

```
R version 4.3.1 (2023-06-16 ucrt) -- "Beagle Scouts"
Copyright (C) 2023 The R Foundation for Statistical Computing
Platform: x86_64-w64-mingw32/x64 (64-bit)
```

```
R is free software and comes with ABSOLUTELY NO WARRANTY.
You are welcome to redistribute it under certain conditions.
Type 'license()' or 'licence()' for distribution details.
```

```
Natural language support but running in an English locale
```

```
R is a collaborative project with many contributors.
Type 'contributors()' for more information and
'citation()' on how to cite R or R packages in publications.
```

```
Type 'demo()' for some demos, 'help()' for on-line help, or
'help.start()' for an HTML browser interface to help.
Type 'q()' to quit R.
```

```
> install.packages("readxl")
Installing package into 'C:/Users/minhas01/AppData/Local/R/win-library/4.3'
(as 'lib' is unspecified)
--- Please select a CRAN mirror for use in this session ---
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/readxl_1.4.3.zip'
Content type 'application/zip' length 1197261 bytes (1.1 MB)
downloaded 1.1 MB
```

```
package 'readxl' successfully unpacked and MD5 sums checked
```

```
The downloaded binary packages are in
      C:\Users\minhas01\AppData\Local\Temp\RtmpGAggMH\downloaded_packages
> install.packages("seasonal")
Installing package into 'C:/Users/minhas01/AppData/Local/R/win-library/4.3'
(as 'lib' is unspecified)
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/seasonal_1.9.0.zip'
Content type 'application/zip' length 549590 bytes (536 KB)
downloaded 536 KB
```

```
package 'seasonal' successfully unpacked and MD5 sums checked
```

```
The downloaded binary packages are in
      C:\Users\minhas01\AppData\Local\Temp\RtmpGAggMH\downloaded_packages
> library(readxl)
Warning message:
package 'readxl' was built under R version 4.3.3
> library(seasonal)
Warning message:
package 'seasonal' was built under R version 4.3.3
> data <- read.csv("C:\Users\minhas01\Desktop\Nahayan Minhas\US Net Capital Mthly Inflows Level Ch
anged Qrtly.csv")
Error in file(file, "rt") : cannot open the connection
In addition: Warning message:
In file(file, "rt") :
  cannot open file 'C:\Users\minhas01\Desktop\Nahayan Minhas\US Net Capital Mthly Inflows Level Ch
anged Qrtly.csv': No such file or directory
> data <- read.csv("C:\Users\minhas01\Desktop\Nahayan Minhas\US Net Capital Mthly Inflows Level Ch
anged Qrtly.csv")
Error in file(file, "rt") : cannot open the connection
In addition: Warning message:
In file(file, "rt") :
  cannot open file 'C:\Users\minhas01\Desktop\Nahayan Minhas\US Net Capital Mthly Inflows Level Ch
anged Qrtly.csv': No such file or directory
> data <- read.csv("C:\Users\minhas01\Desktop\Nahayan Minhas\Data for R Analysis\US Net Capital Mt
hly Inflows Level Changed Qrtly.csv")
Error in file(file, "rt") : cannot open the connection
In addition: Warning message:
In file(file, "rt") :
  cannot open file 'C:\Users\minhas01\Desktop\Nahayan Minhas\Data for R Analysis\US Net Capital Mt
hly Inflows Level Changed Qrtly.csv': No such file or directory
> data <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/Data for R Analysis/US Net Capital M
```

```

thly Inflows Level Changed Qrtly.csv")
Error: bidi formatting not allowed, use escapes instead (\u202a) (<input>:1:19)
> data <- read.csv("C:/Users/minhas01/Desktop/USDebt.csv")
> data$Date <- sub("^00(\\d{2})", "19\\1", data$Date)
> head(data$Date)
[1] "3/31/1994" "6/30/1994" "9/30/1994" "12/31/1994" "3/31/1995" "6/30/1995"
> data$Date <- as.Date(data$Date, format="%m/%d/%Y")
> head(data$Date)
[1] "1994-03-31" "1994-06-30" "1994-09-30" "1994-12-31" "1995-03-31" "1995-06-30"
> if (!any(is.na(data$Date))) {
+   data$Year <- as.numeric(format(data$Date, "%Y"))
+   data$Quarter <- ceiling(as.numeric(format(data$Date, "%m")) / 3)
+   head(data$Year)
+   head(data$Quarter)
+ } else {
+   print("There was an error converting the dates.")
+ }
[1] 1 2 3 4 1 2
> ts_data <- ts(data$Value, frequency=4, start=c(min(data$Year), min(data$Quarter)))
Error in ts(data$Value, frequency = 4, start = c(min(data$Year), min(data$Quarter))) :
  'ts' object must have one or more observations
> data <- read.csv("C:/Users/minhas01/Desktop/USDebt.csv")
> data$Date <- sub("^00(\\d{2})", "19\\1", data$Date)
> head(data$Date)
[1] "3/31/1994" "6/30/1994" "9/30/1994" "12/31/1994" "3/31/1995" "6/30/1995"
> data$Date <- as.Date(data$Date, format="%m/%d/%Y")
> head(data$Date)
[1] "1994-03-31" "1994-06-30" "1994-09-30" "1994-12-31" "1995-03-31" "1995-06-30"
> if (!any(is.na(data$Date))) {
+   data$Year <- as.numeric(format(data$Date, "%Y"))
+   data$Quarter <- ceiling(as.numeric(format(data$Date, "%m")) / 3)
+   head(data$Year)
+   head(data$Quarter)
+ } else {
Error: unexpected '}' in:
"+   head(data$Quarter)
+ }"
> +   print("There was an error converting the dates.")
[1] "There was an error converting the dates."
Error in +print("There was an error converting the dates.") :
  invalid argument to unary operator
> + }
Error: unexpected '}' in "+ }"
> if (!any(is.na(data$Date))) {
+   data$Year <- as.numeric(format(data$Date, "%Y"))
+   data$Quarter <- ceiling(as.numeric(format(data$Date, "%m")) / 3)
+   head(data$Year)
+   head(data$Quarter)
+ } else {
+   print("There was an error converting the dates.")
+ }
[1] 1 2 3 4 1 2
> ts_data <- ts(data$Value, frequency=4, start=c(min(data$Year), min(data$Quarter)))
> sa_results <- seas(ts_data)
Model used in SEATS is different: (0 0 0)
> adjusted <- final(sa_results)
> plot(ts_data, main = "Original vs. Seasonally Adjusted", col = "blue", ylab="Value", xlab="Time
")
> lines(adjusted, col = "red")
> legend("topright", legend = c("Original", "Adjusted"), col = c("blue", "red"), lty = 1, bty = "
n")
Error in (function (s, units = "user", cex = NULL, font = NULL, vfont = NULL, :
  plot.new has not been called yet

> > data <- read.csv("C:/Users/minhas01/Desktop/USDXY.csv")
> data$Date <- sub("^00(\\d{2})", "19\\1", data$Date)
> head(data$Date)
[1] "3/31/1994" "6/30/1994" "9/30/1994" "12/30/1994" "3/31/1995" "9/29/1995"
> data$Date <- as.Date(data$Date, format="%m/%d/%Y")
>

```

```
> data$Date <- as.Date(data$Date, format="%m/%d/%Y")
> head(data$Date)
[1] "1994-03-31" "1994-06-30" "1994-09-30" "1994-12-30" "1995-03-31" "1995-09-29"
> if (!any(is.na(data$Date))) {
+   data$Year <- as.numeric(format(data$Date, "%Y"))
+   data$Quarter <- ceiling(as.numeric(format(data$Date, "%m")) / 3)
+   head(data$Year)
+   head(data$Quarter)
+ } else {
+   print("There was an error converting the dates.")
+ }
[1] 1 2 3 4 1 3
> ts_data <- ts(data$Value, frequency=4, start=c(min(data$Year), min(data$Quarter)))
> sa_results <- seas(ts_data)
Model used in SEATS is different: (0 0 0)
> summary(sa_results)
```

```
Call:
seas(x = ts_data)
```

```
Coefficients:
```

```
              Estimate Std. Error z value Pr(>|z|)
MA-Nonseasonal-01 -0.34150    0.08656  -3.945 7.97e-05 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
SEATS adj. ARIMA: (0 0 1) Obs.: 119 Transform: none
AICc: 681.8, BIC: 687.3 QS (no seasonality in final): 0
Box-Ljung (no autocorr.): 17.08 Shapiro (normality): 0.9864
Messages generated by X-13:
Warnings:
```

```
- Automatic transformation selection cannot be done on a series with zero or negative values.
```

```
Notes:
```

```
- Model used for SEATS decomposition is different from the model estimated in the regARIMA modeling module of X-13ARIMA-SEATS.
```

```
> install.packages("vars")
Installing package into 'C:/Users/minhas01/AppData/Local/R/win-library/4.3'
(as 'lib' is unspecified)
also installing the dependencies 'zoo', 'strucchange', 'urca', 'lmtest', 'sandwich'
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/zoo_1.8-12.zip'
Content type 'application/zip' length 1020531 bytes (996 KB)
downloaded 996 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/strucchange_1.5-3.zip'
Content type 'application/zip' length 947106 bytes (924 KB)
downloaded 924 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/urca_1.3-3.zip'
Content type 'application/zip' length 1109075 bytes (1.1 MB)
downloaded 1.1 MB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/lmtest_0.9-40.zip'
Content type 'application/zip' length 405925 bytes (396 KB)
downloaded 396 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/sandwich_3.1-0.zip'
Content type 'application/zip' length 1508756 bytes (1.4 MB)
downloaded 1.4 MB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/vars_1.6-1.zip'
Content type 'application/zip' length 425536 bytes (415 KB)
downloaded 415 KB
```

```
package 'zoo' successfully unpacked and MD5 sums checked
package 'strucchange' successfully unpacked and MD5 sums checked
package 'urca' successfully unpacked and MD5 sums checked
package 'lmtest' successfully unpacked and MD5 sums checked
```

```
package 'sandwich' successfully unpacked and MD5 sums checked
package 'vars' successfully unpacked and MD5 sums checked
```

```
The downloaded binary packages are in
```

```
C:\Users\minhas01\AppData\Local\Temp\RtmpGAggMH\downloaded_packages
```

```
> install.packages("readr")
```

```
Installing package into 'C:/Users/minhas01/AppData/Local/R/win-library/4.3'
```

```
(as 'lib' is unspecified)
```

```
also installing the dependencies 'bit', 'bit64', 'tidyselect', 'withr', 'clipr', 'vroom', 'tzdb'
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/bit_4.0.5.zip'
```

```
Content type 'application/zip' length 1136720 bytes (1.1 MB)
```

```
downloaded 1.1 MB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/bit64_4.0.5.zip'
```

```
Content type 'application/zip' length 494921 bytes (483 KB)
```

```
downloaded 483 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/tidyselect_1.2.1.zip'
```

```
Content type 'application/zip' length 225188 bytes (219 KB)
```

```
downloaded 219 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/withr_3.0.0.zip'
```

```
Content type 'application/zip' length 246001 bytes (240 KB)
```

```
downloaded 240 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/clipr_0.8.0.zip'
```

```
Content type 'application/zip' length 54687 bytes (53 KB)
```

```
downloaded 53 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/vroom_1.6.5.zip'
```

```
Content type 'application/zip' length 1331241 bytes (1.3 MB)
```

```
downloaded 1.3 MB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/tzdb_0.4.0.zip'
```

```
Content type 'application/zip' length 1032572 bytes (1008 KB)
```

```
downloaded 1008 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/readr_2.1.5.zip'
```

```
Content type 'application/zip' length 1172532 bytes (1.1 MB)
```

```
downloaded 1.1 MB
```

```
package 'bit' successfully unpacked and MD5 sums checked
```

```
package 'bit64' successfully unpacked and MD5 sums checked
```

```
package 'tidyselect' successfully unpacked and MD5 sums checked
```

```
package 'withr' successfully unpacked and MD5 sums checked
```

```
package 'clipr' successfully unpacked and MD5 sums checked
```

```
package 'vroom' successfully unpacked and MD5 sums checked
```

```
package 'tzdb' successfully unpacked and MD5 sums checked
```

```
package 'readr' successfully unpacked and MD5 sums checked
```

```
The downloaded binary packages are in
```

```
C:\Users\minhas01\AppData\Local\Temp\RtmpGAggMH\downloaded_packages
```

```
> library(vars)
```

```
Loading required package: MASS
```

```
Loading required package: strucchange
```

```
Loading required package: zoo
```

```
Attaching package: 'zoo'
```

```
The following objects are masked from 'package:base':
```

```
as.Date, as.Date.numeric
```

```
Loading required package: sandwich
```

```
Loading required package: urca
```

```
Loading required package: lmtest
```

```
Warning messages:
```

```
1: package 'vars' was built under R version 4.3.3
```

```
2: package 'strucchange' was built under R version 4.3.3
```

```

— Column specification — Rows: 120 Columns: 2

```

- 1 Use ``spec()`` to retrieve the full column specification for this data.
- 2 Specify the column types or set ``show_col_types = FALSE`` to quiet this message.

```
+ > AAAAA
Error: object 'AAAAA' not found
> library(vars)
>
> library(readr)
>
> data1 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> data2 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US CPI SA.csv")
> data3 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US IP SA.csv")
> data4 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US Unemployment SA.csv")
> data5 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/USDebt SA.csv")
> data6 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/USDXY SA.csv")
> data1$Date <- as.Date(data1$Date, format="%m/%d/%Y")
> data2$Date <- as.Date(data2$Date, format="%m/%d/%Y")
> data3$Date <- as.Date(data3$Date, format="%m/%d/%Y")
> data4$Date <- as.Date(data4$Date, format="%m/%d/%Y")
> data5$Date <- as.Date(data5$Date, format="%m/%d/%Y")
> data6$Date <- as.Date(data6$Date, format="%m/%d/%Y")
> anyNA(data1$Date)
[1] FALSE
> anyNA(data2$Date)
[1] FALSE
> anyNA(data3$Date)
[1] FALSE
> anyNA(data4$Date)
[1] FALSE
> anyNA(data5$Date)
[1] FALSE
> anyNA(data6$Date)
[1] FALSE
> ts1 <- ts(data1[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
Error in year(min(data1$Date)) : could not find function "year"
> install.packages("lubridate")
Installing package into 'C:/Users/minhas01/AppData/Local/R/win-library/4.3'
(as 'lib' is unspecified)
```

also installing the dependencies 'generics', 'timechange'

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/generics_0.1.3.zip'
Content type 'application/zip' length 80415 bytes (78 KB)
downloaded 78 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/timechange_0.3.0.zip'
Content type 'application/zip' length 507755 bytes (495 KB)
downloaded 495 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/lubridate_1.9.3.zip'
Content type 'application/zip' length 984899 bytes (961 KB)
downloaded 961 KB
```

```
package 'generics' successfully unpacked and MD5 sums checked
package 'timechange' successfully unpacked and MD5 sums checked
package 'lubridate' successfully unpacked and MD5 sums checked
```

```
The downloaded binary packages are in
      C:\Users\minhas01\AppData\Local\Temp\RtmpGAggMH\downloaded_packages
> library(lubridate)
```

Attaching package: 'lubridate'

The following objects are masked from 'package:base':

```
date, intersect, setdiff, union
```

Warning message:

```
package 'lubridate' was built under R version 4.3.3
> ts1 <- ts(data1[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
> ts2 <- ts(data2[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
> ts3 <- ts(data3[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
> ts4 <- ts(data4[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
> ts5 <- ts(data5[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
> ts6 <- ts(data6[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
> mts_data <- cbind(ts1, ts2, ts3, ts4, ts5, ts6)
> var_model <- VAR(mts_data, p=8)
Error in VAR(mts_data, p = 8) :
NAs in y.
> data1 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> data2 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US CPI SA.csv")
Error: unexpected '>' in ">"
> data3 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US IP SA.csv")
Error: unexpected '>' in ">"
> data4 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US Unemployment SA.csv")
Error: unexpected '>' in ">"
> data5 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/USDebt SA.csv")
Error: unexpected '>' in ">"
> data6 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/USDXY SA.csv")
Error: unexpected '>' in ">"
> data1$Date <- as.Date(data1$Date, format="%m/%d/%Y")
Error: unexpected '>' in ">"
> data2$Date <- as.Date(data2$Date, format="%m/%d/%Y")
Error: unexpected '>' in ">"
> data3$Date <- as.Date(data3$Date, format="%m/%d/%Y")
Error: unexpected '>' in ">"
> data4$Date <- as.Date(data4$Date, format="%m/%d/%Y")
Error: unexpected '>' in ">"
> data5$Date <- as.Date(data5$Date, format="%m/%d/%Y")
Error: unexpected '>' in ">"
> data6$Date <- as.Date(data6$Date, format="%m/%d/%Y")
Error: unexpected '>' in ">"
> data2 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> data3 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> data4 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> data5 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> data6 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> ts1 <- ts(data1[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
Error in as.POSIXlt.character(x, tz = tz(x)) :
```

```

character string is not in a standard unambiguous format
> ts1 <- ts(data1[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
Error in as.POSIXlt.character(x, tz = tz(x)) :
  character string is not in a standard unambiguous format
> library(lubridate)
> ts1 <- ts(data1[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
Error in as.POSIXlt.character(x, tz = tz(x)) :
  character string is not in a standard unambiguous format
> data1 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
> ts1 <- ts(data1[,2], start=c(year(min(data1$Date)), month(min(data1$Date))), frequency=4)
Error in as.POSIXlt.character(x, tz = tz(x)) :
  character string is not in a standard unambiguous format
> data1$Date <- as.Date(data1$Date, format="%m/%d/%Y")
> str(data1$Date)
Date[1:120], format: "1994-03-31" "1994-06-30" "1994-09-30" "1994-12-31" "1995-03-31" "1995-06-30"
0" "1995-09-30" "1995-12-31" "1996-03-31" "1996-06-30" "1996-09-30" "1996-12-31" "1997-03-31" "19
97-06-30" "1997-09-30" "1997-12-31" ...
> start_year <- year(min(data1$Date))
> start_month <- month(min(data1$Date))
> print(start_year)
[1] 1994
> print(start_month)
[1] 3
> ts1 <- ts(data1[,2], start=c(start_year, start_month), frequency=4)
> ts2 <- ts(data1[,2], start=c(start_year, start_month), frequency=4)
> ts2 <- ts(data2[,2], start=c(start_year, start_month), frequency=4)
> ts1 <- ts(data1[,2], start=c(start_year, start_month), frequency=4)
> ts3 <- ts(data3[,2], start=c(start_year, start_month), frequency=4)
> ts4 <- ts(data4[,2], start=c(start_year, start_month), frequency=4)
> ts5 <- ts(data5[,2], start=c(start_year, start_month), frequency=4)
> ts6 <- ts(data6[,2], start=c(start_year, start_month), frequency=4)
> anyNA(data1$Date)
[1] FALSE
> anyNA(data2$Date)
[1] FALSE
> anyNA(data3$Date)
[1] FALSE
> anyNA(data4$Date)
[1] FALSE
> anyNA(data5$Date)
[1] FALSE
> anyNA(data6$Date)
[1] FALSE
> mts_data <- cbind(ts1, ts2, ts3, ts4, ts5, ts6)
> var_model <- VAR(mts_data, p=8)
> summary(var_model)
Error in solve.default(Sigma) :
  Lapack routine dgesv: system is exactly singular: U[2,2] = 0
> apply(data1[, -1], 2, var)
Error in apply(data1[, -1], 2, var) : dim(X) must have a positive length
> apply(data1[, -1, drop = FALSE], 2, var)
  Value
0.2255839
> apply(data2[, -1, drop = FALSE], 2, var)
  Value
0.2255839
> apply(data3[, -1, drop = FALSE], 2, var)
  Value
0.2255839
> apply(data4[, -1, drop = FALSE], 2, var)
  Value
0.2255839
> apply(data5[, -1, drop = FALSE], 2, var)
  Value
0.2255839
> apply(data6[, -1, drop = FALSE], 2, var)
  Value
0.2255839
> install.packages("car")
Installing package into 'C:/Users/minhas01/AppData/Local/R/win-library/4.3'

```

```
(as 'lib' is unspecified)
also installing the dependencies 'fs', 'pkgbuild', 'rprojroot', 'diffobj', 'rematch2', 'stringi',
  'brio', 'callr', 'desc', 'digest', 'evaluate', 'jsonlite', 'pkgload', 'praise', 'processx', 'ps',
  'waldo', 'backports', 'ellipsis', 'purrr', 'stringr', 'tidyr', 'Matrix', 'testthat', 'colorspac
e', 'broom', 'dplyr', 'numDeriv', 'SparseM', 'MatrixModels', 'minqa', 'nloptr', 'Rcpp', 'RcppEige
n', 'farver', 'labeling', 'munsell', 'RColorBrewer', 'viridisLite', 'carData', 'abind', 'pbkrtest
', 'quantreg', 'lme4', 'scales'
```

There is a binary version available but the source version is later:

|          | binary | source  | needs_compilation |
|----------|--------|---------|-------------------|
| testthat | 3.2.1  | 3.2.1.1 | TRUE              |

```
Binaries will be installed
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/fs_1.6.3.zip'
Content type 'application/zip' length 393952 bytes (384 KB)
downloaded 384 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/pkgbuild_1.4.4.zip'
Content type 'application/zip' length 202485 bytes (197 KB)
downloaded 197 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/rprojroot_2.0.4.zip'
Content type 'application/zip' length 113611 bytes (110 KB)
downloaded 110 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/diffobj_0.3.5.zip'
Content type 'application/zip' length 1006897 bytes (983 KB)
downloaded 983 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/rematch2_2.1.2.zip'
Content type 'application/zip' length 47517 bytes (46 KB)
downloaded 46 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/stringi_1.8.3.zip'
Content type 'application/zip' length 14998651 bytes (14.3 MB)
downloaded 14.3 MB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/brio_1.1.4.zip'
Content type 'application/zip' length 40388 bytes (39 KB)
downloaded 39 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/callr_3.7.6.zip'
Content type 'application/zip' length 460456 bytes (449 KB)
downloaded 449 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/desc_1.4.3.zip'
Content type 'application/zip' length 329808 bytes (322 KB)
downloaded 322 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/digest_0.6.35.zip'
Content type 'application/zip' length 217636 bytes (212 KB)
downloaded 212 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/evaluate_0.23.zip'
Content type 'application/zip' length 84130 bytes (82 KB)
downloaded 82 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/jsonlite_1.8.8.zip'
Content type 'application/zip' length 1105680 bytes (1.1 MB)
downloaded 1.1 MB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/pkgload_1.3.4.zip'
Content type 'application/zip' length 179711 bytes (175 KB)
downloaded 175 KB
```

```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/praise_1.0.0.zip'
Content type 'application/zip' length 19864 bytes (19 KB)
downloaded 19 KB
```



```
trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/processx_3.8.4.zip'
Content type 'application/zip' length 686717 bytes (670 KB)
downloaded 670 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/ps_1.7.6.zip'
Content type 'application/zip' length 553130 bytes (540 KB)
downloaded 540 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/waldo_0.5.2.zip'
Content type 'application/zip' length 105112 bytes (102 KB)
downloaded 102 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/backports_1.4.1.zip'
Content type 'application/zip' length 101330 bytes (98 KB)
downloaded 98 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/ellipsis_0.3.2.zip'
Content type 'application/zip' length 40504 bytes (39 KB)
downloaded 39 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/purrr_1.0.2.zip'
Content type 'application/zip' length 499240 bytes (487 KB)
downloaded 487 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/stringr_1.5.1.zip'
Content type 'application/zip' length 319042 bytes (311 KB)
downloaded 311 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/tidyr_1.3.1.zip'
Content type 'application/zip' length 1267041 bytes (1.2 MB)
downloaded 1.2 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/Matrix_1.6-5.zip'
Content type 'application/zip' length 4556853 bytes (4.3 MB)
downloaded 4.3 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/testthat_3.2.1.zip'
Content type 'application/zip' length 2222964 bytes (2.1 MB)
downloaded 2.1 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/colourspace_2.1-0.zip'
Content type 'application/zip' length 2629637 bytes (2.5 MB)
downloaded 2.5 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/broom_1.0.5.zip'
Content type 'application/zip' length 1862685 bytes (1.8 MB)
downloaded 1.8 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/dplyr_1.1.4.zip'
Content type 'application/zip' length 1560172 bytes (1.5 MB)
downloaded 1.5 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/numDeriv_2016.8-1.1.zip'
Content type 'application/zip' length 116116 bytes (113 KB)
downloaded 113 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/SparseM_1.81.zip'
Content type 'application/zip' length 1042203 bytes (1017 KB)
downloaded 1017 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/MatrixModels_0.5-3.zip'
Content type 'application/zip' length 414375 bytes (404 KB)
downloaded 404 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/minqa_1.2.6.zip'
Content type 'application/zip' length 459251 bytes (448 KB)
downloaded 448 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/nloptr_2.0.3.zip'
Content type 'application/zip' length 1011763 bytes (988 KB)
```

downloaded 988 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/Rcpp\_1.0.12.zip'  
Content type 'application/zip' length 2877947 bytes (2.7 MB)  
downloaded 2.7 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/RcppEigen\_0.3.4.0.0.zip'  
Content type 'application/zip' length 2611015 bytes (2.5 MB)  
downloaded 2.5 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/farver\_2.1.1.zip'  
Content type 'application/zip' length 1505868 bytes (1.4 MB)  
downloaded 1.4 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/labeling\_0.4.3.zip'  
Content type 'application/zip' length 62568 bytes (61 KB)  
downloaded 61 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/munsell\_0.5.1.zip'  
Content type 'application/zip' length 245466 bytes (239 KB)  
downloaded 239 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/RColorBrewer\_1.1-3.zip'  
Content type 'application/zip' length 56066 bytes (54 KB)  
downloaded 54 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/viridisLite\_0.4.2.zip'  
Content type 'application/zip' length 1300105 bytes (1.2 MB)  
downloaded 1.2 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/carData\_3.0-5.zip'  
Content type 'application/zip' length 1822266 bytes (1.7 MB)  
downloaded 1.7 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/abind\_1.4-5.zip'  
Content type 'application/zip' length 63774 bytes (62 KB)  
downloaded 62 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/pbkrtest\_0.5.2.zip'  
Content type 'application/zip' length 191208 bytes (186 KB)  
downloaded 186 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/quantreg\_5.97.zip'  
Content type 'application/zip' length 1562933 bytes (1.5 MB)  
downloaded 1.5 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/lme4\_1.1-35.2.zip'  
Content type 'application/zip' length 4557183 bytes (4.3 MB)  
downloaded 4.3 MB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/scales\_1.3.0.zip'  
Content type 'application/zip' length 703730 bytes (687 KB)  
downloaded 687 KB

trying URL 'https://cran.case.edu/bin/windows/contrib/4.3/car\_3.1-2.zip'  
Content type 'application/zip' length 1707812 bytes (1.6 MB)  
downloaded 1.6 MB

package 'fs' successfully unpacked and MD5 sums checked  
package 'pkgbuild' successfully unpacked and MD5 sums checked  
package 'rprojroot' successfully unpacked and MD5 sums checked  
package 'diffobj' successfully unpacked and MD5 sums checked  
package 'rematch2' successfully unpacked and MD5 sums checked  
package 'stringi' successfully unpacked and MD5 sums checked  
package 'brio' successfully unpacked and MD5 sums checked  
package 'callr' successfully unpacked and MD5 sums checked  
package 'desc' successfully unpacked and MD5 sums checked  
package 'digest' successfully unpacked and MD5 sums checked  
package 'evaluate' successfully unpacked and MD5 sums checked  
package 'jsonlite' successfully unpacked and MD5 sums checked

```

package 'pkgload' successfully unpacked and MD5 sums checked
package 'praise' successfully unpacked and MD5 sums checked
package 'processx' successfully unpacked and MD5 sums checked
package 'ps' successfully unpacked and MD5 sums checked
package 'waldo' successfully unpacked and MD5 sums checked
package 'backports' successfully unpacked and MD5 sums checked
package 'ellipsis' successfully unpacked and MD5 sums checked
package 'purrr' successfully unpacked and MD5 sums checked
package 'stringr' successfully unpacked and MD5 sums checked
package 'tidyr' successfully unpacked and MD5 sums checked
package 'Matrix' successfully unpacked and MD5 sums checked
package 'testthat' successfully unpacked and MD5 sums checked
package 'colorspace' successfully unpacked and MD5 sums checked
package 'broom' successfully unpacked and MD5 sums checked
package 'dplyr' successfully unpacked and MD5 sums checked
package 'numDeriv' successfully unpacked and MD5 sums checked
package 'SparseM' successfully unpacked and MD5 sums checked
package 'MatrixModels' successfully unpacked and MD5 sums checked
package 'minqa' successfully unpacked and MD5 sums checked
package 'nloptr' successfully unpacked and MD5 sums checked
package 'Rcpp' successfully unpacked and MD5 sums checked
package 'RcppEigen' successfully unpacked and MD5 sums checked
package 'farver' successfully unpacked and MD5 sums checked
package 'labeling' successfully unpacked and MD5 sums checked
package 'munsell' successfully unpacked and MD5 sums checked
package 'RColorBrewer' successfully unpacked and MD5 sums checked
package 'viridisLite' successfully unpacked and MD5 sums checked
package 'carData' successfully unpacked and MD5 sums checked
package 'abind' successfully unpacked and MD5 sums checked
package 'pbkrtest' successfully unpacked and MD5 sums checked
package 'quantreg' successfully unpacked and MD5 sums checked
package 'lme4' successfully unpacked and MD5 sums checked
package 'scales' successfully unpacked and MD5 sums checked
package 'car' successfully unpacked and MD5 sums checked

```

The downloaded binary packages are in

```
C:\Users\minhas01\AppData\Local\Temp\RtmpGAggMH\downloaded_packages
```

```
> library(car)
```

```
Loading required package: carData
```

```
Warning messages:
```

```
1: package 'car' was built under R version 4.3.3
2: package 'carData' was built under R version 4.3.3
```

```
> data2 <- read.csv("C:.csv")
```

```
Error in file(file, "rt") : cannot open the connection
```

```
In addition: Warning message:
```

```
In file(file, "rt") : cannot open file 'C:.csv': No such file or directory
```

```
> data1 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/3M TBill SA.csv")
```

```
> data2 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US CPI SA.csv")
```

```
> data3 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US IP SA.csv")
```

```
> data4 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/US Unemployment SA.csv")
```

```
> data5 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/USDebt SA.csv")
```

```
> data6 <- read.csv("C:/Users/minhas01/Desktop/Nahayan Minhas/CSV Data/USDXY SA.csv")
```

```
> data1$Date <- as.Date(data1$Date, format="%m/%d/%Y")
```

```
> data2$Date <- as.Date(data2$Date, format="%m/%d/%Y")
```

```
> data3$Date <- as.Date(data3$Date, format="%m/%d/%Y")
```

```
> data4$Date <- as.Date(data4$Date, format="%m/%d/%Y")
```

```
> data5$Date <- as.Date(data5$Date, format="%m/%d/%Y")
```

```
> data6$Date <- as.Date(data6$Date, format="%m/%d/%Y")
```

```
> ts1 <- ts(data1[,2], start=c(start_year, start_month), frequency=4)
```

```
> ts2 <- ts(data2[,2], start=c(start_year, start_month), frequency=4)
```

```
> ts3 <- ts(data3[,2], start=c(start_year, start_month), frequency=4)
```

```
> ts4 <- ts(data4[,2], start=c(start_year, start_month), frequency=4)
```

```
> ts5 <- ts(data5[,2], start=c(start_year, start_month), frequency=4)
```

```
> ts6 <- ts(data6[,2], start=c(start_year, start_month), frequency=4)
```

```
> mts_data <- cbind(ts1, ts2, ts3, ts4, ts5, ts6)
```

```
> var_model <- VAR(mts_data, p=8)
```

```
> summary(var_model)
```

VAR Estimation Results:

```
=====
```

Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6

Deterministic variables: const

Sample size: 112

Log Likelihood: -1247.121

Roots of the characteristic polynomial:

```
0.9322 0.9322 0.9244 0.9244 0.9186 0.9186 0.9141 0.9125 0.9125 0.9087 0.9087 0.8834 0.8834 0.8809
0.8809 0.8802 0.8802 0.8776 0.8776 0.8762 0.8762 0.871 0.871 0.8668 0.8668 0.8598 0.8598 0.8584
0.8584 0.8548 0.8548 0.8527 0.8527 0.8301 0.8301 0.8201 0.8201 0.8155 0.8155 0.7974 0.7974 0.7737
0.7737 0.6445 0.6445 0.6214 0.6214 0.2645
```

Call:

```
VAR(y = mts_data, p = 8)
```

Estimation results for equation ts1:

```
=====
ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
+ ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + ts1.
l8 + ts2.l8 + ts3.l8 + ts4.l8 + ts5.l8 + ts6.l8 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |    |
|--------|------------|------------|---------|----------|----|
| ts1.l1 | 0.4071621  | 0.1451618  | 2.805   | 0.00669  | ** |
| ts2.l1 | 0.0160823  | 0.0396411  | 0.406   | 0.68634  |    |
| ts3.l1 | 0.1195472  | 0.0477696  | 2.503   | 0.01494  | *  |
| ts4.l1 | 0.0432812  | 0.0983072  | 0.440   | 0.66125  |    |
| ts5.l1 | 0.0007044  | 0.0006794  | 1.037   | 0.30375  |    |
| ts6.l1 | 0.0057486  | 0.0118797  | 0.484   | 0.63014  |    |
| ts1.l2 | -0.1947620 | 0.1685946  | -1.155  | 0.25237  |    |
| ts2.l2 | 0.0161757  | 0.0411035  | 0.394   | 0.69525  |    |
| ts3.l2 | -0.0204315 | 0.0523692  | -0.390  | 0.69775  |    |
| ts4.l2 | -0.1183711 | 0.1024953  | -1.155  | 0.25250  |    |
| ts5.l2 | 0.0006939  | 0.0009093  | 0.763   | 0.44826  |    |
| ts6.l2 | 0.0073743  | 0.0123723  | 0.596   | 0.55329  |    |
| ts1.l3 | 0.0849648  | 0.1746813  | 0.486   | 0.62837  |    |
| ts2.l3 | -0.0032184 | 0.0469967  | -0.068  | 0.94562  |    |
| ts3.l3 | -0.0430236 | 0.0585651  | -0.735  | 0.46529  |    |
| ts4.l3 | -0.1986572 | 0.1109458  | -1.791  | 0.07817  | .  |
| ts5.l3 | 0.0010374  | 0.0010648  | 0.974   | 0.33365  |    |
| ts6.l3 | -0.0144268 | 0.0124745  | -1.157  | 0.25184  |    |
| ts1.l4 | 0.1131031  | 0.1790124  | 0.632   | 0.52979  |    |
| ts2.l4 | -0.0006448 | 0.0506800  | -0.013  | 0.98989  |    |
| ts3.l4 | -0.0916920 | 0.0542368  | -1.691  | 0.09586  | .  |
| ts4.l4 | -0.2188471 | 0.1040333  | -2.104  | 0.03941  | *  |
| ts5.l4 | 0.0014324  | 0.0011043  | 1.297   | 0.19930  |    |
| ts6.l4 | 0.0011384  | 0.0131941  | 0.086   | 0.93152  |    |
| ts1.l5 | -0.1747809 | 0.1942699  | -0.900  | 0.37172  |    |
| ts2.l5 | 0.0278041  | 0.0442002  | 0.629   | 0.53159  |    |
| ts3.l5 | 0.0416449  | 0.0549159  | 0.758   | 0.45107  |    |
| ts4.l5 | -0.1203155 | 0.1035908  | -1.161  | 0.24984  |    |
| ts5.l5 | 0.0017232  | 0.0011043  | 1.560   | 0.12367  |    |
| ts6.l5 | -0.0057851 | 0.0135024  | -0.428  | 0.66979  |    |
| ts1.l6 | -0.0141550 | 0.1968825  | -0.072  | 0.94291  |    |
| ts2.l6 | -0.0466317 | 0.0435009  | -1.072  | 0.28782  |    |
| ts3.l6 | -0.0707582 | 0.0557233  | -1.270  | 0.20882  |    |
| ts4.l6 | -0.1279168 | 0.1057858  | -1.209  | 0.23110  |    |
| ts5.l6 | 0.0013684  | 0.0010859  | 1.260   | 0.21228  |    |
| ts6.l6 | 0.0009172  | 0.0132262  | 0.069   | 0.94494  |    |
| ts1.l7 | 0.0065570  | 0.1919249  | 0.034   | 0.97285  |    |
| ts2.l7 | 0.0066008  | 0.0417085  | 0.158   | 0.87476  |    |
| ts3.l7 | -0.0252425 | 0.0537202  | -0.470  | 0.64006  |    |
| ts4.l7 | -0.1068979 | 0.1097950  | -0.974  | 0.33397  |    |
| ts5.l7 | -0.0001113 | 0.0010061  | -0.111  | 0.91225  |    |
| ts6.l7 | -0.0241840 | 0.0122268  | -1.978  | 0.05231  | .  |
| ts1.l8 | -0.1285223 | 0.1697864  | -0.757  | 0.45189  |    |
| ts2.l8 | 0.0218230  | 0.0409548  | 0.533   | 0.59601  |    |
| ts3.l8 | -0.0206138 | 0.0515219  | -0.400  | 0.69044  |    |
| ts4.l8 | -0.0259381 | 0.1000662  | -0.259  | 0.79632  |    |
| ts5.l8 | 0.0002990  | 0.0008101  | 0.369   | 0.71333  |    |
| ts6.l8 | 0.0026337  | 0.0116856  | 0.225   | 0.82241  |    |

```
const -0.0458964 0.0860694 -0.533 0.59574
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.3882 on 63 degrees of freedom
```

```
Multiple R-Squared: 0.6109, Adjusted R-squared: 0.3144
```

```
F-statistic: 2.06 on 48 and 63 DF, p-value: 0.003652
```

```
Estimation results for equation ts2:
```

```
=====
```

```
ts2 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
+ ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + ts1.
l8 + ts2.l8 + ts3.l8 + ts4.l8 + ts5.l8 + ts6.l8 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t )   |
|--------|------------|------------|---------|------------|
| ts1.l1 | 0.4865300  | 0.4837906  | 1.006   | 0.31843    |
| ts2.l1 | 0.1234462  | 0.1321146  | 0.934   | 0.35367    |
| ts3.l1 | 0.2699293  | 0.1592050  | 1.695   | 0.09492 .  |
| ts4.l1 | 0.0280901  | 0.3276353  | 0.086   | 0.93195    |
| ts5.l1 | -0.0027140 | 0.0022642  | -1.199  | 0.23516    |
| ts6.l1 | -0.0787097 | 0.0395924  | -1.988  | 0.05116 .  |
| ts1.l2 | -1.4108009 | 0.5618866  | -2.511  | 0.01462 *  |
| ts2.l2 | 0.2894691  | 0.1369884  | 2.113   | 0.03856 *  |
| ts3.l2 | -0.1208490 | 0.1745345  | -0.692  | 0.49123    |
| ts4.l2 | -0.3626595 | 0.3415932  | -1.062  | 0.29244    |
| ts5.l2 | -0.0046366 | 0.0030306  | -1.530  | 0.13104    |
| ts6.l2 | 0.0799286  | 0.0412340  | 1.938   | 0.05706 .  |
| ts1.l3 | 0.3459173  | 0.5821722  | 0.594   | 0.55452    |
| ts2.l3 | 0.2939428  | 0.1566291  | 1.877   | 0.06519 .  |
| ts3.l3 | 0.0396321  | 0.1951839  | 0.203   | 0.83975    |
| ts4.l3 | 0.0894819  | 0.3697567  | 0.242   | 0.80956    |
| ts5.l3 | -0.0002310 | 0.0035486  | -0.065  | 0.94831    |
| ts6.l3 | -0.0155464 | 0.0415745  | -0.374  | 0.70970    |
| ts1.l4 | 1.9633173  | 0.5966070  | 3.291   | 0.00164 ** |
| ts2.l4 | -0.1915373 | 0.1689046  | -1.134  | 0.26109    |
| ts3.l4 | -0.3217123 | 0.1807587  | -1.780  | 0.07993 .  |
| ts4.l4 | -0.2089925 | 0.3467190  | -0.603  | 0.54882    |
| ts5.l4 | 0.0002785  | 0.0036803  | 0.076   | 0.93992    |
| ts6.l4 | -0.0003043 | 0.0439728  | -0.007  | 0.99450    |
| ts1.l5 | -0.6630368 | 0.6474565  | -1.024  | 0.30972    |
| ts2.l5 | 0.0998861  | 0.1473090  | 0.678   | 0.50021    |
| ts3.l5 | -0.0694694 | 0.1830218  | -0.380  | 0.70554    |
| ts4.l5 | -0.0101821 | 0.3452442  | -0.029  | 0.97657    |
| ts5.l5 | 0.0021201  | 0.0036805  | 0.576   | 0.56665    |
| ts6.l5 | 0.0240804  | 0.0450003  | 0.535   | 0.59445    |
| ts1.l6 | -0.3933298 | 0.6561637  | -0.599  | 0.55103    |
| ts2.l6 | 0.1674896  | 0.1449786  | 1.155   | 0.25234    |
| ts3.l6 | 0.0545068  | 0.1857127  | 0.294   | 0.77010    |
| ts4.l6 | 0.6846945  | 0.3525595  | 1.942   | 0.05660 .  |
| ts5.l6 | 0.0025139  | 0.0036191  | 0.695   | 0.48986    |
| ts6.l6 | -0.0232343 | 0.0440799  | -0.527  | 0.59998    |
| ts1.l7 | -0.0266272 | 0.6396413  | -0.042  | 0.96693    |
| ts2.l7 | -0.0225375 | 0.1390048  | -0.162  | 0.87172    |
| ts3.l7 | 0.0153348  | 0.1790370  | 0.086   | 0.93201    |
| ts4.l7 | 0.3914556  | 0.3659214  | 1.070   | 0.28880    |
| ts5.l7 | -0.0007959 | 0.0033532  | -0.237  | 0.81315    |
| ts6.l7 | 0.0086331  | 0.0407490  | 0.212   | 0.83290    |
| ts1.l8 | 0.6623238  | 0.5658587  | 1.170   | 0.24622    |
| ts2.l8 | -0.1013002 | 0.1364930  | -0.742  | 0.46075    |
| ts3.l8 | 0.0234016  | 0.1717105  | 0.136   | 0.89203    |
| ts4.l8 | 0.7121714  | 0.3334976  | 2.135   | 0.03662 *  |
| ts5.l8 | -0.0004209 | 0.0027000  | -0.156  | 0.87663    |
| ts6.l8 | -0.0005662 | 0.0389453  | -0.015  | 0.98845    |
| const  | 0.5705940  | 0.2868495  | 1.989   | 0.05103 .  |

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 1.294 on 63 degrees of freedom  
 Multiple R-Squared: 0.6563, Adjusted R-squared: 0.3944  
 F-statistic: 2.506 on 48 and 63 DF, p-value: 0.0003387

Estimation results for equation ts3:

=====

ts3 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + ts5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 + ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6 + ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + ts1.l8 + ts2.l8 + ts3.l8 + ts4.l8 + ts5.l8 + ts6.l8 + const

|        | Estimate   | Std. Error | t value | Pr(> t ) |    |
|--------|------------|------------|---------|----------|----|
| ts1.l1 | 0.7472428  | 0.4412190  | 1.694   | 0.09528  | .  |
| ts2.l1 | 0.2792941  | 0.1204890  | 2.318   | 0.02371  | *  |
| ts3.l1 | 0.4702884  | 0.1451956  | 3.239   | 0.00192  | ** |
| ts4.l1 | 0.8176421  | 0.2988047  | 2.736   | 0.00806  | ** |
| ts5.l1 | -0.0057669 | 0.0020650  | -2.793  | 0.00691  | ** |
| ts6.l1 | -0.0126742 | 0.0361084  | -0.351  | 0.72676  |    |
| ts1.l2 | -0.0164987 | 0.5124428  | -0.032  | 0.97442  |    |
| ts2.l2 | -0.2214761 | 0.1249340  | -1.773  | 0.08111  | .  |
| ts3.l2 | 0.2572225  | 0.1591762  | 1.616   | 0.11110  |    |
| ts4.l2 | 0.5165079  | 0.3115343  | 1.658   | 0.10230  |    |
| ts5.l2 | -0.0041990 | 0.0027639  | -1.519  | 0.13371  |    |
| ts6.l2 | 0.0697133  | 0.0376056  | 1.854   | 0.06845  | .  |
| ts1.l3 | 1.5272667  | 0.5309434  | 2.877   | 0.00548  | ** |
| ts2.l3 | -0.4227306 | 0.1428464  | -2.959  | 0.00434  | ** |
| ts3.l3 | -0.0860550 | 0.1780085  | -0.483  | 0.63047  |    |
| ts4.l3 | -0.2863717 | 0.3372196  | -0.849  | 0.39898  |    |
| ts5.l3 | -0.0024300 | 0.0032364  | -0.751  | 0.45554  |    |
| ts6.l3 | -0.0951239 | 0.0379162  | -2.509  | 0.01470  | *  |
| ts1.l4 | -0.9112222 | 0.5441080  | -1.675  | 0.09895  | .  |
| ts2.l4 | 0.1171806  | 0.1540417  | 0.761   | 0.44967  |    |
| ts3.l4 | -0.0290964 | 0.1648527  | -0.176  | 0.86047  |    |
| ts4.l4 | -0.0106475 | 0.3162091  | -0.034  | 0.97324  |    |
| ts5.l4 | -0.0024404 | 0.0033564  | -0.727  | 0.46986  |    |
| ts6.l4 | 0.0662106  | 0.0401034  | 1.651   | 0.10372  |    |
| ts1.l5 | -1.1586452 | 0.5904829  | -1.962  | 0.05416  | .  |
| ts2.l5 | 0.1581621  | 0.1343464  | 1.177   | 0.24352  |    |
| ts3.l5 | 0.1179862  | 0.1669167  | 0.707   | 0.48226  |    |
| ts4.l5 | -0.1008534 | 0.3148641  | -0.320  | 0.74980  |    |
| ts5.l5 | 0.0015400  | 0.0033567  | 0.459   | 0.64796  |    |
| ts6.l5 | -0.0192163 | 0.0410405  | -0.468  | 0.64124  |    |
| ts1.l6 | 1.1171412  | 0.5984239  | 1.867   | 0.06658  | .  |
| ts2.l6 | -0.1439382 | 0.1322210  | -1.089  | 0.28047  |    |
| ts3.l6 | -0.1336546 | 0.1693707  | -0.789  | 0.43300  |    |
| ts4.l6 | 0.3625947  | 0.3215357  | 1.128   | 0.26372  |    |
| ts5.l6 | 0.0046882  | 0.0033007  | 1.420   | 0.16043  |    |
| ts6.l6 | 0.0289977  | 0.0402011  | 0.721   | 0.47338  |    |
| ts1.l7 | -0.2820099 | 0.5833555  | -0.483  | 0.63047  |    |
| ts2.l7 | 0.2033183  | 0.1267729  | 1.604   | 0.11376  |    |
| ts3.l7 | 0.0533235  | 0.1632825  | 0.327   | 0.74507  |    |
| ts4.l7 | 0.6368697  | 0.3337218  | 1.908   | 0.06090  | .  |
| ts5.l7 | -0.0007831 | 0.0030581  | -0.256  | 0.79874  |    |
| ts6.l7 | 0.0682590  | 0.0371632  | 1.837   | 0.07097  | .  |
| ts1.l8 | 0.4824547  | 0.5160654  | 0.935   | 0.35342  |    |
| ts2.l8 | -0.1014239 | 0.1244822  | -0.815  | 0.41828  |    |
| ts3.l8 | -0.0111756 | 0.1566007  | -0.071  | 0.94333  |    |
| ts4.l8 | 0.0666626  | 0.3041511  | 0.219   | 0.82722  |    |
| ts5.l8 | 0.0005343  | 0.0024624  | 0.217   | 0.82892  |    |
| ts6.l8 | -0.0622793 | 0.0355182  | -1.753  | 0.08439  | .  |
| const  | 0.3379266  | 0.2616079  | 1.292   | 0.20117  |    |

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.18 on 63 degrees of freedom

Multiple R-Squared: 0.6628,      Adjusted R-squared: 0.406  
 F-statistic: 2.58 on 48 and 63 DF,   p-value: 0.0002283

Estimation results for equation ts4:

=====

$$\text{ts4} = \text{ts1.11} + \text{ts2.11} + \text{ts3.11} + \text{ts4.11} + \text{ts5.11} + \text{ts6.11} + \text{ts1.12} + \text{ts2.12} + \text{ts3.12} + \text{ts4.12} + \text{ts5.12} + \text{ts6.12} + \text{ts1.13} + \text{ts2.13} + \text{ts3.13} + \text{ts4.13} + \text{ts5.13} + \text{ts6.13} + \text{ts1.14} + \text{ts2.14} + \text{ts3.14} + \text{ts4.14} + \text{ts5.14} + \text{ts6.14} + \text{ts1.15} + \text{ts2.15} + \text{ts3.15} + \text{ts4.15} + \text{ts5.15} + \text{ts6.15} + \text{ts1.16} + \text{ts2.16} + \text{ts3.16} + \text{ts4.16} + \text{ts5.16} + \text{ts6.16} + \text{ts1.17} + \text{ts2.17} + \text{ts3.17} + \text{ts4.17} + \text{ts5.17} + \text{ts6.17} + \text{ts1.18} + \text{ts2.18} + \text{ts3.18} + \text{ts4.18} + \text{ts5.18} + \text{ts6.18} + \text{const}$$

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.11 | -6.604e-01 | 2.161e-01  | -3.057  | 0.003280 | **  |
| ts2.11 | -7.504e-02 | 5.900e-02  | -1.272  | 0.208077 |     |
| ts3.11 | -2.625e-01 | 7.110e-02  | -3.692  | 0.000467 | *** |
| ts4.11 | -3.571e-01 | 1.463e-01  | -2.440  | 0.017497 | *   |
| ts5.11 | 4.593e-03  | 1.011e-03  | 4.542   | 2.58e-05 | *** |
| ts6.11 | 1.378e-02  | 1.768e-02  | 0.780   | 0.438570 |     |
| ts1.12 | 1.900e-01  | 2.509e-01  | 0.757   | 0.451838 |     |
| ts2.12 | 1.358e-01  | 6.118e-02  | 2.220   | 0.030052 | *   |
| ts3.12 | 1.740e-01  | 7.794e-02  | 2.233   | 0.029131 | *   |
| ts4.12 | 2.349e-01  | 1.526e-01  | 1.539   | 0.128691 |     |
| ts5.12 | 5.182e-03  | 1.353e-03  | 3.829   | 0.000299 | *** |
| ts6.12 | -1.219e-02 | 1.841e-02  | -0.662  | 0.510561 |     |
| ts1.13 | -4.195e-01 | 2.600e-01  | -1.614  | 0.111599 |     |
| ts2.13 | -2.317e-02 | 6.995e-02  | -0.331  | 0.741600 |     |
| ts3.13 | 1.949e-02  | 8.717e-02  | 0.224   | 0.823757 |     |
| ts4.13 | -4.530e-02 | 1.651e-01  | -0.274  | 0.784747 |     |
| ts5.13 | 2.854e-03  | 1.585e-03  | 1.801   | 0.076514 | .   |
| ts6.13 | 3.606e-02  | 1.857e-02  | 1.942   | 0.056619 | .   |
| ts1.14 | 5.691e-01  | 2.664e-01  | 2.136   | 0.036563 | *   |
| ts2.14 | -1.151e-01 | 7.543e-02  | -1.526  | 0.131948 |     |
| ts3.14 | -1.009e-01 | 8.072e-02  | -1.250  | 0.215845 |     |
| ts4.14 | -2.302e-01 | 1.548e-01  | -1.486  | 0.142156 |     |
| ts5.14 | 3.183e-03  | 1.644e-03  | 1.937   | 0.057258 | .   |
| ts6.14 | -4.774e-02 | 1.964e-02  | -2.431  | 0.017909 | *   |
| ts1.15 | 8.159e-02  | 2.891e-01  | 0.282   | 0.778739 |     |
| ts2.15 | 3.875e-02  | 6.579e-02  | 0.589   | 0.557979 |     |
| ts3.15 | -1.158e-01 | 8.174e-02  | -1.417  | 0.161493 |     |
| ts4.15 | -1.606e-01 | 1.542e-01  | -1.041  | 0.301674 |     |
| ts5.15 | 1.890e-03  | 1.644e-03  | 1.150   | 0.254530 |     |
| ts6.15 | 8.140e-04  | 2.010e-02  | 0.041   | 0.967818 |     |
| ts1.16 | -6.167e-01 | 2.930e-01  | -2.105  | 0.039315 | *   |
| ts2.16 | 9.863e-02  | 6.475e-02  | 1.523   | 0.132672 |     |
| ts3.16 | 3.402e-02  | 8.294e-02  | 0.410   | 0.683094 |     |
| ts4.16 | -1.319e-01 | 1.574e-01  | -0.838  | 0.405402 |     |
| ts5.16 | -8.530e-04 | 1.616e-03  | -0.528  | 0.599514 |     |
| ts6.16 | 5.265e-03  | 1.969e-02  | 0.267   | 0.790008 |     |
| ts1.17 | 4.386e-01  | 2.857e-01  | 1.535   | 0.129710 |     |
| ts2.17 | -7.969e-02 | 6.208e-02  | -1.284  | 0.203921 |     |
| ts3.17 | 4.159e-02  | 7.996e-02  | 0.520   | 0.604771 |     |
| ts4.17 | -1.462e-02 | 1.634e-01  | -0.089  | 0.928981 |     |
| ts5.17 | -2.419e-06 | 1.497e-03  | -0.002  | 0.998716 |     |
| ts6.17 | -1.855e-02 | 1.820e-02  | -1.019  | 0.311904 |     |
| ts1.18 | -2.756e-01 | 2.527e-01  | -1.090  | 0.279669 |     |
| ts2.18 | 8.396e-02  | 6.096e-02  | 1.377   | 0.173268 |     |
| ts3.18 | 5.434e-02  | 7.668e-02  | 0.709   | 0.481183 |     |
| ts4.18 | 1.344e-01  | 1.489e-01  | 0.903   | 0.370123 |     |
| ts5.18 | 9.899e-04  | 1.206e-03  | 0.821   | 0.414780 |     |
| ts6.18 | 2.300e-02  | 1.739e-02  | 1.323   | 0.190740 |     |
| const  | -7.036e-02 | 1.281e-01  | -0.549  | 0.584778 |     |

---  
 Signif. codes:   0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.5778 on 63 degrees of freedom  
 Multiple R-Squared: 0.6891,      Adjusted R-squared: 0.4522  
 F-statistic: 2.909 on 48 and 63 DF,   p-value: 4.108e-05

## Estimation results for equation ts5:

=====

```
ts5 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + ts5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 + ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16 + ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + ts1.18 + ts2.18 + ts3.18 + ts4.18 + ts5.18 + ts6.18 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t )   |
|--------|------------|------------|---------|------------|
| ts1.11 | 32.821601  | 27.033668  | 1.214   | 0.22924    |
| ts2.11 | -7.535064  | 7.382412   | -1.021  | 0.31131    |
| ts3.11 | -4.901373  | 8.896192   | -0.551  | 0.58362    |
| ts4.11 | -28.279361 | 18.307885  | -1.545  | 0.12744    |
| ts5.11 | -0.715936  | 0.126522   | -5.659  | 4e-07 ***  |
| ts6.11 | -1.911617  | 2.212377   | -0.864  | 0.39084    |
| ts1.12 | -10.316124 | 31.397584  | -0.329  | 0.74357    |
| ts2.12 | -0.744272  | 7.654756   | -0.097  | 0.92285    |
| ts3.12 | -9.517544  | 9.752789   | -0.976  | 0.33286    |
| ts4.12 | -26.782217 | 19.087838  | -1.403  | 0.16550    |
| ts5.12 | -0.518616  | 0.169346   | -3.062  | 0.00323 ** |
| ts6.12 | -1.342462  | 2.304108   | -0.583  | 0.56222    |
| ts1.13 | -39.274415 | 32.531121  | -1.207  | 0.23183    |
| ts2.13 | 16.461617  | 8.752257   | 1.881   | 0.06462 .  |
| ts3.13 | 10.636012  | 10.906657  | 0.975   | 0.33320    |
| ts4.13 | 9.670365   | 20.661584  | 0.468   | 0.64137    |
| ts5.13 | -0.315262  | 0.198294   | -1.590  | 0.11687    |
| ts6.13 | 3.705391   | 2.323138   | 1.595   | 0.11572    |
| ts1.14 | -16.773062 | 33.337720  | -0.503  | 0.61663    |
| ts2.14 | -11.905202 | 9.438200   | -1.261  | 0.21182    |
| ts3.14 | -7.586657  | 10.100592  | -0.751  | 0.45538    |
| ts4.14 | -4.201211  | 19.374262  | -0.217  | 0.82903    |
| ts5.14 | -0.035127  | 0.205649   | -0.171  | 0.86492    |
| ts6.14 | -0.898736  | 2.457151   | -0.366  | 0.71577    |
| ts1.15 | 24.980211  | 36.179131  | 0.690   | 0.49244    |
| ts2.15 | 0.268073   | 8.231459   | 0.033   | 0.97412    |
| ts3.15 | 7.462809   | 10.227052  | 0.730   | 0.46827    |
| ts4.15 | 18.674524  | 19.291855  | 0.968   | 0.33675    |
| ts5.15 | 0.062026   | 0.205664   | 0.302   | 0.76396    |
| ts6.15 | -0.947200  | 2.514567   | -0.377  | 0.70767    |
| ts1.16 | 1.468969   | 36.665682  | 0.040   | 0.96817    |
| ts2.16 | 8.156117   | 8.101237   | 1.007   | 0.31789    |
| ts3.16 | -2.270087  | 10.377414  | -0.219  | 0.82755    |
| ts4.16 | -32.350416 | 19.700624  | -1.642  | 0.10555    |
| ts5.16 | -0.001018  | 0.202233   | -0.005  | 0.99600    |
| ts6.16 | 3.019005   | 2.463135   | 1.226   | 0.22488    |
| ts1.17 | -35.046546 | 35.742430  | -0.981  | 0.33057    |
| ts2.17 | 0.113709   | 7.767430   | 0.015   | 0.98837    |
| ts3.17 | -10.646313 | 10.004385  | -1.064  | 0.29132    |
| ts4.17 | 4.647118   | 20.447272  | 0.227   | 0.82095    |
| ts5.17 | 0.291681   | 0.187372   | 1.557   | 0.12455    |
| ts6.17 | -1.695982  | 2.277006   | -0.745  | 0.45914    |
| ts1.18 | 56.023073  | 31.619541  | 1.772   | 0.08127 .  |
| ts2.18 | -0.099078  | 7.627075   | -0.013  | 0.98968    |
| ts3.18 | -5.057765  | 9.594990   | -0.527  | 0.59996    |
| ts4.18 | 3.962720   | 18.635465  | 0.213   | 0.83229    |
| ts5.18 | 0.035074   | 0.150872   | 0.232   | 0.81692    |
| ts6.18 | -0.494233  | 2.176216   | -0.227  | 0.82108    |
| const  | 1.440807   | 16.028825  | 0.090   | 0.92866    |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 72.3 on 63 degrees of freedom

Multiple R-Squared: 0.6379, Adjusted R-squared: 0.3621

F-statistic: 2.313 on 48 and 63 DF, p-value: 0.0009478

## Estimation results for equation ts6:

=====



```
ts6 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
  ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
  + ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + ts1.
18 + ts2.l8 + ts3.l8 + ts4.l8 + ts5.l8 + ts6.l8 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |
|--------|------------|------------|---------|----------|
| ts1.l1 | -1.2293446 | 1.6530222  | -0.744  | 0.4598   |
| ts2.l1 | 0.0007628  | 0.4514108  | 0.002   | 0.9987   |
| ts3.l1 | -0.2504653 | 0.5439737  | -0.460  | 0.6468   |
| ts4.l1 | -0.1770179 | 1.1194686  | -0.158  | 0.8749   |
| ts5.l1 | -0.0079054 | 0.0077364  | -1.022  | 0.3108   |
| ts6.l1 | 0.3103586  | 0.1352797  | 2.294   | 0.0251 * |
| ts1.l2 | 0.6311613  | 1.9198617  | 0.329   | 0.7434   |
| ts2.l2 | 1.1230868  | 0.4680638  | 2.399   | 0.0194 * |
| ts3.l2 | 1.2723178  | 0.5963518  | 2.134   | 0.0368 * |
| ts4.l2 | 0.3478962  | 1.1671602  | 0.298   | 0.7666   |
| ts5.l2 | -0.0067309 | 0.0103549  | -0.650  | 0.5180   |
| ts6.l2 | -0.0605006 | 0.1408888  | -0.429  | 0.6691   |
| ts1.l3 | -1.0904248 | 1.9891739  | -0.548  | 0.5855   |
| ts2.l3 | -0.0556761 | 0.5351725  | -0.104  | 0.9175   |
| ts3.l3 | -0.8555631 | 0.6669071  | -1.283  | 0.2042   |
| ts4.l3 | -1.3537068 | 1.2633897  | -1.071  | 0.2880   |
| ts5.l3 | -0.0061007 | 0.0121251  | -0.503  | 0.6166   |
| ts6.l3 | 0.1425150  | 0.1420525  | 1.003   | 0.3196   |
| ts1.l4 | 1.4591287  | 2.0384948  | 0.716   | 0.4768   |
| ts2.l4 | -0.0770539 | 0.5771157  | -0.134  | 0.8942   |
| ts3.l4 | -0.7536060 | 0.6176189  | -1.220  | 0.2269   |
| ts4.l4 | -0.6162567 | 1.1846741  | -0.520  | 0.6048   |
| ts5.l4 | -0.0019804 | 0.0125748  | -0.157  | 0.8754   |
| ts6.l4 | -0.1046583 | 0.1502469  | -0.697  | 0.4886   |
| ts1.l5 | -0.6576626 | 2.2122380  | -0.297  | 0.7672   |
| ts2.l5 | 0.0877852  | 0.5033273  | 0.174   | 0.8621   |
| ts3.l5 | 0.3905925  | 0.6253515  | 0.625   | 0.5345   |
| ts4.l5 | 1.1187548  | 1.1796351  | 0.948   | 0.3466   |
| ts5.l5 | 0.0001960  | 0.0125757  | 0.016   | 0.9876   |
| ts6.l5 | 0.0291660  | 0.1537577  | 0.190   | 0.8502   |
| ts1.l6 | 0.3196639  | 2.2419890  | 0.143   | 0.8871   |
| ts2.l6 | -0.5319242 | 0.4953647  | -1.074  | 0.2870   |
| ts3.l6 | 0.3735680  | 0.6345456  | 0.589   | 0.5582   |
| ts4.l6 | -0.0524203 | 1.2046301  | -0.044  | 0.9654   |
| ts5.l6 | 0.0004142  | 0.0123659  | 0.033   | 0.9734   |
| ts6.l6 | 0.0842294  | 0.1506128  | 0.559   | 0.5780   |
| ts1.l7 | 2.4135478  | 2.1855351  | 1.104   | 0.2737   |
| ts2.l7 | -0.4375741 | 0.4749535  | -0.921  | 0.3604   |
| ts3.l7 | -0.5854969 | 0.6117361  | -0.957  | 0.3422   |
| ts4.l7 | -0.5107655 | 1.2502852  | -0.409  | 0.6843   |
| ts5.l7 | -0.0089175 | 0.0114572  | -0.778  | 0.4393   |
| ts6.l7 | -0.1444436 | 0.1392316  | -1.037  | 0.3035   |
| ts1.l8 | -1.8050282 | 1.9334337  | -0.934  | 0.3541   |
| ts2.l8 | 0.0699947  | 0.4663712  | 0.150   | 0.8812   |
| ts3.l8 | 0.6028339  | 0.5867029  | 1.027   | 0.3081   |
| ts4.l8 | -0.2138626 | 1.1394990  | -0.188  | 0.8517   |
| ts5.l8 | -0.0151946 | 0.0092253  | -1.647  | 0.1045   |
| ts6.l8 | -0.0334160 | 0.1330687  | -0.251  | 0.8025   |
| const  | -0.5054263 | 0.9801113  | -0.516  | 0.6079   |

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.421 on 63 degrees of freedom  
Multiple R-Squared: 0.431, Adjusted R-squared: -0.002592  
F-statistic: 0.994 on 48 and 63 DF, p-value: 0.5039

Covariance matrix of residuals:

|     | ts1     | ts2    | ts3    | ts4      | ts5     | ts6     |
|-----|---------|--------|--------|----------|---------|---------|
| ts1 | 0.15073 | 0.1485 | 0.1092 | 0.01212  | -6.5221 | 0.2990  |
| ts2 | 0.14846 | 1.6742 | 0.1149 | -0.17243 | -9.8369 | -1.0350 |

```
ts3  0.10916  0.1149  1.3925 -0.26579  -10.1710  -0.5622
ts4  0.01212 -0.1724  -0.2658  0.33391  -0.2102  -0.2496
ts5 -6.52208 -9.8369 -10.1710 -0.21022 5227.6613 -25.0753
ts6  0.29901 -1.0350  -0.5622 -0.24961  -25.0753  19.5459
```

Correlation matrix of residuals:

```
      ts1      ts2      ts3      ts4      ts5      ts6
ts1  1.00000  0.29554  0.23827  0.054045 -0.232344  0.17420
ts2  0.29554  1.00000  0.07523 -0.230618 -0.105148 -0.18093
ts3  0.23827  0.07523  1.00000 -0.389787 -0.119208 -0.10775
ts4  0.05404 -0.23062 -0.38979  1.000000 -0.005032 -0.09770
ts5 -0.23234 -0.10515 -0.11921 -0.005032  1.000000 -0.07844
ts6  0.17420 -0.18093 -0.10775 -0.097704 -0.078445  1.00000
```

```
> save.image("C:\\Users\\minhas01\\Desktop\\Nahayan Minhas\\Workspace main")
> AIC <- AIC(var_model)
> BIC <- BIC(var_model)
> HQC <- summary(var_model)$criteria['HQ']
> cat("AIC:", AIC, "\n")
AIC: 3082.242
> cat("BIC:", BIC, "\n")
BIC: 3881.481
> cat("HQC:", HQC, "\n")
HQC:
> log_likelihood <- logLik(var_model)
> num_parameters <- length(coef(var_model))num_parameters <- length(coef(var_model))
Error: unexpected symbol in "num_parameters <- length(coef(var_model))num_parameters"
> num_parameters <- length(coef(var_model))
> num_observations <- length(var_model$y)/ncol(var_model$y)
> residual_variance <- as.numeric(-2 * log_likelihood / num_observations)
> HQC <- log(residual_variance) + (2 * log(log(num_observations)) * num_parameters) / num_observa
tions
> cat("HQC:", HQC, "\n")
HQC: 3.190849
> num_observations <- nobs(var_model)
Error in nobs.default(var_model) : no 'nobs' method is available
> num_observations <- length(residuals(var_model))
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> cat("HQC:", HQC, "\n")
HQC: 2516.723
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> cat("HQC:", HQC, "\n")
HQC: 2516.723
> train_set <- window(mts_data, end = c(110))
Error in window.default(x, ...) : 'start' cannot be after 'end'
> train_set <- window(mts_data, start=c(1994, 1), end=c(2020, 4))
+
+
+
+ aaaaa
Error: unexpected symbol in:
"
aaaaa"
> train_set <- window(mts_data, start=c(1994, 1), end=c(2020, 4))
+ test_set <- window(mts_data, start=c(2021, 1), end=c(2023, 4))
Error: unexpected symbol in:
"train_set <- window(mts_data, start=c(1994, 1), end=c(2020, 4))
test_set"
> train_set <- window(mts_data, start=c(1994,1), end=c(2020,4))
Warning message:
In window.default(x, ...) : 'start' value not changed
> library(vars)
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, function(f) f$fcst)
Error in f$fcst : $ operator is invalid for atomic vectors
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, `[`, "mean")
Error in FUN(X[[i]], ...) : subscript out of bounds
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
```

```

> actual_values <- as.matrix(test_set)
Error: object 'test_set' not found
> test_set <- window(mts_data, start=c(2021,1), end=c(2023,4))
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> MAPE <- colMeans(abs((actual_values - forecasted_values)/actual_values)) * 100
> cat("RMSE:", RMSE, "\n")
RMSE: 0.7471908 2.856689 1.446747 1.328938 108.0238 5.661724
> cat("MAE:", MAE, "\n")
MAE: 0.5584822 2.180331 1.221535 0.8079338 81.23333 4.588206
> cat("MAPE:", MAPE, "\n")
MAPE: Inf 49.41089 149.4332 Inf 319.6007 116.1832
> forecast_times <- time(test_set)
> for (i in 1:ncol(actual_values)) {
+ ts.plot(test_set[, i], col = "black", lwd = 2,
+         ylab = paste("Variable", i), xlab = "Time",
+         main = paste("Actual vs. Forecasted for Variable", i))
+ lines(forecast_times, forecasted_values[, i], col = "red", lwd = 2)
+ legend("topleft", legend = c("Actual", "Forecasted"),
+       col = c("black", "red"), lty = 1, cex = 0.8)
+ if (interactive()) {
+   readline(prompt="Press [enter] to continue")
+ }
+ }
Error in plot.xy(xy.coords(x, y), type = type, ...) : invalid plot type
> for (i in 1:ncol(actual_values)) {
+ plot(forecast_times, type = "n", ylim = range(c(test_set[, i], forecasted_values[, i])),
+      ylab = paste("Variable", i), xlab = "Time",
+      main = paste("Actual vs. Forecasted for Variable", i))
+ lines(test_set[, i], col = "black", lwd = 2)
+ lines(forecast_times, forecasted_values[, i], col = "red", lwd = 2)
+ legend("topleft", legend = c("Actual", "Forecasted"), col = c("black", "red"), lty = 1, cex = 0.8)
+ if (interactive()) {
+   readline(prompt="Press [enter] to continue")
+ }
+ }
Error in plot.xy(xy.coords(x, y), type = type, ...) : invalid plot type
> install.packages("stats")
Warning: package 'stats' is in use and will not be installed
> for (i in 1:ncol(forecasted_values)) {
+ forecast_time_index <- time(test_set)[(length(test_set) - nrow(forecasted_values) + 1):length(test_set)]
+ forecast_ts <- ts(forecasted_values[, i], start=start(forecast_time_index), frequency=frequency(test_set))
+ ts.plot(test_set[, i], col = "black", lwd = 2,
+         ylab = paste("Variable", i), xlab = "Time",
+         main = paste("Actual vs. Forecasted for Variable", i))
+ lines(forecast_ts, col = "red", lwd = 2)
+ legend("topleft", legend = c("Actual", "Forecasted"), col = c("black", "red"), lty = 1, cex = 0.8)
+ if (interactive()) {
+   readline(prompt="Press [enter] to continue")
+ }
+ }
Press [enter] to continue
Press [enter] to continue
Press [enter] to continueaaaaa
Press [enter] to continue
Press [enter] to continue
Press [enter] to continue
> for (i in 1:ncol(forecasted_values)) {
+ ts.plot(test_set[, i], col = "black", lwd = 2,
+         ylab = paste("Variable", i), xlab = "Time",
+         main = paste("Actual vs. Forecasted for Variable", i))
+ forecast_indices <- (length(test_set) - nrow(forecasted_values) + 1):length(test_set)
+ lines(forecast_indices, forecasted_values[, i], col = "red", lwd = 2)
+
+ legend("topleft", legend = c("Actual", "Forecasted"), col = c("black", "red"), lty = 1, cex = 0

```

```
.8)
+ if (interactive()) {
+   readline(prompt="Press [enter] to continue")
+ }
+ }
Press [enter] to continue
Press [enter] to continue
Press [enter] to continue
Press [enter] to continue
Press [enter] to continue
Press [enter] to continue
> par(mfrow=c(2, 1))
> for(i in 1:ncol(forecasted_values)) {
+ plot(test_set[,i], type='l', col='black', lwd=2,
+ main=paste("Actual Values for Variable", i), ylab="Value", xlab="Time")
+ plot(forecasted_values[,i], type='l', col='red', lwd=2,
+ main=paste("Forecasted Values for Variable", i), ylab="Value", xlab="Time")
+ par(mfrow=c(2, 1))
+ }
>
> par(mfrow=c(1, 1))
>
> par(mfrow=c(2, 1))
> > for(i in 1:ncol(forecasted_values)) {
Error: unexpected '>' in ">"
> + plot(test_set[,i], type='l', col='black', lwd=2,
+ + main=paste("Actual Values for Variable", i), ylab="Value", xlab="Time")
Error: unexpected '=' in:
"+ plot(test_set[,i], type='l', col='black', lwd=2,
+ main="
> + plot(forecasted_values[,i], type='l', col='red', lwd=2,
+ + main=paste("Forecasted Values for Variable", i), ylab="Value", xlab="Time")
Error: unexpected '=' in:
"+ plot(forecasted_values[,i], type='l', col='red', lwd=2,
+ main="
> + par(mfrow=c(2, 1))
Error in +par(mfrow = c(2, 1)) : invalid argument to unary operator
> + }
Error: unexpected '}' in "+ }"
> >
Error: unexpected '>' in ">"
> > par(mfrow=c(1, 1))
Error: unexpected '>' in ">"
> var_model <- VAR(train_set, p=8)
> summary(var_model)
```

#### VAR Estimation Results:

```
=====
Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6
Deterministic variables: const
Sample size: 98
Log Likelihood: -1014.959
Roots of the characteristic polynomial:
1.094 1.094 0.9913 0.9913 0.9637 0.9637 0.9473 0.9473 0.9265 0.9265 0.9251 0.9251 0.9218 0.9218
0.92 0.92 0.9198 0.9198 0.9177 0.9177 0.9169 0.9169 0.9139 0.9139 0.8999 0.8999 0.8973 0.8973 0.
8631 0.8631 0.8561 0.8561 0.8373 0.8373 0.8255 0.8255 0.8179 0.8179 0.8123 0.8123 0.7111 0.6886 0.
.6886 0.642 0.642 0.6283 0.6283 0.3564
Call:
VAR(y = train_set, p = 8)
```

#### Estimation results for equation ts1:

```
=====
ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
+ ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + ts1.
l8 + ts2.l8 + ts3.l8 + ts4.l8 + ts5.l8 + ts6.l8 + const
```

Estimate Std. Error t value Pr(>|t|)

```

ts1.11  3.888e-01  1.620e-01  2.400  0.0202 *
ts2.11 -5.645e-02  5.901e-02 -0.957  0.3435
ts3.11  9.902e-02  5.621e-02  1.762  0.0844 .
ts4.11  9.614e-02  2.971e-01  0.324  0.7476
ts5.11  1.374e-03  7.807e-04  1.760  0.0846 .
ts6.11  9.391e-03  1.474e-02  0.637  0.5269
ts1.12 -1.809e-01  1.784e-01 -1.014  0.3155
ts2.12 -5.880e-02  5.753e-02 -1.022  0.3117
ts3.12 -1.245e-02  6.771e-02 -0.184  0.8548
ts4.12 -3.388e-01  2.970e-01 -1.141  0.2596
ts5.12  1.555e-03  1.058e-03  1.471  0.1477
ts6.12 -5.677e-03  1.502e-02 -0.378  0.7071
ts1.13 -2.115e-02  1.854e-01 -0.114  0.9097
ts2.13 -6.714e-02  6.222e-02 -1.079  0.2858
ts3.13 -1.527e-02  7.526e-02 -0.203  0.8401
ts4.13  1.041e-01  3.157e-01  0.330  0.7430
ts5.13  1.307e-03  1.181e-03  1.107  0.2738
ts6.13 -1.979e-02  1.414e-02 -1.400  0.1678
ts1.14  1.701e-01  1.988e-01  0.856  0.3964
ts2.14 -5.874e-02  6.508e-02 -0.903  0.3711
ts3.14 -4.008e-02  7.074e-02 -0.566  0.5736
ts4.14 -1.261e-01  3.237e-01 -0.390  0.6986
ts5.14  1.991e-03  1.247e-03  1.596  0.1170
ts6.14 -5.549e-04  1.512e-02 -0.037  0.9709
ts1.15 -3.929e-02  2.327e-01 -0.169  0.8666
ts2.15 -1.914e-02  6.363e-02 -0.301  0.7648
ts3.15  3.618e-02  7.559e-02  0.479  0.6343
ts4.15 -2.443e-01  3.184e-01 -0.767  0.4466
ts5.15  2.003e-03  1.270e-03  1.577  0.1212
ts6.15 -1.418e-02  1.528e-02 -0.928  0.3578
ts1.16  1.244e-02  2.234e-01  0.056  0.9558
ts2.16 -8.284e-02  5.990e-02 -1.383  0.1729
ts3.16 -5.789e-02  7.714e-02 -0.750  0.4566
ts4.16 -2.612e-01  3.206e-01 -0.815  0.4193
ts5.16  1.406e-03  1.266e-03  1.111  0.2722
ts6.16 -5.797e-03  1.471e-02 -0.394  0.6952
ts1.17  1.332e-02  2.237e-01  0.060  0.9528
ts2.17 -2.387e-03  5.884e-02 -0.041  0.9678
ts3.17 -2.957e-02  6.987e-02 -0.423  0.6740
ts4.17  1.075e-01  3.251e-01  0.331  0.7423
ts5.17 -6.405e-05  1.180e-03 -0.054  0.9569
ts6.17 -2.630e-02  1.378e-02 -1.909  0.0621 .
ts1.18 -2.910e-02  2.044e-01 -0.142  0.8874
ts2.18  2.689e-02  5.596e-02  0.481  0.6330
ts3.18 -1.117e-02  7.089e-02 -0.158  0.8754
ts4.18 -1.370e-01  2.443e-01 -0.561  0.5777
ts5.18  3.232e-04  9.702e-04  0.333  0.7405
ts6.18  2.111e-03  1.371e-02  0.154  0.8782
const   2.843e-01  1.780e-01  1.597  0.1167
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 0.3943 on 49 degrees of freedom  
Multiple R-Squared: 0.5879, Adjusted R-squared: 0.1843  
F-statistic: 1.456 on 48 and 49 DF, p-value: 0.09669

Estimation results for equation ts2:

```

=====
ts2 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
  + ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + ts1.
18 + ts2.18 + ts3.18 + ts4.18 + ts5.18 + ts6.18 + const

      Estimate Std. Error t value Pr(>|t|)
ts1.11  0.2772192  0.4397575   0.630  0.53137
ts2.11 -0.1507859  0.1601658  -0.941  0.35110
ts3.11  0.4057433  0.1525649   2.659  0.01055 *

```

```

ts4.11  1.1368778  0.8063147  1.410  0.16487
ts5.11 -0.0005565  0.0021192 -0.263  0.79395
ts6.11 -0.0758518  0.0399995 -1.896  0.06382 .
ts1.12 -1.2020952  0.4841759 -2.483  0.01651 *
ts2.12 -0.0605471  0.1561489 -0.388  0.69988
ts3.12 -0.0066271  0.1837769 -0.036  0.97138
ts4.12  0.2251081  0.8062536  0.279  0.78126
ts5.12 -0.0005438  0.0028705 -0.189  0.85053
ts6.12  0.0178090  0.0407650  0.437  0.66412
ts1.13  0.0654249  0.5032301  0.130  0.89709
ts2.13  0.0520050  0.1688847  0.308  0.75944
ts3.13  0.2149429  0.2042909  1.052  0.29790
ts4.13  0.8573614  0.8569640  1.000  0.32200
ts5.13  0.0013373  0.0032057  0.417  0.67837
ts6.13 -0.0270714  0.0383704 -0.706  0.48382
ts1.14  1.6545641  0.5396850  3.066  0.00353 **
ts2.14 -0.2526795  0.1766595 -1.430  0.15897
ts3.14 -0.0602645  0.1920248 -0.314  0.75498
ts4.14 -0.8267311  0.8787425 -0.941  0.35142
ts5.14  0.0003415  0.0033861  0.101  0.92007
ts6.14 -0.0251445  0.0410445 -0.613  0.54296
ts1.15 -0.1361573  0.6315640 -0.216  0.83020
ts2.15 -0.0579167  0.1727148 -0.335  0.73881
ts3.15 -0.0347546  0.2051902 -0.169  0.86620
ts4.15  0.1796939  0.8641608  0.208  0.83614
ts5.15  0.0008931  0.0034476  0.259  0.79669
ts6.15  0.0208927  0.0414719  0.504  0.61667
ts1.16  0.0327067  0.6064792  0.054  0.95721
ts2.16  0.1493519  0.1625822  0.919  0.36279
ts3.16  0.0618919  0.2093813  0.296  0.76879
ts4.16 -0.8368070  0.8703586 -0.961  0.34105
ts5.16  0.0021055  0.0034360  0.613  0.54286
ts6.16 -0.0252839  0.0399239 -0.633  0.52948
ts1.17 -0.0253028  0.6073194 -0.042  0.96694
ts2.17 -0.2177220  0.1597082 -1.363  0.17904
ts3.17 -0.3336727  0.1896517 -1.759  0.08475 .
ts4.17 -0.8450244  0.8825113 -0.958  0.34300
ts5.17  0.0002157  0.0032036  0.067  0.94660
ts6.17 -0.0415216  0.0373952 -1.110  0.27227
ts1.18  0.3703350  0.5548984  0.667  0.50765
ts2.18 -0.0525210  0.1519007 -0.346  0.73100
ts3.18  0.0516054  0.1924210  0.268  0.78968
ts4.18  0.6608800  0.6632525  0.996  0.32394
ts5.18 -0.0013918  0.0026335 -0.529  0.59953
ts6.18 -0.0103010  0.0372051 -0.277  0.78304
const  1.6114561  0.4830836  3.336  0.00163 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 1.07 on 49 degrees of freedom  
Multiple R-Squared: 0.6605, Adjusted R-squared: 0.328  
F-statistic: 1.986 on 48 and 49 DF, p-value: 0.009174

Estimation results for equation ts3:

```

=====
ts3 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
  + ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + ts1.
18 + ts2.18 + ts3.18 + ts4.18 + ts5.18 + ts6.18 + const

```

|        | Estimate   | Std. Error | t value | Pr(> t )   |
|--------|------------|------------|---------|------------|
| ts1.11 | 0.5119577  | 0.4806638  | 1.065   | 0.29205    |
| ts2.11 | 0.2384904  | 0.1750644  | 1.362   | 0.17933    |
| ts3.11 | 0.4718298  | 0.1667565  | 2.829   | 0.00674 ** |
| ts4.11 | -0.4042375 | 0.8813181  | -0.459  | 0.64850    |
| ts5.11 | -0.0056023 | 0.0023164  | -2.419  | 0.01934 *  |
| ts6.11 | 0.0030191  | 0.0437203  | 0.069   | 0.94523    |

```

ts1.12 -0.2410915  0.5292140 -0.456  0.65072
ts2.12 -0.2825685  0.1706739 -1.656  0.10419
ts3.12  0.1733873  0.2008719  0.863  0.39225
ts4.12  0.8506004  0.8812513  0.965  0.33917
ts5.12 -0.0036700  0.0031375 -1.170  0.24777
ts6.12  0.0401858  0.0445570  0.902  0.37152
ts1.13  1.4919480  0.5500405  2.712  0.00919 **
ts2.13 -0.4484613  0.1845943 -2.429  0.01883 *
ts3.13  0.0033176  0.2232940  0.015  0.98821
ts4.13  0.5794116  0.9366788  0.619  0.53906
ts5.13 -0.0013277  0.0035038 -0.379  0.70638
ts6.13 -0.0591642  0.0419397 -1.411  0.16465
ts1.14 -1.1553367  0.5898865 -1.959  0.05587 .
ts2.14  0.1122970  0.1930924  0.582  0.56352
ts3.14 -0.0547100  0.2098870 -0.261  0.79544
ts4.14 -1.2683593  0.9604831 -1.321  0.19279
ts5.14 -0.0002296  0.0037010 -0.062  0.95079
ts6.14  0.0460984  0.0448625  1.028  0.30921
ts1.15 -1.1309214  0.6903121 -1.638  0.10777
ts2.15 -0.0741047  0.1887808 -0.393  0.69636
ts3.15  0.0516540  0.2242770  0.230  0.81881
ts4.15  0.2417122  0.9445450  0.256  0.79910
ts5.15  0.0035323  0.0037683  0.937  0.35317
ts6.15 -0.0289577  0.0453296 -0.639  0.52591
ts1.16  1.0000511  0.6628939  1.509  0.13782
ts2.16 -0.0656989  0.1777056 -0.370  0.71319
ts3.16  0.0550860  0.2288580  0.241  0.81079
ts4.16  0.3791976  0.9513193  0.399  0.69192
ts5.16  0.0068015  0.0037556  1.811  0.07627 .
ts6.16  0.0377127  0.0436376  0.864  0.39168
ts1.17 -0.1802712  0.6638123 -0.272  0.78709
ts2.17  0.0315362  0.1745642  0.181  0.85738
ts3.17 -0.1424177  0.2072931 -0.687  0.49530
ts4.17  0.3810554  0.9646025  0.395  0.69453
ts5.17  0.0025010  0.0035016  0.714  0.47846
ts6.17  0.0439199  0.0408737  1.075  0.28785
ts1.18  0.5987183  0.6065151  0.987  0.32842
ts2.18 -0.1481914  0.1660305 -0.893  0.37646
ts3.18  0.1165951  0.2103200  0.554  0.58185
ts4.18  0.2410075  0.7249483  0.332  0.74097
ts5.18  0.0035263  0.0028785  1.225  0.22642
ts6.18 -0.0866661  0.0406659 -2.131  0.03812 *
const  0.7595119  0.5280200  1.438  0.15667
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 1.17 on 49 degrees of freedom
Multiple R-Squared: 0.7036,    Adjusted R-squared: 0.4133
F-statistic: 2.423 on 48 and 49 DF,  p-value: 0.001248

```

Estimation results for equation ts4:

```

=====
ts4 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
  + ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + ts1.
18 + ts2.18 + ts3.18 + ts4.18 + ts5.18 + ts6.18 + const

```

```

      Estimate Std. Error t value Pr(>|t|)
ts1.11 -0.4353793  0.2078551 -2.095 0.041397 *
ts2.11 -0.0990816  0.0757037 -1.309 0.196705
ts3.11 -0.2971111  0.0721111 -4.120 0.000145 ***
ts4.11  0.1268702  0.3811114  0.333 0.740633
ts5.11  0.0041293  0.0010017  4.122 0.000144 ***
ts6.11  0.0062610  0.0189061  0.331 0.741933
ts1.12  0.1015347  0.2288498  0.444 0.659232
ts2.12  0.1603727  0.0738051  2.173 0.034650 *
ts3.12  0.2034917  0.0868637  2.343 0.023252 *

```

```

ts4.12  0.5022207  0.3810825  1.318  0.193672
ts5.12  0.0040661  0.0013568  2.997  0.004272 **
ts6.12 -0.0055761  0.0192679 -0.289  0.773498
ts1.13 -0.3840651  0.2378559 -1.615  0.112798
ts2.13 -0.0147841  0.0798248 -0.185  0.853832
ts3.13  0.0658622  0.0965598  0.682  0.498395
ts4.13 -0.1717089  0.4050512 -0.424  0.673480
ts5.13  0.0022691  0.0015152  1.498  0.140653
ts6.13  0.0354104  0.0181361  1.952  0.056606 .
ts1.14  0.7361307  0.2550867  2.886  0.005791 **
ts2.14 -0.2001837  0.0834996 -2.397  0.020368 *
ts3.14 -0.0944939  0.0907621 -1.041  0.302932
ts4.14 -0.4576574  0.4153450 -1.102  0.275900
ts5.14  0.0026731  0.0016004  1.670  0.101252
ts6.14 -0.0357749  0.0194000 -1.844  0.071224 .
ts1.15  0.2065767  0.2985140  0.692  0.492193
ts2.15 -0.0176911  0.0816351 -0.217  0.829334
ts3.15 -0.1905154  0.0969849 -1.964  0.055171 .
ts4.15 -0.8066930  0.4084528 -1.975  0.053917 .
ts5.15  0.0015098  0.0016295  0.926  0.358730
ts6.15 -0.0237373  0.0196020 -1.211  0.231718
ts1.16 -0.6074479  0.2866575 -2.119  0.039177 *
ts2.16  0.0500911  0.0768459  0.652  0.517551
ts3.16 -0.0598851  0.0989659 -0.605  0.547899
ts4.16  0.8268062  0.4113823  2.010  0.049973 *
ts5.16 -0.0012275  0.0016240 -0.756  0.453388
ts6.16 -0.0033739  0.0188704 -0.179  0.858836
ts1.17  0.4823234  0.2870546  1.680  0.099274 .
ts2.17  0.0568832  0.0754874  0.754  0.454728
ts3.17  0.2136873  0.0896404  2.384  0.021052 *
ts4.17  0.8302606  0.4171264  1.990  0.052137 .
ts5.17 -0.0001368  0.0015142 -0.090  0.928363
ts6.17  0.0007237  0.0176752  0.041  0.967506
ts1.18 -0.0447484  0.2622774 -0.171  0.865229
ts2.18  0.0872184  0.0717972  1.215  0.230268
ts3.18  0.0580298  0.0909494  0.638  0.526415
ts4.18 -0.1656471  0.3134919 -0.528  0.599611
ts5.18  0.0005543  0.0012448  0.445  0.658073
ts6.18  0.0361394  0.0175853  2.055  0.045221 *
const  0.0413252  0.2283335  0.181  0.857125
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 0.5058 on 49 degrees of freedom  
Multiple R-Squared: 0.7648, Adjusted R-squared: 0.5344  
F-statistic: 3.319 on 48 and 49 DF, p-value: 2.565e-05

Estimation results for equation ts5:

```

=====
ts5 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
  + ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + ts1.
18 + ts2.18 + ts3.18 + ts4.18 + ts5.18 + ts6.18 + const

```

|        | Estimate   | Std. Error | t value | Pr(> t )     |
|--------|------------|------------|---------|--------------|
| ts1.11 | 22.103024  | 29.654221  | 0.745   | 0.4596       |
| ts2.11 | 4.355831   | 10.800480  | 0.403   | 0.6885       |
| ts3.11 | -2.646260  | 10.287928  | -0.257  | 0.7981       |
| ts4.11 | -31.641276 | 54.372311  | -0.582  | 0.5633       |
| ts5.11 | -0.795820  | 0.142907   | -5.569  | 1.07e-06 *** |
| ts6.11 | -0.321302  | 2.697294   | -0.119  | 0.9057       |
| ts1.12 | -17.619879 | 32.649491  | -0.540  | 0.5919       |
| ts2.12 | 9.324108   | 10.529608  | 0.886   | 0.3802       |
| ts3.12 | -15.543638 | 12.392652  | -1.254  | 0.2157       |
| ts4.12 | -70.043450 | 54.368190  | -1.288  | 0.2037       |
| ts5.12 | -0.489705  | 0.193565   | -2.530  | 0.0147 *     |
| ts6.12 | 1.847834   | 2.748914   | 0.672   | 0.5046       |



```

ts1.13 -38.212653 33.934372 -1.126 0.2656
ts2.13 20.077931 11.388419 1.763 0.0841 .
ts3.13 4.247677 13.775972 0.308 0.7591
ts4.13 -15.718776 57.787751 -0.272 0.7868
ts5.13 -0.234119 0.216167 -1.083 0.2841
ts6.13 2.613557 2.587438 1.010 0.3174
ts1.14 -17.774213 36.392644 -0.488 0.6274
ts2.14 -20.051622 11.912703 -1.683 0.0987 .
ts3.14 -15.713108 12.948832 -1.213 0.2308
ts4.14 27.195589 59.256342 0.459 0.6483
ts5.14 0.066064 0.228333 0.289 0.7735
ts6.14 -1.342280 2.767761 -0.485 0.6299
ts1.15 17.795550 42.588329 0.418 0.6779
ts2.15 -0.850904 11.646700 -0.073 0.9421
ts3.15 6.935349 13.836617 0.501 0.6185
ts4.15 70.184807 58.273053 1.204 0.2342
ts5.15 0.190401 0.232482 0.819 0.4168
ts6.15 0.093683 2.796578 0.033 0.9734
ts1.16 -11.088090 40.896780 -0.271 0.7874
ts2.16 7.816160 10.963427 0.713 0.4793
ts3.16 6.378182 14.119237 0.452 0.6535
ts4.16 -85.934898 58.690992 -1.464 0.1495
ts5.16 0.126141 0.231699 0.544 0.5886
ts6.16 2.553165 2.692192 0.948 0.3476
ts1.17 -43.059326 40.953440 -1.051 0.2982
ts2.17 -5.874419 10.769621 -0.545 0.5879
ts3.17 -8.647705 12.788802 -0.676 0.5021
ts4.17 40.108814 59.510488 0.674 0.5035
ts5.17 0.224537 0.216027 1.039 0.3037
ts6.17 -1.930724 2.521677 -0.766 0.4476
ts1.18 83.100294 37.418532 2.221 0.0310 *
ts2.18 -8.296082 10.243140 -0.810 0.4219
ts3.18 -6.092281 12.975550 -0.470 0.6408
ts4.18 28.601288 44.725185 0.639 0.5255
ts5.18 0.008444 0.177587 0.048 0.9623
ts6.18 -0.847643 2.508855 -0.338 0.7369
const 4.674013 32.575834 0.143 0.8865
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 72.17 on 49 degrees of freedom  
Multiple R-Squared: 0.6617, Adjusted R-squared: 0.3303  
F-statistic: 1.997 on 48 and 49 DF, p-value: 0.008744

Estimation results for equation ts6:

```

=====
ts6 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
+ ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + ts1.
18 + ts2.18 + ts3.18 + ts4.18 + ts5.18 + ts6.18 + const

```

|        | Estimate  | Std. Error | t value | Pr(> t )   |
|--------|-----------|------------|---------|------------|
| ts1.11 | -0.944115 | 1.736076   | -0.544  | 0.58903    |
| ts2.11 | 0.316332  | 0.632303   | 0.500   | 0.61911    |
| ts3.11 | 0.205208  | 0.602296   | 0.341   | 0.73478    |
| ts4.11 | 6.054055  | 3.183172   | 1.902   | 0.06307 .  |
| ts5.11 | -0.010638 | 0.008366   | -1.272  | 0.20954    |
| ts6.11 | 0.426197  | 0.157910   | 2.699   | 0.00952 ** |
| ts1.12 | 1.024999  | 1.911431   | 0.536   | 0.59421    |
| ts2.12 | 0.871818  | 0.616445   | 1.414   | 0.16361    |
| ts3.12 | 0.777524  | 0.725515   | 1.072   | 0.28911    |
| ts4.12 | -4.592783 | 3.182931   | -1.443  | 0.15540    |
| ts5.12 | -0.002925 | 0.011332   | -0.258  | 0.79741    |
| ts6.12 | -0.049909 | 0.160932   | -0.310  | 0.75778    |
| ts1.13 | -1.234249 | 1.986654   | -0.621  | 0.53730    |
| ts2.13 | 0.422228  | 0.666723   | 0.633   | 0.52949    |
| ts3.13 | -0.134983 | 0.806500   | -0.167  | 0.86777    |

```

ts4.13 -0.586096    3.383126   -0.173    0.86318
ts5.13 -0.013575    0.012655   -1.073    0.28868
ts6.13  0.091993    0.151479    0.607    0.54646
ts1.14  0.240225    2.130571    0.113    0.91069
ts2.14 -0.496170    0.697417   -0.711    0.48019
ts3.14 -0.882343    0.758076   -1.164    0.25009
ts4.14 -1.582409    3.469103   -0.456    0.65030
ts5.14 -0.004096    0.013367   -0.306    0.76056
ts6.14 -0.024946    0.162036   -0.154    0.87828
ts1.15  0.609047    2.493291    0.244    0.80804
ts2.15 -0.277880    0.681844   -0.408    0.68539
ts3.15 -0.160250    0.810051   -0.198    0.84400
ts4.15  2.109558    3.411537    0.618    0.53920
ts5.15  0.005717    0.013610    0.420    0.67628
ts6.15 -0.016326    0.163723   -0.100    0.92097
ts1.16 -0.602654    2.394261   -0.252    0.80232
ts2.16 -0.484064    0.641843   -0.754    0.45435
ts3.16  0.617308    0.826596    0.747    0.45875
ts4.16 -3.524934    3.436005   -1.026    0.30999
ts5.16  0.006403    0.013565    0.472    0.63899
ts6.16  0.039240    0.157612    0.249    0.80443
ts1.17  0.722014    2.397578    0.301    0.76458
ts2.17 -0.684562    0.630497   -1.086    0.28290
ts3.17 -0.474010    0.748708   -0.633    0.52961
ts4.17  4.388731    3.483981    1.260    0.21375
ts5.17 -0.006961    0.012647   -0.550    0.58457
ts6.17 -0.163340    0.147629   -1.106    0.27395
ts1.18  0.027887    2.190630    0.013    0.98989
ts2.18 -0.089745    0.599674   -0.150    0.88165
ts3.18  0.717322    0.759640    0.944    0.34965
ts4.18 -3.369816    2.618391   -1.287    0.20415
ts5.18 -0.014468    0.010397   -1.392    0.17033
ts6.18 -0.044903    0.146878   -0.306    0.76112
const -0.058494    1.907119   -0.031    0.97566
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 4.225 on 49 degrees of freedom
Multiple R-Squared: 0.5295,    Adjusted R-squared: 0.06854
F-statistic: 1.149 on 48 and 49 DF,  p-value: 0.3152

```

```

Covariance matrix of residuals:
      ts1      ts2      ts3      ts4      ts5      ts6
ts1  0.15545  0.060102  0.1058  0.029054  -6.4796  0.2663
ts2  0.06010  1.145312 -0.1839  0.006626   3.1475 -1.8510
ts3  0.10578 -0.183950  1.3683 -0.184275 -10.7013 -0.8301
ts4  0.02905  0.006626 -0.1843  0.255869   0.7299 -0.2049
ts5 -6.47956  3.147488 -10.7013  0.729924 5207.9905 -52.7097
ts6  0.26630 -1.850953 -0.8301 -0.204857 -52.7097 17.8499

```

```

Correlation matrix of residuals:
      ts1      ts2      ts3      ts4      ts5      ts6
ts1  1.0000  0.14244  0.2294  0.14568 -0.22773  0.15986
ts2  0.1424  1.00000 -0.1469  0.01224  0.04075 -0.40937
ts3  0.2294 -0.14694  1.0000 -0.31143 -0.12677 -0.16796
ts4  0.1457  0.01224 -0.3114  1.00000  0.02000 -0.09586
ts5 -0.2277  0.04075 -0.1268  0.02000  1.00000 -0.17288
ts6  0.1599 -0.40937 -0.1680 -0.09586 -0.17288  1.00000

```

```
> serial.test(var_model)
```

```
Portmanteau Test (asymptotic)
```

```

data: Residuals of VAR object var_model
Chi-squared = 380.62, df = 288, p-value = 0.000203

```

```
> stability(var_model)
$ts1
```

```
Empirical Fluctuation Process: OLS-based CUSUM test
```

```
Call: efp(formula = formula, data = data, type = type, h = h, dynamic = dynamic,
  rescale = rescale)
```

```
$ts2
```

```
Empirical Fluctuation Process: OLS-based CUSUM test
```

```
Call: efp(formula = formula, data = data, type = type, h = h, dynamic = dynamic,
  rescale = rescale)
```

```
$ts3
```

```
Empirical Fluctuation Process: OLS-based CUSUM test
```

```
Call: efp(formula = formula, data = data, type = type, h = h, dynamic = dynamic,
  rescale = rescale)
```

```
$ts4
```

```
Empirical Fluctuation Process: OLS-based CUSUM test
```

```
Call: efp(formula = formula, data = data, type = type, h = h, dynamic = dynamic,
  rescale = rescale)
```

```
$ts5
```

```
Empirical Fluctuation Process: OLS-based CUSUM test
```

```
Call: efp(formula = formula, data = data, type = type, h = h, dynamic = dynamic,
  rescale = rescale)
```

```
$ts6
```

```
Empirical Fluctuation Process: OLS-based CUSUM test
```

```
Call: efp(formula = formula, data = data, type = type, h = h, dynamic = dynamic,
  rescale = rescale)
```

```
> cat("AIC:", AIC, "\n")
```

```
AIC: 3082.242
```

```
> cat("MAE:", MAE, "\n")
```

```
MAE: 0.5584822 2.180331 1.221535 0.8079338 81.23333 4.588206
```

```
> cat("BIC:", BIC, "\n")
```

```
BIC: 3881.481
```

```
> AIC <- AIC(var_model)
```

```
> BIC <- BIC(var_model)
```

```
> cat("AIC:", AIC, "\n")
```

```
AIC: 2617.918
```

```
> cat("MAE:", MAE, "\n")
```

```
MAE: 0.5584822 2.180331 1.221535 0.8079338 81.23333 4.588206
```

```
> cat("BIC:", BIC, "\n")
```

```
BIC: 3377.898
```

```
> log_likelihood <- logLik(var_model)
```

```
> num_parameters <- length(coef(var_model))
```

```
Error: unexpected '>' in ">"
```

```
> num_parameters <- length(coef(var_model))
```

```
> num_observations <- length(residuals(var_model))
```

```
>
```

```
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
```

```
> cat("HQC:", HQC, "\n")
HQC: 2052.15
> plot(stability(var_model))
> library(strucchange)
> sctest(var_model)
Error in root.matrix(J) : matrix is not positive semidefinite
> var_model <- VAR(train_set, p = 6)
> summary(var_model)
```

# VAR Estimation Results:

```
=====
```

Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6

Deterministic variables: const

Sample size: 100

Log Likelihood: -1107.519

Roots of the characteristic polynomial:

```
1.039 1.039 0.9714 0.9714 0.9356 0.9356 0.9193 0.9193 0.8815 0.8815 0.8686 0.8638 0.8638 0.8446 0
.8446 0.8378 0.8378 0.8375 0.8375 0.8206 0.8206 0.8104 0.8104 0.7739 0.7699 0.7699 0.7671 0.7671
0.7064 0.7022 0.6313 0.6313 0.5934 0.5934 0.08558 0.02735
```

Call:

```
VAR(y = train_set, p = 6)
```

# Estimation results for equation ts1:

```
=====
```

```
ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
+ ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |    |
|--------|------------|------------|---------|----------|----|
| ts1.l1 | 0.3993327  | 0.1424386  | 2.804   | 0.00671  | ** |
| ts2.l1 | -0.0368948 | 0.0500013  | -0.738  | 0.46333  |    |
| ts3.l1 | 0.0613918  | 0.0477061  | 1.287   | 0.20285  |    |
| ts4.l1 | -0.0043827 | 0.2493946  | -0.018  | 0.98603  |    |
| ts5.l1 | 0.0011343  | 0.0006993  | 1.622   | 0.10981  |    |
| ts6.l1 | 0.0034892  | 0.0125045  | 0.279   | 0.78113  |    |
| ts1.l2 | -0.1669370 | 0.1611954  | -1.036  | 0.30434  |    |
| ts2.l2 | -0.0258270 | 0.0511556  | -0.505  | 0.61541  |    |
| ts3.l2 | 0.0030604  | 0.0550645  | 0.056   | 0.95585  |    |
| ts4.l2 | -0.4101436 | 0.2645095  | -1.551  | 0.12601  |    |
| ts5.l2 | 0.0011831  | 0.0009436  | 1.254   | 0.21453  |    |
| ts6.l2 | 0.0036951  | 0.0128900  | 0.287   | 0.77531  |    |
| ts1.l3 | 0.0379798  | 0.1687013  | 0.225   | 0.82261  |    |
| ts2.l3 | -0.0762394 | 0.0498434  | -1.530  | 0.13113  |    |
| ts3.l3 | -0.0308826 | 0.0632075  | -0.489  | 0.62683  |    |
| ts4.l3 | 0.0044648  | 0.2711599  | 0.016   | 0.98692  |    |
| ts5.l3 | 0.0015149  | 0.0010809  | 1.401   | 0.16597  |    |
| ts6.l3 | -0.0168879 | 0.0125526  | -1.345  | 0.18333  |    |
| ts1.l4 | 0.2610010  | 0.1752303  | 1.489   | 0.14135  |    |
| ts2.l4 | -0.0539568 | 0.0513543  | -1.051  | 0.29742  |    |
| ts3.l4 | -0.0573034 | 0.0608821  | -0.941  | 0.35019  |    |
| ts4.l4 | -0.0257171 | 0.2684395  | -0.096  | 0.92398  |    |
| ts5.l4 | 0.0017795  | 0.0011127  | 1.599   | 0.11478  |    |
| ts6.l4 | -0.0089075 | 0.0129641  | -0.687  | 0.49455  |    |
| ts1.l5 | -0.1895490 | 0.1857801  | -1.020  | 0.31149  |    |
| ts2.l5 | -0.0066573 | 0.0513556  | -0.130  | 0.89727  |    |
| ts3.l5 | -0.0017998 | 0.0580404  | -0.031  | 0.97536  |    |
| ts4.l5 | -0.1617013 | 0.2600373  | -0.622  | 0.53629  |    |
| ts5.l5 | 0.0020698  | 0.0010200  | 2.029   | 0.04668  | *  |
| ts6.l5 | -0.0066482 | 0.0121526  | -0.547  | 0.58627  |    |
| ts1.l6 | -0.0035666 | 0.1684029  | -0.021  | 0.98317  |    |
| ts2.l6 | -0.0377571 | 0.0475724  | -0.794  | 0.43036  |    |
| ts3.l6 | -0.0036133 | 0.0589233  | -0.061  | 0.95130  |    |
| ts4.l6 | -0.0508250 | 0.2188595  | -0.232  | 0.81711  |    |
| ts5.l6 | 0.0016055  | 0.0008002  | 2.006   | 0.04912  | *  |
| ts6.l6 | -0.0068688 | 0.0114845  | -0.598  | 0.55192  |    |
| const  | 0.2045831  | 0.1312636  | 1.559   | 0.12411  |    |

```
---
```

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3758 on 63 degrees of freedom  
 Multiple R-Squared: 0.5224, Adjusted R-squared: 0.2495  
 F-statistic: 1.914 on 36 and 63 DF, p-value: 0.0119

#### Estimation results for equation ts2:

=====

ts2 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + ts5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 + ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6 + ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + const

|        | Estimate   | Std. Error | t value | Pr(> t ) |    |
|--------|------------|------------|---------|----------|----|
| ts1.l1 | 0.3516867  | 0.4046050  | 0.869   | 0.38803  |    |
| ts2.l1 | -0.1123494 | 0.1420315  | -0.791  | 0.43190  |    |
| ts3.l1 | 0.3711596  | 0.1355119  | 2.739   | 0.00801  | ** |
| ts4.l1 | 0.4735754  | 0.7084198  | 0.668   | 0.50626  |    |
| ts5.l1 | -0.0003239 | 0.0019865  | -0.163  | 0.87099  |    |
| ts6.l1 | -0.0657810 | 0.0355197  | -1.852  | 0.06872  | .  |
| ts1.l2 | -1.2662786 | 0.4578848  | -2.765  | 0.00745  | ** |
| ts2.l2 | -0.0361196 | 0.1453103  | -0.249  | 0.80450  |    |
| ts3.l2 | -0.0066108 | 0.1564138  | -0.042  | 0.96642  |    |
| ts4.l2 | -0.1936674 | 0.7513546  | -0.258  | 0.79743  |    |
| ts5.l2 | -0.0008519 | 0.0026804  | -0.318  | 0.75167  |    |
| ts6.l2 | 0.0331385  | 0.0366147  | 0.905   | 0.36888  |    |
| ts1.l3 | 0.2375565  | 0.4792058  | 0.496   | 0.62181  |    |
| ts2.l3 | 0.1057892  | 0.1415832  | 0.747   | 0.45773  |    |
| ts3.l3 | 0.1671209  | 0.1795446  | 0.931   | 0.35551  |    |
| ts4.l3 | 0.6716619  | 0.7702456  | 0.872   | 0.38651  |    |
| ts5.l3 | 0.0019686  | 0.0030705  | 0.641   | 0.52377  |    |
| ts6.l3 | -0.0249910 | 0.0356563  | -0.701  | 0.48596  |    |
| ts1.l4 | 1.5463912  | 0.4977518  | 3.107   | 0.00284  | ** |
| ts2.l4 | -0.2157977 | 0.1458750  | -1.479  | 0.14403  |    |
| ts3.l4 | -0.2022837 | 0.1729391  | -1.170  | 0.24654  |    |
| ts4.l4 | -0.6206363 | 0.7625179  | -0.814  | 0.41875  |    |
| ts5.l4 | 0.0013717  | 0.0031608  | 0.434   | 0.66578  |    |
| ts6.l4 | -0.0227435 | 0.0368254  | -0.618  | 0.53906  |    |
| ts1.l5 | -0.0941702 | 0.5277193  | -0.178  | 0.85894  |    |
| ts2.l5 | 0.0521765  | 0.1458786  | 0.358   | 0.72179  |    |
| ts3.l5 | 0.0059451  | 0.1648671  | 0.036   | 0.97135  |    |
| ts4.l5 | 0.3302946  | 0.7386510  | 0.447   | 0.65629  |    |
| ts5.l5 | 0.0017194  | 0.0028974  | 0.593   | 0.55502  |    |
| ts6.l5 | 0.0161644  | 0.0345203  | 0.468   | 0.64122  |    |
| ts1.l6 | -0.2407568 | 0.4783581  | -0.503  | 0.61651  |    |
| ts2.l6 | 0.1638016  | 0.1351322  | 1.212   | 0.22998  |    |
| ts3.l6 | 0.0742198  | 0.1673752  | 0.443   | 0.65897  |    |
| ts4.l6 | -0.1873444 | 0.6216831  | -0.301  | 0.76414  |    |
| ts5.l6 | 0.0018468  | 0.0022730  | 0.812   | 0.41958  |    |
| ts6.l6 | -0.0196942 | 0.0326224  | -0.604  | 0.54821  |    |
| const  | 0.9723899  | 0.3728619  | 2.608   | 0.01136  | *  |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.068 on 63 degrees of freedom  
 Multiple R-Squared: 0.5662, Adjusted R-squared: 0.3183  
 F-statistic: 2.284 on 36 and 63 DF, p-value: 0.00202

#### Estimation results for equation ts3:

=====

ts3 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + ts5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 + ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6 + ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + const

|        | Estimate  | Std. Error | t value | Pr(> t ) |
|--------|-----------|------------|---------|----------|
| ts1.l1 | 0.6302660 | 0.4295291  | 1.467   | 0.147258 |

```

ts2.11  0.2466693  0.1507808  1.636 0.106838
ts3.11  0.5113840  0.1438596  3.555 0.000724 ***
ts4.11  0.2811282  0.7520592  0.374 0.709800
ts5.11 -0.0046679  0.0021089  -2.213 0.030497 *
ts6.11  0.0078489  0.0377077  0.208 0.835783
ts1.12 -0.1512031  0.4860909  -0.311 0.756782
ts2.12 -0.2976059  0.1542616  -1.929 0.058209 .
ts3.12  0.1374093  0.1660491  0.828 0.411065
ts4.12  0.5810524  0.7976388  0.728 0.469028
ts5.12 -0.0034088  0.0028455  -1.198 0.235419
ts6.12  0.0274209  0.0388702  0.705 0.483132
ts1.13  1.4970026  0.5087254  2.943 0.004550 **
ts2.13 -0.4664646  0.1503049  -3.103 0.002863 **
ts3.13  0.0067850  0.1906047  0.036 0.971716
ts4.13  0.5360291  0.8176935  0.656 0.514508
ts5.13 -0.0013435  0.0032596  -0.412 0.681621
ts6.13 -0.0570899  0.0378528  -1.508 0.136500
ts1.14 -1.0493630  0.5284138  -1.986 0.051403 .
ts2.14  0.0943631  0.1548610  0.609 0.544490
ts3.14 -0.0388996  0.1835923  -0.212 0.832884
ts4.14 -0.7108420  0.8094898  -0.878 0.383207
ts5.14  0.0001430  0.0033555  0.043 0.966139
ts6.14  0.0386814  0.0390939  0.989 0.326228
ts1.15 -0.9172519  0.5602274  -1.637 0.106557
ts2.15 -0.0281823  0.1548648  -0.182 0.856183
ts3.15  0.1631116  0.1750231  0.932 0.354924
ts4.15  0.6342832  0.7841527  0.809 0.421630
ts5.15  0.0017775  0.0030759  0.578 0.565418
ts6.15 -0.0358875  0.0366468  -0.979 0.331186
ts1.16  1.1836405  0.5078255  2.331 0.022978 *
ts2.16 -0.1959234  0.1434565  -1.366 0.176879
ts3.16  0.0008319  0.1776857  0.005 0.996279
ts4.16  0.1863819  0.6599794  0.282 0.778558
ts5.16  0.0042649  0.0024131  1.767 0.082003 .
ts6.16  0.0365702  0.0346319  1.056 0.295015
const  0.7883349  0.3958305  1.992 0.050755 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 1.133 on 63 degrees of freedom  
Multiple R-Squared: 0.643, Adjusted R-squared: 0.4391  
F-statistic: 3.153 on 36 and 63 DF, p-value: 3.248e-05

Estimation results for equation ts4:

```

=====
ts4 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
  + ts3.16 + ts4.16 + ts5.16 + ts6.16 + const

```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.11 | -0.5888588 | 0.1974809  | -2.982  | 0.004070 | **  |
| ts2.11 | -0.0850125 | 0.0693232  | -1.226  | 0.224642 |     |
| ts3.11 | -0.2395710 | 0.0661411  | -3.622  | 0.000584 | *** |
| ts4.11 | 0.3511968  | 0.3457677  | 1.016   | 0.313657 |     |
| ts5.11 | 0.0036703  | 0.0009696  | 3.785   | 0.000345 | *** |
| ts6.11 | 0.0050300  | 0.0173365  | 0.290   | 0.772662 |     |
| ts1.12 | 0.1479508  | 0.2234858  | 0.662   | 0.510376 |     |
| ts2.12 | 0.1715084  | 0.0709235  | 2.418   | 0.018500 | *   |
| ts3.12 | 0.2288847  | 0.0763430  | 2.998   | 0.003885 | **  |
| ts4.12 | 0.5470340  | 0.3667235  | 1.492   | 0.140774 |     |
| ts5.12 | 0.0043816  | 0.0013083  | 3.349   | 0.001372 | **  |
| ts6.12 | 0.0032691  | 0.0178710  | 0.183   | 0.855441 |     |
| ts1.13 | -0.4010107 | 0.2338923  | -1.715  | 0.091351 | .   |
| ts2.13 | 0.0160928  | 0.0691044  | 0.233   | 0.816612 |     |
| ts3.13 | -0.0011818 | 0.0876327  | -0.013  | 0.989282 |     |
| ts4.13 | -0.1031242 | 0.3759438  | -0.274  | 0.784746 |     |
| ts5.13 | 0.0025029  | 0.0014987  | 1.670   | 0.099858 | .   |

```

ts6.13  0.0272682  0.0174033   1.567  0.122160
ts1.14  0.5978428  0.2429442   2.461  0.016614 *
ts2.14 -0.1203163  0.0711991  -1.690  0.095999 .
ts3.14 -0.0248111  0.0844087  -0.294  0.769770
ts4.14 -0.4544397  0.3721721  -1.221  0.226618
ts5.14  0.0017579  0.0015427   1.139  0.258811
ts6.14 -0.0327939  0.0179738  -1.825  0.072814 .
ts1.15  0.0740184  0.2575709   0.287  0.774771
ts2.15 -0.0293209  0.0712009  -0.412  0.681880
ts3.15 -0.1923951  0.0804688  -2.391  0.019806 *
ts4.15 -0.7052887  0.3605231  -1.956  0.054867 .
ts5.15  0.0010615  0.0014142   0.751  0.455663
ts6.15 -0.0067378  0.0168488  -0.400  0.690583
ts1.16 -0.3716870  0.2334785  -1.592  0.116401
ts2.16  0.0754668  0.0659557   1.144  0.256868
ts3.16  0.0156771  0.0816930   0.192  0.848436
ts4.16  0.3503245  0.3034330   1.155  0.252641
ts5.16 -0.0010830  0.0011094  -0.976  0.332695
ts6.16  0.0025153  0.0159224   0.158  0.874982
const   0.0314753  0.1819876   0.173  0.863243
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 0.5211 on 63 degrees of freedom  
Multiple R-Squared: 0.6791, Adjusted R-squared: 0.4958  
F-statistic: 3.704 on 36 and 63 DF, p-value: 2.713e-06

Estimation results for equation ts5:

```

=====
ts5 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
  + ts3.16 + ts4.16 + ts5.16 + ts6.16 + const

```

|        | Estimate  | Std. Error | t value | Pr(> t )     |
|--------|-----------|------------|---------|--------------|
| ts1.11 | 22.22439  | 27.15134   | 0.819   | 0.41614      |
| ts2.11 | 5.11473   | 9.53114    | 0.537   | 0.59341      |
| ts3.11 | -0.65822  | 9.09363    | -0.072  | 0.94253      |
| ts4.11 | -58.49053 | 47.53907   | -1.230  | 0.22313      |
| ts5.11 | -0.79909  | 0.13331    | -5.994  | 1.09e-07 *** |
| ts6.11 | 0.09445   | 2.38357    | 0.040   | 0.96852      |
| ts1.12 | -16.50234 | 30.72672   | -0.537  | 0.59311      |
| ts2.12 | 7.37752   | 9.75117    | 0.757   | 0.45212      |
| ts3.12 | -10.52632 | 10.49627   | -1.003  | 0.31976      |
| ts4.12 | -61.13503 | 50.42025   | -1.213  | 0.22984      |
| ts5.12 | -0.48377  | 0.17987    | -2.690  | 0.00915 **   |
| ts6.12 | 0.88300   | 2.45706    | 0.359   | 0.72052      |
| ts1.13 | -41.43015 | 32.15749   | -1.288  | 0.20234      |
| ts2.13 | 10.33020  | 9.50105    | 1.087   | 0.28106      |
| ts3.13 | -4.99547  | 12.04848   | -0.415  | 0.67983      |
| ts4.13 | -39.15288 | 51.68794   | -0.757  | 0.45158      |
| ts5.13 | -0.12359  | 0.20605    | -0.600  | 0.55078      |
| ts6.13 | 2.22875   | 2.39275    | 0.931   | 0.35517      |
| ts1.14 | -2.62882  | 33.40203   | -0.079  | 0.93752      |
| ts2.14 | -10.28289 | 9.78906    | -1.050  | 0.29753      |
| ts3.14 | -14.61109 | 11.60522   | -1.259  | 0.21267      |
| ts4.14 | 58.34992  | 51.16937   | 1.140   | 0.25847      |
| ts5.14 | 0.10682   | 0.21211    | 0.504   | 0.61631      |
| ts6.14 | -2.04474  | 2.47120    | -0.827  | 0.41112      |
| ts1.15 | 7.47251   | 35.41302   | 0.211   | 0.83356      |
| ts2.15 | 5.07122   | 9.78930    | 0.518   | 0.60625      |
| ts3.15 | 13.19080  | 11.06354   | 1.192   | 0.23762      |
| ts4.15 | 93.07276  | 49.56776   | 1.878   | 0.06505 .    |
| ts5.15 | 0.07903   | 0.19443    | 0.406   | 0.68578      |
| ts6.15 | -0.01320  | 2.31651    | -0.006  | 0.99547      |
| ts1.16 | 15.26546  | 32.10060   | 0.476   | 0.63604      |
| ts2.16 | 5.43738   | 9.06815    | 0.600   | 0.55091      |
| ts3.16 | 5.08323   | 11.23184   | 0.453   | 0.65241      |

```
ts4.l6 -22.01262    41.71854   -0.528    0.59960
ts5.l6  -0.09027     0.15253   -0.592    0.55612
ts6.l6   1.21225     2.18915    0.554    0.58171
const  -18.56872    25.02119   -0.742    0.46077
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 71.64 on 63 degrees of freedom
Multiple R-Squared: 0.5714,    Adjusted R-squared: 0.3265
F-statistic: 2.333 on 36 and 63 DF,  p-value: 0.00159
```

```
Estimation results for equation ts6:
```

```
=====
```

```
ts6 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
  ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
  + ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + const
```

|        | Estimate  | Std. Error | t value | Pr(> t ) |
|--------|-----------|------------|---------|----------|
| ts1.l1 | -0.446445 | 1.577532   | -0.283  | 0.7781   |
| ts2.l1 | 0.005009  | 0.553773   | 0.009   | 0.9928   |
| ts3.l1 | -0.219165 | 0.528353   | -0.415  | 0.6797   |
| ts4.l1 | 3.708764  | 2.762089   | 1.343   | 0.1842   |
| ts5.l1 | -0.016156 | 0.007745   | -2.086  | 0.0410 * |
| ts6.l1 | 0.284513  | 0.138489   | 2.054   | 0.0441 * |
| ts1.l2 | 0.455663  | 1.785267   | 0.255   | 0.7994   |
| ts2.l2 | 1.085992  | 0.566557   | 1.917   | 0.0598 . |
| ts3.l2 | 0.881482  | 0.609849   | 1.445   | 0.1533   |
| ts4.l2 | -3.991887 | 2.929490   | -1.363  | 0.1778   |
| ts5.l2 | -0.010295 | 0.010451   | -0.985  | 0.3283   |
| ts6.l2 | 0.025610  | 0.142759   | 0.179   | 0.8582   |
| ts1.l3 | -1.050209 | 1.868397   | -0.562  | 0.5760   |
| ts2.l3 | 0.434230  | 0.552025   | 0.787   | 0.4345   |
| ts3.l3 | -0.033704 | 0.700034   | -0.048  | 0.9618   |
| ts4.l3 | -1.514924 | 3.003144   | -0.504  | 0.6157   |
| ts5.l3 | -0.013322 | 0.011972   | -1.113  | 0.2700   |
| ts6.l3 | 0.146518  | 0.139022   | 1.054   | 0.2959   |
| ts1.l4 | 0.390153  | 1.940706   | 0.201   | 0.8413   |
| ts2.l4 | -0.154531 | 0.568758   | -0.272  | 0.7867   |
| ts3.l4 | -0.787964 | 0.674280   | -1.169  | 0.2470   |
| ts4.l4 | 0.696308  | 2.973015   | 0.234   | 0.8156   |
| ts5.l4 | -0.006093 | 0.012324   | -0.494  | 0.6228   |
| ts6.l4 | -0.055558 | 0.143580   | -0.387  | 0.7001   |
| ts1.l5 | 0.822663  | 2.057548   | 0.400   | 0.6906   |
| ts2.l5 | -0.537268 | 0.568772   | -0.945  | 0.3485   |
| ts3.l5 | -0.514212 | 0.642808   | -0.800  | 0.4267   |
| ts4.l5 | 0.401441  | 2.879959   | 0.139   | 0.8896   |
| ts5.l5 | 0.005965  | 0.011297   | 0.528   | 0.5993   |
| ts6.l5 | -0.091194 | 0.134593   | -0.678  | 0.5005   |
| ts1.l6 | -0.898359 | 1.865091   | -0.482  | 0.6317   |
| ts2.l6 | 0.041930  | 0.526873   | 0.080   | 0.9368   |
| ts3.l6 | 0.678195  | 0.652586   | 1.039   | 0.3027   |
| ts4.l6 | -2.365936 | 2.423908   | -0.976  | 0.3328   |
| ts5.l6 | 0.006178  | 0.008862   | 0.697   | 0.4883   |
| ts6.l6 | 0.093337  | 0.127193   | 0.734   | 0.4658   |
| const  | -1.181516 | 1.453767   | -0.813  | 0.4194   |

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 4.162 on 63 degrees of freedom
Multiple R-Squared: 0.4147,    Adjusted R-squared: 0.08024
F-statistic: 1.24 on 36 and 63 DF,  p-value: 0.2244
```

```
Covariance matrix of residuals:
```

```
      ts1      ts2      ts3      ts4      ts5      ts6
```



```
ts1  0.14126  0.07200  0.06795  0.02601  -4.774  0.2707
ts2  0.07200  1.13976 -0.16257 -0.03392   7.265 -1.3727
ts3  0.06795 -0.16257  1.28450 -0.18913  -6.548 -0.5653
ts4  0.02601 -0.03392 -0.18913  0.27152  -3.267 -0.2381
ts5 -4.77351  7.26488 -6.54757 -3.26672 5132.542 -25.3430
ts6  0.27072 -1.37272 -0.56525 -0.23809  -25.343 17.3263
```

Correlation matrix of residuals:

```
      ts1      ts2      ts3      ts4      ts5      ts6
ts1  1.0000  0.17945  0.15952  0.13282 -0.17728  0.17305
ts2  0.1794  1.00000 -0.13436 -0.06098  0.09499 -0.30890
ts3  0.1595 -0.13436  1.00000 -0.32025 -0.08064 -0.11982
ts4  0.1328 -0.06098 -0.32025  1.00000 -0.08751 -0.10977
ts5 -0.1773  0.09499 -0.08064 -0.08751  1.00000 -0.08498
ts6  0.1730 -0.30890 -0.11982 -0.10977 -0.08498  1.00000
```

```
> AIC <- AIC(var_model)
> BIC <- BIC(var_model)
> log_likelihoood <- logLik(var_model)
> num_parameters <- length(coef(var_model))
> num_observations <- length(residuals(var_model))
> HQC <- -2 * as.numeric(log_likelihoood) + 2 * num_parameters * log(log(num_observations))
> cat("AIC:", AIC, "\n")
AIC: 2659.037
> cat("BIC:", BIC, "\n")
BIC: 3237.385
> cat("HQC:", HQC, "\n")

> cat("HQC:", HQC, "\n")
HQC: 2237.307
> plot(stability(var_model))
>
> plot(stability(var_model))

> > plot(stability(var_model))

> > var_model <- VAR(train_set, p=4)
> summary(var_model)
```

VAR Estimation Results:

=====

Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6

Deterministic variables: const

Sample size: 102

Log Likelihood: -1170.018

Roots of the characteristic polynomial:

```
0.8863 0.8863 0.8767 0.8767 0.8516 0.8516 0.7875 0.7875 0.7841 0.7841 0.7568 0.7568 0.7361 0.7361
0.7163 0.6682 0.6182 0.6182 0.612 0.612 0.5685 0.5685 0.5632 0.1848
```

Call:

```
VAR(y = train_set, p = 4)
```

Estimation results for equation ts1:

=====

```
ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
ts4.l4 + ts5.l4 + ts6.l4 + const
```

```
      Estimate Std. Error t value Pr(>|t|)
ts1.l1  0.4797857  0.1333638   3.598 0.000565 ***
ts2.l1 -0.0578105  0.0428449  -1.349 0.181196
ts3.l1  0.0743429  0.0453503   1.639 0.105230
ts4.l1  0.0640175  0.2283825   0.280 0.779993
ts5.l1  0.0012148  0.0006346   1.914 0.059304 .
ts6.l1 -0.0006399  0.0112343  -0.057 0.954728
ts1.l2 -0.1544148  0.1485713  -1.039 0.301903
ts2.l2 -0.0504768  0.0417713  -1.208 0.230588
ts3.l2 -0.0105790  0.0509044  -0.208 0.835918
ts4.l2 -0.3022957  0.2251394  -1.343 0.183313
```

```

ts5.12  0.0009611  0.0008178  1.175  0.243515
ts6.12 -0.0045412  0.0116445 -0.390  0.697623
ts1.13  0.0680637  0.1515233  0.449  0.654552
ts2.13 -0.0565972  0.0448140 -1.263  0.210423
ts3.13 -0.0151400  0.0535943 -0.282  0.778324
ts4.13  0.0484179  0.2282270  0.212  0.832552
ts5.13  0.0005824  0.0008557  0.681  0.498134
ts6.13 -0.0124449  0.0109597 -1.136  0.259682
ts1.14  0.1596151  0.1431112  1.115  0.268181
ts2.14 -0.0323151  0.0426247 -0.758  0.450688
ts3.14 -0.0511891  0.0497556 -1.029  0.306789
ts4.14 -0.0826371  0.1979312 -0.418  0.677472
ts5.14  0.0001090  0.0007152  0.152  0.879253
ts6.14 -0.0094814  0.0107402 -0.883  0.380098
const   0.1614949  0.0943631  1.711  0.091029 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 0.3725 on 77 degrees of freedom  
Multiple R-Squared: 0.4282, Adjusted R-squared: 0.2499  
F-statistic: 2.402 on 24 and 77 DF, p-value: 0.002037

Estimation results for equation ts2:

```

=====
ts2 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
ts4.14 + ts5.14 + ts6.14 + const

```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.11 | 0.5370662  | 0.3609675  | 1.488   | 0.14087  |     |
| ts2.11 | -0.1349416 | 0.1159656  | -1.164  | 0.24817  |     |
| ts3.11 | 0.3691023  | 0.1227469  | 3.007   | 0.00356  | **  |
| ts4.11 | 0.6263615  | 0.6181489  | 1.013   | 0.31410  |     |
| ts5.11 | -0.0004986 | 0.0017176  | -0.290  | 0.77236  |     |
| ts6.11 | -0.0767809 | 0.0304073  | -2.525  | 0.01362  | *   |
| ts1.12 | -1.2535946 | 0.4021287  | -3.117  | 0.00257  | **  |
| ts2.12 | -0.0856362 | 0.1130598  | -0.757  | 0.45110  |     |
| ts3.12 | -0.0306416 | 0.1377797  | -0.222  | 0.82459  |     |
| ts4.12 | 0.0200778  | 0.6093710  | 0.033   | 0.97380  |     |
| ts5.12 | -0.0017358 | 0.0022135  | -0.784  | 0.43532  |     |
| ts6.12 | 0.0203107  | 0.0315174  | 0.644   | 0.52121  |     |
| ts1.13 | 0.1717025  | 0.4101188  | 0.419   | 0.67663  |     |
| ts2.13 | 0.1418569  | 0.1212953  | 1.170   | 0.24580  |     |
| ts3.13 | 0.1803652  | 0.1450603  | 1.243   | 0.21750  |     |
| ts4.13 | 1.0688602  | 0.6177280  | 1.730   | 0.08758  | .   |
| ts5.13 | 0.0005150  | 0.0023160  | 0.222   | 0.82461  |     |
| ts6.13 | -0.0173708 | 0.0296640  | -0.586  | 0.55987  |     |
| ts1.14 | 1.4340243  | 0.3873504  | 3.702   | 0.00040  | *** |
| ts2.14 | -0.1702685 | 0.1153697  | -1.476  | 0.14406  |     |
| ts3.14 | -0.1178673 | 0.1346703  | -0.875  | 0.38417  |     |
| ts4.14 | -0.7626061 | 0.5357283  | -1.423  | 0.15863  |     |
| ts5.14 | -0.0001471 | 0.0019358  | -0.076  | 0.93962  |     |
| ts6.14 | 0.0073443  | 0.0290700  | 0.253   | 0.80122  |     |
| const  | 1.2144271  | 0.2554068  | 4.755   | 9.07e-06 | *** |

```

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 1.008 on 77 degrees of freedom  
Multiple R-Squared: 0.5271, Adjusted R-squared: 0.3797  
F-statistic: 3.577 on 24 and 77 DF, p-value: 1.141e-05

Estimation results for equation ts3:

```

=====
ts3 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
ts4.14 + ts5.14 + ts6.14 + const

```

|        | Estimate  | Std. Error | t value | Pr(> t )   |
|--------|-----------|------------|---------|------------|
| ts1.11 | 0.535703  | 0.414889   | 1.291   | 0.20050    |
| ts2.11 | 0.166623  | 0.133289   | 1.250   | 0.21505    |
| ts3.11 | 0.469442  | 0.141083   | 3.327   | 0.00135 ** |
| ts4.11 | -0.015251 | 0.710489   | -0.021  | 0.98293    |
| ts5.11 | -0.003798 | 0.001974   | -1.924  | 0.05805 .  |
| ts6.11 | 0.005621  | 0.034950   | 0.161   | 0.87265    |
| ts1.12 | 0.004915  | 0.462199   | 0.011   | 0.99154    |
| ts2.12 | -0.201035 | 0.129949   | -1.547  | 0.12596    |
| ts3.12 | 0.169532  | 0.158362   | 1.071   | 0.28772    |
| ts4.12 | 0.721785  | 0.700400   | 1.031   | 0.30599    |
| ts5.12 | -0.003436 | 0.002544   | -1.350  | 0.18084    |
| ts6.12 | 0.005883  | 0.036225   | 0.162   | 0.87142    |
| ts1.13 | 1.233313  | 0.471383   | 2.616   | 0.01069 *  |
| ts2.13 | -0.334634 | 0.139415   | -2.400  | 0.01880 *  |
| ts3.13 | 0.062646  | 0.166730   | 0.376   | 0.70815    |
| ts4.13 | 0.453315  | 0.710005   | 0.638   | 0.52506    |
| ts5.13 | -0.002545 | 0.002662   | -0.956  | 0.34201    |
| ts6.13 | -0.030393 | 0.034095   | -0.891  | 0.37548    |
| ts1.14 | -0.958308 | 0.445213   | -2.152  | 0.03449 *  |
| ts2.14 | 0.146455  | 0.132604   | 1.104   | 0.27284    |
| ts3.14 | -0.037092 | 0.154788   | -0.240  | 0.81125    |
| ts4.14 | -0.213232 | 0.615756   | -0.346  | 0.73007    |
| ts5.14 | -0.001842 | 0.002225   | -0.828  | 0.41034    |
| ts6.14 | 0.017850  | 0.033412   | 0.534   | 0.59472    |
| const  | 0.335995  | 0.293560   | 1.145   | 0.25594    |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.159 on 77 degrees of freedom  
Multiple R-Squared: 0.5441, Adjusted R-squared: 0.402  
F-statistic: 3.828 on 24 and 77 DF, p-value: 3.89e-06

Estimation results for equation ts4:

=====

ts4 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + ts5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 + ts4.14 + ts5.14 + ts6.14 + const

|        | Estimate   | Std. Error | t value | Pr(> t )     |
|--------|------------|------------|---------|--------------|
| ts1.11 | -0.5390232 | 0.1876856  | -2.872  | 0.005267 **  |
| ts2.11 | -0.0827985 | 0.0602965  | -1.373  | 0.173679     |
| ts3.11 | -0.2271005 | 0.0638224  | -3.558  | 0.000643 *** |
| ts4.11 | 0.4329284  | 0.3214074  | 1.347   | 0.181939     |
| ts5.11 | 0.0037736  | 0.0008931  | 4.225   | 6.49e-05 *** |
| ts6.11 | 0.0030229  | 0.0158103  | 0.191   | 0.848872     |
| ts1.12 | 0.1686587  | 0.2090874  | 0.807   | 0.422357     |
| ts2.12 | 0.1013583  | 0.0587856  | 1.724   | 0.088684 .   |
| ts3.12 | 0.1942387  | 0.0716388  | 2.711   | 0.008260 **  |
| ts4.12 | 0.5608290  | 0.3168433  | 1.770   | 0.080677 .   |
| ts5.12 | 0.0046631  | 0.0011509  | 4.052   | 0.000120 *** |
| ts6.12 | 0.0058002  | 0.0163875  | 0.354   | 0.724351     |
| ts1.13 | -0.2653442 | 0.2132419  | -1.244  | 0.217151     |
| ts2.13 | -0.0361373 | 0.0630677  | -0.573  | 0.568319     |
| ts3.13 | -0.0208079 | 0.0754243  | -0.276  | 0.783381     |
| ts4.13 | -0.0914995 | 0.3211886  | -0.285  | 0.776503     |
| ts5.13 | 0.0027648  | 0.0012042  | 2.296   | 0.024401 *   |
| ts6.13 | 0.0164019  | 0.0154238  | 1.063   | 0.290919     |
| ts1.14 | 0.4476005  | 0.2014034  | 2.222   | 0.029191 *   |
| ts2.14 | -0.1656239 | 0.0599867  | -2.761  | 0.007200 **  |
| ts3.14 | -0.0223376 | 0.0700220  | -0.319  | 0.750584     |
| ts4.14 | -0.2876048 | 0.2785527  | -1.032  | 0.305071     |
| ts5.14 | 0.0014665  | 0.0010065  | 1.457   | 0.149172     |
| ts6.14 | -0.0355479 | 0.0151150  | -2.352  | 0.021238 *   |
| const  | 0.2289915  | 0.1327991  | 1.724   | 0.088658 .   |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.5242 on 77 degrees of freedom  
 Multiple R-Squared: 0.6034, Adjusted R-squared: 0.4797  
 F-statistic: 4.881 on 24 and 77 DF, p-value: 5.353e-08

Estimation results for equation ts5:

=====

ts5 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + ts5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 + ts4.l4 + ts5.l4 + ts6.l4 + const

|        | Estimate  | Std. Error | t value | Pr(> t )     |
|--------|-----------|------------|---------|--------------|
| ts1.l1 | 27.86456  | 24.50639   | 1.137   | 0.2591       |
| ts2.l1 | 1.00957   | 7.87300    | 0.128   | 0.8983       |
| ts3.l1 | -4.82298  | 8.33339    | -0.579  | 0.5644       |
| ts4.l1 | -50.88143 | 41.96666   | -1.212  | 0.2291       |
| ts5.l1 | -0.83229  | 0.11661    | -7.137  | 4.56e-10 *** |
| ts6.l1 | -1.46154  | 2.06438    | -0.708  | 0.4811       |
| ts1.l2 | -19.81451 | 27.30086   | -0.726  | 0.4702       |
| ts2.l2 | 14.56731  | 7.67573    | 1.898   | 0.0615 .     |
| ts3.l2 | -4.42326  | 9.35398    | -0.473  | 0.6376       |
| ts4.l2 | -25.66520 | 41.37072   | -0.620  | 0.5368       |
| ts5.l2 | -0.61851  | 0.15027    | -4.116  | 9.60e-05 *** |
| ts6.l2 | 1.25707   | 2.13974    | 0.587   | 0.5586       |
| ts1.l3 | -51.54289 | 27.84332   | -1.851  | 0.0680 .     |
| ts2.l3 | 11.70394  | 8.23484    | 1.421   | 0.1593       |
| ts3.l3 | -0.75408  | 9.84827    | -0.077  | 0.9392       |
| ts4.l3 | -28.42012 | 41.93809   | -0.678  | 0.5000       |
| ts5.l3 | -0.25136  | 0.15724    | -1.599  | 0.1140       |
| ts6.l3 | 3.01960   | 2.01392    | 1.499   | 0.1379       |
| ts1.l4 | 8.54014   | 26.29755   | 0.325   | 0.7463       |
| ts2.l4 | -5.66713  | 7.83255    | -0.724  | 0.4715       |
| ts3.l4 | -10.37861 | 9.14288    | -1.135  | 0.2598       |
| ts4.l4 | 35.07306  | 36.37105   | 0.964   | 0.3379       |
| ts5.l4 | -0.01002  | 0.13142    | -0.076  | 0.9395       |
| ts6.l4 | -1.02674  | 1.97358    | -0.520  | 0.6044       |
| const  | -15.54829 | 17.33978   | -0.897  | 0.3727       |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 68.45 on 77 degrees of freedom  
 Multiple R-Squared: 0.5219, Adjusted R-squared: 0.3729  
 F-statistic: 3.503 on 24 and 77 DF, p-value: 1.568e-05

Estimation results for equation ts6:

=====

ts6 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + ts5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 + ts4.l4 + ts5.l4 + ts6.l4 + const

|        | Estimate  | Std. Error | t value | Pr(> t )   |
|--------|-----------|------------|---------|------------|
| ts1.l1 | 0.196734  | 1.442135   | 0.136   | 0.89185    |
| ts2.l1 | 0.252990  | 0.463305   | 0.546   | 0.58661    |
| ts3.l1 | -0.099466 | 0.490398   | -0.203  | 0.83981    |
| ts4.l1 | 4.056119  | 2.469625   | 1.642   | 0.10458    |
| ts5.l1 | -0.015470 | 0.006862   | -2.254  | 0.02701 *  |
| ts6.l1 | 0.313804  | 0.121483   | 2.583   | 0.01169 *  |
| ts1.l2 | -0.274742 | 1.606582   | -0.171  | 0.86466    |
| ts2.l2 | 1.200873  | 0.451696   | 2.659   | 0.00954 ** |
| ts3.l2 | 0.908221  | 0.550457   | 1.650   | 0.10303    |
| ts4.l2 | -3.115066 | 2.434555   | -1.280  | 0.20456    |
| ts5.l2 | -0.015311 | 0.008843   | -1.731  | 0.08739 .  |
| ts6.l2 | -0.013644 | 0.125918   | -0.108  | 0.91400    |
| ts1.l3 | -0.417360 | 1.638504   | -0.255  | 0.79962    |
| ts2.l3 | 0.454878  | 0.484598   | 0.939   | 0.35084    |
| ts3.l3 | -0.307640 | 0.579544   | -0.531  | 0.59706    |

```
ts4.13 -3.308247  2.467943 -1.340  0.18403
ts5.13 -0.017321  0.009253 -1.872  0.06501 .
ts6.13  0.152797  0.118513  1.289  0.20116
ts1.14 -0.570530  1.547540 -0.369  0.71339
ts2.14  0.072479  0.460925  0.157  0.87546
ts3.14 -0.958335  0.538034 -1.781  0.07883 .
ts4.14 -0.256628  2.140338 -0.120  0.90487
ts5.14 -0.014349  0.007734 -1.855  0.06738 .
ts6.14  0.002621  0.116140  0.023  0.98206
const -2.252502  1.020400 -2.207  0.03026 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 4.028 on 77 degrees of freedom
Multiple R-Squared: 0.3499,    Adjusted R-squared: 0.1472
F-statistic: 1.727 on 24 and 77 DF,  p-value: 0.03804
```

Covariance matrix of residuals:

|     | ts1      | ts2      | ts3      | ts4      | ts5      | ts6      |
|-----|----------|----------|----------|----------|----------|----------|
| ts1 | 0.13876  | 0.07500  | 0.08695  | 0.02488  | -4.979   | 0.3196   |
| ts2 | 0.07500  | 1.01657  | -0.17241 | -0.02577 | 6.309    | -1.0695  |
| ts3 | 0.08695  | -0.17241 | 1.34297  | -0.22554 | -5.641   | -0.2223  |
| ts4 | 0.02488  | -0.02577 | -0.22554 | 0.27483  | -4.124   | -0.2283  |
| ts5 | -4.97938 | 6.30900  | -5.64061 | -4.12393 | 4685.543 | -24.1934 |
| ts6 | 0.31957  | -1.06954 | -0.22231 | -0.22830 | -24.193  | 16.2261  |

Correlation matrix of residuals:

|     | ts1     | ts2      | ts3      | ts4      | ts5      | ts6      |
|-----|---------|----------|----------|----------|----------|----------|
| ts1 | 1.0000  | 0.19970  | 0.20142  | 0.12742  | -0.19528 | 0.21297  |
| ts2 | 0.1997  | 1.00000  | -0.14756 | -0.04876 | 0.09141  | -0.26334 |
| ts3 | 0.2014  | -0.14756 | 1.00000  | -0.37124 | -0.07111 | -0.04762 |
| ts4 | 0.1274  | -0.04876 | -0.37124 | 1.00000  | -0.11492 | -0.10811 |
| ts5 | -0.1953 | 0.09141  | -0.07111 | -0.11492 | 1.00000  | -0.08774 |
| ts6 | 0.2130  | -0.26334 | -0.04762 | -0.10811 | -0.08774 | 1.00000  |

```
> AIC <- AIC(var_model)
> BIC <- BIC(var_model)log_likelihood <- logLik(var_model)num_parameters <- length(coef(var_model))
Error: unexpected symbol in "BIC <- BIC(var_model)log_likelihood"
> BIC <- BIC(var_model)
> log_likelihood <- logLik(var_model)
> num_parameters <- length(coef(var_model))
>
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> cat("AIC:", AIC, "\n")
AIC: 2640.037
> cat("BIC:", BIC, "\n")
BIC: 3033.783
> cat("HQC:", HQC, "\n")
HQC: 2362.307
> plot(stability(var_model))
> var_model <- VAR(train_set, p=2)
> summary(var_model)
```

VAR Estimation Results:

=====

Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6

Deterministic variables: const

Sample size: 104

Log Likelihood: -1252.276

Roots of the characteristic polynomial:

0.8271 0.722 0.722 0.6885 0.6885 0.6141 0.6141 0.5519 0.5519 0.4364 0.1571 0.1571

Call:

VAR(y = train\_set, p = 2)

## Estimation results for equation ts1:

=====

```
ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.l1 | 0.5109403  | 0.1196802  | 4.269   | 4.81e-05 | *** |
| ts2.l1 | -0.0608881 | 0.0386110  | -1.577  | 0.1183   |     |
| ts3.l1 | 0.0801893  | 0.0389629  | 2.058   | 0.0424   | *   |
| ts4.l1 | 0.0549885  | 0.1917670  | 0.287   | 0.7750   |     |
| ts5.l1 | 0.0008186  | 0.0005436  | 1.506   | 0.1356   |     |
| ts6.l1 | -0.0084201 | 0.0096910  | -0.869  | 0.3872   |     |
| ts1.l2 | -0.0280974 | 0.1231998  | -0.228  | 0.8201   |     |
| ts2.l2 | -0.0627634 | 0.0352148  | -1.782  | 0.0780   | .   |
| ts3.l2 | -0.0392048 | 0.0444841  | -0.881  | 0.3805   |     |
| ts4.l2 | -0.2425311 | 0.1682944  | -1.441  | 0.1530   |     |
| ts5.l2 | 0.0005318  | 0.0005881  | 0.904   | 0.3682   |     |
| ts6.l2 | -0.0108716 | 0.0096258  | -1.129  | 0.2617   |     |
| const  | 0.0804778  | 0.0640603  | 1.256   | 0.2122   |     |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3682 on 91 degrees of freedom  
Multiple R-Squared: 0.3815, Adjusted R-squared: 0.2999  
F-statistic: 4.677 on 12 and 91 DF, p-value: 6.957e-06

## Estimation results for equation ts2:

=====

```
ts2 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + const
```

|        | Estimate  | Std. Error | t value | Pr(> t ) |     |
|--------|-----------|------------|---------|----------|-----|
| ts1.l1 | 0.162817  | 0.356882   | 0.456   | 0.6493   |     |
| ts2.l1 | -0.069194 | 0.115137   | -0.601  | 0.5494   |     |
| ts3.l1 | 0.480720  | 0.116186   | 4.138   | 7.82e-05 | *** |
| ts4.l1 | 0.643854  | 0.571843   | 1.126   | 0.2632   |     |
| ts5.l1 | -0.002209 | 0.001621   | -1.363  | 0.1764   |     |
| ts6.l1 | -0.054734 | 0.028898   | -1.894  | 0.0614   | .   |
| ts1.l2 | -0.678929 | 0.367377   | -1.848  | 0.0678   | .   |
| ts2.l2 | -0.156407 | 0.105009   | -1.489  | 0.1398   |     |
| ts3.l2 | -0.061970 | 0.132650   | -0.467  | 0.6415   |     |
| ts4.l2 | -0.742538 | 0.501848   | -1.480  | 0.1424   |     |
| ts5.l2 | -0.002866 | 0.001754   | -1.634  | 0.1057   |     |
| ts6.l2 | -0.001921 | 0.028704   | -0.067  | 0.9468   |     |
| const  | 1.142811  | 0.191026   | 5.983   | 4.27e-08 | *** |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.098 on 91 degrees of freedom  
Multiple R-Squared: 0.338, Adjusted R-squared: 0.2507  
F-statistic: 3.873 on 12 and 91 DF, p-value: 8.673e-05

## Estimation results for equation ts3:

=====

```
ts3 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + const
```

|        | Estimate  | Std. Error | t value | Pr(> t ) |     |
|--------|-----------|------------|---------|----------|-----|
| ts1.l1 | 0.635412  | 0.387479   | 1.640   | 0.104486 |     |
| ts2.l1 | 0.108243  | 0.125008   | 0.866   | 0.388829 |     |
| ts3.l1 | 0.466353  | 0.126147   | 3.697   | 0.000373 | *** |
| ts4.l1 | -0.016150 | 0.620868   | -0.026  | 0.979305 |     |
| ts5.l1 | -0.003175 | 0.001760   | -1.804  | 0.074525 | .   |
| ts6.l1 | -0.022326 | 0.031376   | -0.712  | 0.478542 |     |
| ts1.l2 | 0.245733  | 0.398874   | 0.616   | 0.539389 |     |
| ts2.l2 | -0.116831 | 0.114012   | -1.025  | 0.308211 |     |

```

ts3.12  0.161525    0.144023    1.122 0.265015
ts4.12  0.893332    0.544873    1.640 0.104557
ts5.12 -0.001392    0.001904   -0.731 0.466540
ts6.12  0.021388    0.031165    0.686 0.494280
const   0.107322    0.207403    0.517 0.606091
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 1.192 on 91 degrees of freedom
Multiple R-Squared: 0.4359,    Adjusted R-squared: 0.3615
F-statistic: 5.86 on 12 and 91 DF,  p-value: 1.974e-07

```

Estimation results for equation ts4:

```

=====
ts4 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + const

```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.11 | -0.4413287 | 0.1735718  | -2.543  | 0.012691 | *   |
| ts2.11 | -0.0658387 | 0.0559975  | -1.176  | 0.242764 |     |
| ts3.11 | -0.2162729 | 0.0565078  | -3.827  | 0.000237 | *** |
| ts4.11 | 0.3896131  | 0.2781191  | 1.401   | 0.164649 |     |
| ts5.11 | 0.0025951  | 0.0007884  | 3.291   | 0.001420 | **  |
| ts6.11 | -0.0050794 | 0.0140548  | -0.361  | 0.718636 |     |
| ts1.12 | 0.2068214  | 0.1786763  | 1.158   | 0.250089 |     |
| ts2.12 | 0.0656297  | 0.0510720  | 1.285   | 0.202038 |     |
| ts3.12 | 0.1119968  | 0.0645152  | 1.736   | 0.085953 | .   |
| ts4.12 | 0.2782495  | 0.2440768  | 1.140   | 0.257275 |     |
| ts5.12 | 0.0023369  | 0.0008529  | 2.740   | 0.007398 | **  |
| ts6.12 | -0.0014864 | 0.0139603  | -0.106  | 0.915439 |     |
| const  | 0.0623817  | 0.0929064  | 0.671   | 0.503637 |     |

```

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 0.534 on 91 degrees of freedom
Multiple R-Squared: 0.5161,    Adjusted R-squared: 0.4522
F-statistic: 8.086 on 12 and 91 DF,  p-value: 4.124e-10

```

Estimation results for equation ts5:

```

=====
ts5 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + const

```

|        | Estimate | Std. Error | t value | Pr(> t ) |     |
|--------|----------|------------|---------|----------|-----|
| ts1.11 | 32.7141  | 22.3948    | 1.461   | 0.1475   |     |
| ts2.11 | 4.6170   | 7.2250     | 0.639   | 0.5244   |     |
| ts3.11 | -1.5461  | 7.2908     | -0.212  | 0.8325   |     |
| ts4.11 | -38.4677 | 35.8839    | -1.072  | 0.2866   |     |
| ts5.11 | -0.7168  | 0.1017     | -7.047  | 3.43e-10 | *** |
| ts6.11 | -1.2129  | 1.8134     | -0.669  | 0.5053   |     |
| ts1.12 | -43.6693 | 23.0534    | -1.894  | 0.0614   | .   |
| ts2.12 | 13.7932  | 6.5895     | 2.093   | 0.0391   | *   |
| ts3.12 | -5.2913  | 8.3240     | -0.636  | 0.5266   |     |
| ts4.12 | 8.9991   | 31.4916    | 0.286   | 0.7757   |     |
| ts5.12 | -0.4481  | 0.1100     | -4.072  | 9.93e-05 | *** |
| ts6.12 | 1.4847   | 1.8012     | 0.824   | 0.4119   |     |
| const  | -16.0056 | 11.9871    | -1.335  | 0.1851   |     |

```

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 68.9 on 91 degrees of freedom
Multiple R-Squared: 0.4277,    Adjusted R-squared: 0.3522
F-statistic: 5.666 on 12 and 91 DF,  p-value: 3.488e-07

```

Estimation results for equation ts6:

=====

ts6 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + ts5.l2 + ts6.l2 + const

|        | Estimate  | Std. Error | t value | Pr(> t )  |
|--------|-----------|------------|---------|-----------|
| ts1.l1 | 0.538616  | 1.304592   | 0.413   | 0.6807    |
| ts2.l1 | 0.259848  | 0.420885   | 0.617   | 0.5385    |
| ts3.l1 | -0.157208 | 0.424721   | -0.370  | 0.7121    |
| ts4.l1 | 3.788641  | 2.090385   | 1.812   | 0.0732 .  |
| ts5.l1 | -0.008785 | 0.005926   | -1.482  | 0.1417    |
| ts6.l1 | 0.329939  | 0.105638   | 3.123   | 0.0024 ** |
| ts1.l2 | -0.883599 | 1.342958   | -0.658  | 0.5122    |
| ts2.l2 | 0.998203  | 0.383865   | 2.600   | 0.0109 *  |
| ts3.l2 | 0.578495  | 0.484906   | 1.193   | 0.2360    |
| ts4.l2 | -3.516961 | 1.834518   | -1.917  | 0.0584 .  |
| ts5.l2 | -0.002348 | 0.006411   | -0.366  | 0.7150    |
| ts6.l2 | -0.022794 | 0.104928   | -0.217  | 0.8285    |
| const  | -1.763918 | 0.698299   | -2.526  | 0.0133 *  |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.014 on 91 degrees of freedom  
Multiple R-Squared: 0.2448, Adjusted R-squared: 0.1452  
F-statistic: 2.458 on 12 and 91 DF, p-value: 0.007972

Covariance matrix of residuals:

|     | ts1      | ts2      | ts3      | ts4      | ts5      | ts6     |
|-----|----------|----------|----------|----------|----------|---------|
| ts1 | 0.13557  | 0.10268  | 0.08213  | 0.02869  | -5.058   | 0.2359  |
| ts2 | 0.10268  | 1.20550  | -0.21583 | 0.01775  | -1.080   | -1.0859 |
| ts3 | 0.08213  | -0.21583 | 1.42106  | -0.25239 | -8.951   | -0.1723 |
| ts4 | 0.02869  | 0.01775  | -0.25239 | 0.28515  | -4.141   | -0.2625 |
| ts5 | -5.05829 | -1.08027 | -8.95067 | -4.14145 | 4746.909 | 7.8483  |
| ts6 | 0.23592  | -1.08585 | -0.17229 | -0.26252 | 7.848    | 16.1089 |

Correlation matrix of residuals:

|     | ts1     | ts2      | ts3      | ts4      | ts5      | ts6      |
|-----|---------|----------|----------|----------|----------|----------|
| ts1 | 1.0000  | 0.25399  | 0.18713  | 0.14590  | -0.19940 | 0.15964  |
| ts2 | 0.2540  | 1.00000  | -0.16490 | 0.03028  | -0.01428 | -0.24641 |
| ts3 | 0.1871  | -0.16490 | 1.00000  | -0.39649 | -0.10898 | -0.03601 |
| ts4 | 0.1459  | 0.03028  | -0.39649 | 1.00000  | -0.11257 | -0.12249 |
| ts5 | -0.1994 | -0.01428 | -0.10898 | -0.11257 | 1.00000  | 0.02838  |
| ts6 | 0.1596  | -0.24641 | -0.03601 | -0.12249 | 0.02838  | 1.00000  |

```
> AIC <- AIC(var_model)
> BIC <- BIC(var_model)
> log_likelihood <- logLik(var_model)
> num_parameters <- length(coef(var_model))
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> cat("AIC:", AIC, "\n")
AIC: 2660.552
> cat("BIC:", BIC, "\n")
BIC: 2866.815
> cat("HQC:", HQC, "\n")
HQC: 2526.822
> cat("RMSE:", RMSE, "\n")
RMSE: 0.7471908 2.856689 1.446747 1.328938 108.0238 5.661724
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 1.218561 3.226323 2.612527 2.221969 115.7346 9.460426
> cat("MAE:", MAE, "\n")
MAE: 1.075512 2.474723 1.908565 1.494408 86.37605 6.855286
```



```
> plot(stability(var_model))
> var_model <- VAR(train_set, p=3)
> summary(var_model)
```

# VAR Estimation Results:

```
=====
```

Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6

Deterministic variables: const

Sample size: 103

Log Likelihood: -1214.572

Roots of the characteristic polynomial:

```
0.8392 0.8392    0.8 0.7267 0.7267 0.7248 0.7248 0.6774 0.6774 0.6124 0.5922 0.4858 0.4858 0.4432
0.4432 0.2755 0.2573 0.2573
```

Call:

```
VAR(y = train_set, p = 3)
```

# Estimation results for equation ts1:

```
=====
```

```
ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.l1 | 0.4549455  | 0.1234002  | 3.687   | 0.000402 | *** |
| ts2.l1 | -0.0431743 | 0.0402585  | -1.072  | 0.286599 |     |
| ts3.l1 | 0.0921593  | 0.0414750  | 2.222   | 0.028969 | *   |
| ts4.l1 | 0.1256885  | 0.2090803  | 0.601   | 0.549359 |     |
| ts5.l1 | 0.0010047  | 0.0005844  | 1.719   | 0.089250 | .   |
| ts6.l1 | 0.0007158  | 0.0106713  | 0.067   | 0.946683 |     |
| ts1.l2 | -0.1064368 | 0.1412808  | -0.753  | 0.453334 |     |
| ts2.l2 | -0.0585144 | 0.0394590  | -1.483  | 0.141839 |     |
| ts3.l2 | -0.0262984 | 0.0476558  | -0.552  | 0.582523 |     |
| ts4.l2 | -0.3621294 | 0.2041859  | -1.774  | 0.079766 | .   |
| ts5.l2 | 0.0008457  | 0.0007141  | 1.184   | 0.239678 |     |
| ts6.l2 | -0.0057821 | 0.0104343  | -0.554  | 0.580956 |     |
| ts1.l3 | 0.0987710  | 0.1283778  | 0.769   | 0.443827 |     |
| ts2.l3 | -0.0695740 | 0.0386313  | -1.801  | 0.075296 | .   |
| ts3.l3 | -0.0315957 | 0.0480135  | -0.658  | 0.512300 |     |
| ts4.l3 | 0.0140845  | 0.1886988  | 0.075   | 0.940678 |     |
| ts5.l3 | 0.0004956  | 0.0006619  | 0.749   | 0.456134 |     |
| ts6.l3 | -0.0159360 | 0.0098268  | -1.622  | 0.108620 |     |
| const  | 0.1213626  | 0.0770483  | 1.575   | 0.118981 |     |

```
---
```

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3653 on 84 degrees of freedom

Multiple R-Squared: 0.4047, Adjusted R-squared: 0.2772

F-statistic: 3.173 on 18 and 84 DF, p-value: 0.0001805

# Estimation results for equation ts2:

```
=====
```

```
ts2 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + const
```

|        | Estimate  | Std. Error | t value | Pr(> t ) |     |
|--------|-----------|------------|---------|----------|-----|
| ts1.l1 | 0.194819  | 0.373292   | 0.522   | 0.603118 |     |
| ts2.l1 | -0.016817 | 0.121784   | -0.138  | 0.890499 |     |
| ts3.l1 | 0.480425  | 0.125464   | 3.829   | 0.000247 | *** |
| ts4.l1 | 0.607044  | 0.632479   | 0.960   | 0.339917 |     |
| ts5.l1 | -0.001548 | 0.001768   | -0.876  | 0.383700 |     |
| ts6.l1 | -0.057365 | 0.032281   | -1.777  | 0.079183 | .   |
| ts1.l2 | -1.126237 | 0.427382   | -2.635  | 0.010012 | *   |
| ts2.l2 | -0.123767 | 0.119366   | -1.037  | 0.302771 |     |
| ts3.l2 | -0.107790 | 0.144161   | -0.748  | 0.456727 |     |
| ts4.l2 | -0.413334 | 0.617673   | -0.669  | 0.505215 |     |
| ts5.l2 | -0.002562 | 0.002160   | -1.186  | 0.238948 |     |
| ts6.l2 | 0.020927  | 0.031564   | 0.663   | 0.509156 |     |
| ts1.l3 | 0.757063  | 0.388350   | 1.949   | 0.054580 | .   |

```

ts2.l3 -0.023893    0.116862   -0.204  0.838495
ts3.l3  0.046108    0.145243    0.317  0.751687
ts4.l3  0.101173    0.570823    0.177  0.859746
ts5.l3  0.001141    0.002002    0.570  0.570199
ts6.l3 -0.038147    0.029727   -1.283  0.202928
const   1.073932    0.233075    4.608  1.44e-05 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 1.105 on 84 degrees of freedom
Multiple R-Squared: 0.3807,    Adjusted R-squared: 0.2479
F-statistic: 2.868 on 18 and 84 DF,  p-value: 0.0006053

```

Estimation results for equation ts3:

```

=====
ts3 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + const

```

|        | Estimate  | Std. Error | t value | Pr(> t ) |    |
|--------|-----------|------------|---------|----------|----|
| ts1.l1 | 0.577711  | 0.386960   | 1.493   | 0.13920  |    |
| ts2.l1 | 0.093424  | 0.126243   | 0.740   | 0.46134  |    |
| ts3.l1 | 0.387815  | 0.130058   | 2.982   | 0.00375  | ** |
| ts4.l1 | -0.158861 | 0.655637   | -0.242  | 0.80914  |    |
| ts5.l1 | -0.002664 | 0.001832   | -1.454  | 0.14977  |    |
| ts6.l1 | 0.005706  | 0.033463   | 0.171   | 0.86501  |    |
| ts1.l2 | -0.027696 | 0.443030   | -0.063  | 0.95030  |    |
| ts2.l2 | -0.158470 | 0.123736   | -1.281  | 0.20382  |    |
| ts3.l2 | 0.198724  | 0.149440   | 1.330   | 0.18719  |    |
| ts4.l2 | 0.729629  | 0.640289   | 1.140   | 0.25772  |    |
| ts5.l2 | -0.001839 | 0.002239   | -0.821  | 0.41388  |    |
| ts6.l2 | 0.009074  | 0.032720   | 0.277   | 0.78220  |    |
| ts1.l3 | 0.761998  | 0.402569   | 1.893   | 0.06182  | .  |
| ts2.l3 | -0.313724 | 0.121140   | -2.590  | 0.01132  | *  |
| ts3.l3 | 0.089961  | 0.150561   | 0.598   | 0.55178  |    |
| ts4.l3 | 0.919907  | 0.591724   | 1.555   | 0.12380  |    |
| ts5.l3 | -0.001367 | 0.002076   | -0.658  | 0.51207  |    |
| ts6.l3 | -0.014674 | 0.030815   | -0.476  | 0.63516  |    |
| const  | 0.507450  | 0.241609   | 2.100   | 0.03870  | *  |

```

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 1.145 on 84 degrees of freedom
Multiple R-Squared: 0.5188,    Adjusted R-squared: 0.4156
F-statistic: 5.031 on 18 and 84 DF,  p-value: 1.544e-07

```

Estimation results for equation ts4:

```

=====
ts4 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + const

```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.l1 | -0.4843539 | 0.1833409  | -2.642  | 0.009833 | **  |
| ts2.l1 | -0.0545079 | 0.0598137  | -0.911  | 0.364748 |     |
| ts3.l1 | -0.1939360 | 0.0616212  | -3.147  | 0.002281 | **  |
| ts4.l1 | 0.4365386  | 0.3106394  | 1.405   | 0.163623 |     |
| ts5.l1 | 0.0030079  | 0.0008682  | 3.464   | 0.000839 | *** |
| ts6.l1 | -0.0033920 | 0.0158548  | -0.214  | 0.831110 |     |
| ts1.l2 | 0.2219207  | 0.2099069  | 1.057   | 0.293436 |     |
| ts2.l2 | 0.0874366  | 0.0586259  | 1.491   | 0.139594 |     |
| ts3.l2 | 0.1405658  | 0.0708043  | 1.985   | 0.050377 | .   |
| ts4.l2 | 0.3576114  | 0.3033676  | 1.179   | 0.241804 |     |
| ts5.l2 | 0.0033402  | 0.0010610  | 3.148   | 0.002275 | **  |
| ts6.l2 | 0.0022714  | 0.0155027  | 0.147   | 0.883865 |     |
| ts1.l3 | -0.0466213 | 0.1907364  | -0.244  | 0.807496 |     |
| ts2.l3 | -0.0301661 | 0.0573961  | -0.526  | 0.600567 |     |
| ts3.l3 | -0.0569996 | 0.0713357  | -0.799  | 0.426525 |     |

```
ts4.l3 -0.2928155  0.2803578  -1.044  0.299281
ts5.l3  0.0016311  0.0009835   1.659  0.100938
ts6.l3  0.0013619  0.0146002   0.093  0.925901
const   0.0571082  0.1144739   0.499  0.619171
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.5427 on 84 degrees of freedom
Multiple R-Squared: 0.5381,    Adjusted R-squared: 0.4391
F-statistic: 5.436 on 18 and 84 DF,  p-value: 3.653e-08
```

Estimation results for equation ts5:

```
=====
```

```
ts5 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + const
```

|        | Estimate | Std. Error | t value | Pr(> t )     |
|--------|----------|------------|---------|--------------|
| ts1.l1 | 35.8678  | 22.8177    | 1.572   | 0.1197       |
| ts2.l1 | 1.1287   | 7.4441     | 0.152   | 0.8798       |
| ts3.l1 | -2.0429  | 7.6691     | -0.266  | 0.7906       |
| ts4.l1 | -36.5638 | 38.6607    | -0.946  | 0.3470       |
| ts5.l1 | -0.8288  | 0.1081     | -7.670  | 2.76e-11 *** |
| ts6.l1 | -1.4683  | 1.9732     | -0.744  | 0.4589       |
| ts1.l2 | -14.6104 | 26.1240    | -0.559  | 0.5775       |
| ts2.l2 | 12.3492  | 7.2963     | 1.693   | 0.0943 .     |
| ts3.l2 | -5.5043  | 8.8120     | -0.625  | 0.5339       |
| ts4.l2 | -21.8757 | 37.7556    | -0.579  | 0.5639       |
| ts5.l2 | -0.5949  | 0.1320     | -4.505  | 2.13e-05 *** |
| ts6.l2 | -0.2010  | 1.9294     | -0.104  | 0.9173       |
| ts1.l3 | -52.6180 | 23.7381    | -2.217  | 0.0294 *     |
| ts2.l3 | 11.7977  | 7.1432     | 1.652   | 0.1024       |
| ts3.l3 | -2.0408  | 8.8781     | -0.230  | 0.8188       |
| ts4.l3 | 8.4254   | 34.8919    | 0.241   | 0.8098       |
| ts5.l3 | -0.2566  | 0.1224     | -2.096  | 0.0391 *     |
| ts6.l3 | 3.3246   | 1.8171     | 1.830   | 0.0709 .     |
| const  | -22.0362 | 14.2469    | -1.547  | 0.1257       |

```
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 67.54 on 84 degrees of freedom
Multiple R-Squared: 0.4922,    Adjusted R-squared: 0.3834
F-statistic: 4.524 on 18 and 84 DF,  p-value: 9.876e-07
```

Estimation results for equation ts6:

```
=====
```

```
ts6 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + const
```

|        | Estimate  | Std. Error | t value | Pr(> t )   |
|--------|-----------|------------|---------|------------|
| ts1.l1 | 0.536324  | 1.372424   | 0.391   | 0.69694    |
| ts2.l1 | 0.178136  | 0.447744   | 0.398   | 0.69175    |
| ts3.l1 | -0.139811 | 0.461274   | -0.303  | 0.76256    |
| ts4.l1 | 3.978406  | 2.325335   | 1.711   | 0.09079 .  |
| ts5.l1 | -0.011755 | 0.006499   | -1.809  | 0.07408 .  |
| ts6.l1 | 0.339792  | 0.118683   | 2.863   | 0.00530 ** |
| ts1.l2 | -0.184351 | 1.571287   | -0.117  | 0.90688    |
| ts2.l2 | 1.167328  | 0.438853   | 2.660   | 0.00936 ** |
| ts3.l2 | 0.741483  | 0.530015   | 1.399   | 0.16550    |
| ts4.l2 | -4.020334 | 2.270900   | -1.770  | 0.08029 .  |
| ts5.l2 | -0.006396 | 0.007942   | -0.805  | 0.42289    |
| ts6.l2 | -0.082598 | 0.116048   | -0.712  | 0.47858    |
| ts1.l3 | -0.895204 | 1.427784   | -0.627  | 0.53237    |
| ts2.l3 | 0.220073  | 0.429647   | 0.512   | 0.60984    |
| ts3.l3 | -0.402536 | 0.533993   | -0.754  | 0.45306    |
| ts4.l3 | -0.518608 | 2.098657   | -0.247  | 0.80542    |
| ts5.l3 | -0.006708 | 0.007362   | -0.911  | 0.36483    |

```
ts6.13  0.182244  0.109292  1.667  0.09914 .
const -1.959342  0.856910 -2.287  0.02474 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 4.063 on 84 degrees of freedom
Multiple R-Squared: 0.2789, Adjusted R-squared: 0.1244
F-statistic: 1.805 on 18 and 84 DF, p-value: 0.03775
```

```
Covariance matrix of residuals:
```

|     | ts1      | ts2      | ts3      | ts4      | ts5      | ts6      |
|-----|----------|----------|----------|----------|----------|----------|
| ts1 | 0.13343  | 0.09719  | 0.06935  | 0.03000  | -4.192   | 0.31250  |
| ts2 | 0.09719  | 1.22098  | -0.26367 | 0.02554  | 4.172    | -0.98236 |
| ts3 | 0.06935  | -0.26367 | 1.31203  | -0.25088 | -5.505   | -0.08785 |
| ts4 | 0.03000  | 0.02554  | -0.25088 | 0.29453  | -3.663   | -0.28646 |
| ts5 | -4.19240 | 4.17164  | -5.50489 | -3.66327 | 4561.988 | -9.89003 |
| ts6 | 0.31250  | -0.98236 | -0.08785 | -0.28646 | -9.890   | 16.50391 |

```
Correlation matrix of residuals:
```

|     | ts1     | ts2     | ts3      | ts4      | ts5      | ts6      |
|-----|---------|---------|----------|----------|----------|----------|
| ts1 | 1.0000  | 0.2408  | 0.16575  | 0.15135  | -0.16993 | 0.21059  |
| ts2 | 0.2408  | 1.0000  | -0.20832 | 0.04260  | 0.05590  | -0.21884 |
| ts3 | 0.1658  | -0.2083 | 1.00000  | -0.40359 | -0.07115 | -0.01888 |
| ts4 | 0.1514  | 0.0426  | -0.40359 | 1.00000  | -0.09994 | -0.12993 |
| ts5 | -0.1699 | 0.0559  | -0.07115 | -0.09994 | 1.00000  | -0.03604 |
| ts6 | 0.2106  | -0.2188 | -0.01888 | -0.12993 | -0.03604 | 1.00000  |

```
> AIC <- AIC(var_model)
> > BIC <- BIC(var_model)
Error: unexpected '>' in ">"
> > log_likelihood <- logLik(var_model)
Error: unexpected '>' in ">"
> > num_parameters <- length(coef(var_model))
Error: unexpected '>' in ">"
> > HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
Error: unexpected '>' in ">"
> > cat("AIC:", AIC, "\n") BIC <- BIC(var_model)
Error: unexpected '>' in ">"
> log_likelihood <- logLik(var_model)
> num_parameters <- length(coef(var_model))
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> cat("AIC:", AIC, "\n")
AIC: 2657.144
> BIC <- BIC(var_model)
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 1.218561 3.226323 2.612527 2.221969 115.7346 9.460426
> cat("BIC:", BIC, "\n")
BIC: 2957.503
> cat("HQC:", HQC, "\n")
HQC: 2451.413
> cat("MAE:", MAE, "\n")
MAE: 1.075512 2.474723 1.908565 1.494408 86.37605 6.855286
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 1.291972 3.484975 4.335526 2.264448 105.2608 9.354743
> cat("MAE:", MAE, "\n")
MAE: 1.132891 2.464543 3.474136 1.427417 89.69872 6.875458
> plot(stability(var_model))
```

```
> var_model <- VAR(train_set, p=5)
> summary(var_model)
```

# VAR Estimation Results:

```
=====
```

```
Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6
```

```
Deterministic variables: const
```

```
Sample size: 101
```

```
Log Likelihood: -1141.051
```

```
Roots of the characteristic polynomial:
```

```
0.9732 0.9732 0.9224 0.9224 0.8895 0.8895 0.8344 0.8344 0.8271 0.8271 0.8218 0.8218 0.8119 0.8119
0.8058 0.7857 0.7857 0.7845 0.7845 0.7719 0.7719 0.7499 0.6004 0.6004 0.5451 0.5451 0.527 0.527
0.1885 0.1885
```

```
Call:
```

```
VAR(y = train_set, p = 5)
```

# Estimation results for equation ts1:

```
=====
```

```
ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |    |
|--------|------------|------------|---------|----------|----|
| ts1.l1 | 0.4453813  | 0.1361192  | 3.272   | 0.00166  | ** |
| ts2.l1 | -0.0380034 | 0.0491104  | -0.774  | 0.44163  |    |
| ts3.l1 | 0.0682744  | 0.0457614  | 1.492   | 0.14020  |    |
| ts4.l1 | 0.0157340  | 0.2415402  | 0.065   | 0.94825  |    |
| ts5.l1 | 0.0014147  | 0.0006729  | 2.102   | 0.03911  | *  |
| ts6.l1 | 0.0052705  | 0.0119904  | 0.440   | 0.66161  |    |
| ts1.l2 | -0.1332913 | 0.1567414  | -0.850  | 0.39801  |    |
| ts2.l2 | -0.0368791 | 0.0442508  | -0.833  | 0.40745  |    |
| ts3.l2 | 0.0029547  | 0.0537855  | 0.055   | 0.95635  |    |
| ts4.l2 | -0.3339464 | 0.2444370  | -1.366  | 0.17625  |    |
| ts5.l2 | 0.0011973  | 0.0008879  | 1.348   | 0.18186  |    |
| ts6.l2 | -0.0039795 | 0.0121436  | -0.328  | 0.74411  |    |
| ts1.l3 | 0.0513737  | 0.1587735  | 0.324   | 0.74723  |    |
| ts2.l3 | -0.0789673 | 0.0468977  | -1.684  | 0.09667  | .  |
| ts3.l3 | -0.0234467 | 0.0581788  | -0.403  | 0.68817  |    |
| ts4.l3 | 0.1067969  | 0.2467255  | 0.433   | 0.66645  |    |
| ts5.l3 | 0.0010162  | 0.0010083  | 1.008   | 0.31705  |    |
| ts6.l3 | -0.0170164 | 0.0117983  | -1.442  | 0.15368  |    |
| ts1.l4 | 0.3100195  | 0.1619140  | 1.915   | 0.05962  | .  |
| ts2.l4 | -0.0491538 | 0.0481931  | -1.020  | 0.31127  |    |
| ts3.l4 | -0.0480214 | 0.0546269  | -0.879  | 0.38237  |    |
| ts4.l4 | -0.0158223 | 0.2468636  | -0.064  | 0.94908  |    |
| ts5.l4 | 0.0007834  | 0.0009455  | 0.829   | 0.41017  |    |
| ts6.l4 | -0.0109975 | 0.0116037  | -0.948  | 0.34651  |    |
| ts1.l5 | -0.2314414 | 0.1614064  | -1.434  | 0.15605  |    |
| ts2.l5 | 0.0123697  | 0.0457775  | 0.270   | 0.78779  |    |
| ts3.l5 | -0.0031569 | 0.0533868  | -0.059  | 0.95302  |    |
| ts4.l5 | -0.2457563 | 0.2054571  | -1.196  | 0.23568  |    |
| ts5.l5 | 0.0006726  | 0.0007566  | 0.889   | 0.37703  |    |
| ts6.l5 | -0.0051031 | 0.0112010  | -0.456  | 0.65009  |    |
| const  | 0.1512376  | 0.1137010  | 1.330   | 0.18779  |    |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

```
Residual standard error: 0.3713 on 70 degrees of freedom
Multiple R-Squared: 0.4832, Adjusted R-squared: 0.2617
F-statistic: 2.181 on 30 and 70 DF, p-value: 0.003898
```

# Estimation results for equation ts2:

```
=====
```

```
ts2 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.11 | 5.316e-01  | 3.847e-01  | 1.382   | 0.171467 |     |
| ts2.11 | -1.094e-01 | 1.388e-01  | -0.788  | 0.433414 |     |
| ts3.11 | 3.660e-01  | 1.293e-01  | 2.830   | 0.006076 | **  |
| ts4.11 | 5.609e-01  | 6.827e-01  | 0.822   | 0.414123 |     |
| ts5.11 | 2.642e-07  | 1.902e-03  | 0.000   | 0.999890 |     |
| ts6.11 | -6.923e-02 | 3.389e-02  | -2.043  | 0.044855 | *   |
| ts1.12 | -1.230e+00 | 4.430e-01  | -2.775  | 0.007065 | **  |
| ts2.12 | -6.810e-02 | 1.251e-01  | -0.544  | 0.587851 |     |
| ts3.12 | -4.596e-03 | 1.520e-01  | -0.030  | 0.975970 |     |
| ts4.12 | 1.147e-02  | 6.909e-01  | 0.017   | 0.986803 |     |
| ts5.12 | -1.627e-03 | 2.510e-03  | -0.648  | 0.519018 |     |
| ts6.12 | 1.957e-02  | 3.432e-02  | 0.570   | 0.570496 |     |
| ts1.13 | 2.529e-01  | 4.488e-01  | 0.564   | 0.574884 |     |
| ts2.13 | 1.107e-01  | 1.326e-01  | 0.835   | 0.406427 |     |
| ts3.13 | 1.368e-01  | 1.644e-01  | 0.832   | 0.408422 |     |
| ts4.13 | 1.019e+00  | 6.974e-01  | 1.461   | 0.148555 |     |
| ts5.13 | 6.335e-04  | 2.850e-03  | 0.222   | 0.824753 |     |
| ts6.13 | -2.734e-02 | 3.335e-02  | -0.820  | 0.415133 |     |
| ts1.14 | 1.536e+00  | 4.577e-01  | 3.356   | 0.001280 | **  |
| ts2.14 | -1.869e-01 | 1.362e-01  | -1.372  | 0.174497 |     |
| ts3.14 | -1.513e-01 | 1.544e-01  | -0.980  | 0.330375 |     |
| ts4.14 | -6.027e-01 | 6.978e-01  | -0.864  | 0.390632 |     |
| ts5.14 | -7.637e-05 | 2.672e-03  | -0.029  | 0.977284 |     |
| ts6.14 | 1.674e-03  | 3.280e-02  | 0.051   | 0.959439 |     |
| ts1.15 | -2.683e-01 | 4.562e-01  | -0.588  | 0.558431 |     |
| ts2.15 | 9.903e-02  | 1.294e-01  | 0.765   | 0.446611 |     |
| ts3.15 | 9.691e-02  | 1.509e-01  | 0.642   | 0.522849 |     |
| ts4.15 | -8.534e-03 | 5.807e-01  | -0.015  | 0.988317 |     |
| ts5.15 | 3.435e-05  | 2.139e-03  | 0.016   | 0.987230 |     |
| ts6.15 | 1.362e-02  | 3.166e-02  | 0.430   | 0.668476 |     |
| const  | 1.104e+00  | 3.214e-01  | 3.435   | 0.000999 | *** |

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.049 on 70 degrees of freedom  
Multiple R-Squared: 0.5342, Adjusted R-squared: 0.3346  
F-statistic: 2.676 on 30 and 70 DF, p-value: 0.0003752

Estimation results for equation ts3:

=====

$$ts3 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + ts5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 + ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + const$$

|        | Estimate  | Std. Error | t value | Pr(> t ) |    |
|--------|-----------|------------|---------|----------|----|
| ts1.11 | 0.544368  | 0.429343   | 1.268   | 0.20903  |    |
| ts2.11 | 0.217964  | 0.154902   | 1.407   | 0.16382  |    |
| ts3.11 | 0.455728  | 0.144339   | 3.157   | 0.00235  | ** |
| ts4.11 | 0.082845  | 0.761858   | 0.109   | 0.91372  |    |
| ts5.11 | -0.004007 | 0.002122   | -1.888  | 0.06319  | .  |
| ts6.11 | 0.008893  | 0.037820   | 0.235   | 0.81479  |    |
| ts1.12 | -0.063108 | 0.494388   | -0.128  | 0.89879  |    |
| ts2.12 | -0.160314 | 0.139574   | -1.149  | 0.25463  |    |
| ts3.12 | 0.155537  | 0.169649   | 0.917   | 0.36239  |    |
| ts4.12 | 1.050579  | 0.770995   | 1.363   | 0.17737  |    |
| ts5.12 | -0.003635 | 0.002801   | -1.298  | 0.19862  |    |
| ts6.12 | 0.019265  | 0.038303   | 0.503   | 0.61656  |    |
| ts1.13 | 1.326602  | 0.500798   | 2.649   | 0.00997  | ** |
| ts2.13 | -0.395076 | 0.147923   | -2.671  | 0.00940  | ** |
| ts3.13 | 0.104963  | 0.183505   | 0.572   | 0.56916  |    |
| ts4.13 | 0.655727  | 0.778213   | 0.843   | 0.40232  |    |
| ts5.13 | -0.002631 | 0.003180   | -0.827  | 0.41084  |    |
| ts6.13 | -0.030172 | 0.037214   | -0.811  | 0.42024  |    |
| ts1.14 | -0.690518 | 0.510703   | -1.352  | 0.18070  |    |
| ts2.14 | 0.024195  | 0.152009   | 0.159   | 0.87399  |    |
| ts3.14 | -0.018711 | 0.172302   | -0.109  | 0.91384  |    |
| ts4.14 | -0.539951 | 0.778649   | -0.693  | 0.49032  |    |

```
ts5.14 -0.002496    0.002982   -0.837    0.40541
ts6.14  0.012291    0.036600    0.336    0.73801
ts1.15 -0.498984    0.509102   -0.980    0.33040
ts2.15 -0.136967    0.144390   -0.949    0.34609
ts3.15  0.060796    0.168391    0.361    0.71916
ts4.15 -0.247074    0.648046   -0.381    0.70416
ts5.15 -0.001619    0.002386   -0.678    0.49985
ts6.15 -0.032062    0.035330   -0.908    0.36725
const   0.538390    0.358632    1.501    0.13779
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 1.171 on 70 degrees of freedom
Multiple R-Squared: 0.5767,    Adjusted R-squared: 0.3952
F-statistic: 3.178 on 30 and 70 DF,  p-value: 3.603e-05
```

```
Estimation results for equation ts4:
```

```
=====
```

```
ts4 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.11 | -0.5683068 | 0.1887627  | -3.011  | 0.003623 | **  |
| ts2.11 | -0.0808045 | 0.0681036  | -1.186  | 0.239439 |     |
| ts3.11 | -0.2305508 | 0.0634594  | -3.633  | 0.000530 | *** |
| ts4.11 | 0.4233215  | 0.3349549  | 1.264   | 0.210488 |     |
| ts5.11 | 0.0036420  | 0.0009331  | 3.903   | 0.000216 | *** |
| ts6.11 | 0.0027864  | 0.0166277  | 0.168   | 0.867399 |     |
| ts1.12 | 0.1538198  | 0.2173605  | 0.708   | 0.481499 |     |
| ts2.12 | 0.1077958  | 0.0613646  | 1.757   | 0.083352 | .   |
| ts3.12 | 0.2160283  | 0.0745869  | 2.896   | 0.005034 | **  |
| ts4.12 | 0.3630048  | 0.3389720  | 1.071   | 0.287893 |     |
| ts5.12 | 0.0047424  | 0.0012313  | 3.851   | 0.000257 | *** |
| ts6.12 | 0.0038560  | 0.0168400  | 0.229   | 0.819554 |     |
| ts1.13 | -0.3905309 | 0.2201785  | -1.774  | 0.080462 | .   |
| ts2.13 | -0.0096661 | 0.0650352  | -0.149  | 0.882274 |     |
| ts3.13 | -0.0082082 | 0.0806791  | -0.102  | 0.919255 |     |
| ts4.13 | -0.0184566 | 0.3421455  | -0.054  | 0.957134 |     |
| ts5.13 | 0.0032093  | 0.0013983  | 2.295   | 0.024729 | *   |
| ts6.13 | 0.0206879  | 0.0163612  | 1.264   | 0.210262 |     |
| ts1.14 | 0.4944273  | 0.2245335  | 2.202   | 0.030961 | *   |
| ts2.14 | -0.1098459 | 0.0668316  | -1.644  | 0.104739 |     |
| ts3.14 | 0.0083304  | 0.0757536  | 0.110   | 0.912750 |     |
| ts4.14 | -0.3039160 | 0.3423371  | -0.888  | 0.377706 |     |
| ts5.14 | 0.0027907  | 0.0013112  | 2.128   | 0.036825 | *   |
| ts6.14 | -0.0293694 | 0.0160914  | -1.825  | 0.072242 | .   |
| ts1.15 | -0.0443027 | 0.2238296  | -0.198  | 0.843673 |     |
| ts2.15 | 0.0050439  | 0.0634817  | 0.079   | 0.936898 |     |
| ts3.15 | -0.1581064 | 0.0740339  | -2.136  | 0.036213 | *   |
| ts4.15 | -0.3537797 | 0.2849168  | -1.242  | 0.218494 |     |
| ts5.15 | 0.0019676  | 0.0010492  | 1.875   | 0.064913 | .   |
| ts6.15 | -0.0015406 | 0.0155330  | -0.099  | 0.921275 |     |
| const  | 0.1471301  | 0.1576744  | 0.933   | 0.353963 |     |

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.5149 on 70 degrees of freedom
Multiple R-Squared: 0.652,    Adjusted R-squared: 0.5029
F-statistic: 4.372 on 30 and 70 DF,  p-value: 1.917e-07
```

```
Estimation results for equation ts5:
```

```
=====
```

```
ts5 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + const
```

|        | Estimate | Std. Error | t value | Pr(> t )     |
|--------|----------|------------|---------|--------------|
| ts1.11 | 20.3971  | 25.4853    | 0.800   | 0.42622      |
| ts2.11 | 5.3050   | 9.1948     | 0.577   | 0.56582      |
| ts3.11 | -2.4480  | 8.5678     | -0.286  | 0.77594      |
| ts4.11 | -61.0758 | 45.2230    | -1.351  | 0.18119      |
| ts5.11 | -0.8298  | 0.1260     | -6.587  | 7.01e-09 *** |
| ts6.11 | -0.1976  | 2.2449     | -0.088  | 0.93011      |
| ts1.12 | -22.1735 | 29.3463    | -0.756  | 0.45244      |
| ts2.12 | 12.5068  | 8.2850     | 1.510   | 0.13565      |
| ts3.12 | -9.4899  | 10.0701    | -0.942  | 0.34924      |
| ts4.12 | -49.0788 | 45.7654    | -1.072  | 0.28722      |
| ts5.12 | -0.5501  | 0.1662     | -3.309  | 0.00148 **   |
| ts6.12 | 1.4180   | 2.2736     | 0.624   | 0.53486      |
| ts1.13 | -43.9311 | 29.7268    | -1.478  | 0.14394      |
| ts2.13 | 12.3120  | 8.7805     | 1.402   | 0.16528      |
| ts3.13 | -6.2053  | 10.8927    | -0.570  | 0.57072      |
| ts4.13 | -54.0150 | 46.1938    | -1.169  | 0.24624      |
| ts5.13 | -0.1430  | 0.1888     | -0.757  | 0.45135      |
| ts6.13 | 2.7821   | 2.2090     | 1.259   | 0.21205      |
| ts1.14 | -4.9492  | 30.3148    | -0.163  | 0.87078      |
| ts2.14 | -10.1227 | 9.0231     | -1.122  | 0.26575      |
| ts3.14 | -15.4202 | 10.2277    | -1.508  | 0.13613      |
| ts4.14 | 45.7672  | 46.2197    | 0.990   | 0.32548      |
| ts5.14 | 0.1176   | 0.1770     | 0.664   | 0.50860      |
| ts6.14 | -1.2108  | 2.1725     | -0.557  | 0.57909      |
| ts1.15 | 14.8657  | 30.2198    | 0.492   | 0.62431      |
| ts2.15 | 1.1024   | 8.5708     | 0.129   | 0.89803      |
| ts3.15 | 12.9867  | 9.9955     | 1.299   | 0.19812      |
| ts4.15 | 63.4106  | 38.4673    | 1.648   | 0.10375      |
| ts5.15 | 0.1521   | 0.1417     | 1.074   | 0.28653      |
| ts6.15 | -0.3776  | 2.0971     | -0.180  | 0.85763      |
| const  | -14.7144 | 21.2880    | -0.691  | 0.49172      |

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 69.52 on 70 degrees of freedom  
Multiple R-Squared: 0.5516, Adjusted R-squared: 0.3595  
F-statistic: 2.871 on 30 and 70 DF, p-value: 0.0001503

Estimation results for equation ts6:

=====

$$ts6 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + ts5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 + ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + const$$

|        | Estimate  | Std. Error | t value | Pr(> t ) |
|--------|-----------|------------|---------|----------|
| ts1.11 | 0.136342  | 1.511756   | 0.090   | 0.9284   |
| ts2.11 | 0.080767  | 0.545426   | 0.148   | 0.8827   |
| ts3.11 | -0.161139 | 0.508231   | -0.317  | 0.7521   |
| ts4.11 | 4.205649  | 2.682574   | 1.568   | 0.1214   |
| ts5.11 | -0.016278 | 0.007473   | -2.178  | 0.0328 * |
| ts6.11 | 0.288624  | 0.133167   | 2.167   | 0.0336 * |
| ts1.12 | 0.134179  | 1.740789   | 0.077   | 0.9388   |
| ts2.12 | 1.198790  | 0.491454   | 2.439   | 0.0173 * |
| ts3.12 | 0.911445  | 0.597349   | 1.526   | 0.1316   |
| ts4.12 | -2.545942 | 2.714746   | -0.938  | 0.3516   |
| ts5.12 | -0.015830 | 0.009862   | -1.605  | 0.1130   |
| ts6.12 | -0.029888 | 0.134868   | -0.222  | 0.8253   |
| ts1.13 | -1.137283 | 1.763358   | -0.645  | 0.5211   |
| ts2.13 | 0.410124  | 0.520851   | 0.787   | 0.4337   |
| ts3.13 | -0.097730 | 0.646140   | -0.151  | 0.8802   |
| ts4.13 | -2.379067 | 2.740162   | -0.868  | 0.3882   |
| ts5.13 | -0.017958 | 0.011199   | -1.604  | 0.1133   |
| ts6.13 | 0.179671  | 0.131033   | 1.371   | 0.1747   |
| ts1.14 | 0.186618  | 1.798235   | 0.104   | 0.9176   |
| ts2.14 | 0.136653  | 0.535238   | 0.255   | 0.7992   |
| ts3.14 | -0.621140 | 0.606692   | -1.024  | 0.3094   |



```

ts4.14 -0.435747    2.741697   -0.159    0.8742
ts5.14 -0.014278    0.010501   -1.360    0.1783
ts6.14  0.001352    0.128872    0.010    0.9917
ts1.15 -0.068182    1.792598   -0.038    0.9698
ts2.15 -0.482803    0.508410   -0.950    0.3456
ts3.15 -0.605014    0.592920   -1.020    0.3111
ts4.15 -2.311830    2.281831   -1.013    0.3145
ts5.15 -0.001145    0.008403   -0.136    0.8920
ts6.15 -0.050608    0.124400   -0.407    0.6854
const  -1.525881    1.262777   -1.208    0.2310
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 4.124 on 70 degrees of freedom
Multiple R-Squared: 0.367,    Adjusted R-squared: 0.09566
F-statistic: 1.353 on 30 and 70 DF,  p-value: 0.1508

```

```

Covariance matrix of residuals:
      ts1      ts2      ts3      ts4      ts5      ts6
ts1  0.13787  0.07484  0.07923  0.01923  -5.184   0.2947
ts2  0.07484  1.10145 -0.19022 -0.02574   6.683  -1.1368
ts3  0.07923 -0.19022  1.37160 -0.21884  -5.404  -0.3770
ts4  0.01923 -0.02574 -0.21884  0.26513  -3.823  -0.2912
ts5 -5.18450  6.68272 -5.40391 -3.82271 4832.815 -17.4674
ts6  0.29473 -1.13678 -0.37705 -0.29123  -17.467  17.0053

```

```

Correlation matrix of residuals:
      ts1      ts2      ts3      ts4      ts5      ts6
ts1  1.0000  0.19206  0.18220  0.10060 -0.20085  0.19249
ts2  0.1921  1.00000 -0.15476 -0.04763  0.09159 -0.26266
ts3  0.1822 -0.15476  1.00000 -0.36290 -0.06637 -0.07807
ts4  0.1006 -0.04763 -0.36290  1.00000 -0.10679 -0.13716
ts5 -0.2009  0.09159 -0.06637 -0.10679  1.00000 -0.06093
ts6  0.1925 -0.26266 -0.07807 -0.13716 -0.06093  1.00000

```

```

> AIC <- AIC(var_model)
> BIC <- BIC(var_model)
> log_likelihood <- logLik(var_model)
>
> num_parameters <- length(coef(var_model))
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> forecasts <- predict(var_model, n.ahead=12)
>
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 1.775888 6.981608 11.98211 3.997824 295.6232 16.81454
> cat("MAE:", MAE, "\n")
MAE: 1.624689 5.30327 10.40162 3.508354 251.81 13.81874
> cat("AIC:", AIC, "\n")
AIC: 2654.103
> cat("BIC:", BIC, "\n")
BIC: 3140.515
> cat("HQC:", HQC, "\n")
HQC: 2304.372
> plot(stability(var_model))
> var_model <- VAR(train_set, p=7)
> summary(var_model)

```

VAR Estimation Results:

```

=====
Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6
Deterministic variables: const
Sample size: 99

```

Log Likelihood: -1062.158

Roots of the characteristic polynomial:

1.075 1.075 0.9802 0.9802 0.9381 0.9381 0.931 0.931 0.9252 0.9252 0.891 0.891 0.889 0.889 0.8854  
0.8854 0.8661 0.8661 0.8505 0.8505 0.8484 0.8484 0.8405 0.8405 0.8403 0.8403 0.8203 0.8203 0.8116  
0.8116 0.8096 0.8096 0.783 0.783 0.7584 0.7584 0.7119 0.7107 0.7107 0.5811 0.5811 0.547

Call:

VAR(y = train\_set, p = 7)

Estimation results for equation ts1:

=====

ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t  
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 + t  
s4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6  
+ ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + cons  
t

|        | Estimate   | Std. Error | t value | Pr(> t ) |
|--------|------------|------------|---------|----------|
| ts1.l1 | 0.3848253  | 0.1476293  | 2.607   | 0.0117 * |
| ts2.l1 | -0.0348605 | 0.0530620  | -0.657  | 0.5139   |
| ts3.l1 | 0.0949452  | 0.0522415  | 1.817   | 0.0745 . |
| ts4.l1 | 0.0680395  | 0.2705909  | 0.251   | 0.8024   |
| ts5.l1 | 0.0012233  | 0.0007171  | 1.706   | 0.0936 . |
| ts6.l1 | 0.0074730  | 0.0135192  | 0.553   | 0.5826   |
| ts1.l2 | -0.1864568 | 0.1691006  | -1.103  | 0.2749   |
| ts2.l2 | -0.0350430 | 0.0529415  | -0.662  | 0.5107   |
| ts3.l2 | -0.0168493 | 0.0589044  | -0.286  | 0.7759   |
| ts4.l2 | -0.4170275 | 0.2725528  | -1.530  | 0.1316   |
| ts5.l2 | 0.0014438  | 0.0009924  | 1.455   | 0.1513   |
| ts6.l2 | 0.0011537  | 0.0134362  | 0.086   | 0.9319   |
| ts1.l3 | 0.0316481  | 0.1753939  | 0.180   | 0.8575   |
| ts2.l3 | -0.0605202 | 0.0576893  | -1.049  | 0.2987   |
| ts3.l3 | -0.0299487 | 0.0657402  | -0.456  | 0.6505   |
| ts4.l3 | 0.0345111  | 0.2954466  | 0.117   | 0.9074   |
| ts5.l3 | 0.0013964  | 0.0011202  | 1.247   | 0.2178   |
| ts6.l3 | -0.0180730 | 0.0134210  | -1.347  | 0.1835   |
| ts1.l4 | 0.2046413  | 0.1896824  | 1.079   | 0.2853   |
| ts2.l4 | -0.0486607 | 0.0555011  | -0.877  | 0.3844   |
| ts3.l4 | -0.0540416 | 0.0665291  | -0.812  | 0.4201   |
| ts4.l4 | -0.0910159 | 0.2947235  | -0.309  | 0.7586   |
| ts5.l4 | 0.0018230  | 0.0011756  | 1.551   | 0.1266   |
| ts6.l4 | -0.0035980 | 0.0139187  | -0.259  | 0.7970   |
| ts1.l5 | -0.1504124 | 0.2045407  | -0.735  | 0.4652   |
| ts2.l5 | -0.0128393 | 0.0556621  | -0.231  | 0.8184   |
| ts3.l5 | 0.0172867  | 0.0663153  | 0.261   | 0.7953   |
| ts4.l5 | -0.1371478 | 0.2876660  | -0.477  | 0.6354   |
| ts5.l5 | 0.0018894  | 0.0011749  | 1.608   | 0.1134   |
| ts6.l5 | -0.0101641 | 0.0137818  | -0.737  | 0.4639   |
| ts1.l6 | 0.0411011  | 0.1992817  | 0.206   | 0.8373   |
| ts2.l6 | -0.0637801 | 0.0542128  | -1.176  | 0.2444   |
| ts3.l6 | -0.0299428 | 0.0652752  | -0.459  | 0.6482   |
| ts4.l6 | -0.2026193 | 0.2839365  | -0.714  | 0.4784   |
| ts5.l6 | 0.0013337  | 0.0011028  | 1.209   | 0.2316   |
| ts6.l6 | -0.0021965 | 0.0127005  | -0.173  | 0.8633   |
| ts1.l7 | -0.0712866 | 0.1838378  | -0.388  | 0.6997   |
| ts2.l7 | -0.0048269 | 0.0507397  | -0.095  | 0.9246   |
| ts3.l7 | -0.0205575 | 0.0614021  | -0.335  | 0.7390   |
| ts4.l7 | -0.0121909 | 0.2277988  | -0.054  | 0.9575   |
| ts5.l7 | -0.0004106 | 0.0008782  | -0.468  | 0.6419   |
| ts6.l7 | -0.0215926 | 0.0121508  | -1.777  | 0.0810 . |
| const  | 0.2221141  | 0.1491325  | 1.489   | 0.1420   |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3826 on 56 degrees of freedom

Multiple R-Squared: 0.56, Adjusted R-squared: 0.2301

F-statistic: 1.697 on 42 and 56 DF, p-value: 0.0322

## Estimation results for equation ts2:

=====

```
ts2 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
  ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
  + ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + cons
t
```

|        | Estimate   | Std. Error | t value | Pr(> t )   |
|--------|------------|------------|---------|------------|
| ts1.l1 | 0.2476765  | 0.4023550  | 0.616   | 0.54067    |
| ts2.l1 | -0.0921348 | 0.1446174  | -0.637  | 0.52666    |
| ts3.l1 | 0.4028071  | 0.1423811  | 2.829   | 0.00647 ** |
| ts4.l1 | 0.9175761  | 0.7374797  | 1.244   | 0.21861    |
| ts5.l1 | -0.0002914 | 0.0019545  | -0.149  | 0.88203    |
| ts6.l1 | -0.0628527 | 0.0368457  | -1.706  | 0.09358 .  |
| ts1.l2 | -1.1573504 | 0.4608737  | -2.511  | 0.01494 *  |
| ts2.l2 | -0.0462905 | 0.1442889  | -0.321  | 0.74954    |
| ts3.l2 | -0.0036558 | 0.1605405  | -0.023  | 0.98191    |
| ts4.l2 | 0.0462628  | 0.7428268  | 0.062   | 0.95056    |
| ts5.l2 | -0.0008501 | 0.0027048  | -0.314  | 0.75446    |
| ts6.l2 | 0.0111362  | 0.0366195  | 0.304   | 0.76217    |
| ts1.l3 | 0.1309454  | 0.4780259  | 0.274   | 0.78515    |
| ts2.l3 | 0.0058777  | 0.1572287  | 0.037   | 0.97031    |
| ts3.l3 | 0.1528053  | 0.1791710  | 0.853   | 0.39738    |
| ts4.l3 | 0.7641783  | 0.8052225  | 0.949   | 0.34668    |
| ts5.l3 | 0.0013004  | 0.0030531  | 0.426   | 0.67179    |
| ts6.l3 | -0.0259838 | 0.0365782  | -0.710  | 0.48043    |
| ts1.l4 | 1.7570321  | 0.5169684  | 3.399   | 0.00125 ** |
| ts2.l4 | -0.2352392 | 0.1512650  | -1.555  | 0.12555    |
| ts3.l4 | -0.1324370 | 0.1813212  | -0.730  | 0.46819    |
| ts4.l4 | -0.7680382 | 0.8032518  | -0.956  | 0.34310    |
| ts5.l4 | 0.0011243  | 0.0032041  | 0.351   | 0.72697    |
| ts6.l4 | -0.0340352 | 0.0379345  | -0.897  | 0.37345    |
| ts1.l5 | -0.5102096 | 0.5574636  | -0.915  | 0.36399    |
| ts2.l5 | 0.0400303  | 0.1517039  | 0.264   | 0.79285    |
| ts3.l5 | 0.0867905  | 0.1807383  | 0.480   | 0.63296    |
| ts4.l5 | 0.4631194  | 0.7840168  | 0.591   | 0.55710    |
| ts5.l5 | 0.0011554  | 0.0032021  | 0.361   | 0.71959    |
| ts6.l5 | 0.0347688  | 0.0375616  | 0.926   | 0.35860    |
| ts1.l6 | 0.0393331  | 0.5431307  | 0.072   | 0.94253    |
| ts2.l6 | 0.1736695  | 0.1477538  | 1.175   | 0.24481    |
| ts3.l6 | 0.1423562  | 0.1779036  | 0.800   | 0.42698    |
| ts4.l6 | -0.3686846 | 0.7738524  | -0.476  | 0.63562    |
| ts5.l6 | 0.0023504  | 0.0030057  | 0.782   | 0.43752    |
| ts6.l6 | -0.0220268 | 0.0346145  | -0.636  | 0.52714    |
| ts1.l7 | 0.1811811  | 0.5010392  | 0.362   | 0.71900    |
| ts2.l7 | -0.2004607 | 0.1382880  | -1.450  | 0.15275    |
| ts3.l7 | -0.3275716 | 0.1673477  | -1.957  | 0.05529 .  |
| ts4.l7 | -0.8741975 | 0.6208524  | -1.408  | 0.16464    |
| ts5.l7 | 0.0009072  | 0.0023934  | 0.379   | 0.70610    |
| ts6.l7 | -0.0350228 | 0.0331162  | -1.058  | 0.29479    |
| const  | 1.3306523  | 0.4064519  | 3.274   | 0.00182 ** |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.043 on 56 degrees of freedom

Multiple R-Squared: 0.6318, Adjusted R-squared: 0.3556

F-statistic: 2.288 on 42 and 56 DF, p-value: 0.001975

## Estimation results for equation ts3:

=====

```
ts3 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + ts1.l2 + ts2.l2 + ts3.l2 + ts4.l2 + t
s5.l2 + ts6.l2 + ts1.l3 + ts2.l3 + ts3.l3 + ts4.l3 + ts5.l3 + ts6.l3 + ts1.l4 + ts2.l4 + ts3.l4 +
  ts4.l4 + ts5.l4 + ts6.l4 + ts1.l5 + ts2.l5 + ts3.l5 + ts4.l5 + ts5.l5 + ts6.l5 + ts1.l6 + ts2.l6
  + ts3.l6 + ts4.l6 + ts5.l6 + ts6.l6 + ts1.l7 + ts2.l7 + ts3.l7 + ts4.l7 + ts5.l7 + ts6.l7 + cons
t
```

Estimate Std. Error t value Pr(&gt;|t|)

```

ts1.11  0.6856479  0.4536382  1.511  0.13630
ts2.11  0.2411581  0.1630500  1.479  0.14473
ts3.11  0.4860782  0.1605287  3.028  0.00372 **
ts4.11 -0.0366387  0.8314771 -0.044  0.96501
ts5.11 -0.0046096  0.0022036 -2.092  0.04100 *
ts6.11  0.0158982  0.0415420  0.383  0.70339
ts1.12 -0.1147025  0.5196156 -0.221  0.82609
ts2.12 -0.2766573  0.1626797 -1.701  0.09456 .
ts3.12  0.1677991  0.1810026  0.927  0.35788
ts4.12  0.6147822  0.8375058  0.734  0.46597
ts5.12 -0.0032579  0.0030495 -1.068  0.28996
ts6.12  0.0292931  0.0412870  0.710  0.48096
ts1.13  1.4724184  0.5389539  2.732  0.00841 **
ts2.13 -0.4972126  0.1772688 -2.805  0.00691 **
ts3.13 -0.0249381  0.2020078 -0.123  0.90219
ts4.13  0.7329376  0.9078543  0.807  0.42289
ts5.13 -0.0008968  0.0034422 -0.261  0.79541
ts6.13 -0.0659077  0.0412404 -1.598  0.11564
ts1.14 -0.9954749  0.5828600 -1.708  0.09319 .
ts2.14  0.0897936  0.1705449  0.527  0.60061
ts3.14 -0.0249459  0.2044320 -0.122  0.90332
ts4.14 -0.7560613  0.9056324 -0.835  0.40735
ts5.14  0.0002684  0.0036124  0.074  0.94104
ts6.14  0.0326726  0.0427696  0.764  0.44812
ts1.15 -0.9935098  0.6285167 -1.581  0.11957
ts2.15  0.0311471  0.1710397  0.182  0.85616
ts3.15  0.1829046  0.2037748  0.898  0.37325
ts4.15  0.5033933  0.8839457  0.569  0.57130
ts5.15  0.0010429  0.0036102  0.289  0.77375
ts6.15 -0.0339157  0.0423491 -0.801  0.42660
ts1.16  0.9955462  0.6123569  1.626  0.10962
ts2.16 -0.1098427  0.1665862 -0.659  0.51236
ts3.16  0.0060837  0.2005788  0.030  0.97591
ts4.16  0.2124151  0.8724858  0.243  0.80854
ts5.16  0.0032134  0.0033887  0.948  0.34707
ts6.16  0.0452190  0.0390264  1.159  0.25150
ts1.17  0.2392391  0.5649005  0.424  0.67355
ts2.17  0.1207636  0.1559139  0.775  0.44186
ts3.17 -0.0831872  0.1886775 -0.441  0.66099
ts4.17  0.1501994  0.6999848  0.215  0.83088
ts5.17 -0.0006483  0.0026985 -0.240  0.81102
ts6.17  0.0148425  0.0373371  0.398  0.69249
const   0.5551316  0.4582573  1.211  0.23083
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 1.176 on 56 degrees of freedom
Multiple R-Squared: 0.6578, Adjusted R-squared: 0.4012
F-statistic: 2.563 on 42 and 56 DF, p-value: 0.0005351

```

Estimation results for equation ts4:

```

=====
ts4 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
  ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
  + ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + cons
t

```

```

      Estimate Std. Error t value Pr(>|t|)
ts1.11 -0.5419428  0.1944572  -2.787 0.007251 **
ts2.11 -0.1099678  0.0698932  -1.573 0.121267
ts3.11 -0.2877533  0.0688124  -4.182 0.000103 ***
ts4.11  0.1773038  0.3564221   0.497 0.620816
ts5.11  0.0035126  0.0009446   3.719 0.000465 ***
ts6.11 -0.0027489  0.0178074  -0.154 0.877873
ts1.12  0.1187303  0.2227391   0.533 0.596110
ts2.12  0.1914040  0.0697345   2.745 0.008123 **
ts3.12  0.2604782  0.0775888   3.357 0.001421 **

```

```

ts4.12  0.5929259  0.3590063  1.652 0.104219
ts5.12  0.0037470  0.0013072  2.866 0.005840 **
ts6.12  0.0095586  0.0176981  0.540 0.591277
ts1.13 -0.3889656  0.2310287 -1.684 0.097821 .
ts2.13 -0.0095401  0.0759883 -0.126 0.900540
ts3.13  0.0252544  0.0865929  0.292 0.771636
ts4.13 -0.3519142  0.3891620 -0.904 0.369717
ts5.13  0.0023956  0.0014756  1.624 0.110093
ts6.13  0.0329661  0.0176781  1.865 0.067453 .
ts1.14  0.7178236  0.2498495  2.873 0.005734 **
ts2.14 -0.1759576  0.0731060 -2.407 0.019412 *
ts3.14 -0.1031408  0.0876321 -1.177 0.244184
ts4.14 -0.3884578  0.3882096 -1.001 0.321305
ts5.14  0.0020705  0.0015485  1.337 0.186602
ts6.14 -0.0403421  0.0183337 -2.200 0.031917 *
ts1.15  0.1359609  0.2694208  0.505 0.615791
ts2.15 -0.0354119  0.0733181 -0.483 0.630985
ts3.15 -0.2415022  0.0873504 -2.765 0.007699 **
ts4.15 -0.8138442  0.3789133 -2.148 0.036068 *
ts5.15  0.0015706  0.0015475  1.015 0.314506
ts6.15 -0.0174079  0.0181534 -0.959 0.341714
ts1.16 -0.6035860  0.2624937 -2.299 0.025232 *
ts2.16  0.0688295  0.0714090  0.964 0.339252
ts3.16  0.0047173  0.0859804  0.055 0.956442
ts4.16  0.9090348  0.3740009  2.431 0.018304 *
ts5.16 -0.0011877  0.0014526 -0.818 0.417039
ts6.16  0.0012890  0.0167291  0.077 0.938857
ts1.17  0.4129837  0.2421510  1.705 0.093647 .
ts2.17  0.0219237  0.0668343  0.328 0.744112
ts3.17  0.2082080  0.0808787  2.574 0.012715 *
ts4.17  0.4013407  0.3000564  1.338 0.186450
ts5.17 -0.0003837  0.0011567 -0.332 0.741323
ts6.17  0.0099132  0.0160050  0.619 0.538174
const  0.1064759  0.1964372  0.542 0.589944
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 0.504 on 56 degrees of freedom  
Multiple R-Squared: 0.7332, Adjusted R-squared: 0.533  
F-statistic: 3.663 on 42 and 56 DF, p-value: 3.841e-06

Estimation results for equation ts5:

```

=====
ts5 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
+ ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + cons
t

```

|        | Estimate  | Std. Error | t value | Pr(> t )     |
|--------|-----------|------------|---------|--------------|
| ts1.11 | 9.87952   | 27.52114   | 0.359   | 0.7210       |
| ts2.11 | 9.06943   | 9.89185    | 0.917   | 0.3631       |
| ts3.11 | 2.58995   | 9.73889    | 0.266   | 0.7913       |
| ts4.11 | -27.97215 | 50.44371   | -0.555  | 0.5814       |
| ts5.11 | -0.76833  | 0.13369    | -5.747  | 3.91e-07 *** |
| ts6.11 | 1.36429   | 2.52025    | 0.541   | 0.5904       |
| ts1.12 | -8.68218  | 31.52382   | -0.275  | 0.7840       |
| ts2.12 | 7.32642   | 9.86938    | 0.742   | 0.4610       |
| ts3.12 | -11.36367 | 10.98099   | -1.035  | 0.3052       |
| ts4.12 | -65.17827 | 50.80945   | -1.283  | 0.2048       |
| ts5.12 | -0.46337  | 0.18501    | -2.505  | 0.0152 *     |
| ts6.12 | 0.53185   | 2.50478    | 0.212   | 0.8326       |
| ts1.13 | -49.13533 | 32.69703   | -1.503  | 0.1385       |
| ts2.13 | 13.04727  | 10.75447   | 1.213   | 0.2301       |
| ts3.13 | -5.84349  | 12.25532   | -0.477  | 0.6354       |
| ts4.13 | -32.78424 | 55.07733   | -0.595  | 0.5541       |
| ts5.13 | -0.19081  | 0.20883    | -0.914  | 0.3648       |
| ts6.13 | 2.44589   | 2.50195    | 0.978   | 0.3325       |

```

ts1.14 -14.09548    35.36071   -0.399    0.6917
ts2.14 -10.58840    10.34655   -1.023    0.3105
ts3.14 -15.26826    12.40239   -1.231    0.2234
ts4.14  28.07429    54.94253    0.511    0.6114
ts5.14  0.12934     0.21916    0.590    0.5575
ts6.14 -1.31476     2.59473   -0.507    0.6144
ts1.15 -5.68241    38.13059   -0.149    0.8821
ts2.15  9.04701    10.37657    0.872    0.3870
ts3.15 16.71817    12.36253    1.352    0.1817
ts4.15 83.58404    53.62685    1.559    0.1247
ts5.15  0.16177     0.21902    0.739    0.4632
ts6.15  1.80007     2.56922    0.701    0.4864
ts1.16 12.70427    37.15021    0.342    0.7337
ts2.16  1.62882    10.10638    0.161    0.8725
ts3.16  4.13566    12.16863    0.340    0.7352
ts4.16 -71.32762    52.93161   -1.348    0.1832
ts5.16  0.09941     0.20559    0.484    0.6306
ts6.16  1.56258     2.36764    0.660    0.5120
ts1.17  0.86277    34.27115    0.025    0.9800
ts2.17 -13.25748     9.45892   -1.402    0.1666
ts3.17 -15.14504    11.44661   -1.323    0.1912
ts4.17 14.66747    42.46639    0.345    0.7311
ts5.17  0.24521     0.16371    1.498    0.1398
ts6.17 -3.31951     2.26515   -1.465    0.1484
const -9.81898     27.80136   -0.353    0.7253

```

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 71.33 on 56 degrees of freedom

Multiple R-Squared: 0.6223, Adjusted R-squared: 0.3391

F-statistic: 2.197 on 42 and 56 DF, p-value: 0.003044

Estimation results for equation ts6:

=====

```

ts6 = ts1.11 + ts2.11 + ts3.11 + ts4.11 + ts5.11 + ts6.11 + ts1.12 + ts2.12 + ts3.12 + ts4.12 + t
s5.12 + ts6.12 + ts1.13 + ts2.13 + ts3.13 + ts4.13 + ts5.13 + ts6.13 + ts1.14 + ts2.14 + ts3.14 +
ts4.14 + ts5.14 + ts6.14 + ts1.15 + ts2.15 + ts3.15 + ts4.15 + ts5.15 + ts6.15 + ts1.16 + ts2.16
+ ts3.16 + ts4.16 + ts5.16 + ts6.16 + ts1.17 + ts2.17 + ts3.17 + ts4.17 + ts5.17 + ts6.17 + cons
t

```

|        | Estimate  | Std. Error | t value | Pr(> t ) |
|--------|-----------|------------|---------|----------|
| ts1.11 | -0.829961 | 1.644587   | -0.505  | 0.6158   |
| ts2.11 | 0.252116  | 0.591110   | 0.427   | 0.6714   |
| ts3.11 | -0.080245 | 0.581969   | -0.138  | 0.8908   |
| ts4.11 | 4.146146  | 3.014377   | 1.375   | 0.1745   |
| ts5.11 | -0.014487 | 0.007989   | -1.813  | 0.0751 . |
| ts6.11 | 0.373363  | 0.150603   | 2.479   | 0.0162 * |
| ts1.12 | 0.919737  | 1.883777   | 0.488   | 0.6273   |
| ts2.12 | 1.133363  | 0.589767   | 1.922   | 0.0597 . |
| ts3.12 | 0.782728  | 0.656194   | 1.193   | 0.2380   |
| ts4.12 | -4.189147 | 3.036233   | -1.380  | 0.1732   |
| ts5.12 | -0.008217 | 0.011056   | -0.743  | 0.4604   |
| ts6.12 | 0.012787  | 0.149679   | 0.085   | 0.9322   |
| ts1.13 | -1.112409 | 1.953885   | -0.569  | 0.5714   |
| ts2.13 | 0.480150  | 0.642657   | 0.747   | 0.4581   |
| ts3.13 | -0.099066 | 0.732344   | -0.135  | 0.8929   |
| ts4.13 | -0.775915 | 3.291270   | -0.236  | 0.8145   |
| ts5.13 | -0.016810 | 0.012479   | -1.347  | 0.1834   |
| ts6.13 | 0.118844  | 0.149510   | 0.795   | 0.4300   |
| ts1.14 | -0.096891 | 2.113059   | -0.046  | 0.9636   |
| ts2.14 | -0.241477 | 0.618281   | -0.391  | 0.6976   |
| ts3.14 | -1.000040 | 0.741133   | -1.349  | 0.1827   |
| ts4.14 | 0.039856  | 3.283214   | 0.012   | 0.9904   |
| ts5.14 | -0.006279 | 0.013096   | -0.479  | 0.6335   |
| ts6.14 | -0.023358 | 0.155054   | -0.151  | 0.8808   |
| ts1.15 | 0.371867  | 2.278579   | 0.163   | 0.8709   |
| ts2.15 | -0.254466 | 0.620075   | -0.410  | 0.6831   |
| ts3.15 | -0.184856 | 0.738751   | -0.250  | 0.8033   |

```

ts4.15  0.051350    3.204593    0.016    0.9873
ts5.15  0.005924    0.013088    0.453    0.6526
ts6.15 -0.011148    0.153529   -0.073    0.9424
ts1.16 -1.819496    2.219994   -0.820    0.4159
ts2.16 -0.045361    0.603929   -0.075    0.9404
ts3.16  0.685269    0.727164    0.942    0.3500
ts4.16 -4.592078    3.163047   -1.452    0.1521
ts5.16  0.006934    0.012285    0.564    0.5747
ts6.16  0.140915    0.141483    0.996    0.3235
ts1.17  1.053940    2.047950    0.515    0.6088
ts2.17 -0.608825    0.565239   -1.077    0.2860
ts3.17 -0.526377    0.684018   -0.770    0.4448
ts4.17  1.738842    2.537675    0.685    0.4960
ts5.17  0.002046    0.009783    0.209    0.8351
ts6.17 -0.163626    0.135359   -1.209    0.2318
const  -0.938108    1.661333   -0.565    0.5746
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 4.262 on 56 degrees of freedom
Multiple R-Squared: 0.4529,    Adjusted R-squared: 0.04249
F-statistic: 1.104 on 42 and 56 DF,  p-value: 0.3616

```

Covariance matrix of residuals:

```

      ts1      ts2      ts3      ts4      ts5      ts6
ts1  0.14640  0.06260  0.08365  0.03256  -6.0721  0.2561
ts2  0.06260  1.08743 -0.14284 -0.01365  5.4561 -1.5730
ts3  0.08365 -0.14284  1.38230 -0.20386  -6.6302 -0.6541
ts4  0.03256 -0.01365 -0.20386  0.25400  -0.3859 -0.1916
ts5 -6.07206  5.45608 -6.63024 -0.38593 5087.6201 -52.9670
ts6  0.25614 -1.57303 -0.65415 -0.19157 -52.9670 18.1675

```

Correlation matrix of residuals:

```

      ts1      ts2      ts3      ts4      ts5      ts6
ts1  1.0000  0.15690  0.18594  0.16885 -0.22249  0.15706
ts2  0.1569  1.00000 -0.11650 -0.02597  0.07335 -0.35391
ts3  0.1859 -0.11650  1.00000 -0.34404 -0.07906 -0.13053
ts4  0.1688 -0.02597 -0.34404  1.00000 -0.01074 -0.08918
ts5 -0.2225  0.07335 -0.07906 -0.01074  1.00000 -0.17422
ts6  0.1571 -0.35391 -0.13053 -0.08918 -0.17422  1.00000

```

```

> AIC <- AIC(var_model)
> BIC <- BIC(var_model)
> log_likelihood <- logLik(var_model)
> num_parameters <- length(coef(var_model))
>
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 1.571786 8.003734 9.532438 4.896223 280.9148 20.49107
> cat("MAE:", MAE, "\n")
MAE: 1.299165 6.451585 7.913661 4.26102 250.31 16.44372
> cat("AIC:", AIC, "\n")
AIC: 2640.316
> cat("BIC:", BIC, "\n")
BIC: 3309.857
> cat("HQC:", HQC, "\n")
HQC: 2146.586
> plot(stability(var_model))
> var_model <- VAR(train_set, p=1)
> summary(var_model)

```

## VAR Estimation Results:

=====

Endogenous variables: ts1, ts2, ts3, ts4, ts5, ts6

Deterministic variables: const

Sample size: 105

Log Likelihood: -1306.379

Roots of the characteristic polynomial:

0.6814 0.5379 0.3565 0.342 0.342 0.1817

Call:

VAR(y = train\_set, p = 1)

## Estimation results for equation ts1:

=====

ts1 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + const

|        | Estimate   | Std. Error | t value | Pr(> t ) |     |
|--------|------------|------------|---------|----------|-----|
| ts1.l1 | 0.5263648  | 0.0983910  | 5.350   | 5.78e-07 | *** |
| ts2.l1 | -0.0693572 | 0.0328392  | -2.112  | 0.0372   | *   |
| ts3.l1 | 0.0620016  | 0.0354376  | 1.750   | 0.0833   | .   |
| ts4.l1 | 0.0418705  | 0.1573654  | 0.266   | 0.7907   |     |
| ts5.l1 | 0.0006097  | 0.0004745  | 1.285   | 0.2018   |     |
| ts6.l1 | -0.0124116 | 0.0089251  | -1.391  | 0.1675   |     |
| const  | 0.0248458  | 0.0518312  | 0.479   | 0.6328   |     |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3647 on 98 degrees of freedom

Multiple R-Squared: 0.3564, Adjusted R-squared: 0.317

F-statistic: 9.044 on 6 and 98 DF, p-value: 7.307e-08

## Estimation results for equation ts2:

=====

ts2 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + const

|        | Estimate  | Std. Error | t value | Pr(> t ) |     |
|--------|-----------|------------|---------|----------|-----|
| ts1.l1 | -0.107102 | 0.306294   | -0.350  | 0.7273   |     |
| ts2.l1 | -0.016967 | 0.102229   | -0.166  | 0.8685   |     |
| ts3.l1 | 0.493503  | 0.110318   | 4.473   | 2.08e-05 | *** |
| ts4.l1 | 0.953042  | 0.489883   | 1.945   | 0.0546   | .   |
| ts5.l1 | -0.001637 | 0.001477   | -1.108  | 0.2705   |     |
| ts6.l1 | -0.043771 | 0.027784   | -1.575  | 0.1184   |     |
| const  | 0.917863  | 0.161352   | 5.689   | 1.33e-07 | *** |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.135 on 98 degrees of freedom

Multiple R-Squared: 0.2381, Adjusted R-squared: 0.1915

F-statistic: 5.104 on 6 and 98 DF, p-value: 0.0001341

## Estimation results for equation ts3:

=====

ts3 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + const

|        | Estimate  | Std. Error | t value | Pr(> t ) |     |
|--------|-----------|------------|---------|----------|-----|
| ts1.l1 | 0.735265  | 0.320775   | 2.292   | 0.0240   | *   |
| ts2.l1 | 0.164595  | 0.107063   | 1.537   | 0.1274   |     |
| ts3.l1 | 0.491289  | 0.115534   | 4.252   | 4.84e-05 | *** |
| ts4.l1 | 0.145679  | 0.513044   | 0.284   | 0.7770   |     |
| ts5.l1 | -0.002867 | 0.001547   | -1.854  | 0.0668   | .   |
| ts6.l1 | -0.011623 | 0.029098   | -0.399  | 0.6904   |     |
| const  | -0.059581 | 0.168981   | -0.353  | 0.7252   |     |

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1



Residual standard error: 1.189 on 98 degrees of freedom  
 Multiple R-Squared: 0.3981, Adjusted R-squared: 0.3613  
 F-statistic: 10.8 on 6 and 98 DF, p-value: 3.365e-09

Estimation results for equation ts4:

=====

```
ts4 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + const
```

|        | Estimate   | Std. Error | t value | Pr(> t )     |
|--------|------------|------------|---------|--------------|
| ts1.l1 | -0.3753888 | 0.1517320  | -2.474  | 0.015079 *   |
| ts2.l1 | -0.0620682 | 0.0506424  | -1.226  | 0.223279     |
| ts3.l1 | -0.2170941 | 0.0546495  | -3.972  | 0.000136 *** |
| ts4.l1 | 0.0837932  | 0.2426783  | 0.345   | 0.730620     |
| ts5.l1 | 0.0018562  | 0.0007317  | 2.537   | 0.012762 *   |
| ts6.l1 | -0.0101462 | 0.0137638  | -0.737  | 0.462782     |
| const  | 0.1541826  | 0.0799306  | 1.929   | 0.056629 .   |

---  
 Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.5624 on 98 degrees of freedom  
 Multiple R-Squared: 0.424, Adjusted R-squared: 0.3888  
 F-statistic: 12.03 on 6 and 98 DF, p-value: 4.397e-10

Estimation results for equation ts5:

=====

```
ts5 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + const
```

|        | Estimate | Std. Error | t value | Pr(> t )     |
|--------|----------|------------|---------|--------------|
| ts1.l1 | 7.11422  | 19.98664   | 0.356   | 0.723        |
| ts2.l1 | 8.60523  | 6.67078    | 1.290   | 0.200        |
| ts3.l1 | 5.29414  | 7.19862    | 0.735   | 0.464        |
| ts4.l1 | 10.48015 | 31.96641   | 0.328   | 0.744        |
| ts5.l1 | -0.57131 | 0.09638    | -5.928  | 4.59e-08 *** |
| ts6.l1 | 0.41529  | 1.81301    | 0.229   | 0.819        |
| const  | -9.33297 | 10.52873   | -0.886  | 0.378        |

---  
 Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 74.08 on 98 degrees of freedom  
 Multiple R-Squared: 0.2876, Adjusted R-squared: 0.2439  
 F-statistic: 6.593 on 6 and 98 DF, p-value: 7.087e-06

Estimation results for equation ts6:

=====

```
ts6 = ts1.l1 + ts2.l1 + ts3.l1 + ts4.l1 + ts5.l1 + ts6.l1 + const
```

|        | Estimate  | Std. Error | t value | Pr(> t )   |
|--------|-----------|------------|---------|------------|
| ts1.l1 | -0.079754 | 1.149213   | -0.069  | 0.94481    |
| ts2.l1 | 0.339864  | 0.383563   | 0.886   | 0.37775    |
| ts3.l1 | 0.118802  | 0.413914   | 0.287   | 0.77470    |
| ts4.l1 | 0.862654  | 1.838037   | 0.469   | 0.63987    |
| ts5.l1 | -0.006020 | 0.005542   | -1.086  | 0.28004    |
| ts6.l1 | 0.322732  | 0.104246   | 3.096   | 0.00256 ** |
| const  | -0.656965 | 0.605392   | -1.085  | 0.28050    |

---  
 Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.26 on 98 degrees of freedom  
 Multiple R-Squared: 0.09725, Adjusted R-squared: 0.04198  
 F-statistic: 1.759 on 6 and 98 DF, p-value: 0.1154

Covariance matrix of residuals:

|     | ts1      | ts2      | ts3      | ts4      | ts5      | ts6     |
|-----|----------|----------|----------|----------|----------|---------|
| ts1 | 0.13300  | 0.11380  | 0.07229  | 0.02151  | -5.791   | 0.1943  |
| ts2 | 0.11380  | 1.28887  | -0.18128 | -0.06151 | 4.790    | -1.0820 |
| ts3 | 0.07229  | -0.18128 | 1.41363  | -0.24608 | -8.815   | -0.5194 |
| ts4 | 0.02151  | -0.06151 | -0.24608 | 0.31629  | -9.006   | -0.1244 |
| ts5 | -5.79093 | 4.79009  | -8.81463 | -9.00603 | 5487.983 | 13.6857 |
| ts6 | 0.19434  | -1.08201 | -0.51944 | -0.12439 | 13.686   | 18.1440 |

Correlation matrix of residuals:

|     | ts1     | ts2      | ts3     | ts4      | ts5      | ts6      |
|-----|---------|----------|---------|----------|----------|----------|
| ts1 | 1.0000  | 0.27486  | 0.1667  | 0.10486  | -0.21435 | 0.12511  |
| ts2 | 0.2749  | 1.00000  | -0.1343 | -0.09634 | 0.05696  | -0.22375 |
| ts3 | 0.1667  | -0.13430 | 1.0000  | -0.36802 | -0.10008 | -0.10257 |
| ts4 | 0.1049  | -0.09634 | -0.3680 | 1.00000  | -0.21616 | -0.05193 |
| ts5 | -0.2143 | 0.05696  | -0.1001 | -0.21616 | 1.00000  | 0.04337  |
| ts6 | 0.1251  | -0.22375 | -0.1026 | -0.05193 | 0.04337  | 1.00000  |

```

> AIC <- AIC(var_model)
> BIC <- BIC(var_model)
> log_likelihood <- logLik(var_model)
> num_parameters <- length(coef(var_model))
> HQC <- -2 * as.numeric(log_likelihood) + 2 * num_parameters * log(log(num_observations))
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 0.7700858 3.510706 2.092037 1.554113 117.4166 5.734688
> cat("MAE:", MAE, "\n")
MAE: 0.6087649 2.83258 1.533186 0.9359122 93.49757 4.648526
> cat("AIC:", AIC, "\n")
AIC: 2696.757
> cat("BIC:", BIC, "\n")
BIC: 2808.224
> cat("HQC:", HQC, "\n")
HQC: 2635.027
> var_model <- VAR(train_set, p=6)
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 1.627494 6.797625 10.82598 4.592681 355.325 20.5848
> cat("MAE:", MAE, "\n")
MAE: 1.419453 5.258024 9.007064 4.040439 309.1655 17.83669
> plot(stability(var_model))
> var_model <- VAR(train_set, p=1)
> plot(stability(var_model))
> var_model <- VAR(train_set, p=4)
> forecasts <- predict(var_model, n.ahead=12)
> forecasted_values <- sapply(forecasts$fcst, function(x) x[, "fcst"])
> actual_values <- as.matrix(test_set)
> RMSE <- sqrt(colMeans((actual_values - forecasted_values)^2))
> MAE <- colMeans(abs(actual_values - forecasted_values))
> cat("RMSE:", RMSE, "\n")
RMSE: 1.710565 5.458001 5.021193 2.495168 179.2677 11.66931
> cat("MAE:", MAE, "\n")
MAE: 1.472663 3.71091 4.567531 1.682052 132.45 8.403488
> save.image("C:\\Users\\minhas01\\Desktop\\Nahayan Minhas\\Workspace main")
>

```