

Big O Notations

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Understanding Big O

How efficient is an algorithm or piece of code?

01

CPU (time) usage

02

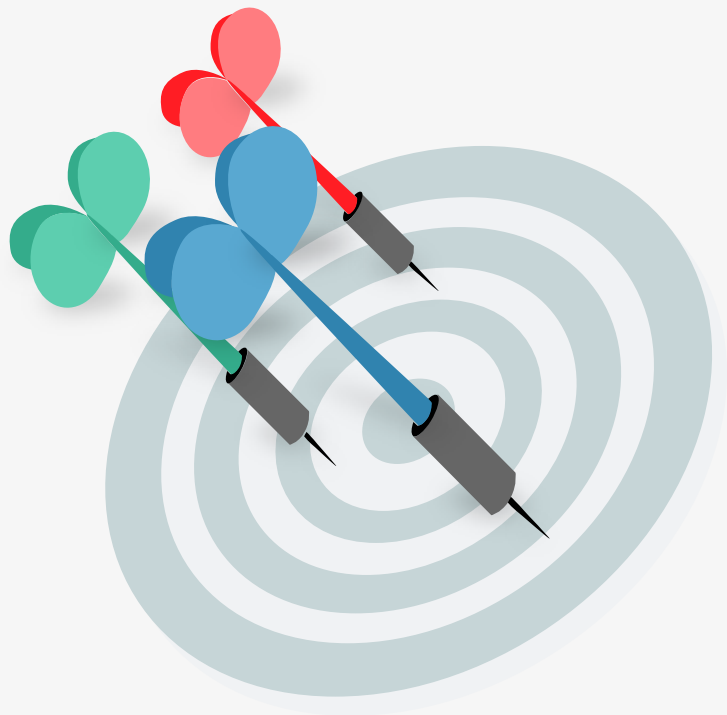
Memory usage

03

Disk usage

04

Network usage



Common Confusion

PERFORMANCE

COMPLEXITY

Complexity Measurement

1

One Arithmetic Operation

2

One Assignment

3

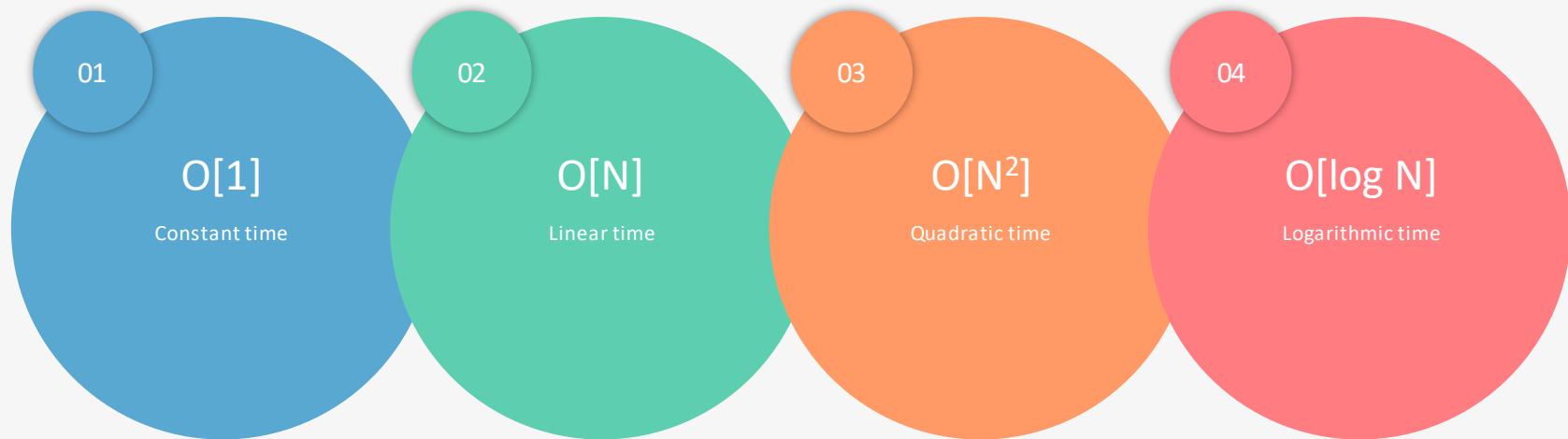
One read

4

One write



Big-O Notation



Time Complexity

Constant Time

When we are adding two number programmatically

E.g.: $10 + 12 = 22$

$10 \Rightarrow O[1]$

$12 \Rightarrow O[1]$

$22 \Rightarrow O[1]$

$O[1] + O[1] + O[1] \Rightarrow O[3]$

$O[3] \Rightarrow O[C]$

$\sim O[1]$

Linear time

Linear to the number of inputs and time

Find the sum of all the elements in the Array

Input = {1,2,3,4,5,6,7,8,9,10}

$$1 \Rightarrow O[1] + 2 \Rightarrow O[1] + \dots + 10 \Rightarrow O[1]$$

$$O[1] + O[1] + \dots + O[1] \Rightarrow O[10] \Rightarrow O[N]$$

Problem

Given an array of integers, sort the array without inbuilt function

15 Minutes

Quadratic time

Squared result in time for every increase in input

Input = {3,5,7,1,10,8}

Sorting 3



$O[N]$

Sorting 5



$O[N]$

⋮

Sorting 8



$O[N]$

$O[N]$

+

$O[N]$

+

$O[N]$

+

...

+

$O[N]$



$O[N*N]$

~

$O[N^2]$

Logarithmic time

Running time grows in proportion to the logarithm of the input size

Find the atmost divisible by 2 for the any given number



~

O[logn]

Some rules to remember

Different Steps Added

$O[a] + O[b] \Rightarrow O[a+b] \Rightarrow O[1]$

2 conditions outside the loop*

Drop Constants

$O[2N] \Rightarrow O[N]$

2 individual for loops*

Different inputs \Rightarrow Different variables

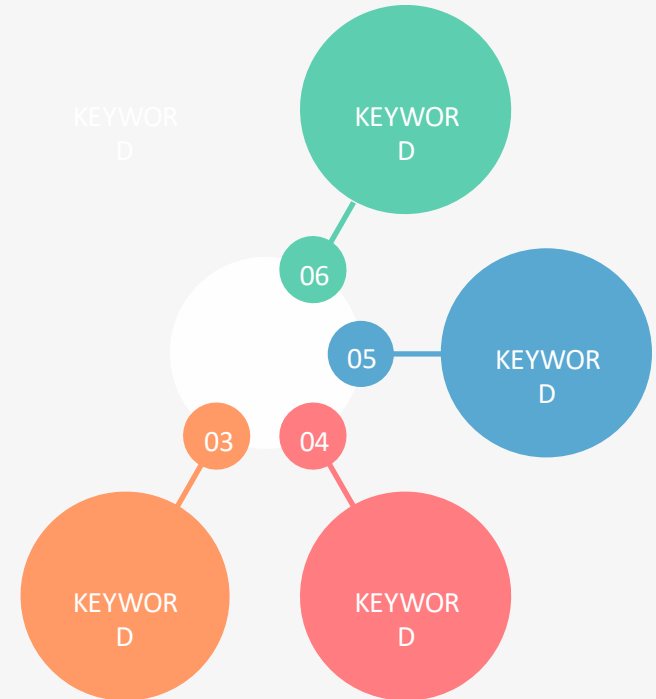
$O[NXM]$ Not equal to $O[N^2]$

2 for loops inner with different variables

Drop Non dominate terms

$O[N^2] + O[N] + O[1] \Rightarrow O[N^2]$

3 loops with one inner and one external and with one condition outside of all loop



Space Complexity

Constant Time

When we are adding two number programmatically

E.g.: $10 + 12 = 22$

$10 \Rightarrow$ **4 Bytes**

$12 \Rightarrow$ **4 Bytes**

$22 \Rightarrow$ **4 Bytes**

$4 + 4 + 4 \Rightarrow$ **12**

$12 \Rightarrow$ **$O[C]$** \sim **$O[1]$**

Linear time

Linear to the number of inputs and time

Input = {1,2,3,4,5,6,7,8,9,10}

1 => 4 Bytes

+

2 => 4 Bytes

+

...

+

10 => 4 Bytes

4 Bytes + 4 Bytes + ... + 4 Bytes => 40 Bytes



$O[N]$

Complexity

	Static Array	Dynamic Array
Access	$O(1)$	$O(1)$
Search	$O(n)$	$O(n)$
Insertion	N/A	$O(n)$
Appending	N/A	$O(1)$
Deletion	N/A	$O(n)$

First Problem

Given an array of integers, reverse the array without inbuilt function

5 Minutes