Code for problem 1:

```
import sys
# Diptangshu Dey, 20CS8018
def getCostMatrix():
    numRows = int(input('Enter the number of rows : '))+1
    numCols = int(input('Enter the number of cols : '))+1
    costMatrix = []
    for i in range(numRows-1):
        rowCostArray=list(map(int, input('Enter the costs for row %s and
the total supply at the end, separated by space(n'\%(i+1)).split())
        costMatrix.append(rowCostArray)
    rowCostArray = list(map(int, input('Enter the demand values for each
col separated by space\n').split()))
    costMatrix.append(rowCostArray)
    if len(costMatrix[numRows-1]) != numCols:
        costMatrix[numRows-1].append(0)
    return costMatrix
def printMatrix(matrixType, matrix):
    print("-----
----")
    if matrixType=='cost':
        print("Cost Matrix")
    elif matrixType=='allocation':
        print("Allocation Matrix")
    for i in range(len(matrix[0])-1):
        print('\tD%s'%(i+1), end='')
    print('\tSupply')
    for i in range(len(matrix)-1):
        print('S%s'%(i+1), end='')
        for j in range(len(matrix[0])):
            print('\t%s'%(matrix[i][j]), end='')
        print()
    print('Demand', end='')
    for i in range(len(matrix[0])):
        print('\t%s'%(matrix[-1][i]), end='')
    print("\n-----
----")
    print()
def isBalanced(costMatrix):
    return sum(costMatrix[-1])==sum([costMatrix[i][-1] for i in
range(len(costMatrix))])
def getTotalCost(costMatrix):
    m = len(costMatrix)
    n = len(costMatrix[0])
    allocMatrix = [[0 \text{ for } \_ \text{ in range}(len(costMatrix}[0]))] \text{ for } \_ \text{ in }
range(len(costMatrix))]
```

```
numAllocated = 0
    totalCost = 0
    i =0
    j=⊙
    while i < m-1 and j < n-1:
        x = min(costMatrix[i][n-1], costMatrix[m-1][j])
        costMatrix[m-1][j] -= x
        costMatrix[i][n-1] -= x
        numAllocated += 1
        allocMatrix[i][j] = x
        allocMatrix[m-1][j] = costMatrix[m-1][j]
        allocMatrix[i][n-1] = costMatrix[i][n-1]
        totalCost = totalCost + x*costMatrix[i][j]
        if costMatrix[m-1][j] < costMatrix[i][n-1]:
        elif costMatrix[m-1][j] > costMatrix[i][n-1]:
            <u>i+=1</u>
        else:
            i+=1
            j+=1
    return totalCost, numAllocated, allocMatrix
# Diptangshu Dey, 20CS8018
def isDegenerate(costMatrix, numAllocated):
    m = len(costMatrix)-1
    n = len(costMatrix[0])-1
    return numAllocated!=(m+n-1)
def balanceProblem(costMatrix):
    totalDemand = sum(costMatrix[-1])
    totalSupply = sum([x[-1] for x in costMatrix])
    if totalDemand > totalSupply:
        #add new row
        dummySource = [0 for _ in range(len(costMatrix[0]))]
        dummySource[-1] = totalDemand-totalSupply
        costMatrix.insert(-1, dummySource)
    else:
        for cost in costMatrix:
            cost.insert(-1, 0)
        costMatrix[-1].insert(-1, totalSupply-totalDemand)
        pass
    return costMatrix
def isIndependentAllocation( allocMatrix ):
    elimRows = [0 for _ in range(len(allocMatrix))]
    elimCols = [0 for _ in range(len(allocMatrix[0]))]
    while 1:
        flag = 0
        #eliminate row
        for i in range(len(allocMatrix)):
```

```
if elimRows[i]==0:
                if len([allocMatrix[i][j] for j in
range(len(allocMatrix[0])) if (elimCols[j]==0 and (allocMatrix[i][j]!=0 and
allocMatrix[i][j]!=-1)))) < 2:
                    elimRows[i]=1
                    flag=1
        #eliminate column
        for j in range(len(allocMatrix[0])):
            if elimCols[j]==0:
                if len([allocMatrix[i][j] for i in range(len(allocMatrix))
if (elimRows[i]==0 and allocMatrix[i][j]!=0 and allocMatrix[i][j]!=-1) ])
< 2:
                    elimCols[j]=1
                    flag=1
        if flag==0:
            #either all cells are eliminated ---> independent allocation
            if 0 not in elimRows and 0 not in elimCols:
                return True, 1, 1
            else:
                #dependent allocation
                return False, elimRows, elimCols
def findUV( costMatrix, allocMat ):
    #find the max allocated row/col
    u = [None for _ in range(len(allocMat))]
    v = [None for _ in range(len(allocMat[0]))]
    maxRow=[-1,0] #(row no., allocs)
    for i in range(len(allocMat)):
        allocs = len([allocMat[i][j] for j in range(len(allocMat[0])) if
allocMat[i][j]!=0]
        if allocs > maxRow[1]:
            \max Row[0] = i
            maxRow[1] = allocs
    maxCol = [-1, 0]
    for j in range(len(allocMat[0])):
        allocs = len([ allocMat[i][j] for i in range(len(allocMat)) if
allocMat[i][j]!=0 ])
        if allocs > maxCol[1]:
            \max Col[0] = j
            maxCol[1] = allocs
    if maxRow[1] > maxCol[1] :
        u[maxRow[0]] = 0
        for j in range(len(v)):
            if allocMat[maxRow[0]][j]!=0 and v[j] is None:
                v[j] = costMatrix[maxRow[0]][j] - u[maxRow[0]]
        for i in range(len(u)):
            for j in range(len(v)):
                if allocMat[i][j]!=0 and v[j] is not None and u[i] is None:
```

```
u[i] = costMatrix[i][j] - v[j]
    else:
        v[maxCol[0]] = 0
        for i in range(len(u)):
            if allocMat[i][maxCol[0]]!=0 and u[i] is None:
                u[i] = costMatrix[i][maxCol[0]] - v[maxCol[0]]
        for j in range(len(v)):
            for i in range(len(u)):
                if allocMat[i][j]!=0 and v[j] is None and u[i] is not None:
                    v[j] = costMatrix[i][j] - u[i]
#
    while None in u or None in v:
        if None in u:
            ind = u.index(None)
            for j in range(len(v)):
                if allocMat[ind][j]!=0 and v[j] is not None:
                    u[ind] = costMatrix[ind][j] - v[j]
        if None in v:
            ind = v.index(None)
            for i in range(len(u)):
                if allocMat[i][ind]!=0 and u[i] is not None:
                    v[ind] = costMatrix[i][ind] - u[i]
    return u, v
def findDeltas(cstMat, allMat, u,v ):
    deltas = [[None for _ in range(len(allMat[0]))] for _ in
range(len(allMat))]
    for i in range(len(allMat)):
        for j in range(len(allMat[0])):
            if allMat[i][j]==0:
                deltas[i][j] = cstMat[i][j] - u[i] - v[j]
    return deltas
def isOptimal(deltas):
    for i in range(len(deltas)):
        for j in range(len(deltas[0])):
            if deltas[i][j] is not None and deltas[i][j] < 0:
                return False
    return True
def newAlloc(allMat, deltas):
    #find the most negative
    ij = [-1, -1]
    mostNeg = 1
    for i in range(len(deltas)):
        for j in range(len(deltas[0])):
            if deltas[i][j] is not None and deltas[i][j] < 0 and deltas[i]
[j] < mostNeg:</pre>
                mostNeg = deltas[i][j]
                ij[0] = i
```

```
ij[1] = j
    #find loop
    allMat[ij[0]][ij[1]] = sys.maxsize
    __,elimRows,elimCols = isIndependentAllocation( allMat )
    rowinds = [i for i in range(len(elimRows)) if elimRows[i]==0]
    colinds = [i for i in range(len(elimCols)) if elimCols[i]==0]
    path = [[ij[0],ij[1]]]
    indices = [[x,y]] for x in rowinds for y in colinds if al[Mat[x]][y]!=0
    indices.remove(path[0])
    dist = sys.maxsize
    inds = []
    n = len(indices) + 1
    while len(path)!=n:
        t = len(indices)
        dist = sys.maxsize
        for i in range(t):
            d = abs(path[-1][0]-indices[i][0])+abs(path[-1][1] - indices[i]
[1])
            if d < dist:</pre>
                dist = d
                inds.append([indices[i][0], indices[i][1]])
        path.append(inds[0])
        inds.clear()
        indices.remove(path[-1])
    #modify allocation
    val = min([allMat[path[t][0]][path[t][1]]) for t in range(1, len(path), 2)
if allMat[path[t][0]][path[t][1]]!=0.000001])
    allMat[path[0][0]][path[0][1]] = 0
    for i in range(len(path)):
        if i%2==0:
            allMat[path[i][0]][path[i][1]] += val
        else:
            allMat[path[i][0]][path[i][1]] -= val
    #num Allocs
    numAlloc=0
    for i in range(len(allMat)):
        for j in range(len(allMat[0])):
            if allMat[i][j]>0:
                numAlloc+=1
    return allMat, numAlloc
def removeDeg(allMat, cstMat):
    for i in range(len(allMat)):
        for j in range(len(allMat[0])):
            if allMat[i][j]==0:
                allMat[i][j] = 0.000001
                isIndep = isIndependentAllocation( allMat )[0]
                if isIndep:
                    return allMat
                else:
```

```
allMat[i][j] = 0
    return allMat
def main():
    print("Diptangshu Dey, 20CS8018")
    #1. get the cost matrix
    costMatrix = getCostMatrix()
    printMatrix('cost', costMatrix)
    #2. check if the problem is balanced
    isBal = isBalanced(costMatrix)
    if isBal:
        print('It is a balanced problem')
    else:
        print('It is an unbalanced problem')
        costMatrix = balanceProblem(costMatrix)
    #3. calculate the cost
    cost, numAllocated, allocMatrix = getTotalCost(costMatrix)
    printMatrix('allocation', allocMatrix)
    print('Calculated total cost = ',cost)
    cstMat = [x[:-1] for x in costMatrix]
    cstMat.pop()
    allMat = [x[:-1] for x in allocMatrix]
    allMat.pop()
    while 1:
        #4. check for degeneracy
        isDeg = isDegenerate(costMatrix, numAllocated)
        if isDeg:
            print('It is a degenerate solution\nMaking it a non-degenerate
solution...\n')
            allMat = removeDeg(allMat, cstMat)
            numAllocated+=1
            print('\nModified Non-degenerate allocation\n')
            for i in range(len(allMat[0])):
                print('\t\tD%s'%(i+1), end='')
            print()
            for i in range(len(allMat)):
                print('S%s'%(i+1), end='')
                for j in range(len(allMat[0])):
                    print('\t\t',allMat[i][j],end='')
                print()
            print()
            continue
            return
        else:
            print('It is a non-degenerate solution')
        #5 check for independent allocation position
        isIndep = isIndependentAllocation( allMat )[0]
        if isIndep:
            print( 'The allocation positions are independent' )
```

```
print( 'The allocation positions are not independent' )
            return
        #6 calculate u and v values
        u,v = findUV(cstMat, allMat)
        print('u values = ',u)
        print('v values = ',v)
        #find delta[i,j] at unallocated positions
        deltas = findDeltas(cstMat, allMat,u,v)
        if (isOptimal(deltas)):
            print('Optimal allocation : \n')
            for i in range(len(allMat[0])):
                print('\t\tD%s'%(i+1), end='')
            print()
            for i in range(len(allMat)):
                print('S%s'%(i+1), end='')
                for j in range(len(allMat[0])):
                    print('\t\t',allMat[i][j],end='')
                print()
            print()
            cost = 0
            for i in range(len(cstMat)):
                for j in range(len(cstMat[0])):
                    cost = cost + cstMat[i][j]*allMat[i][j]
            print('Optimal cost = ',cost)
            return
        else:
            print('It is a non-optimal solution')
            allocMatrix, numAllocated = newAlloc(allMat, deltas)
            print('\nModified Allocation\n')
            for i in range(len(allMat[0])):
                print('\t\tD%s'%(i+1), end='')
            print()
            for i in range(len(allMat)):
                print('S%s'%(i+1), end='')
                for j in range(len(allMat[0])):
                    print('\t\t',allMat[i][j],end='')
                print()
            print()
main()
```

Output for problem 1:

Diptangshu Dey, 20CS8018

Enter the number of rows : 3

Enter the number of cols: 4

Enter the costs for row 1 and the total supply at the end, separated by space 23 27 16 18 30

Enter the costs for row 2 and the total supply at the end, separated by space 12 17 20 51 40

Enter the costs for row 3 and the total supply at the end, separated by space 22 28 12 32 53

Enter the demand values for each col separated by space

22 35 25 41

Cost Ma	trix					
	D1	D2	D3	D4	Supply	
S1	23	27	16	18	30	
S2	12	17	20	51	40	
S3	22	28	12	32	53	
Demand	22	35	25	41	0	

It is a balanced problem

Allocation Matrix						
	D1	D2	D3	D4	Supply	
S1	22	8	0	0	0	
S2	0	27	13	0	0	
S3	0	0	12	41	0	
Demand	0	0	0	0	0	

Calculated total cost = 2897

It is a non-degenerate solution

The allocation positions are independent

u values = [27, 17, 9]

v values = [-4, 0, 3, 23]

It is a non-optimal solution

Modified Allocation

	D1	D2	D3	D4
S1	22	0	0	8
S2	0	35	5	Θ
S3	0	0	20	33

It is a non-degenerate solution

The allocation positions are independent

u values = [-2, 20, 12]

v values = [25, -3, 0, 20]

It is a non-optimal solution

Modified Allocation

	D1	D2	D3	D4
S1	17	0	0	13
S2	5	35	0	0
S3	0	0	25	28

It is a non-degenerate solution
The allocation positions are independent
u values = [23, 12, 37]
v values = [0, 5, -25, -5]
It is a non-optimal solution

Modified Allocation

	D1	D2	D3	D4
S1	0	0	0	30
S2	5	35	0	0
S3	17	0	25	11

It is a non-degenerate solution
The allocation positions are independent
u values = [-14, -10, 0]
v values = [22, 27, 12, 32]
Optimal allocation :

	D1	D2	D3	D4
S1	0	0	0	30
S2 S3	5	35	0	Θ
S3	17	0	25	11

Optimal cost = 2221

Code for problem 2:

```
import sys
# Diptangshu Dey, 20CS8018
def getCostMatrix():
   numRows = int(input('Enter the number of rows : '))+1
   numCols = int(input('Enter the number of cols : '))+1
   costMatrix = []
   for i in range(numRows-1):
        rowCostArray=list(map(int, input('Enter the costs for row %s and
the total supply at the end, separated by space(n'\%(i+1)).split())
       costMatrix.append(rowCostArray)
    rowCostArray = list(map(int, input('Enter the demand values for each
col separated by space\n').split()))
   costMatrix.append(rowCostArray)
   if len(costMatrix[numRows-1]) != numCols:
       costMatrix[numRows-1].append(0)
   return costMatrix
def printMatrix(matrixType, matrix):
   print("-----
----")
   if matrixType=='cost':
       print("Cost Matrix")
   elif matrixType=='allocation':
       print("Allocation Matrix")
   for i in range(len(matrix[0])-1):
        print('\tD%s'%(i+1), end='')
   print('\tSupply')
   for i in range(len(matrix)-1):
        print('S%s'%(i+1), end='')
        for j in range(len(matrix[0])):
            print('\t%s'%(matrix[i][j]), end='')
        print()
   print('Demand', end='')
   for i in range(len(matrix[0])):
        print('\t%s'%(matrix[-1][i]), end='')
   print("\n-----
 ----")
   print()
def isBalanced(costMatrix):
    return sum(costMatrix[-1])==sum([costMatrix[i][-1] for i in
range(len(costMatrix))])
def getTotalCost(costMatrix):
   m = len(costMatrix)
```

```
n = len(costMatrix[0])
    allocMatrix = [[0 for _ in range(len(costMatrix[0]))] for _ in
range(len(costMatrix))]
    numAllocated = 0
    totalCost = 0
    i=0
    j=0
    while i < m-1 and j < n-1:
        x = min(costMatrix[i][n-1], costMatrix[m-1][j])
        costMatrix[m-1][j] -= x
        costMatrix[i][n-1] -= x
        numAllocated += 1
        allocMatrix[i][j] = x
        allocMatrix[m-1][j] = costMatrix[m-1][j]
        allocMatrix[i][n-1] = costMatrix[i][n-1]
        totalCost = totalCost + x*costMatrix[i][j]
        if costMatrix[m-1][j] < costMatrix[i][n-1]:</pre>
        elif costMatrix[m-1][j] > costMatrix[i][n-1]:
            i+=1
        else:
            i+=1
            j+=1
    return totalCost, numAllocated, allocMatrix
# Diptangshu Dey, 20CS8018
def isDegenerate(costMatrix, numAllocated):
    m = len(costMatrix)-1
    n = len(costMatrix[0])-1
    return numAllocated!=(m+n-1)
def balanceProblem(costMatrix):
    totalDemand = sum(costMatrix[-1])
    totalSupply = sum([x[-1] for x in costMatrix])
    if totalDemand > totalSupply:
        #add new row
        dummySource = [0 for _ in range(len(costMatrix[0]))]
        dummySource[-1] = totalDemand-totalSupply
        costMatrix.insert(-1, dummySource)
    else:
        for cost in costMatrix:
            cost.insert(-1, 0)
        costMatrix[-1].insert(-1, totalSupply-totalDemand)
        pass
    return costMatrix
def isIndependentAllocation( allocMatrix ):
    elimRows = [0 for _ in range(len(allocMatrix))]
    elimCols = [0 for _ in range(len(allocMatrix[0]))]
    while 1:
```

```
flag = 0
        #eliminate row
        for i in range(len(allocMatrix)):
            if elimRows[i]==0:
                if len([allocMatrix[i][j] for j in
range(len(allocMatrix[0])) if (elimCols[j]==0 and (allocMatrix[i][j]!=0 and
allocMatrix[i][j]!=-1)))) < 2:
                    elimRows[i]=1
                    flag=1
        #eliminate column
        for j in range(len(allocMatrix[0])):
            if elimCols[j]==0:
                if len([allocMatrix[i][j] for i in range(len(allocMatrix))
if (elimRows[i]==0 and allocMatrix[i][j]!=0 and allocMatrix[i][j]!=-1) ])
< 2:
                    elimCols[j]=1
                    flag=1
        if flag==0:
            #either all cells are eliminated ---> independent allocation
            if 0 not in elimRows and 0 not in elimCols:
                return True, 1, 1
            else:
                #dependent allocation
                return False, elimRows, elimCols
def findUV( costMatrix, allocMat ):
    #find the max allocated row/col
    u = [None for _ in range(len(allocMat))]
    v = [None for _ in range(len(allocMat[0]))]
    \max Row = [-1, 0] \#(row no., allocs)
    for i in range(len(allocMat)):
        allocs = len([allocMat[i][j] for j in range(len(allocMat[0])) if
allocMat[i][j]!=0]
        if allocs > maxRow[1]:
            \max Row[0] = i
            maxRow[1] = allocs
    maxCol = [-1, 0]
    for j in range(len(allocMat[0])):
        allocs = len([ allocMat[i][j] for i in range(len(allocMat)) if
allocMat[i][j]!=0]
        if allocs > maxCol[1]:
            \max Col[0] = j
            maxCol[1] = allocs
    if maxRow[1] > maxCol[1] :
        u[maxRow[0]] = 0
        for j in range(len(v)):
            if allocMat[maxRow[0]][j]!=0 and v[j] is None:
                v[j] = costMatrix[maxRow[0]][j] - u[maxRow[0]]
```

```
for i in range(len(u)):
            for j in range(len(v)):
                if allocMat[i][j]!=0 and v[j] is not None and u[i] is None:
                    u[i] = costMatrix[i][j] - v[j]
    else:
        v[maxCol[0]] = 0
        for i in range(len(u)):
            if allocMat[i][maxCol[0]]!=0 and u[i] is None:
                u[i] = costMatrix[i][maxCol[0]] - v[maxCol[0]]
        for j in range(len(v)):
            for i in range(len(u)):
                if allocMat[i][j]!=0 and v[j] is None and u[i] is not None:
                    v[j] = costMatrix[i][j] - u[i]
#
    while None in u or None in v:
        if None in u:
            ind = u.index(None)
            for j in range(len(v)):
                if allocMat[ind][j]!=0 and v[j] is not None:
                    u[ind] = costMatrix[ind][j] - v[j]
        if None in v:
            ind = v.index(None)
            for i in range(len(u)):
                if allocMat[i][ind]!=0 and u[i] is not None:
                    v[ind] = costMatrix[i][ind] - u[i]
    return u, v
def findDeltas(cstMat, allMat, u,v ):
    deltas = [[None for _ in range(len(allMat[0]))] for _ in
range(len(allMat))]
    for i in range(len(allMat)):
        for j in range(len(allMat[0])):
            if allMat[i][j]==0:
                deltas[i][j] = cstMat[i][j] - u[i] - v[j]
    return deltas
def isOptimal(deltas):
    for i in range(len(deltas)):
        for j in range(len(deltas[0])):
            if deltas[i][j] is not None and deltas[i][j] < 0:
                return False
    return True
def newAlloc(allMat, deltas):
    #find the most negative
    ij = [-1, -1]
    mostNeg = 1
    for i in range(len(deltas)):
        for j in range(len(deltas[0])):
            if deltas[i][j] is not None and deltas[i][j] < 0 and deltas[i]
```

```
[j] < mostNeg:</pre>
                mostNeg = deltas[i][j]
                ij[0] = i
                ij[1] = j
    #find loop
    allMat[ij[0]][ij[1]] = sys.maxsize
    __,elimRows,elimCols = isIndependentAllocation( allMat )
    rowinds = [i for i in range(len(elimRows)) if elimRows[i]==0]
    colinds = [i for i in range(len(elimCols)) if elimCols[i]==0]
    path = [[ij[0],ij[1]]]
    indices = [[x,y] for x in rowinds for y in colinds if allMat[x][y]!=0
    indices.remove(path[0])
    dist = sys.maxsize
    inds = []
    n = len(indices)+1
    while len(path)!=n:
        t = len(indices)
        dist = sys.maxsize
        for i in range(t):
            d = abs(path[-1][0]-indices[i][0])+abs(path[-1][1] - indices[i]
[1])
            if d < dist:
                dist = d
                inds.append([indices[i][0], indices[i][1]])
        path.append(inds[0])
        inds.clear()
        indices.remove(path[-1])
    #modify allocation
    val = min([allMat[path[t][0]][path[t][1]] for t in range(1, len(path), 2)
if allMat[path[t][0]][path[t][1]]!=0.000001])
    allMat[path[0][0]][path[0][1]] = 0
    for i in range(len(path)):
        if i\%2 = = 0:
            allMat[path[i][0]][path[i][1]] += val
        else:
            allMat[path[i][0]][path[i][1]] -= val
    #num Allocs
    numAlloc=0
    for i in range(len(allMat)):
        for j in range(len(allMat[0])):
            if allMat[i][j]>0:
                numAlloc+=1
    return allMat, numAlloc
def removeDeg(allMat, cstMat):
    for i in range(len(allMat)):
        for j in range(len(allMat[0])):
            if allMat[i][j]==0:
                allMat[i][j] = 0.000001
                isIndep = isIndependentAllocation( allMat )[0]
```

```
if isIndep:
                    return allMat
                else:
                    allMat[i][j] = 0
    return allMat
def main():
    print("Diptangshu Dey, 20CS8018")
    #1. get the cost matrix
    costMatrix = getCostMatrix()
    printMatrix('cost', costMatrix)
    #2. check if the problem is balanced
    isBal = isBalanced(costMatrix)
    if isBal:
        print('It is a balanced problem')
    else:
        print('It is an unbalanced problem')
        costMatrix = balanceProblem(costMatrix)
    #3. calculate the cost
    cost, numAllocated, allocMatrix = getTotalCost(costMatrix)
    printMatrix('allocation', allocMatrix)
    print('Calculated total cost = ',cost)
    cstMat = [x[:-1] for x in costMatrix]
    cstMat.pop()
    allMat = [x[:-1] for x in allocMatrix]
    allMat.pop()
    while 1:
        #4. check for degeneracy
        isDeg = isDegenerate(costMatrix, numAllocated)
        if isDeg:
            print('It is a degenerate solution\nMaking it a non-degenerate
solution...\n')
            allMat = removeDeg(allMat, cstMat)
            numAllocated+=1
            print('\nModified Non-degenerate allocation\n')
            for i in range(len(allMat[0])):
                print('\t\tD%s'%(i+1), end='')
            print()
            for i in range(len(allMat)):
                print('S%s'%(i+1), end='')
                for j in range(len(allMat[0])):
                    print('\t\t',allMat[i][j],end='')
                print()
            print()
            continue
            return
        else:
            print('It is a non-degenerate solution')
        #5 check for independent allocation position
```

```
isIndep = isIndependentAllocation( allMat )[0]
        if isIndep:
            print( 'The allocation positions are independent' )
        else:
            print( 'The allocation positions are not independent' )
            return
        #6 calculate u and v values
        u,v = findUV(cstMat, allMat)
        print('u values = ',u)
        print('v values = ',v)
        #find delta[i,j] at unallocated positions
        deltas = findDeltas(cstMat, allMat,u,v)
        if (isOptimal(deltas)):
            print('Optimal allocation : \n')
            for i in range(len(allMat[0])):
                print('\t\tD%s'%(i+1), end='')
            print()
            for i in range(len(allMat)):
                print('S%s'%(i+1), end='')
                for j in range(len(allMat[0])):
                    print('\t\t',allMat[i][j],end='')
                print()
            print()
            cost = ⊙
            for i in range(len(cstMat)):
                for j in range(len(cstMat[0])):
                    cost = cost + cstMat[i][j]*allMat[i][j]
            print('Optimal cost = ',cost)
            return
        else:
            print('It is a non-optimal solution')
            allocMatrix, numAllocated = newAlloc(allMat, deltas)
            print('\nModified Allocation\n')
            for i in range(len(allMat[0])):
                print('\t\tD%s'%(i+1), end='')
            print()
            for i in range(len(allMat)):
                print('S%s'%(i+1), end='')
                for j in range(len(allMat[0])):
                    print('\t\t',allMat[i][j],end='')
                print()
            print()
main()
```

Diptangshu Dey, 20CS8018

Enter the number of rows : 3

Enter the number of cols: 4

Enter the costs for row 1 and the total supply at the end, separated by space 21 16 25 13 11

Enter the costs for row 2 and the total supply at the end, separated by space 17 18 14 23 13

Enter the costs for row 3 and the total supply at the end, separated by space 32 27 18 41 19

Enter the demand values for each col separated by space

6 10 12 15

Cost Ma	trix					
	D1	D2	D3	D4	Supply	
S1	21	16	25	13	11	
S2	17	18	14	23	13	
S3	32	27	18	41	19	
Demand	6	10	12	15	0	

It is a balanced problem

Allocation Matrix						
	D1	D2	D3	D4	Supply	
S1	6	5	Θ	0	0	
S2	0	5	8	0	0	
S3	0	0	4	15	0	
Demand	0	0	0	0	0	

Calculated total cost = 1095

It is a non-degenerate solution

The allocation positions are independent

u values = [16, 18, 22]

v values = [5, 0, -4, 19]

It is a non-optimal solution

Modified Allocation

	D1	D2	D3	D4
S1	6	0	Θ	5
S2	0	10	3	Θ
S3	0	0	9	10

It is a non-degenerate solution

The allocation positions are independent

u values = [-10, 14, 18]

v values = [31, 4, 0, 23]

It is a non-optimal solution

Modified Allocation

	D1	D2	D3	D4
S1	3	0	0	8
S2 S3	3	10	0	Θ
S3	0	0	12	7

It is a non-degenerate solution
The allocation positions are independent
u values = [21, 17, 49]
v values = [0, 1, -31, -8]
It is a non-optimal solution

Modified Allocation

	D1	D2	D3	D4
S1	0	0	0	11
S1 S2 S3	0	13	0	Θ
S3	0	3	12	4

It is a degenerate solution Making it a non-degenerate solution...

Modified Non-degenerate allocation

	D1	D2	D3	D4
S1	1e-06	0	0	11
S2	0	13	0	0
S3	0	3	12	4

It is a non-degenerate solution
The allocation positions are independent
u values = [-28, -9, 0]
v values = [49, 27, 18, 41]
It is a non-optimal solution

Modified Allocation

	D1	D2		D3		D4	
S1	-3.999999		Θ		0		15
S2	4	9		0		0	
S3	0	7		12		0	

It is a degenerate solution
Making it a non-degenerate solution...

Modified Non-degenerate allocation

	D1	D2		D3		D4	
S1	-3.999999		0		0		15
S2	4	9		0		Θ	
S3	0	7		12		Θ	

It is a non-degenerate solution
The allocation positions are independent
u values = [21, 17, 26]
v values = [0, 1, -8, -8]
It is a non-optimal solution

Modified Allocation

	D1	D2	D3	D4			
S1	0.0	-3.999999		0	15		
S2	1.0000000	00139778e-06	12.99999899999999			Θ	0
S3	0	7	12	Θ			

It is a degenerate solution Making it a non-degenerate solution...

Modified Non-degenerate allocation

	D1	D2	D3	D4			
S1	Θ	-3.999999		0	15		
S2	1.0000000	000139778e-06	39778e-06 12.99999899999			0	0
S3	0	7	12	0			

It is a non-degenerate solution
The allocation positions are independent
u values = [16, 18, 27]
v values = [-1, 0, -9, -3]
Optimal allocation :

	D1	D2	D3	D4		
S1	0	-3.999999		Θ	15	
S2	1.0000000	000139778e-06	12.99999899999999		0	0
S3	Θ	7	12	Θ		

Optimal cost = 770.0000150000001