



Ordinary Differential Equations

Math-UA 262-003
MA-UY 4204 B

Instructor Info

- Zhuo-Cheng Xiao
- Office Hrs: Mon & Wed 1-2 pm
- Rm 921, WWH (Courant Bldg)
- Brightspace and Gradescope
- zx555@nyu.edu

Course Info

- Mon & Wed
- 2:00 - 3:15 pm
- 194M Rm 203

Recitation Info

- Fri
- ???
- ???

TA Info

- ???
- Office Hrs:???
- ???

Overview Together, we are involved in one of the most significant human enterprises: describing, analyzing, and predicting the chaotic and unknown future. This course is the first course in ordinary differential equations (ODEs) and an elementary part of a much bigger picture of the dynamical system and applying mathematics to real-world problems.

If predicting the future is a one-million-word novel, then college mathematics such as calculus and linear algebra are ABC about it. Based on that, we will focus on some "grammar" (mathematical theories and proof of ODE) and "making sentences" (solving ODE problems and numerical simulations). I hope this course can also provide a glimpse of more advanced theory courses such as dynamical systems, partial differential equations, and functional analysis, as well as a tryout of solving real-world modelling problems.

Materials

- Required Texts**
Differential Equations and Their Applications. (Braun, 4th edition, 1993, Springer), ("B"). [Accessible for free](#).
- Suggested Reading**
Nonlinear Dynamics and Chaos. (Strogatz, 2nd Edition, 2015, CRC Press), ("S")

Learning Objectives

- Solving linear first and second-order ODEs, and methods of solving a few types of nonlinear ODEs that have exact solutions
- Proving existence and uniqueness of solutions
- Analytical skills: Laplace transforms and series solutions
- N-dim ODE systems: qualitative analysis for linear/nonlinear systems
- Boundary value problems
- More analytical skills: Green's functions and Fourier series. (optional)

Grading Scheme

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|-----|--------------------------|
| 20% | Weekly Homework |
| 10% | Class Participation |
| 40% | Midterm I & II. 20% each |
| 30% | Final Exam |

Grades will follow the standard NYU math scale:

| Letter Grade | A | A- | B+ | B | B- | C+ | C | D | F |
|--------------|----|----|----|----|----|----|----|----|-----|
| Cutoff | 93 | 90 | 87 | 83 | 80 | 75 | 65 | 50 | <50 |

Curving may (or may not) be added to uplift the letter grades during the final evaluation.

Exams Two midterms will be in-class. Although exams will be computation extensive, we will tolerate numerical errors provided that the student correctly and concisely demonstrates all computational steps. On the other hand, only a small portion of scores will be granted if only the final answer is provided without any justifications.

FAQs

? Why there are incomplete information?

! This is a tentative version of syllabus. TA and recitation information will be added soon.

Homework Policy Homework should be submitted as pdf files on Gradescope, which always dues on *Monday, 5pm* unless otherwise specified, and our grader will return your homework grading with an explanation before Saturday. Both handwritten and latex formatted are fine, but the students are responsible for the submitted files' readability and completeness.

We are all affected by the great uncertainty of life, and I understand that unexpected issues are always popping up. Therefore, the lowest two homework grades will be dropped (including the missed ones). In addition, the "late" deadline for each homework is *Monday, 11:59pm* in case of emergent issues. However, submissions after the deadline but before the "late" deadline will receive a grade discounted by 10%, and submissions will not be accepted after the "late" deadline.

Make-up Policy Make-up exams or assignments are allowed in limited scenarios provided that the student gets approval from the instructor *before the due date*. An approval may be granted for typical excuses including medical reasons, religious holidays, and family emergencies.

Class Participation Students are expected to attend the classes, including recitations. Although attendance will not be strictly recorded, 10% of the final evaluation is based on class participation, including in-class interactions and discussions.

Recitations will begin from the second week in Spring 2022. Although there are multiple recitation sessions offered, the students of this section should go to recitation section #? scheduled on #?.

Other Resources

- Tutoring: Courant tutoring center and the university tutoring center.
- Moses Center for Student Accessibility for students with any physical or mental inconveniences.

Academic Integrity All students are expected to adhere to the codes of academic integrity specified by New York Univerisity.

Class Schedule

| Week | Date | Section | Materials |
|--|-------|------------|--|
| MODULE 1: First Order Linear Equations | | | |
| Week 1 | 01/24 | 1.1-2 | Introduction, Solving first order linear equations |
| | 01.26 | 1.2, 1.4 | Separation of variables |
| Week 2 | 01/31 | 1.5-6 | Modelling: Population growth |
| | 02/02 | 1.9 | Exact equations |
| Week 3 | 02/07 | 1.10-11 | The existence-uniqueness theorem; Iterations |
| | 02/09 | 1.11, 1.13 | Numerical methods: Euler's methods from Taylor expansion |
| Week 4 | 02/14 | 1.14-16 | More on numerical methods: Runge-Kutta |
| | 02/16 | | Midterm 1 |
| MODULE 2: Second Order and N-Dimensional Equations | | | |
| Week 5 | 02/21 | | President Day. No class |
| | 02/23 | 2.1 | Second order linear equations |
| Week 6 | 02/28 | 2.2-3 | Constant coefficients: homogeneous equations |
| | 03/02 | 2.3-5 | Constant coefficients: non-homogeneous equations |
| Week 7 | 03/07 | 2.8, 2.8.1 | Series solutions, Singular points |
| | 03/09 | 2.8.2-3 | Method of Frobenius, special functions |
| Week 8 | | | Spring break. No class |
| Week 9 | 03/21 | 3.1 | Solutions of n-dim linear systems |
| | 03/23 | 2.6 | Modelling: Oscillator problems |
| Week 10 | 03/28 | 3.8 | Linear ODE systems: Eigenvalues and eigenvectors |
| | 03/30 | 3.9-10 | Linear ODE systems: Complex & Equal roots |
| Week 11 | 04/04 | 3.11-12 | Linear ODE systems: Matrix solutions |
| | 04/06 | | Midterm 2 |
| MODULE 3: Qualitative analysis to ODE systems & More analytical methods | | | |
| Week 12 | 04/11 | 4.1-3 | Stability |
| | 04/13 | 4.4, 4.7 | The phase plane and phase portraits |
| Week 13 | 04/18 | 4.6, 4.8 | Qualitative properties of orbits |
| | 04/20 | 4.10-13 | Modelling: Populations and epidemiology |

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|---------|--------------|------------|---|
| Week 14 | 04/25 | 5.2-3 | Heat equations and Fourier series |
| | 04/27 | 6.3-4 | Orthogonal bases, Sturm-Liouville theory |
| Week 15 | 05/02 | 2.9-10 | Laplace transform |
| | 05/04 | 2.11, 3.13 | Application of Laplace transforms |
| Week 16 | 05/09 | 2.12-13 | Laplace transform, Dirac function, and Green's function |
| | undetermined | | Final Exam |