# Untitled

KE Lotterhos
9/18/2020

## Calculating environment distances

- 1) Create 3 fake environments
- Correlated with Env 1 ( $\sim 0.5$ )
- Correlated with Env 2 ( $\sim 0.5$ )
- A random environment with mean 0 and sd 1
- 2) Make sure each environment is standardized by subtracting the mean and dividing by the sd. (This should also be true for what is being put into GF)
- 3) Calculate the following between all populations (although technically, only needed for core and edge populations):
- Euclidean distance for selective environments
- Mahalanobis distance for selective environments
- Euclidean distance for ALL environments
- Mahalanobis distance for ALL environments

```
CGfit <- read.csv("Common_Garden_fit.csv")
Popsenv <- read.csv("Pops_env.csv")
head(CGfit)</pre>
```

```
##
     Transplant Home Fitness
                                     D_CI
                                             D_CI_sel Env_sel1 Env_sel2
                                                                             dM
## 1
             T1
                  H1 0.790825 0.000000000 0.00000000
                                                            -1
                                                                     -1 3.9996
## 2
                  H1 0.817109 0.003351372 0.01194520
                                                            -1
                                                                     -1 3.9996
                  H1 0.711378 0.005807787 0.02071331
                                                            -1
                                                                      -1 3.9996
             Т3
## 3
             T4
                  H1 0.521529 0.012116530 0.04544032
                                                                      -1 3.9996
## 4
                                                            -1
## 5
             T5
                  H1 0.321762 0.016701773 0.05602929
                                                            -1
                                                                     -1 3.9996
## 6
                  H1 0.321762 0.016701773 0.05602929
                                                            -1
                                                                     -1 3.9996
```

```
head(Popsenv)
```

```
Pop envPop1 envPop2
##
## 1 P1
             -1.0
## 2 P2
             -0.5
                        -1
      P3
              0.0
                        -1
## 3
      P4
              0.5
                        -1
      P5
              1.0
                        -1
## 5
              1.0
                        -1
```

#### Create fake environments

```
fakeEnv1 <- Popsenv$envPop1 + rnorm(nrow(Popsenv),0,1.3)
# this standard deviation generally produces a correlation between 0.3 and 0.6
cor(Popsenv$envPop1, fakeEnv1)</pre>
```

```
## [1] 0.5616083
```

```
fakeEnv2 <- Popsenv$envPop2 + rnorm(nrow(Popsenv),0,1.3)</pre>
  # this standard deviation generally produces a correlation between 0.3 and 0.6
cor(Popsenv$envPop2, fakeEnv2)
## [1] 0.3862077
fakeEnv3 <- rnorm(nrow(Popsenv),0,1)</pre>
Popsenv$fakeEnv1 <- fakeEnv1
Popsenv$fakeEnv2 <- fakeEnv2
Popsenv$fakeEnv3 <- fakeEnv3
Standardize environments
head(Popsenv)
     Pop envPop1 envPop2
##
                           fakeEnv1
                                      fakeEnv2
                                                  fakeEnv3
## 1 P1
            -1.0
                     -1 0.1527746 -1.6615225 -0.01140918
## 2
     P2
            -0.5
                      -1 -1.0136145 -1.6879409 -0.02823955
            0.0
## 3 P3
                     -1 -2.7328556 -0.5389532 0.47746168
## 4 P4
            0.5
                      -1 1.2059191 -0.8469736 -0.69761620
                      -1 2.6030965 -0.9246118 0.96673902
## 5 P5
            1.0
## 6 P6
             1.0
                      -1 0.6163429 -2.0746797 -0.95398558
means <- colMeans(Popsenv[2:6])</pre>
  # beware of hard coding columns here
sds <- apply(Popsenv[2:6], 2, sd)</pre>
PopsenvStnd <- Popsenv
for (i in 2:6){
  PopsenvStnd[,i] <- (Popsenv[,i] - means[i-1])/sds[i-1]</pre>
head(PopsenvStnd)
    Pop
                      envPop2
                                            fakeEnv2
                                                        fakeEnv3
            envPop1
                                 fakeEnv1
## 1 P1 -1.4071247 -1.407125 0.08864111 -1.0259992 0.08492709
## 2 P2 -0.7035624 -1.407125 -0.75098240 -1.0430964 0.06844054
## 3 P3 0.0000000 -1.407125 -1.98857549 -0.2995067 0.56381119
## 4 P4 0.7035624 -1.407125 0.84674562 -0.4988481 -0.58726194
## 5 P5 1.4071247 -1.407125 1.85250164 -0.5490931 1.04309346
## 6 P6 1.4071247 -1.407125 0.42234001 -1.2933819 -0.83839414
# Check for mistakes
round(colMeans(PopsenvStnd[2:6]))
    envPop1 envPop2 fakeEnv1 fakeEnv2 fakeEnv3
##
##
          0
                   0
                            0
round(apply(PopsenvStnd[2:6], 2, sd))
##
   envPop1 envPop2 fakeEnv1 fakeEnv2 fakeEnv3
```

##

1

1

1

1

#### Understand CG fit

In this dataframe, it appears Home is the site of the common garden. Transplant is the location that the genotype came from Fitness is the average fitness of the individuals from the source location

```
D_CI is GF_offset_genome
```

D\_CI\_sel is GF\_offset for the causal loci

```
head(CGfit)
```

```
##
     Transplant Home Fitness
                                      D_CI
                                             D_CI_sel Env_sel1 Env_sel2
                                                                             dM
## 1
                  H1 0.790825 0.000000000 0.00000000
                                                                      -1 3.9996
             T1
                                                            -1
## 2
             T2
                  H1 0.817109 0.003351372 0.01194520
                                                            -1
                                                                      -1 3.9996
## 3
             Т3
                  H1 0.711378 0.005807787 0.02071331
                                                            -1
                                                                      -1 3.9996
## 4
             T4
                  H1 0.521529 0.012116530 0.04544032
                                                            -1
                                                                      -1 3.9996
## 5
             T5
                  H1 0.321762 0.016701773 0.05602929
                                                            -1
                                                                      -1 3.9996
## 6
             T6
                  H1 0.321762 0.016701773 0.05602929
                                                            -1
                                                                      -1 3.9996
```

### **Understanding Mahalanobis**

?mahalanobis We are interested in calculating the Mahalanobis distance between pop1 and pop2, while controlling for the covariance among the environmental variables in the population

Let's look at an example where we take the Md between population 1 and population 50, for all the environments

```
(envpop1 <- PopsenvStnd[1,2:6])</pre>
##
       envPop1
                 envPop2
                            fakeEnv1 fakeEnv2
                                                  fakeEnv3
## 1 -1.407125 -1.407125 0.08864111 -1.025999 0.08492709
(envpop2 <- PopsenvStnd[50,2:6])
        envPop1 envPop2
##
                            fakeEnv1 fakeEnv2 fakeEnv3
## 50 -1.407125 1.407125 -0.4140336 -1.175834 -1.791025
# We calculate the covariance based on the entire landscape:
cov_allEnv <- cov(PopsenvStnd[,2:6])</pre>
round(cov_allEnv,2)
##
            envPop1 envPop2 fakeEnv1 fakeEnv2 fakeEnv3
## envPop1
               1.00
                        0.00
                                 0.56
                                           0.14
                                                   -0.13
## envPop2
               0.00
                        1.00
                                -0.02
                                           0.39
                                                   -0.06
## fakeEnv1
               0.56
                       -0.02
                                 1.00
                                           0.03
                                                    0.12
## fakeEnv2
               0.14
                        0.39
                                 0.03
                                           1.00
                                                   -0.11
## fakeEnv3
              -0.13
                      -0.06
                                 0.12
                                          -0.11
                                                    1.00
mahalanobis(as.numeric(envpop1),
            as.numeric(envpop2),
            cov_allEnv)
## [1] 13.21649
# sanity check
mahalanobis(as.numeric(envpop1),
            as.numeric(envpop1),
            cov_allEnv)
```

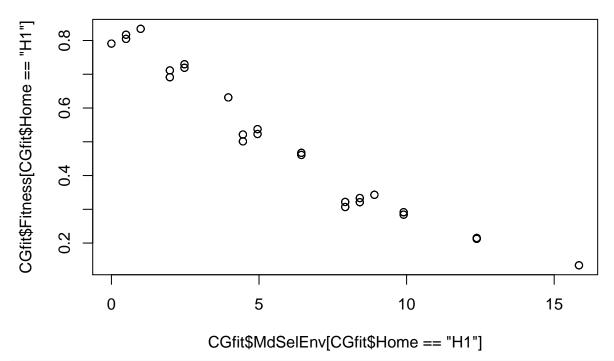
```
#compare to eucl.
dist(rbind(envpop1, envpop2))
## 50 3.42262
Calculate environment distances
cov_allEnv <- cov(PopsenvStnd[,2:6])</pre>
cov_selEnv <- cov(PopsenvStnd[,2:3])</pre>
  # BEWARE HARD CODING HERE for selective envis.
head(PopsenvStnd)
##
     Pop
           envPop1
                     envPop2
                                fakeEnv1
                                           fakeEnv2
                                                       fakeEnv3
## 1 P1 -1.4071247 -1.407125 0.08864111 -1.0259992 0.08492709
## 2 P2 -0.7035624 -1.407125 -0.75098240 -1.0430964 0.06844054
## 3 P3 0.0000000 -1.407125 -1.98857549 -0.2995067 0.56381119
## 4 P4 0.7035624 -1.407125 0.84674562 -0.4988481 -0.58726194
## 5 P5 1.4071247 -1.407125 1.85250164 -0.5490931 1.04309346
## 6 P6 1.4071247 -1.407125 0.42234001 -1.2933819 -0.83839414
CGfit$EdSelEnv <- NA
  # Euclidean distance for selective environments
CGfit$MdSelEnv <- NA
  # Mahalanobis distance for selective environments
CGfit$EdAllEnv <- NA
  # Euclidean distance for ALL environments
CGfit$MdAllEnv <- NA
  # Mahalanobis distance for ALL environments
head(CGfit)
     Transplant Home Fitness
                                    dM
##
                 H1 0.790825 0.000000000 0.00000000
                                                                  -1 3.9996
## 1
            T1
                                                         -1
                 H1 0.817109 0.003351372 0.01194520
                                                                  -1 3.9996
## 2
            T2
## 3
            Т3
                 H1 0.711378 0.005807787 0.02071331
                                                         -1
                                                                  -1 3.9996
## 4
            T4
                 H1 0.521529 0.012116530 0.04544032
                                                         -1
                                                                  -1 3.9996
                 H1 0.321762 0.016701773 0.05602929
                                                         -1
                                                                  -1 3.9996
                                                         -1
                 H1 0.321762 0.016701773 0.05602929
                                                                  -1 3.9996
## 6
            T6
    EdSelEnv MdSelEnv EdAllEnv MdAllEnv
##
## 1
          NA
                  NA
                            NA
## 2
          NA
                   NA
                            NA
                                     NA
## 3
                                     NA
          NA
                   NA
                            NA
## 4
          NA
                   NA
                            NA
                                     NA
## 5
          NA
                   NA
                            NA
                                     NA
## 6
          NA
                   NΑ
                            NΑ
                                     NA
for (i in 1:nrow(CGfit)){
  # get the row in PopsenvStnd for the transplant genotype
 row1 = which(PopsenvStnd==gsub("T","P",as.character(CGfit$Transplant[i])))
    # get the row in PopsenvStnd for the common garden location
```

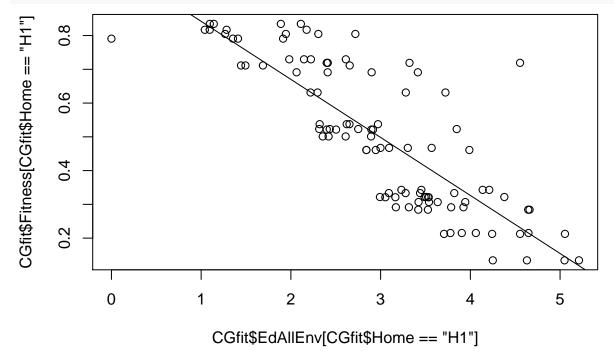
```
row2 = which(PopsenvStnd==gsub("H","P",as.character(CGfit$Home[i])))
# Look up the envi
(envpop1_all <- PopsenvStnd[row1,2:6])</pre>
(envpop2_all <- PopsenvStnd[row2,2:6])</pre>
# Look up the envi
(envpop1_sel <- PopsenvStnd[row1,2:3])</pre>
(envpop2 sel <- PopsenvStnd[row2,2:3])</pre>
# BEWARE HARD CODING
### Calculate the environmental distance between the two rows
CGfit$EdSelEnv[i] <- dist(rbind(envpop1_sel,</pre>
                                  envpop2_sel))
# Euclidean distance for selective environments
CGfit$MdSelEnv[i] <- mahalanobis(as.numeric(envpop1_sel),</pre>
          as.numeric(envpop2_sel),
          cov_selEnv)
# Mahalanobis distance for selective environments
CGfit$EdAllEnv[i] <- dist(rbind(envpop1_all,</pre>
                                  envpop2_all))
# Euclidean distance for ALL environments
CGfit$MdAllEnv[i] <- mahalanobis(as.numeric(envpop1_all),
          as.numeric(envpop2_all),
          cov allEnv)
# Mahalanobis distance for ALL environments
```

#### Calculate environment distances

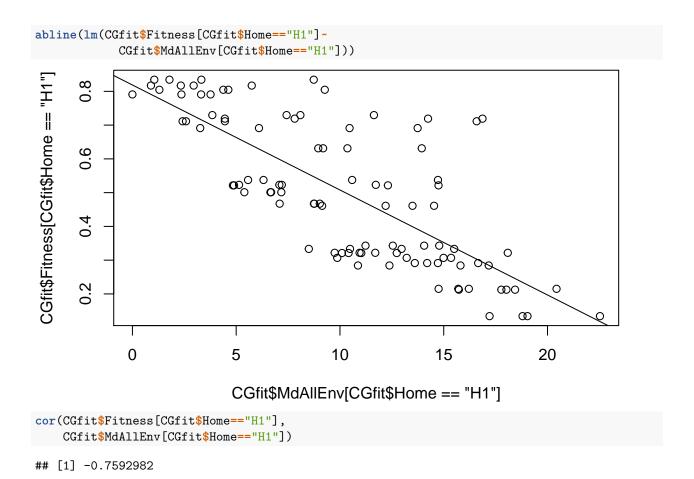
```
head(CGfit)
##
   Transplant Home Fitness
                            D_CI D_CI_sel Env_sel1 Env_sel2
## 1
         T1 H1 0.790825 0.000000000 0.00000000 -1 -1 3.9996
## 2
         T2 H1 0.817109 0.003351372 0.01194520
                                             -1
                                                    -1 3.9996
                                            -1
         T3 H1 0.711378 0.005807787 0.02071331
## 3
                                                    -1 3.9996
                                             -1
## 4
         T4 H1 0.521529 0.012116530 0.04544032
                                                    -1 3.9996
                                                    -1 3.9996
## 5
         T5 H1 0.321762 0.016701773 0.05602929
                                             -1
## 6
             H1 0.321762 0.016701773 0.05602929
                                             -1
                                                    -1 3.9996
    EdSelEnv MdSelEnv EdAllEnv MdAllEnv
##
## 1 0.0000000 0.000 0.000000 0.000000
## 3 1.4071247 1.980 2.655551 16.587568
## 4 2.1106871   4.455 2.399885   4.843426
#any missing data?
sum(!complete.cases(CGfit))
```

```
## [1] 0
# should be 0
plot(CGfit$Fitness[CGfit$Home=="H1"]~
        CGfit$D_CI[CGfit$Home=="H1"])
CGfit$Fitness[CGfit$Home == "H1"]
                               0
       0.8
                          ଡ
               0
                                  8 8
                                           0
       9.0
                                                       88
       0.4
       0.2
                                                                                   0
                                                                                             0
            0.000
                                             0.010
                                                              0.015
                             0.005
                                                                               0.020
                                   CGfit$D_CI[CGfit$Home == "H1"]
plot(CGfit$Fitness[CGfit$Home=="H1"]~
        CGfit$EdSelEnv[CGfit$Home=="H1"])
CGfit$Fitness[CGfit$Home == "H1"]
                                  0
       0.8
                             8
               0
                                              8
                                          8
                                                      0
       9.0
                                                        88
                                                                 0
       0.4
                                                                      88°
       0.2
                                                                                    0
                                                                                             0
                                                      2
                                   1
               0
                                                                          3
                                                                                             4
                                CGfit$EdSelEnv[CGfit$Home == "H1"]
plot(CGfit$Fitness[CGfit$Home=="H1"]~
        CGfit$MdSelEnv[CGfit$Home=="H1"])
```





CGfit\$MdAllEnv[CGfit\$Home=="H1"])



Results for Euclidean Dist and Mahalanobis are similar because we standardize the environments to have an SD=1 prior to analysis