Untitled

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Calculating environment distances

- 1) Create fake environments
- Correlated with Env 1 (~ 0.5)
- Correlated with Env 2 (~ 0.5)
- Random environments with mean 0 and sd 1
- 2) Make sure each environment is standardized by subtracting the mean and dividing by the sd. (This should also be true for what is being put into GF)
- 3) Calculate the following between all populations (although technically, only needed for core and edge populations):
- Euclidean distance for selective environments
- Mahalanobis distance for selective environments
- Euclidean distance for ALL environments
- Mahalanobis distance for ALL environments

```
CGfit <- read.csv("Common_Garden_fit.csv")
Popsenv <- read.csv("Pops_env.csv")
head(CGfit)</pre>
```

```
##
     Transplant Home
                      Fitness
                                      D_CI
                                              D_CI_sel Env_sel1 Env_sel2
                                                                               dM
## 1
             T1
                  H1 0.790825 0.000000000 0.00000000
                                                                       -1 3.9996
                                                              -1
## 2
             T2
                  H1 0.817109 0.003351372 0.01194520
                                                                       -1 3.9996
                                                              -1
                  H1 0.711378 0.005807787 0.02071331
## 3
             Т3
                                                              -1
                                                                       -1 3.9996
                  H1 0.521529 0.012116530 0.04544032
## 4
             T4
                                                              -1
                                                                       -1 3.9996
## 5
             T5
                  H1 0.321762 0.016701773 0.05602929
                                                              -1
                                                                       -1 3.9996
## 6
                  H1 0.321762 0.016701773 0.05602929
                                                              -1
                                                                       -1 3.9996
```

```
head (Popsenv)
```

```
Pop envPop1 envPop2
##
## 1 P1
             -1.0
                         -1
## 2
      P2
             -0.5
                         -1
##
  3
      Р3
              0.0
                         -1
##
  4
      P4
              0.5
                         -1
      P5
               1.0
## 5
                         -1
               1.0
                         -1
```

Create fake environments

Here I am going to create 2 fake environments, each correlated about 0.5 with the selective environment.

In addition, I am going to create 10 more fake environments with a multivariate normal distribution. The covariance matrix for the mynorm was generated with a positive definite matrix/covariance matrix using the genPositiveDefMat function from the clusterGeneration package v1.3.4, using the unifcorrmat option. This generates the covariance matrix by sampling the correlation among variables from a uniform distribution. https://www.rdocumentation.org/packages/clusterGeneration/versions/1.3.4/topics/genPositiveDefMat

```
fakeEnv1 <- Popsenv$envPop1 + rnorm(nrow(Popsenv),0,1.3)</pre>
  # this standard deviation generally produces a correlation between 0.3 and 0.6
cor(Popsenv$envPop1, fakeEnv1)
## [1] 0.4488023
fakeEnv2 <- Popsenv$envPop2 + rnorm(nrow(Popsenv),0,1.3)</pre>
  # this standard deviation generally produces a correlation between 0.3 and 0.6
cor(Popsenv$envPop2, fakeEnv2)
## [1] 0.6069238
Popsenv$fakeEnv1 <- fakeEnv1
Popsenv$fakeEnv2 <- fakeEnv2
dim(Popsenv)
## [1] 100
nfake <- 10
Popsenv[,6:(5+nfake)] <- NA
head(Popsenv)
##
     Pop envPop1 envPop2
                           fakeEnv1 fakeEnv2 V6 V7 V8 V9 V10 V11 V12 V13 V14 V15
## 1
            -1.0
                     -1 -1.55766341 -1.218331 NA NA NA NA
                                                            NA
## 2
     P2
            -0.5
                      -1 -0.30192757 -3.453716 NA NA NA NA
                                                            NA
                                                               NA
                                                                   NA
                                                                       NA
                                                                           NA
                                                                                NA
## 3
     Р3
            0.0
                         0.07655442 -1.083442 NA NA NA NA
                                                            NA
                                                               NA
                                                                   NA
                                                                        NA
                                                                           NA
                                                                                NA
            0.5
## 4
     P4
                                                                       NA
                     -1 1.74133551 -1.534257 NA NA NA NA
                                                           NA
                                                               NA
                                                                   NA
                                                                           NA
                                                                                NA
## 5
     P5
            1.0
                     -1 1.06068083 -1.822725 NA NA NA NA
                                                           NΑ
                                                               NA
                                                                   NΑ
                                                                       NΑ
                                                                           NA
                                                                                NA
## 6 P6
             1.0
                     -1 -1.99403263 -0.799573 NA NA NA NA
                                                           NΑ
                                                               NA
                                                                   NA
                                                                       NΑ
                                                                           NΑ
                                                                               NA
# All I'm doing here is creating environments with a covariance structure
#cov1 <- genPositiveDefMat(nfake, covMethod="eigen", rangeVar=c(1,10))
cov1 <- genPositiveDefMat(nfake,covMethod="unifcorrmat" )</pre>
head(cov1)
## $egvalues
                                                    4.7695312 2.4840682
    [1] 14.3810019 12.3649794 8.1594124 5.3925970
##
    [7] 2.1885882 1.2331614 0.6088628
##
## $Sigma
                            [,2]
                                       [,3]
                                                              [,5]
##
                [,1]
                                                   [,4]
   [1,] 1.46934833 -0.00838753 0.7582294 -0.45018087 -0.7707050 -1.0488042
##
##
   [2,] -0.00838753 4.46040816 1.7888387 0.52981033 2.0275569 -0.9965486
   [3,] 0.75822936 1.78883871 7.1348158 -2.09661109 -0.2773871 -0.2540386
##
   [4,] -0.45018087
                     0.52981033 -2.0966111 5.68883846 0.4832758 0.4856977
##
   [5,] -0.77070500 2.02755687 -0.2773871 0.48327582 5.0120917 -0.8678556
   [6,] -1.04880420 -0.99654860 -0.2540386 0.48569769 -0.8678556 6.3739536
##
    [7,] \quad 0.80878943 \quad -2.78730276 \quad 0.5645447 \quad -2.90927683 \quad -0.6271381 \quad -1.7279472 
##
    [8,] 0.43752124 0.34746691 -1.3908978 -0.09202066 -1.0997294 0.5916816
   [9,] 0.82919724 2.42988097 4.9089904 -0.94865381 -1.8774159 -0.5038826
##
  [10,]
         ##
               [,7]
                           [,8]
                                      [,9]
                                                 [,10]
   [1,] 0.8087894 0.43752124
##
                                0.8291972
                                           0.00191363
##
  [2,] -2.7873028  0.34746691  2.4298810  0.58647739
  [3,] 0.5645447 -1.39089777 4.9089904 0.69480026
## [4,] -2.9092768 -0.09202066 -0.9486538 0.92950386
## [5,] -0.6271381 -1.09972936 -1.8774159 0.66266567
```

```
## [6,] -1.7279472 0.59168161 -0.5038826 -0.51071656
## [7,] 9.5153954 -1.83799111 0.2380995 0.51445578
## [8,] -1.8379911 2.87214294 -0.5554513 -0.61912632
## [9,] 0.2380995 -0.55545131 6.9670571 -0.28461817
## [10,] 0.5144558 -0.61912632 -0.2846182 2.40040127
a<- mvrnorm(nrow(Popsenv), mu=rep(0, nfake), Sigma=cov1$Sigma)
Popsenv[,6:(5+nfake)] <- a
head(Popsenv)
    Pop envPop1 envPop2
##
                          fakeEnv1 fakeEnv2
                                                     ۷6
                                                                ۷7
                                                                           V8
## 1 P1
           -1.0
                    -1 -1.55766341 -1.218331 2.48167095 -2.3266383 -0.9232911
                     -1 -0.30192757 -3.453716 1.54910583 -1.3225897 0.9342882
## 2 P2
           -0.5
## 3
     P3
            0.0
                     -1 0.07655442 -1.083442 0.92022721 1.2784248 -0.6983980
                    -1 1.74133551 -1.534257 -0.12918450 -0.6684629 -1.4975938
     P4
            0.5
## 4
## 5
    P5
            1.0
                    -1 1.06068083 -1.822725 -1.33633610 4.0341913 5.4891920
## 6 P6
            1.0
                     -1 -1.99403263 -0.799573 0.06213316 3.5631245 1.8600332
            ۷9
                     V10
                                V11
                                           V12
                                                     V13
##
## 1 -3.0389792 -0.1175726 -2.6641191 4.5741079 -1.1509603 -0.40881482
## 2 -1.3969036 -1.8124941 -5.4520813 4.4217774 0.7996067
                                                          0.05580681
## 4 -2.2031747 1.9988298 1.4831886 1.2658055 -0.1680325
                                                          0.10422659
## 5 -2.0126869 3.7003157 -6.9057437 -0.3406874 -3.8752309 2.04014323
## 6 1.8319891 3.2122041 -1.8588675 -1.0658706 -2.4939325 0.85259549
##
            V15
## 1 -2.91087895
## 2 2.26405947
## 3 -0.09874303
## 4 -2.88658319
## 5 2.34555500
## 6 1.64360227
tail(Popsenv)
##
       Pop envPop1 envPop2
                                                        ۷6
                                                                   ۷7
                             fakeEnv1
                                        fakeEnv2
## 95
       P95
               1.0
                       -1 0.76484523 -4.6654590 0.7039915 2.7391255
## 96
       P96
               1.0
                       -1 0.07741494 -1.8540389 0.7253867 4.6776082
## 97
       P97
               0.5
                       -1 -0.16833838 -1.7156925
                                                 1.8891493 -1.1020824
## 98
       P98
               0.0
                       -1 1.57707697 -0.4498347
                                                 1.1302106 -0.9258929
## 99
       P99
              -0.5
                       -1 -2.26708942 -2.5682792 -0.6513680 1.2355495
## 100 P100
              -1.0
                       -1 -2.60504819 -1.0895667 0.4221163 0.5499470
              ٧8
                       V9
##
                                V10
                                                     V12
                                                               V13
                                           V11
## 95
      -1.4752431 1.561699 1.5223218 2.5080179 -3.2920535 1.829966 -0.9090794
## 96
       2.3871361 2.033116 3.7923590 -3.1580239 0.5902527
                                                         1.180809 3.9866121
       1.1066143 2.975969 -1.2312342 -2.5732375 5.5336787 -3.068432 2.4378462
## 98
      -1.2135786 4.189807 -0.5734596 -4.8598584 3.4958394 -1.158432 -0.3223391
       4.7008175 4.283219 -1.0114508 -2.9191373 2.2528688 -2.821596 4.8388257
## 100 -0.7851984 3.484999 -3.1363250 0.5727394 -4.9115813 2.972367 1.8102608
##
## 95
       1.1043191816
## 96
      -0.9136777296
## 97
       1.9174247328
## 98
       0.0008324457
## 99
       3.3267511319
```

```
## 100 -0.1886744320

sel_env_cols <- 2:3
all_env_cols <- 2:ncol(Popsenv)
```

Standardize environments

```
head (Popsenv)
     Pop envPop1 envPop2
                            fakeEnv1 fakeEnv2
                                                        V6
                                                                   ۷7
                                                                              ٧8
## 1 P1
           -1.0
                     -1 -1.55766341 -1.218331 2.48167095 -2.3266383 -0.9232911
## 2
     P2
            -0.5
                     -1 -0.30192757 -3.453716 1.54910583 -1.3225897
     Р3
                      -1 0.07655442 -1.083442 0.92022721 1.2784248 -0.6983980
## 3
            0.0
## 4
     P4
            0.5
                         1.74133551 -1.534257 -0.12918450 -0.6684629 -1.4975938
## 5
     P5
            1.0
                     -1 1.06068083 -1.822725 -1.33633610 4.0341913 5.4891920
                      -1 -1.99403263 -0.799573 0.06213316
## 6
            1.0
                                                            3.5631245 1.8600332
##
            ۷9
                      V10
                                             V12
                                                        V13
                                                                    V14
                                  V11
## 1 -3.0389792 -0.1175726 -2.6641191
                                      4.5741079 -1.1509603 -0.40881482
## 2 -1.3969036 -1.8124941 -5.4520813 4.4217774 0.7996067
                                                             0.05580681
## 3 -0.2334544 0.7398533 -0.6867098 2.5490811 2.1866836
                                                             0.73516433
## 4 -2.2031747 1.9988298 1.4831886 1.2658055 -0.1680325
                                                             0.10422659
## 5 -2.0126869 3.7003157 -6.9057437 -0.3406874 -3.8752309
                                                             2.04014323
## 6 1.8319891 3.2122041 -1.8588675 -1.0658706 -2.4939325 0.85259549
##
## 1 -2.91087895
## 2 2.26405947
## 3 -0.09874303
## 4 -2.88658319
## 5 2.34555500
## 6 1.64360227
means <- colMeans(Popsenv[all_env_cols])</pre>
  # beware of hard coding columns here
sds <- apply(Popsenv[all_env_cols], 2, sd)</pre>
PopsenvStnd <- Popsenv
for (i in all_env_cols){
  PopsenvStnd[,i] <- (Popsenv[,i] - means[i-1])/sds[i-1]</pre>
head (PopsenvStnd)
##
            envPop1
                     envPop2
                                                              ۷6
     Pop
                                fakeEnv1
                                           fakeEnv2
## 1 P1 -1.4071247 -1.407125 -0.93917620 -0.7124808
                                                      2.09026753 -1.1305261
## 2 P2 -0.7035624 -1.407125 -0.04072126 -2.0437866 1.30380489 -0.6618167
## 3 P3 0.0000000 -1.407125 0.23007536 -0.6321463 0.77345100 0.5523877
         0.7035624 -1.407125 1.42119435 -0.9006337 -0.11155218 -0.3564575
     Р4
     P5
         1.4071247 -1.407125 0.93419896 -1.0724340 -1.12958257 1.8388333
         1.4071247 -1.407125 -1.25139002 -0.4630854 0.04979225 1.6189301
## 6
     P6
            V8
                       V9
                                   V10
                                              V11
                                                          V12
                                                                      V13
## 1 -0.1822761 -1.4732449 -0.06485067 -0.81207017
                                                   1.4145669 -0.64753382
## 2 0.4805639 -0.7410018 -0.83552324 -1.84712847
                                                    1.3668209 0.45957281
## 3 -0.1020275 -0.2221903 0.32501676 -0.07793756
                                                    0.7798497 1.24685267
## 4 -0.3872046 -1.1005385 0.89746727 0.72765847 0.3776244 -0.08964176
     2.1058905 -1.0155952 1.67112467 -2.38681489 -0.1259090 -2.19378073
## 6 0.8108976 0.6988432 1.44918266 -0.51311259 -0.3532078 -1.40978064
```

```
##
            V14
                        V15
## 1 -0.07983095 -2.1056939
## 2 0.11683709 1.4537763
## 3 0.40439992 -0.1714267
## 4 0.13733253 -2.0889826
## 5 0.95677979 1.5098312
## 6 0.45410693 1.0270081
# Check for mistakes
round(colMeans(PopsenvStnd[all_env_cols]))
    envPop1
                                                      ٧7
                                                               ٧8
                                                                        ۷9
            envPop2 fakeEnv1 fakeEnv2
                                             ۷6
##
                                             0
                                                       0
                                                                0
                                                                        0
##
         0
                   0
                            0
                                     0
##
        V10
                 V11
                          V12
                                   V13
                                            V14
                                                     V15
##
                   0
                            0
                                     0
                                                       0
          0
                                              0
round(apply(PopsenvStnd[all_env_cols], 2, sd))
                                                                        ۷9
            envPop2 fakeEnv1 fakeEnv2
                                             ۷6
                                                      ۷7
                                                               ٧8
##
    envPop1
##
          1
                   1
                            1
                                              1
                                                       1
                                                                1
                                                                        1
##
        V10
                 V11
                          V12
                                   V13
                                            V14
                                                     V15
##
          1
                   1
                            1
                                              1
                                                       1
round(cov(PopsenvStnd[,all_env_cols]),2)
            envPop1 envPop2 fakeEnv1 fakeEnv2
##
                                                 ۷6
                                                       ۷7
                                                             ٧8
                                                                   ۷9
                                                                        V10
                                                                              V11
## envPop1
               1.00
                      0.00
                                0.45
                                        -0.03 -0.08 0.15 0.19
                                                                0.01
                                                                      0.14
                                                                             0.06
## envPop2
              0.00
                       1.00
                               -0.14
                                        0.61 -0.02 -0.12 -0.26
                                                                0.08 -0.19
                                                                             0.17
## fakeEnv1
              0.45
                      -0.14
                                1.00
                                         0.06 -0.16 -0.07 -0.01 -0.10
                                                                      0.18
                                                                            0.03
## fakeEnv2
              -0.03
                               0.06
                                         1.00 -0.11 -0.08 -0.25 0.02 -0.04
                      0.61
                                                                            0.12
## V6
              -0.08
                      -0.02
                               -0.16
                                        -0.11 1.00 0.01 0.16 -0.13 -0.15 -0.50
## V7
               0.15
                      -0.12
                               -0.07
                                        -0.08 0.01 1.00 0.31
                                                                0.16
                                                                      0.51 - 0.27
## V8
                     -0.26
                               -0.01
                                       -0.25 0.16 0.31 1.00 -0.24
                                                                      0.05 -0.17
              0.19
## V9
              0.01
                      0.08
                               -0.10
                                        -0.19
                                        -0.04 -0.15 0.51 0.05 -0.05 1.00 -0.22
## V10
              0.14
                               0.18
## V11
              0.06
                      0.17
                               0.03
                                        0.12 -0.50 -0.27 -0.17 0.10 -0.22 1.00
                                       -0.17 0.30 -0.27 0.20 -0.42 0.00 -0.33
## V12
              0.06
                     -0.13
                               0.14
## V13
              -0.18
                      0.24
                               -0.12
                                        0.22 0.10 0.05 -0.44 0.12 -0.32 0.21
## V14
              0.11
                      -0.14
                               -0.12
                                        -0.24 0.21 0.43 0.71 -0.03 -0.18 -0.18
## V15
                      -0.01
                               -0.12
                                        -0.17 0.02 0.35
                                                         0.29 0.27 0.04 -0.25
              0.10
##
              V12
                   V13
                         V14
                               V15
## envPop1
            0.06 -0.18 0.11
                              0.10
## envPop2
           -0.13 0.24 -0.14 -0.01
## fakeEnv1 0.14 -0.12 -0.12 -0.12
## fakeEnv2 -0.17 0.22 -0.24 -0.17
## V6
            0.30 0.10 0.21 0.02
## V7
            -0.27 0.05 0.43
                              0.35
## V8
            0.20 -0.44 0.71
                              0.29
## V9
            -0.42 0.12 -0.03
## V10
            0.00 -0.32 -0.18 0.04
## V11
            -0.33 0.21 -0.18 -0.25
## V12
            1.00 -0.41 0.19 0.06
## V13
            -0.41 1.00 -0.20 -0.18
            0.19 -0.20 1.00 0.20
## V14
## V15
            0.06 -0.18 0.20
```

Understand CG fit

In this dataframe, it appears Home is the site of the common garden. Transplant is the location that the genotype came from Fitness is the average fitness of the individuals from the source location

```
D_CI is GF offset genome?
```

D_CI_sel is GF_offset for the causal loci?

```
head(CGfit)
```

```
##
     Transplant Home
                      Fitness
                                      D_CI
                                              D_CI_sel Env_sel1 Env_sel2
                                                                              dM
## 1
                  H1 0.790825 0.000000000 0.00000000
                                                                       -1 3.9996
             T1
                                                              -1
## 2
             T2
                  H1 0.817109 0.003351372 0.01194520
                                                              -1
                                                                       -1 3.9996
## 3
             Т3
                  H1 0.711378 0.005807787 0.02071331
                                                              -1
                                                                       -1 3.9996
## 4
             T4
                  H1 0.521529 0.012116530 0.04544032
                                                              -1
                                                                       -1 3.9996
## 5
             T5
                  H1 0.321762 0.016701773 0.05602929
                                                              -1
                                                                       -1 3.9996
## 6
             T6
                  H1 0.321762 0.016701773 0.05602929
                                                              -1
                                                                       -1 3.9996
```

Understanding Mahalanobis

?mahalanobis We are interested in calculating the Mahalanobis distance between pop1 and pop2, while controlling for the covariance among the environmental variables in the population

Let's look at an example where we take the Md between population 1 and population 50, for all the environments

```
(envpop1 <- PopsenvStnd[1,all_env_cols])</pre>
```

```
##
       envPop1
                  envPop2
                            fakeEnv1
                                        fakeEnv2
                                                        V6
                                                                   V7
                                                                               ۷8
## 1 -1.407125 -1.407125 -0.9391762 -0.7124808 2.090268 -1.130526 -0.1822761
##
            ۷9
                        V10
                                    V11
                                              V12
                                                          V13
                                                                      V14
                                                                                 V15
## 1 -1.473245 -0.06485067 -0.8120702 1.414567 -0.6475338 -0.07983095 -2.105694
(envpop2 <- PopsenvStnd[50,all_env_cols])</pre>
```

```
## envPop1 envPop2 fakeEnv1 fakeEnv2 V6 V7 V8
## 50 -1.407125 1.407125 0.1375876 0.7334861 0.01697772 -1.794801 -0.1612388
## V9 V10 V11 V12 V13 V14 V15
## 50 0.2092681 -0.6145491 0.08241598 0.6354016 -0.3926396 -0.01581013 0.1863589
```

```
# We calculate the covariance based on the entire landscape:
cov_allEnv <- cov(PopsenvStnd[,all_env_cols])
round(cov_allEnv,2)</pre>
```

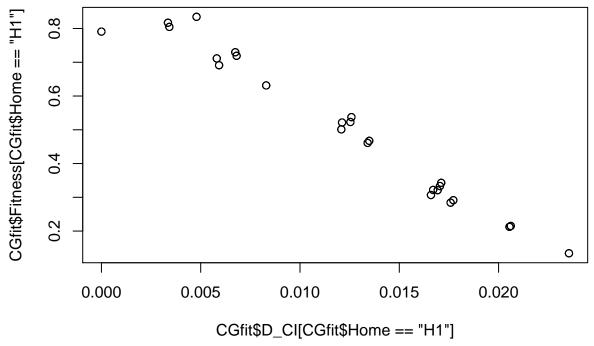
```
##
            envPop1 envPop2 fakeEnv1 fakeEnv2
                                                   ۷6
                                                         ۷7
                                                               V8
                                                                      ۷9
                                                                           V10
                                                                                 V11
## envPop1
               1.00
                        0.00
                                 0.45
                                         -0.03 -0.08
                                                      0.15
                                                             0.19
                                                                   0.01
                                                                          0.14
                                                                                0.06
## envPop2
               0.00
                       1.00
                                -0.14
                                          0.61 -0.02 -0.12 -0.26
                                                                   0.08 - 0.19
                                                                                0.17
                       -0.14
                                 1.00
                                          0.06 -0.16 -0.07 -0.01 -0.10
## fakeEnv1
               0.45
                                                                          0.18
                                                                                0.03
## fakeEnv2
              -0.03
                       0.61
                                 0.06
                                          1.00 -0.11 -0.08 -0.25
                                                                   0.02 - 0.04
                                                                                0.12
## V6
              -0.08
                       -0.02
                                -0.16
                                         -0.11 1.00 0.01 0.16 -0.13 -0.15 -0.50
## V7
               0.15
                       -0.12
                                -0.07
                                         -0.08 0.01
                                                      1.00
                                                            0.31
                                                                   0.16
                                                                          0.51 - 0.27
## V8
               0.19
                       -0.26
                                -0.01
                                         -0.25 0.16
                                                      0.31
                                                             1.00 -0.24
                                                                          0.05 - 0.17
## V9
               0.01
                       0.08
                                -0.10
                                          0.02 -0.13
                                                       0.16 - 0.24
                                                                   1.00 -0.05
                       -0.19
                                 0.18
                                         -0.04 -0.15 0.51 0.05 -0.05
                                                                          1.00 -0.22
## V10
               0.14
                                 0.03
                                          0.12 -0.50 -0.27 -0.17
## V11
               0.06
                       0.17
                                                                   0.10 -0.22 1.00
## V12
               0.06
                       -0.13
                                 0.14
                                         -0.17 0.30 -0.27
                                                             0.20 -0.42 0.00 -0.33
## V13
              -0.18
                       0.24
                                -0.12
                                          0.22
                                                0.10
                                                       0.05 - 0.44
                                                                   0.12 -0.32 0.21
                                         -0.24 0.21 0.43 0.71 -0.03 -0.18 -0.18
## V14
               0.11
                       -0.14
                                -0.12
```

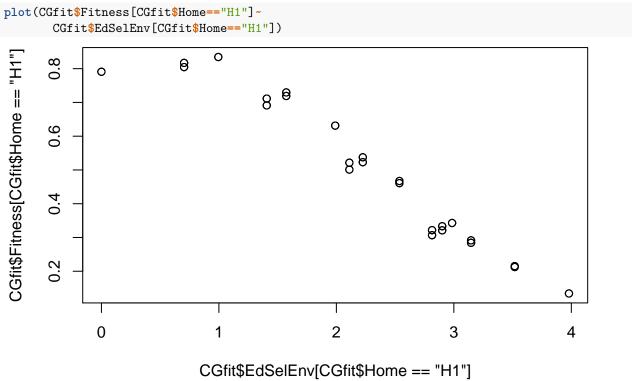
```
## V15
              0.10
                    -0.01
                              -0.12
                                       -0.17 0.02 0.35 0.29 0.27 0.04 -0.25
##
             V12
                   V13
                        V14
                               V15
            0.06 -0.18 0.11 0.10
## envPop1
## envPop2 -0.13 0.24 -0.14 -0.01
## fakeEnv1 0.14 -0.12 -0.12 -0.12
## fakeEnv2 -0.17 0.22 -0.24 -0.17
## V6
            0.30 0.10 0.21 0.02
           -0.27 0.05 0.43 0.35
## V7
## V8
            0.20 -0.44 0.71 0.29
## V9
           -0.42 0.12 -0.03 0.27
## V10
            0.00 -0.32 -0.18 0.04
## V11
           -0.33 0.21 -0.18 -0.25
## V12
            1.00 -0.41 0.19 0.06
## V13
           -0.41 1.00 -0.20 -0.18
## V14
            0.19 -0.20 1.00 0.20
## V15
            0.06 -0.18 0.20 1.00
mahalanobis(as.numeric(envpop1),
           as.numeric(envpop2),
           cov_allEnv)
## [1] 30.95207
# sanity check
mahalanobis(as.numeric(envpop1),
           as.numeric(envpop1),
           cov_allEnv)
## [1] 0
#compare to eucl.
dist(rbind(envpop1, envpop2))
## 50 5.076738
Calculate environment distances
cov_allEnv <- cov(PopsenvStnd[,all_env_cols])</pre>
cov selEnv <- cov(PopsenvStnd[,sel env cols])</pre>
head(PopsenvStnd)
    Pop
           envPop1
                    envPop2
                                fakeEnv1
                                           fakeEnv2
## 1 P1 -1.4071247 -1.407125 -0.93917620 -0.7124808 2.09026753 -1.1305261
## 2 P2 -0.7035624 -1.407125 -0.04072126 -2.0437866 1.30380489 -0.6618167
## 3 P3 0.0000000 -1.407125 0.23007536 -0.6321463 0.77345100 0.5523877
     P4 0.7035624 -1.407125 1.42119435 -0.9006337 -0.11155218 -0.3564575
## 5
    P5 1.4071247 -1.407125 0.93419896 -1.0724340 -1.12958257 1.8388333
## 6 P6 1.4071247 -1.407125 -1.25139002 -0.4630854 0.04979225 1.6189301
##
            V8
                       ۷9
                                  V10
                                              V11
                                                         V12
## 1 -0.1822761 -1.4732449 -0.06485067 -0.81207017 1.4145669 -0.64753382
## 2 0.4805639 -0.7410018 -0.83552324 -1.84712847
                                                  1.3668209 0.45957281
## 3 -0.1020275 -0.2221903 0.32501676 -0.07793756 0.7798497 1.24685267
## 4 -0.3872046 -1.1005385 0.89746727 0.72765847
                                                  0.3776244 -0.08964176
## 5 2.1058905 -1.0155952 1.67112467 -2.38681489 -0.1259090 -2.19378073
```

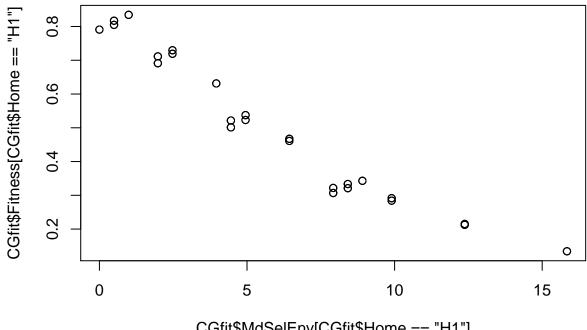
```
## 6 0.8108976 0.6988432 1.44918266 -0.51311259 -0.3532078 -1.40978064
##
            V14
                       V15
## 1 -0.07983095 -2.1056939
## 2 0.11683709 1.4537763
## 3 0.40439992 -0.1714267
## 4 0.13733253 -2.0889826
## 5 0.95677979 1.5098312
## 6 0.45410693 1.0270081
CGfit$EdSelEnv <- NA
  # Euclidean distance for selective environments
CGfit$MdSelEnv <- NA
  # Mahalanobis distance for selective environments
CGfit$EdAllEnv <- NA
  # Euclidean distance for ALL environments
CGfit$MdAllEnv <- NA
  # Mahalanobis distance for ALL environments
head(CGfit)
     Transplant Home Fitness
                                          D CI sel Env sel1 Env sel2
                                    D CI
## 1
         T1
                 H1 0.790825 0.000000000 0.00000000 -1
                                                                  -1 3.9996
## 2
            T2 H1 0.817109 0.003351372 0.01194520
                                                         -1
                                                                  -1 3.9996
            T3 H1 0.711378 0.005807787 0.02071331
## 3
                                                        -1
                                                                   -1 3.9996
                 H1 0.521529 0.012116530 0.04544032
                                                         -1
## 4
            T4
                                                                   -1 3.9996
            T5 H1 0.321762 0.016701773 0.05602929
                                                        -1
## 5
                                                                  -1 3.9996
## 6
            T6 H1 0.321762 0.016701773 0.05602929
                                                        -1
                                                                  -1 3.9996
   EdSelEnv MdSelEnv EdAllEnv MdAllEnv
## 1
          NA
                   NA
                            NA
## 2
          NA
                  NA
                           NA
                                     NA
## 3
         NA
                                     NA
                 NA
                           NA
## 4
          NA
                   NA
                            NA
                                     NA
## 5
          NA
                   NΑ
                            NA
                                     NA
## 6
          NA
                            NA
for (i in 1:nrow(CGfit)){
  # get the row in PopsenvStnd for the transplant genotype
 row1 = which(PopsenvStnd==gsub("T","P",as.character(CGfit$Transplant[i])))
    # get the row in PopsenvStnd for the common garden location
 row2 = which(PopsenvStnd==gsub("H","P",as.character(CGfit$Home[i])))
  # Look up the envi
  (envpop1_all <- PopsenvStnd[row1,all_env_cols])</pre>
  (envpop2_all <- PopsenvStnd[row2,all_env_cols])</pre>
  # Look up the envi
  (envpop1_sel <- PopsenvStnd[row1,sel_env_cols])</pre>
  (envpop2 sel <- PopsenvStnd[row2,sel env cols])</pre>
  # BEWARE HARD CODING
  ### Calculate the environmental distance between the two rows
```

Calculate environment distances

```
head(CGfit)
    Transplant Home Fitness
                                   D_CI_sel Env_sel1 Env_sel2
                               D_CI
                                                               dM
          T1 H1 0.790825 0.000000000 0.00000000
                                               -1
                                                         -1 3.9996
## 1
                                                 -1
## 2
          T2 H1 0.817109 0.003351372 0.01194520
                                                         -1 3.9996
## 3
         T3 H1 0.711378 0.005807787 0.02071331
                                                -1
                                                         -1 3.9996
         T4 H1 0.521529 0.012116530 0.04544032
                                                -1
## 4
                                                         -1 3.9996
                                                -1
-1
          T5 H1 0.321762 0.016701773 0.05602929
                                                         -1 3.9996
## 5
          T6 H1 0.321762 0.016701773 0.05602929
## 6
                                                         -1 3.9996
##
     EdSelEnv MdSelEnv EdAllEnv MdAllEnv
## 1 0.0000000 0.000 0.000000 0.00000
## 3 1.4071247 1.980 4.260254 18.13383
## 5 2.8142495
               7.920 7.784134 45.89380
## 6 2.8142495
               7.920 6.457067 26.25406
#any missing data?
sum(!complete.cases(CGfit))
## [1] 0
# should be 0
plot(CGfit$Fitness[CGfit$Home=="H1"]~
     CGfit$D CI[CGfit$Home=="H1"])
```

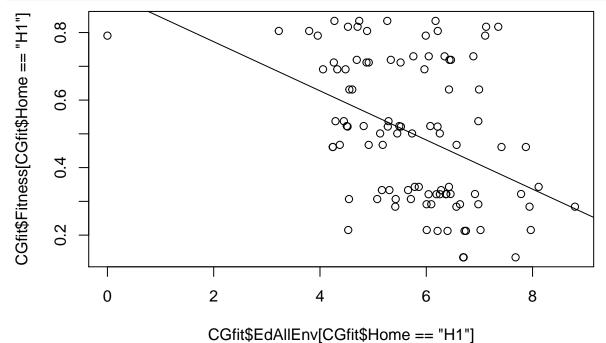






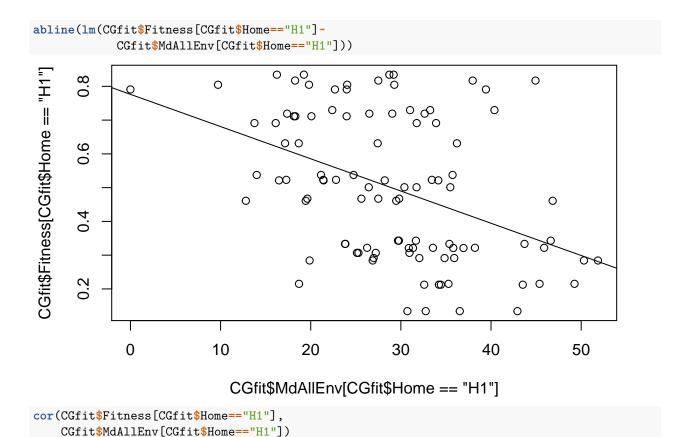
CGfit\$MdSelEnv[CGfit\$Home == "H1"]

```
plot(CGfit$Fitness[CGfit$Home=="H1"]~
       CGfit$EdAllEnv[CGfit$Home=="H1"])
abline(lm(CGfit$Fitness[CGfit$Home=="H1"]~
            CGfit$EdAllEnv[CGfit$Home=="H1"]))
```



```
(cor(CGfit$Fitness[CGfit$Home=="H1"],
    CGfit$EdAllEnv[CGfit$Home=="H1"]))
```

```
## [1] -0.4265559
plot(CGfit$Fitness[CGfit$Home=="H1"]~
       CGfit$MdAllEnv[CGfit$Home=="H1"])
```



[1] -0.4253841

Results for Euclidean Dist and Mahalanobis are similar because we standardize the environments to have an SD=1 prior to analysis

Some notes:

When I first started, I had 2 fake environments (each correlated with one of the selective environments) and 1 random fake environment. This decreased the correlation between EdAllEnv and Fitness, but only slightly (cor \sim -0.8)

Then, I increased it to 10 random fake environments (with no correlation structure), which decreased it more $(cor \sim -0.5)$

Then, I added covariance structure to the environments, which decreased it more (cor \sim -0.35)

I think we should use the type of environmental data that I generated here, because it retains some realism that is present in empirical data