

ALGO 1 : Project

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1 PART 1 : THE SNOWFLOW PROBLEM

A snowplow must clean the snow in front of 1000 houses. The position of each house is represented by a float number (not necessary positive). Initially, the snowplow is in 0. The traveling time of the snowplow is equivalent to the distance that it went through since the beginning of the day. If there are several houses at the same point, it does not take a longer time to clean the snow (the snow is cleaned as soon as the snowplow has passed). However, since the positions of the houses are represented as floats, this should not happen often.

The snowplow must minimize the average waiting time before the snow is cleaned in front of the houses, **from the point of view of the houses**.

A polynomial algorithm based on the positions of the houses must be determined to establish a strategy. If it is not polynomial (if it is exponential for example) we saw in class that it probably could not run.

Conventions : You must write a function that takes as input the positions of the 1000 houses, and outputs the positions of the houses, sorted in the same order as they are cleaned.

Name of the function : `parcours(list)`

returns : list of sorted houses in the relevant order.

test : I generate random initial positions of houses with a normal distribution centered in 0, with `numpy.random.normal(0,1000,1000).tolist()`, and then I statistically evaluate the performance of your algorithm. So `parcours()` receives a **python list** as an argument.

You are encouraged to use python. If you prefer to use another language, you need to ensure that your program can be used from python. I am not sure if it is convenient to do so, but some projects seem to exist <https://cpp.developpez.com/tutoriels/interfacer-cpp-python/>.

I test your solution and compare it to several benchmarks. Your solution should give a waiting time that is smaller to 90 percents of the time that we would obtain with the greedy solution, consisting in going to the closest house at each step.

Please note that you can test your solution yourself, by also implementing the greedy solution, and comparing the results with your solution.

Important : You must add a document to your project explaining why your algorithm runs in polynomial time. A pdf file is preferred. You don't have to be extremely formal, but clear enough to show that you understand why your solution is polynomial.

2 PART 2 : THEORETICAL NOTIONS

You may choose between one of the two following options :

Option 1 : Pick a heuristic of your choice for the coloring problem and implement this heuristic on a reasonable instance (small enough that would run quickly on a normal machine). For instance you can use a graph with around 50 vertices and 100 edges or so. It is required that you provide images illustrating your heuristic, for instance generated with graphviz or networkx.

Option 2 : Write a program that build the line graph of a graph and explain the connection between the Hamiltonian path problem, the Eulerian path problem, and line graphs, with your words and images.

3 ORGANISATION

The project is optional and may provide 2 additional credits. You can send it to me by email as a compressed folder or a link to a repository.

Number of students per group : 1 or 2.

The deadline for submitting the project is **March 22th 2020**

You can reach me by email if you have questions.