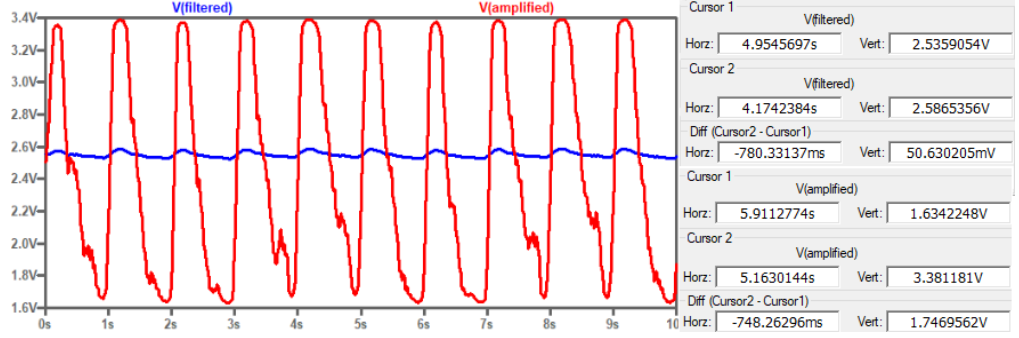


**Figure 2.4:** Amplification of filtered signal

yielded UTP = 2.75 V and LTP = 2.25V, giving a hysteresis width of 0.5 V, exactly as calculated. The cursor at the top right in figure 2.5 measures the narrowest pulse at 150 BPM as to demonstrate compliance with the 150 ms requirement, and the lower right gives the values of the tip points.
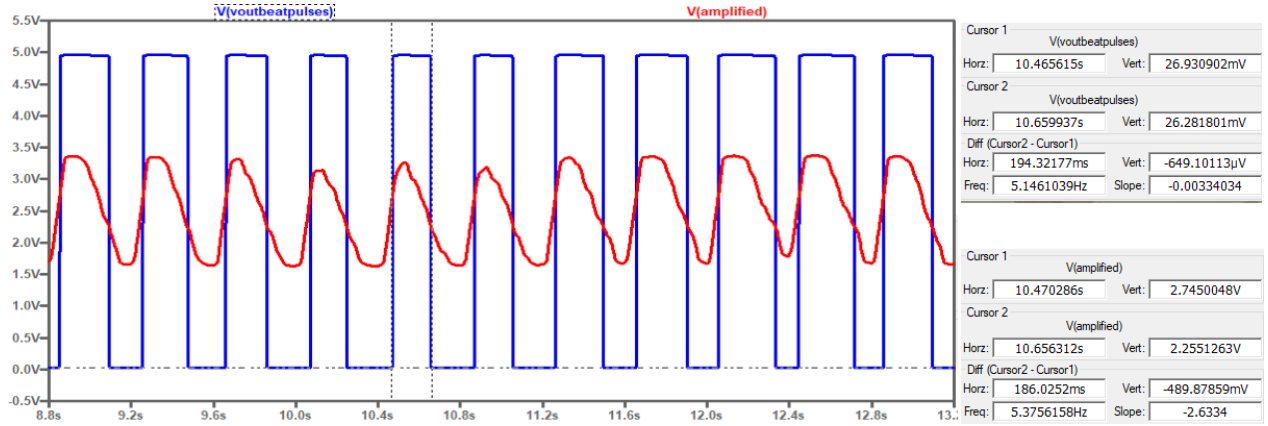


**Figure 2.5:** Pulse signal output

For the analogue transducer, a PWM signal is obtained. Section 2.2 explains the interrelation of the signals, where `voutbeatpulses, pwm, /q` and `rc` correspond to the clock signal, Q, not-Q and the charging capacitor voltage respectively. As shown in figure 2.6, the pulse is high for about 730 ms of every 1 s period in the case of 60 beats per minute. A duty cycle of
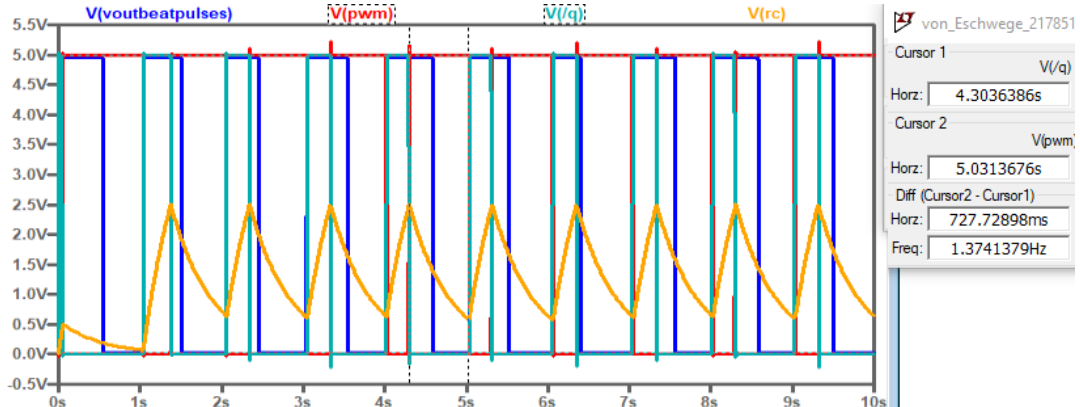


**Figure 2.6:** Pulse width modulation - 60 BPM

73% is thus obtained, and decreases to 56% for 0.223 s high of 0.4 s at 150 beats per minute - see figure 2.7. Finally, amplification and filtering of the PWM signal produces the output shown in figure 2.8a, demonstrating an output range of 4.2 V and a 5% settling time of 9.76 s. In figure 2.8b, total current draw is measured through $R_{sense}$, giving and average of 12.9 mA, meeting the bonus requirement of 15 mA.
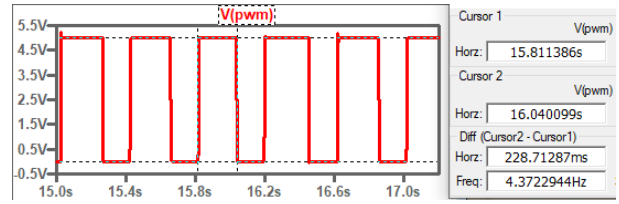


**Figure 2.7:** Pulse width modulation - 150 BPM



**(a)** Analogue voltage output



**(b)** Total current usage
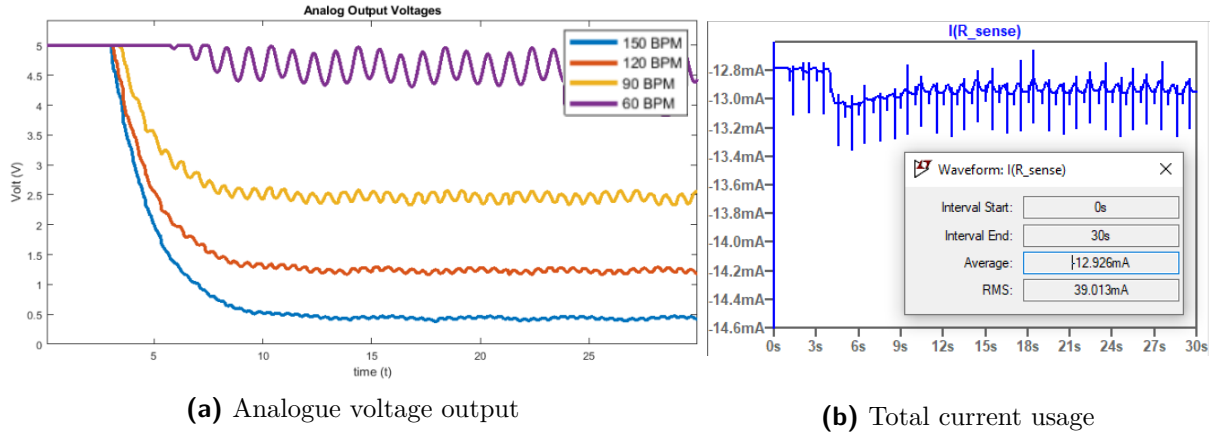
## 2.4. Summary

Concluding, it has been shown that the design performs as expected, meeting the all requirements. Pulse output is produced, with pulse widths broader than the required minimum. Analogue output is generated with discrete, non-overlapping output values having more than the required range, while settling to a final value according to specification. All of the aforementioned has been achieved while maintaining a sub-15 mA current draw. Upon implementation of the microcontroller, be cognizant of the fact that analogue output values scale in a slightly non-linear fashion. This is not a problem, as it can be easily accounted for in software.

# Chapter 3

# System and conclusion

## 3.1. System

The design of the heart-rate sensor goes to show that a noisy input signal, obtained from a sensing device, could effectively be converted to a square wave output as well as an analogue output, allowing for reliable interfacing of real-world measurements with digital systems. The heart-rate sensing circuit can now be integrated with the remainder of the health monitoring system by connecting the analogue output to the microcontroller input, to which the temperature sensor will also be connected - see E344 Assignment 1 **??**. The modular design of different parts of the health-monitoring system allows for simplification of both design and debugging. Due to the second order low-pass filter, the heart-rate sensor is remarkably robust with respect to variations in noise, attenuating noise levels and performs well on a variety of the normalised input data sets, with the exception of minor complications arising from the nature of LTSpice simulation, sometimes, but not often, requiring a restart of the simulation software.

Report on the "so what" or the take-away of the ciruit you designed in this report. Report on noise levels and how the Heart rate sensor will fit into the system (E.g. what the calibration will look like and what the the measurement error will be given the range, quantisation error and noise).

## 3.2. Lessons learnt

1. LTSpice is a blessing, but can be an absolute nightmare with simulations. I have created a rough metric, and it goes to show that 30% of my time was spent on circuit design, 10% on report writing, and 60% on debugging LTSpice simulation problems. I entered E-Design with the belief that simulation would greatly accelerate the pace of the subject, as soldering was eliminated, but I stand firm in my belief that I could have built a practical circuit much faster, as 'timestep too small' does not apply in the beauty of real-world continuity. However, maybe I just stand firm in this belief because I have not dealt with the problems arising from burnt-out components, messy soldering, melted PCB tracks and exploding diodes.

2. I believe to have greatly improved with regards to modularising and debugging not only circuits, but systems in general. Treating everything as a small problem to be solved went a long way towards improving conceptual understanding of component interaction.

3. Don't go surfing for the entirety of the first week of the term. I said this in Assignment 1 as well, and lost a bunch of marks for it, but it is still applicable and true, so I'll say it again.

4. If I could have it all over again, I wouldn't have texted my circuit; she did not reply.

# Bibliography

[1] "E344 assignment 1."

[2] "Difference between active and passive filter."

[3] W. Storr, "Operational amplifiers," 2018. [Online]. Available: https://www.electronics-tutorials.ws/opamp

[4] ——, "Op-amp comparator," 2018. [Online]. Available: https://www.electronics-tutorials.ws/opamp/op-amp-comparator.html

[5] "Analog output - convert pwm to voltage."

# Appendix A

# Social contract

Sign and inlcude.

# Appendix B

# GitHub Activity Heatmap

Take a screenshot of your github version control activity heatmap and insert here.

# Appendix C

# Stuff you want to include

The capacitor charge oscillates between $V_L$ and $V_H$. $V_H = 2.5\,\text{V}$. $V_L$ is reached for the first time at $t_{L_1}$ and $V_H$ at $t_{H_1}$. $V_L$ is then reached at $t_{L_2}$. For $150\,\text{BPM}$ (or $2.5\,\text{Hz}$), the pulse drives high for $0.2\,\text{ms}$. Since the capacitor has to charge faster than $0.2\,\text{ms}$, a charge time of $0.16\,\text{ms}$ was selected to add a 20% margin, accounting for noise. Thus $t_{H_1} - t_{L_1} = 0.16$ and $t_{L_2} = 0.4 - 0.16 = 0.24$ for the 150 BPM signal. Finally,

$$V_L = 5\left(1 - e^{\frac{t_{L_1}}{\tau}}\right)$$

$$V_H = 5\left(1 - e^{\frac{-t_{H_1}}{\tau}}\right)$$

$$V_L = V_H\left(e^{\frac{t_{L_1}}{\tau}}\right)$$

giving $C = 1\mu$.