# CS121 Data Structures Linked Lists

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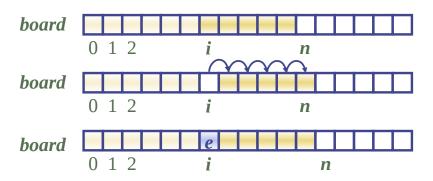
### Important Data and Statistics



- $ightharpoonup \frac{1}{5}$  of the semester passed!
- 24 classes remaining
- 32 days till the Midterm exam I
- ▶ 23 days till the Spring Break
- ▶ HW1 due Sunday, February 25, 23:59

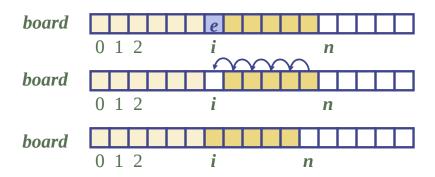
#### Adding an Array Entry

To add an entry e into array board at index i, we need to make room for it by shifting forward the n-i entries  $board[i], \ldots, board[n-1]$ 



#### Removing an Array Entry

To remove the entry e at index i, we need to fill the hole left by e by shifting backward the n-i-1 elements  $board[i+1], \ldots, board[n-1]$ 



## Singly Linked Lists

Drawbacks of array as an ordered data structure:

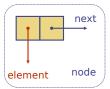
- fixed capacity
- expensive insertions and deletions at interior positions (shifting many elements)

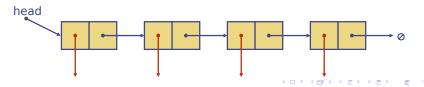
Linked list provides an alternative to an array-based structure.

A linked list is a collection of **nodes** that collectively form a linear sequence.

In a singly linked list, each node stores:

- a reference to an object that is an element of the sequence
- a reference to the next node of the list





#### Linked List Terms

The linked list instance must keep a reference to the first node of the list, known as the **head**.

The last node of the list is known as the tail.

**Traversing** the linked list—starting at the head and moving from one node to another by following each node's next reference.

The tail has **null** as its next reference.

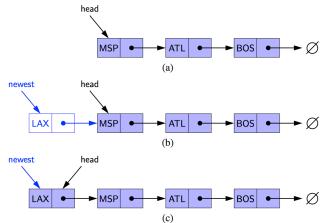
Commonly, a reference to the tail node is also stored, as is the count of the total number of nodes in the list (its **size**).

#### Inserting at the Head

#### **Algorithm** addFirst(e):

$$\label{eq:newest} \begin{split} &\mathsf{newest} = \mathsf{Node}(e) \\ &\mathsf{newest}.\mathsf{next} = \mathsf{head} \\ &\mathsf{head} = \mathsf{newest} \\ &\mathsf{size} = \mathsf{size} + 1 \end{split}$$

{create new node instance storing reference to element e} {set new node's next to reference the old head node} {set variable head to reference the new node} {increment the node count}



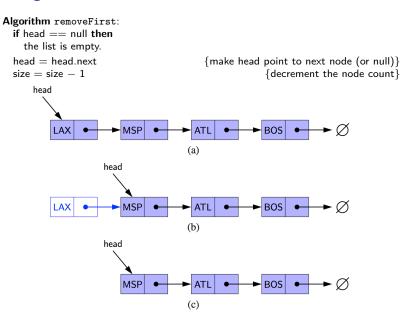
#### Inserting at the Tail

MSP

#### Algorithm addLast(e): newest = Node(e){create new node instance storing reference to element e} {set new node's next to reference the null object} newest.next = nulltail next = newest{make old tail node point to new node} {set variable tail to reference the new node} tail = newest{increment the node count} size = size + 1tail BOS MSP (a) tail newest MSP BOS MIA (b) tail newest

(c)

#### Removing from the Head



#### Removing from the Tail

Removing from the tail of a singly linked list is not efficient!

There is no constant-time way to update the tail to point to the previous node



### Interface of a Singly Linked List

- size() Returns the number of elements in the list.
- isEmpty() Returns true if the list is empty, and false otherwise.

  - last() Returns (but does not remove) the last element in the list.
- addFirst(e) Adds a new element to the front of the list.
- addLast(e) Adds a new element to the end of the list.
- removeFirst() Removes and returns the first element of the list.

#### Singly Linked List Implementation: Node

```
public class SinglyLinkedList<E> {
     //----- nested Node class -----
     private static class Node<E> {
       private E element:
                                       // reference to the element stored at this node
       private Node<E> next;
                                      // reference to the subsequent node in the list
6
       public Node(E e, Node<E> n) {
         element = e;
8
         next = n:
10
       public E getElement() { return element; }
       public Node<E> getNext() { return next; }
12
       public void setNext(Node < E > n) \{ next = n; \}
13
     } //----- end of nested Node class -----
```

# Singly Linked List Implementation I

```
public class SinglyLinkedList<E> {
     (nested Node class goes here)
14
     // instance variables of the SinglyLinkedList
     private Node<E> head = null;  // head node of the list (or null if empty)
15
16
     // number of nodes in the list
17
     private int size = 0;
     public SinglyLinkedList() { }
                                        // constructs an initially empty list
18
     // access methods
19
     public int size() { return size; }
20
21
     public boolean isEmpty() { return size == 0; }
22
     public E first() {
                                  // returns (but does not remove) the first element
23
       if (isEmpty()) return null;
24
       return head.getElement();
25
26
     public E last() {
                                  // returns (but does not remove) the last element
27
       if (isEmpty()) return null;
28
       return tail.getElement();
29
```

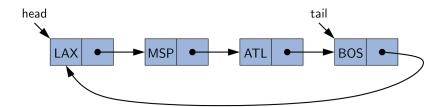
# Singly Linked List Implementation II

```
30
     // update methods
31
     head = new Node<>(e, head); // create and link a new node
32
33
      if (size == 0)
34
        tail = head:
                                     // special case: new node becomes tail also
35
       size++:
36
37
     38
       Node<E> newest = new Node<>(e, null); // node will eventually be the tail
39
      if (isEmpty())
40
        head = newest:
                                     // special case: previously empty list
41
       else
                                    // new node after existing tail
42
        tail.setNext(newest);
43
      tail = newest:
                                     // new node becomes the tail
       size++;
44
45
     public E removeFirst() {
                                     // removes and returns the first element
46
47
       if (isEmpty()) return null;
                                     // nothing to remove
       E answer = head.getElement();
48
49
       head = head.getNext();
                                     // will become null if list had only one node
50
       size--:
51
      if (size == 0)
52
      tail = null:
                                     // special case as list is now empty
53
      return answer:
54
55
```

### Circularly Linked Lists

There are applications in which data can be viewed as having a **cyclic order**, with well-defined neighbouring relationships, but no fixed beginning or end.

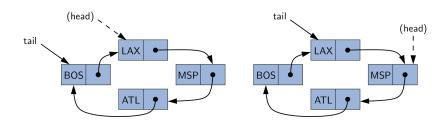
A **circularly linked list** is a singularly linked list in which the next reference of the tail node is set to refer back to the head of the list (rather than **null**).



#### Rotating

We no longer explicitly maintain the head reference. Thus we save a bit on memory usage and make the code simpler and more efficient.

When **rotating** the linked list, we simply advance the tail reference to point to the node that follows it.



## Adding at the Head/Tail

Add at the head:
tail

BOS

ATL

MSP

Add at the tail: add at the head and immediately rotate

## Circularly Linked List Implementation I

```
public class CircularlyLinkedList<E> {
     (nested node class identical to that of the SinglyLinkedList class)
14
     // instance variables of the CircularlyLinkedList
     15
     private int size = 0;
                                           // number of nodes in the list
16
     public CircularlyLinkedList() { }
                                           // constructs an initially empty list
17
     // access methods
18
19
     public int size() { return size; }
     public boolean isEmpty() { return size == 0; }
20
21
     public E first() {
                      // returns (but does not remove) the first element
22
       if (isEmpty()) return null;
23
       return tail.getNext().getElement();  // the head is *after* the tail
24
25
     public E last() {
                                  // returns (but does not remove) the last element
       if (isEmpty()) return null;
26
       return tail.getElement();
27
28
```

# Circularly Linked List Implementation II

```
// update methods
29
30
      31
        if (tail != null)
                                             // if empty, do nothing
32
          tail = tail.getNext();
                                             // the old head becomes the new tail
33
34
      public void addFirst(E e) {
                                             // adds element e to the front of the list
35
        if (size == 0) {
36
          tail = new Node<>(e, null);
37
          tail.setNext(tail);
                                             // link to itself circularly
38
        } else {
39
          Node < E > newest = new Node < > (e, tail.getNext());
          tail.setNext(newest):
40
41
42
        size++:
43
44
      public void addLast(E e) {
                                             // adds element e to the end of the list
                                             // insert new element at front of list
45
        addFirst(e);
                                             // now new element becomes the tail
46
        tail = tail.getNext();
47
48
      public E removeFirst() {
                                             // removes and returns the first element
49
        if (isEmpty()) return null;
                                             // nothing to remove
        Node < E > head = tail.getNext():
50
51
        if (head == tail) tail = null;
                                             // must be the only node left
52
        else tail.setNext(head.getNext());
                                             // removes "head" from the list
        size--:
53
54
        return head.getElement();
55
56
```

### **Doubly Linked Lists**

#### Limitations of singly linked list:

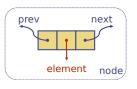
- unable to efficiently delete a node at the tail
- cannot efficiently delete a node from an interior position if given a reference to it (cannot determine the preceding node)

In a **doubly linked list** each node keeps an explicit reference to the node before it and a reference to the node after it.

A doubly linked list can be traversed forward and backward.

#### In a doubly linked list, each node stores:

- a reference to an object that is an element of the sequence
- a reference to the previous node of the list
- ▶ a reference to the next node of the list

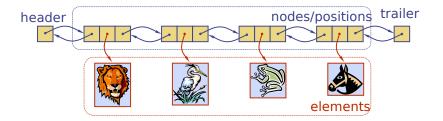


#### Header and Trailer Sentinels

It helps to add special nodes at both ends of the list:

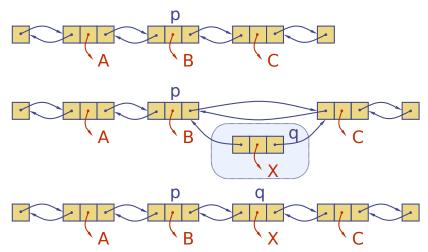
- a header node at the beginning of the list
- a trailer node at the end of the list.

These 'dummy' nodes are known as **sentinels** (or guards). They do not store elements.



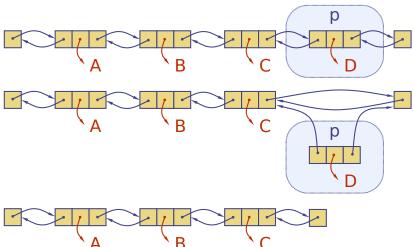
#### Insertion

Every insertion takes place between a pair of existing nodes.



#### Deletion

Every deletion takes place between a pair of existing nodes.



## Interface of a Doubly Linked List

- size() Returns the number of elements in the list.
- isEmpty() Returns true if the list is empty, and false otherwise.

  - last() Returns (but does not remove) the last element in the list.
- addFirst(e) Adds a new element to the front of the list.
- addLast(e) Adds a new element to the end of the list.
- removeFirst() Removes and returns the first element of the list.
- removeLast() Removes and returns the last element of the list.

#### Doubly Linked List Implementation: Node

```
/** A basic doubly linked list implementation. */
    public class DoublyLinkedList<E> {
     //---- nested Node class -----
     private static class Node<E> {
       private E element;
                                       // reference to the element stored at this node
       private Node<E> prev; // reference to the previous node in the list
 6
       private Node<E> next;  // reference to the subsequent node in the list
       public Node(E e, Node<E> p, Node<E> n) {
         element = e:
10
         prev = p;
11
         next = n:
12
13
       public E getElement() { return element; }
14
       public Node<E> getPrev() { return prev; }
15
       public Node<E> getNext() { return next; }
       public void setPrev(Node<E> p) { prev = p; }
16
17
       public void setNext(Node < E > n) \{ next = n; \}
      } //----- end of nested Node class -----
18
19
```

# Doubly Linked List Implementation I

```
// instance variables of the DoublyLinkedList
20
21
      private Node<E> header:
                                                       // header sentinel
22
                                                       // trailer sentinel
      private Node<E> trailer;
23
      private int size = 0;
                                                       // number of elements in the list
24
      /** Constructs a new empty list. */
25
      public DoublyLinkedList() {
26
        header = new Node<>(null, null, null); // create header
27
        trailer = new Node<>(null, header, null); // trailer is preceded by header
28
        header.setNext(trailer);
                                                       // header is followed by trailer
29
30
      /** Returns the number of elements in the linked list. */
31
      public int size() { return size; }
32
      /** Tests whether the linked list is empty. */
33
      public boolean isEmpty() { return size == 0; }
      /** Returns (but does not remove) the first element of the list. */
34
35
      public E first() {
36
        if (isEmpty()) return null;
37
        return header.getNext().getElement(); // first element is beyond header
38
      /** Returns (but does not remove) the last element of the list. */
39
40
      public E last() {
41
        if (isEmpty()) return null;
        return trailer.getPrev().getElement(); // last element is before trailer
42
43
```

## Doubly Linked List Implementation II

```
// public update methods
44
45
      /** Adds element e to the front of the list. */
46
      public void addFirst(E e) {
        addBetween(e, header, header.getNext()); // place just after the header
47
48
      /** Adds element e to the end of the list. */
49
50
      public void addLast(E e) {
51
        addBetween(e, trailer.getPrev(), trailer); // place just before the trailer
52
53
      /** Removes and returns the first element of the list. */
54
      public E removeFirst() {
55
        if (isEmpty()) return null;
                                                      // nothing to remove
56
        return remove(header.getNext());
                                                       // first element is beyond header
57
58
      /** Removes and returns the last element of the list. */
      public E removeLast() {
59
        if (isEmpty()) return null;
60
                                                      // nothing to remove
61
        return remove(trailer.getPrev());
                                                       // last element is before trailer
62
63
```

## Doubly Linked List Implementation III

```
64
      // private update methods
65
      /** Adds element e to the linked list in between the given nodes. */
      private void addBetween(E e, Node<E> predecessor, Node<E> successor) {
66
        // create and link a new node
67
68
        Node < E > newest = new Node < > (e, predecessor, successor);
69
        predecessor.setNext(newest);
70
        successor.setPrev(newest);
71
        size++:
72
73
      /** Removes the given node from the list and returns its element. */
74
      private E remove(Node<E> node) {
75
        Node < E > predecessor = node.getPrev();
        Node<E> successor = node.getNext();
76
        predecessor.setNext(successor);
77
78
        successor.setPrev(predecessor);
79
        size--:
80
        return node.getElement();
81
   } //----- end of DoublyLinkedList class -----
```

# Summary

#### Reading

Sections 3.2–3.6 of the main textbook

#### **Questions?**