

CIT 596 Recitation, Week 5

Honglin Zhang

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Usage of Pumping Lemma

Jean Gallier says in his Notes:

"In order to show that the pumping lemma is contradicted, one needs to show that for some DFA D , for every $m \geq 1$, there is some string $w \in L(D)$ of length at least m , such that for every possible decomposition $w = uxv$ satisfying the constraints $x \neq \epsilon$ and $|ux| \leq m$, there is some $i \geq 0$ such that $ux^i v \notin L(D)$."

[Exercise] @sipser13 [p. 88-91] exercise 1.29, exercise 1.46

Determine if the following language is regular or not.

- ▶ $\{0^n 1^n 2^n \mid n \geq 0\}$
- ▶ $\{a^{2^n} \mid n \geq 0\}$
- ▶ $\{0^m 1^n \mid m \neq n\}$

[Exercise] @sipser13 [p. 90] exercise 1.45

- ▶ Let $A/B = \{w \mid wx \in A \text{ for some } x \in B\}$. Show that if A is regular and B is any language, then A/B is regular.