

Homework Assignment 3 Solution

Exercise 2.12 (18 points)

2.12.1 50000000

2.12.2 overflow

2.12.3 B0000000

2.12.4 no overflow

2.12.5 D0000000

2.12.6 Overflow

Exercise 3.1 (6 points)

5730

Exercise 3.12 (20 points)

Step	Action	Multiplier	Multiplicand	Product
0	Initial Vals	001 010	000 000 110 010	000 000 000 000
1	lsb=0, no op	001 010	000 000 110 010	000 000 000 000
	Lshift Mcand	001 010	000 001 100 100	000 000 000 000
	Rshift Mplier	000 101	000 001 100 100	000 000 000 000
2	Prod=Prod+Mcand	000 101	000 001 100 100	000 001 100 100
	Lshift Mcand	000 101	000 011 001 000	000 001 100 100
	Rshift Mplier	000 010	000 011 001 000	000 001 100 100
3	lsb=0, no op	000 010	000 011 001 000	000 001 100 100
	Lshift Mcand	000 010	000 110 010 000	000 001 100 100
	Rshift Mplier	000 001	000 110 010 000	000 001 100 100
4	Prod=Prod+Mcand	000 001	000 110 010 000	000 111 110 100
	Lshift Mcand	000 001	001 100 100 000	000 111 110 100
	Rshift Mplier	000 000	001 100 100 000	000 111 110 100
5	lsb=0, no op	000 000	001 100 100 000	000 111 110 100
	Lshift Mcand	000 000	011 001 000 000	000 111 110 100
	Rshift Mplier	000 000	011 001 000 000	000 111 110 100
6	lsb=0, no op	000 000	110 010 000 000	000 111 110 100
	Lshift Mcand	000 000	110 010 000 000	000 111 110 100
	Rshift Mplier	000 000	110 010 000 000	000 111 110 100

Exercise 3.21 (6 points)

jal 0x00000000

Exercise 3.22 (10 points)

$$\begin{aligned} 0 \times 0C000000 &= 0000\ 1100\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000 \\ &= 0\ 0001\ 1000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000 \end{aligned}$$

S = 0, sign is positive
exponent = 8+16 = 24
Actual Exponent = 24 - 127 = -103
Fraction = 0

$$\text{Answer} = 1.0 \times 2^{-103}$$

Extra Exercise (20 points)

In normalized binary format

$$a = 1.1011 \times 2^{14}$$

$$b = -1.11 \times 2^{-2}$$

a)

1. Align binary points (shift number with smaller exponent):

$$-1.11 \times 2^{-2} = -0.0000\ 0000\ 0000\ 0001\ 1100\ 000$$

2. Add Significands:

$$\begin{array}{r} 1.1011\ 0000\ 0000\ 0000\ 0000\ 000 \\ -0.0000\ 0000\ 0000\ 0001\ 1100\ 000 \\ \hline 1.1010\ 1111\ 1111\ 1110\ 0100\ 000 \end{array}$$

3. Normalize and round... (no change)

Single precision result: 0100 0110 1101 0111 1111 1111 0010 0000

Normalized binary: + 1.1010 1111 1111 1110 01 $\times 2^{14}$

b)

1. Add exponent:

$$\begin{array}{r} 111\ 11\ 1 \\ 100\ 0110\ 1 \\ + 011\ 1110\ 1 \\ \hline 1000\ 0101\ 0 \\ - 011\ 1111\ 1 \quad (\text{minus bias}) \\ \hline 1111\ 1111 \\ 100\ 0101\ 1 \quad (\text{new exponent}) \end{array}$$

2. Multiply Significands:

$$\begin{array}{r} 1.101\ 1000 \\ \times 1.110\ 0000 \\ \hline 1\ 1011\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000 \\ 11\ 0110\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000 \\ + 10\ 1100\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000 \\ \hline 10.11\ 1101\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000 \end{array}$$

3. Normalize and round:

Exponent: 100 0110 0

Significand: 1.011 1101 0000 0000 0000 0000

4. Signs differ, so result is negative: 1100 0110 0011 1101 0000 0000 0000 0000

Normalized binary: $-1.0111\ 101 \times 2^{13}$