

# Magnetic mapping using a trailed magnetometer

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The realization of a magnetic map of a terrain is a powerful tool especially used in mine warfare. This cartography can be done with a magnetometer, but the task is quite difficult. This is why it is useful to use robots to make this cartography. The problem induced by this solution is the addition of magnetic disturbances related to the structure of the robot and its actuators. It is then possible to drag the magnetometer on a sled behind the robot.

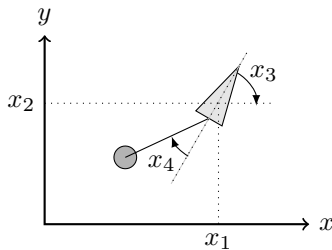
Magnetic | Mapping | Control | Interval Analysis  
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## Modelisation of the system

The system is composed of a vehicle that will drag a sledge that transports a magnetometer. The towing vehicle is a tank type vehicle, and the sled is attached to it with a rope. Assuming that the rope is constantly under tension, we are able to find the equations describing the dynamics of the system. By noting  $x$  the state of the system and  $u$  its inputs, the dynamics of the system is described by :

$$\dot{x} = f(x, u) = \begin{cases} \dot{x}_1 = \frac{u_1 + u_2}{2} \cdot \cos(x_3) & (1) \\ \dot{x}_2 = \frac{u_1 + u_2}{2} \cdot \sin(x_3) & (2) \\ \dot{x}_3 = u_2 - u_1 & (3) \\ \dot{x}_4 = -\frac{u_1 + u_2}{2} \cdot \sin(x_4) - x_3 & (4) \end{cases}$$

Here  $x_1$ ,  $x_2$  and  $x_3$  are respectively the abscissa, the ordinate and the heading of the trailing robot,  $x_4$  is the angle of the sled to the tractor vehicle.



## Simulator

A python simulation was realized using VIBES in order to test the behavior of the system. A class *Tank* has been created to instantiate a vehicle with its sled. Then the script integrates the evolution equation using Euler's method in order to obtain the state of the system  $x$  according to the  $u$  inputs.

We could see that the behavior of the system seems correct and the model is faithful to reality. Moreover, the GNSS sensor and an accelerometer are simulated in order to enclose the real position in a box.

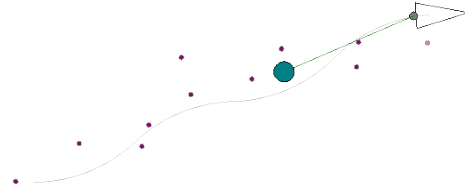


Fig. 1. Simulation of the system

## Reliable set of sled's angle

Considering that the rope remains continuously under tension while the robot is moving, then the evolution of the angle  $x_4$  of the sled relative to the towing vehicle is described by the *Differential Equation 4*.

We are able to find the trajectory of the sled by computing the interval containing the angle  $x_4$ , considering that initially  $x_4$  belongs to  $[-\pi/2; \pi/2]$ . Then by applying the *Differential Equation 4* on this interval, knowing the control vector  $u$ , we end up obtaining a fine interval framing the real angle  $x_4$ , independently of the initial angle as we can see on the FIGURE 2.

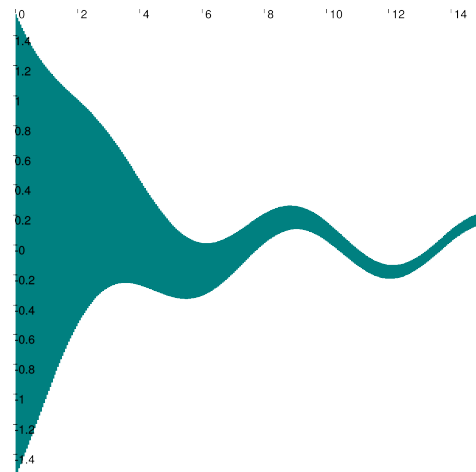


Fig. 2. Integration example using intervals

## Sled localization

By having a box enclosing the trailing robot, and an interval framing the angle  $x_4$ , we are able to obtain a box containing the sled, knowing the length of the rope.

This box has the shape of a pie sector. Equation 5 presents the position of the magnetometer as a function of the state of the system  $x_1$ ,  $x_2$  and  $x_4$ . Here all these variables are intervals. By applying a polar contractor to these intervals, we are able to obtain the intervals containing  $x_m$  and  $y_m$ .

$$\begin{cases} x_m = x_1 - L.\cos(x_4) \\ y_m = x_2 - L.\sin(x_4) \end{cases} \quad (5)$$

## Magnetometer range of measurement

By knowing a box containing the magnetometer and its measuring range, we are able to find all the points seen for sure and all the points that could be seen by the magnetometer. This allows us to recover the coverage of the area by the magnetometer.

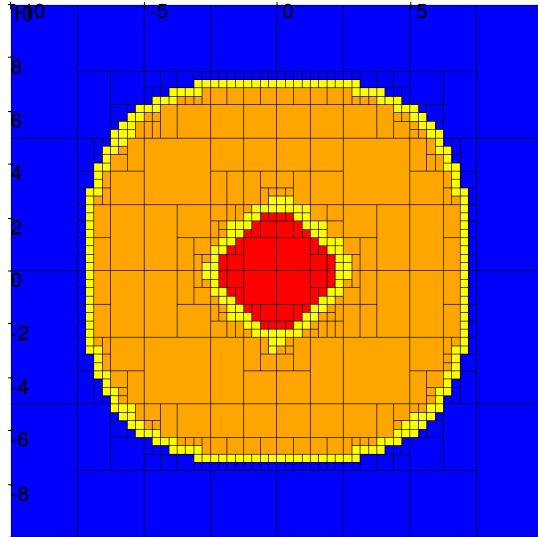


Fig. 3. Measurement range of the magnetometer using Thicksets

The FIGURE 3 shows us these two sets. The blue set is the unseen area, the orange set is the area maybe seen and the red set is the area seen for sure by the magnetometer. The yellow set forms the uncertain boundary between the other sets, which can be adjusted. Thus we have a way to know precisely the coverage of the mapping during the mission.

## Magnetometer Mapping

With a moving box enclosing the magnetometer at any time, this method allows us to recover the coverage of the area by the magnetometer. Thus we have a way to know precisely the coverage of the mapping during the mission, which depends on the uncertainty on the position of the magnetometer and on the maximum distance of each point of the field to be measured. An example of the covered area of a magnetometer on a field is presented by the FIGURE 4.

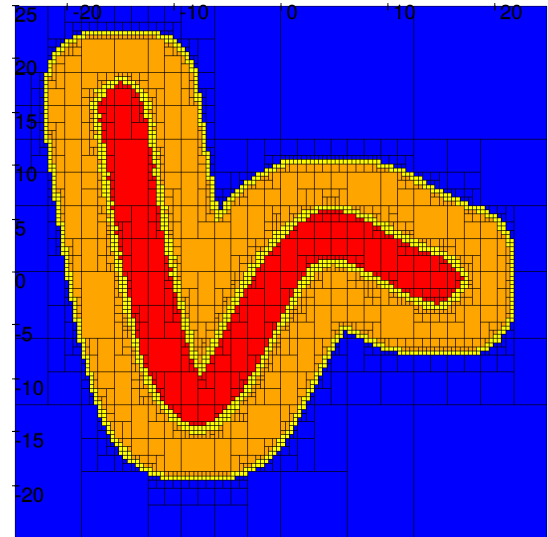


Fig. 4. Coverage of the map by the magnetometer using Thicksets