

Magnetic mapping using a trailed magnetometer

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The realization of a magnetic map of a terrain is a powerful tool especially used in mine warfare. This cartography can be done with a magnetometer, but the task is quite difficult. This is why it is useful to use robots to make this cartography. The problem induced by this solution is the addition of magnetic disturbances related to the structure of the robot and its actuators. It is then possible to drag the magnetometer on a sled behind the robot.

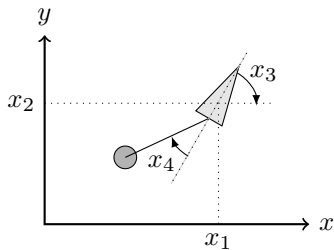
Magnetic | Mapping | Control | Interval Analysis
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Modelisation of the system

The system is composed of a vehicle that will drag a sledge that transports a magnetometer. The towing vehicle is a tank type vehicle, and the sled is attached to it with a rope. Assuming that the rope is constantly under tension, we are able to find the equations describing the dynamics of the system. By noting x the state of the system and u its inputs, the dynamics of the system is described by :

$$\dot{x} = f(x, u) = \begin{cases} \dot{x}_1 = \frac{u_1 + u_2}{2} \cdot \cos(x_3) & (1) \\ \dot{x}_2 = \frac{u_1 + u_2}{2} \cdot \sin(x_3) & (2) \\ \dot{x}_3 = u_2 - u_1 & (3) \\ \dot{x}_4 = -\frac{u_1 + u_2}{2} \cdot \sin(x_4) - x_3 & (4) \end{cases}$$

Here x_1 , x_2 and x_3 are respectively the abscissa, the ordinate and the heading of the trailing robot, x_4 is the angle of the sled to the tractor vehicle.



Simulator

A python simulation was realized using VIBES in order to test the behavior of the system. A class *Tank* has been created to instantiate a vehicle with its sled. Then the script integrates the evolution equation using Euler's method in order to obtain the state of the system x according to the u inputs.

We could see that the behavior of the system seems correct and the model is faithful to reality. Moreover, the GNSS sensor and an accelerometer are simulated in order to enclose the real position in a box.

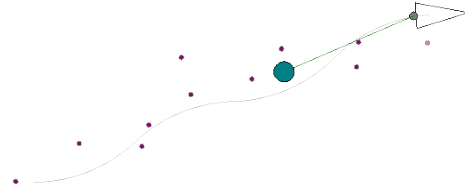


Fig. 1. Simulation of the system

Reliable set of sled's angle

Considering that the rope remains continuously under tension while the robot is moving, then the evolution of the angle x_4 of the sled relative to the towing vehicle is described by the *Differential Equation 4*.

We are able to find the trajectory of the sled by computing the interval containing the angle x_4 , considering that initially x_4 belongs to $[-\pi/2; \pi/2]$. Then by applying the *Differential Equation 4* on this interval, knowing the control vector u , we end up obtaining a fine interval framing the real angle x_4 , independently of the initial angle as we can see on the FIGURE 2.

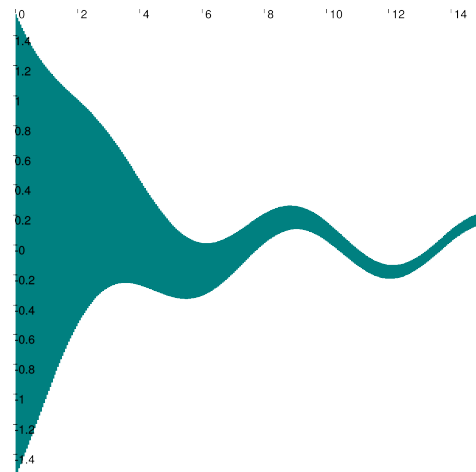


Fig. 2. Integration example using intervals

Sled localization

By having a box enclosing the trailing robot, and an interval framing the angle x_4 , we are able to obtain a box containing the sled, knowing the length of the rope.

This box has the shape of a pie sector. Equation 5 presents the position of the magnetometer as a function of the state of the system x_1, x_2 and x_4 . Here all these variables are intervals. By applying a polar contractor to these intervals, we are able to obtain the intervals containing x_m and y_m .

$$\begin{cases} x_m = x_1 - L \cdot \cos(x_4) \\ y_m = x_2 - L \cdot \sin(x_4) \end{cases} \quad (5)$$

Magnetometer range of measurement

By knowing a box containing the magnetometer and its measuring range, we are able to find all the points seen for sure and all the points that could be seen by the magnetometer. This allows us to recover the coverage of the area by the magnetometer.

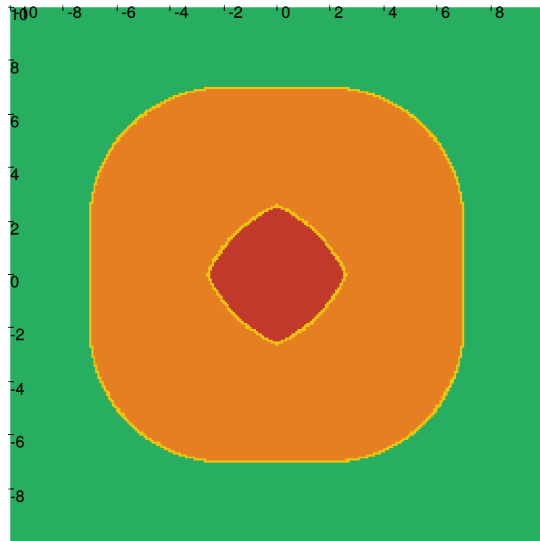


Fig. 3. Measurement range of the magnetometer using Thicksets

The FIGURE 3 shows us these two sets. The blue set is the unseen area, the orange set is the area maybe seen and the red set is the area seen for sure by the magnetometer. The yellow set forms the uncertain boundary between the other sets, which can be adjusted. Thus we have a way to know precisely the coverage of the mapping during the mission.

Magnetometer Mapping

With a moving box enclosing the magnetometer at any time, this method allows us to recover the coverage of the area by the magnetometer. Thus we have a way to know precisely the coverage of the mapping during the mission, which depends on the uncertainty on the position of the magnetometer and on the maximum distance of each point of the field to be measured. An example of the covered area of a magnetometer on a field is presented by the FIGURE 4.



Fig. 4. Coverage of the map by the magnetometer using Thicksets

Application example

Having inputs U and some dated inertial and GNSS measurements G , we are able to get a tube enclosing the trailing robot, available on FIGURE 5a, and a tube enclosing the magnetometer, available on FIGURE 5b. The estimated angle of the sled according to the trailing vehicle is also showed on the FIGURE 5c.

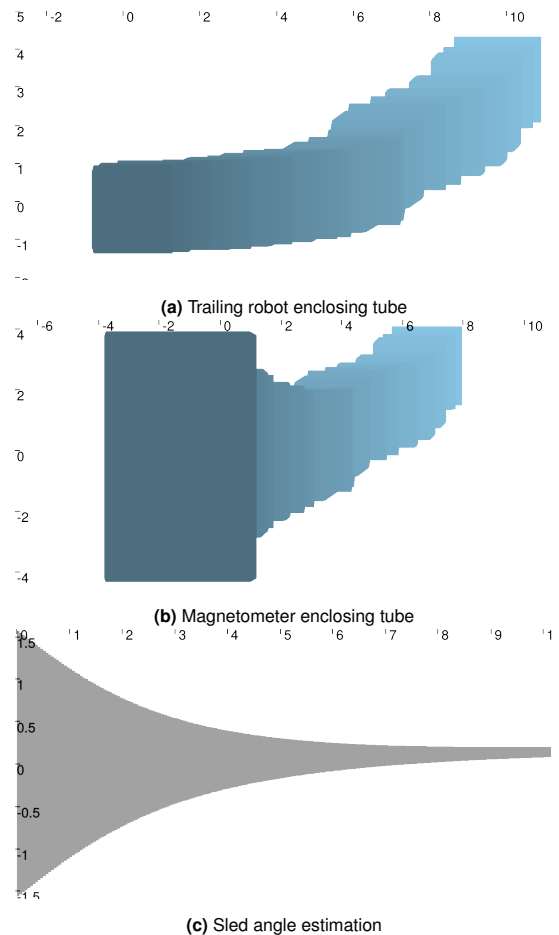


Fig. 5. Example of enclosing tube

We could see that the ϕ angle is quickly bounded regardless of knowing the initial condition. It let us have a more precise box enclosing the magnetometer. Finally, we are able to have a mapping of the coverage of the magnetometer visible on the FIGURE 6. Initially the uncertainty on the position of the magnetometer being large, the set of points that can be seen is large and the set of points seen for sure is very small. Then as the robot moves forward, the position of the magnetometer is better known and the set of points seen for sure is increasing.

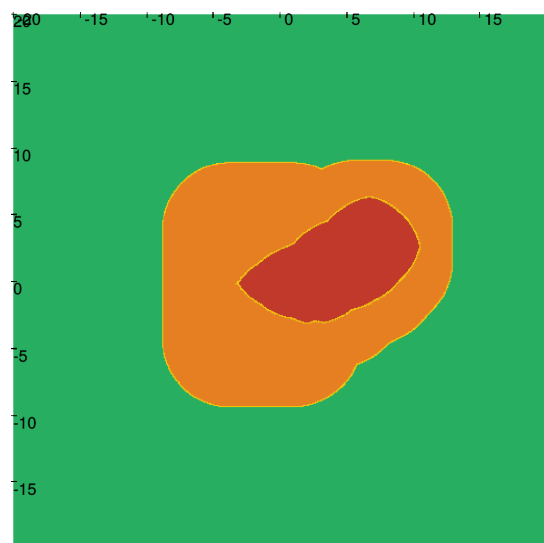


Fig. 6. Mapping coverage