



Graphs 07

Graphs (Part 4)



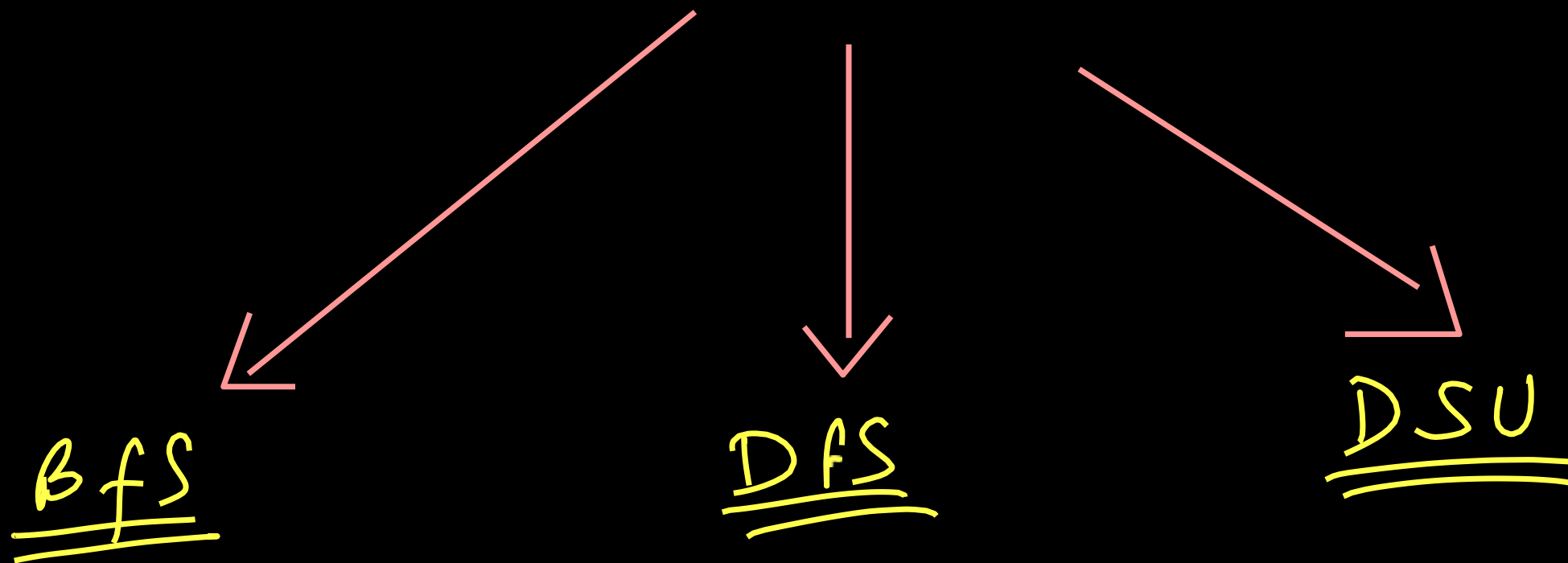
Topological Sorting → DAG

→ cycle

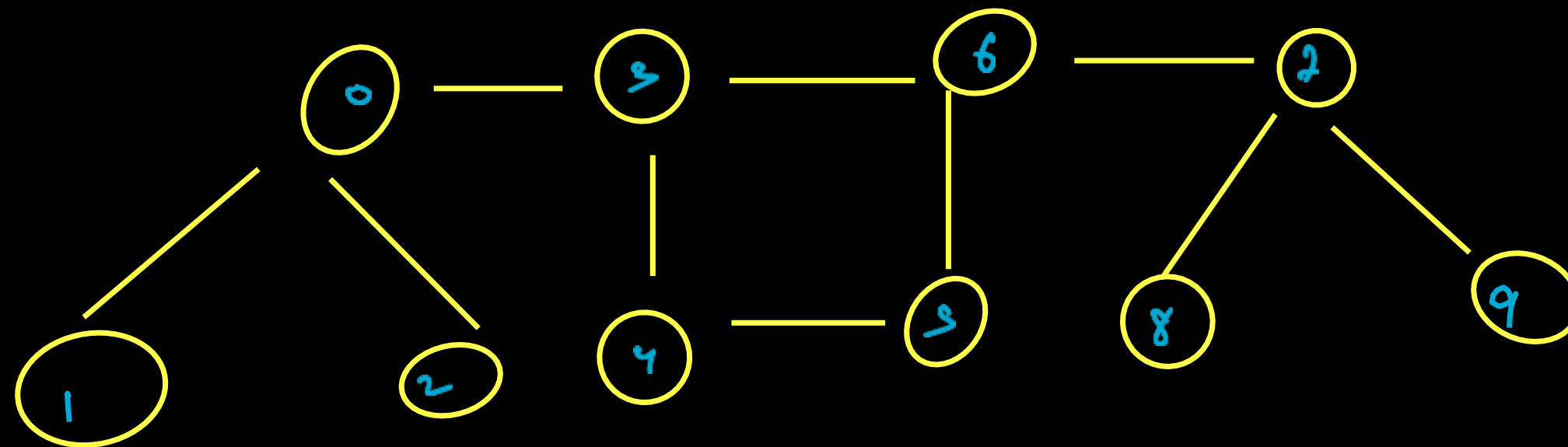
Ques Given a directed graph, detect if it is having cycles or not.

→ Kahn's algo

Q. How to detect cycle in an undirected graph??



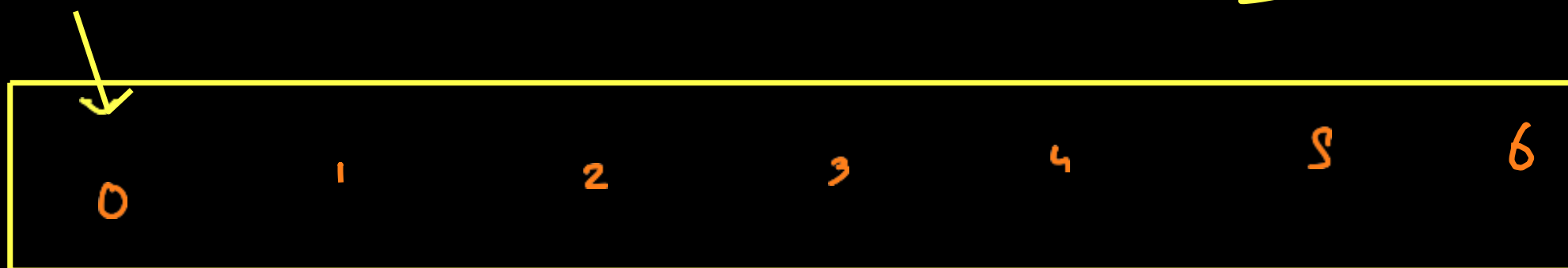
Cycle detection using DSU



Edge list

[0, 1],
[0, 2],
[3, 4],
[5, 6],
[7, 8],
[9, 10],
[10, 11],
...
]

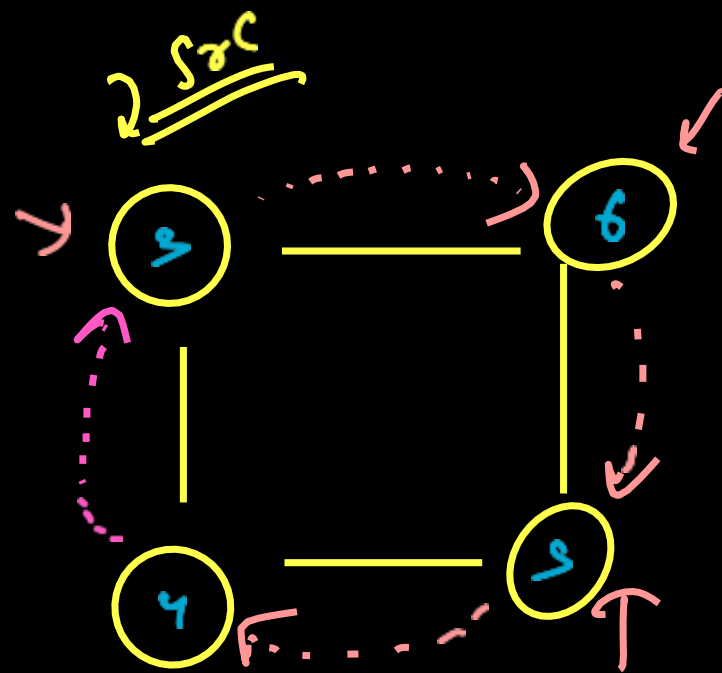
Let's create a dsu



we will read each edge & on the vertices of the edge
apply union operation.

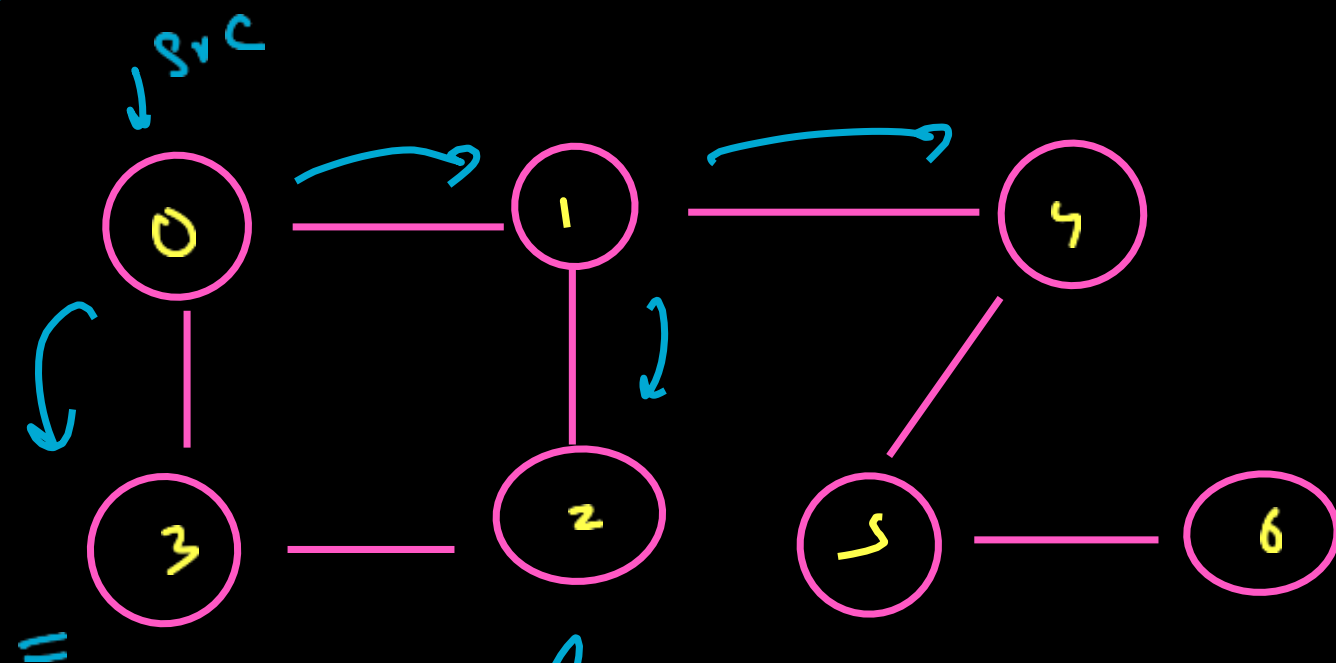
cycle detection using DFS

check if the visited is
not your parent
then there is a
cycle



0, 1, 3, 4, 2 vis

cycle detect using BFS



parent

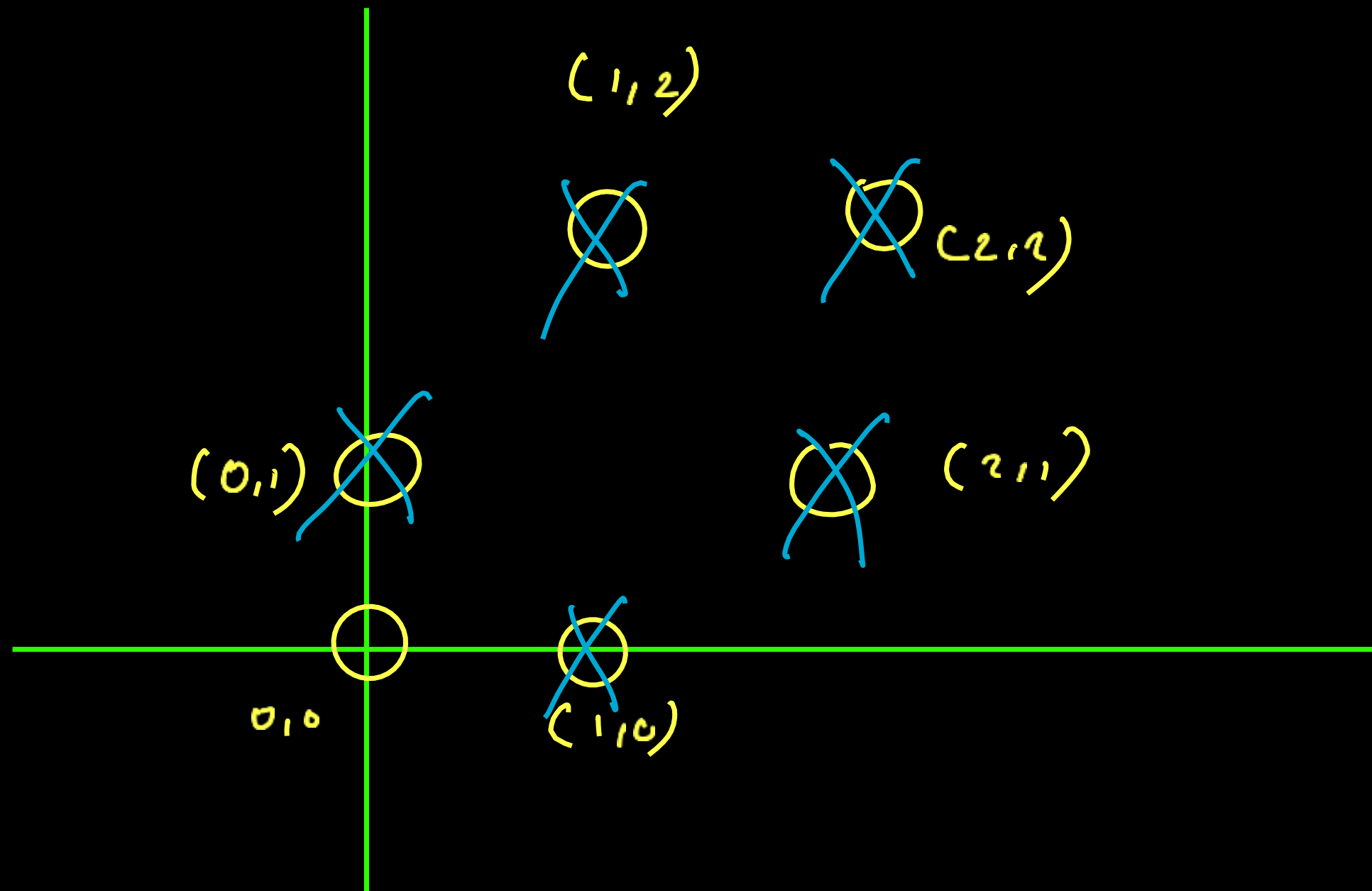
| 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----|---|---|---|---|---|---|
| -1 | 0 | 1 | 0 | 1 | | |

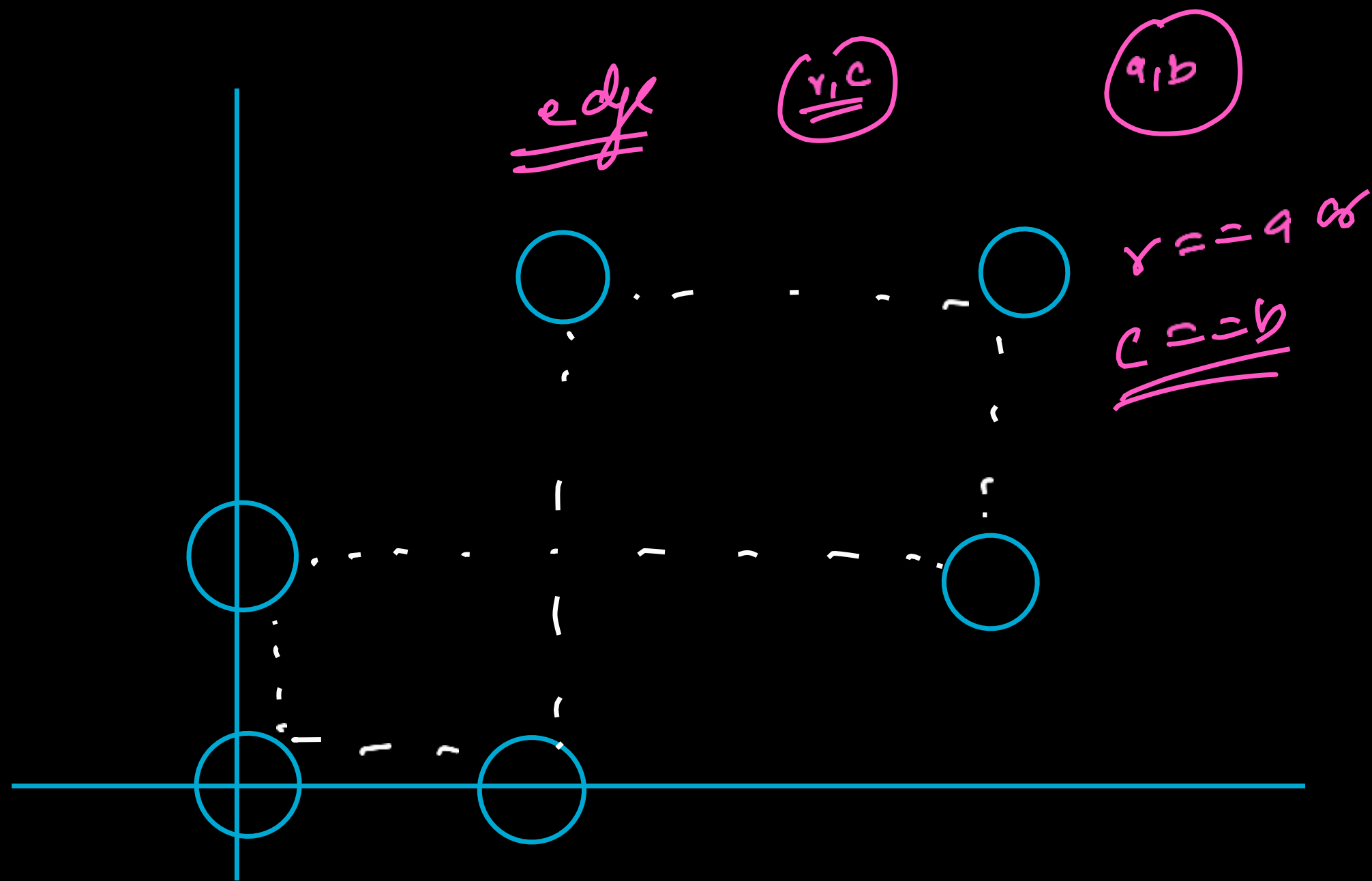
| | | | | | | |
|---|---|---|---|--|--|--|
| 1 | 1 | 4 | 2 | | | |
|---|---|---|---|--|--|--|

queue

if a node is already visited & it is not your parent then you have a cycle.

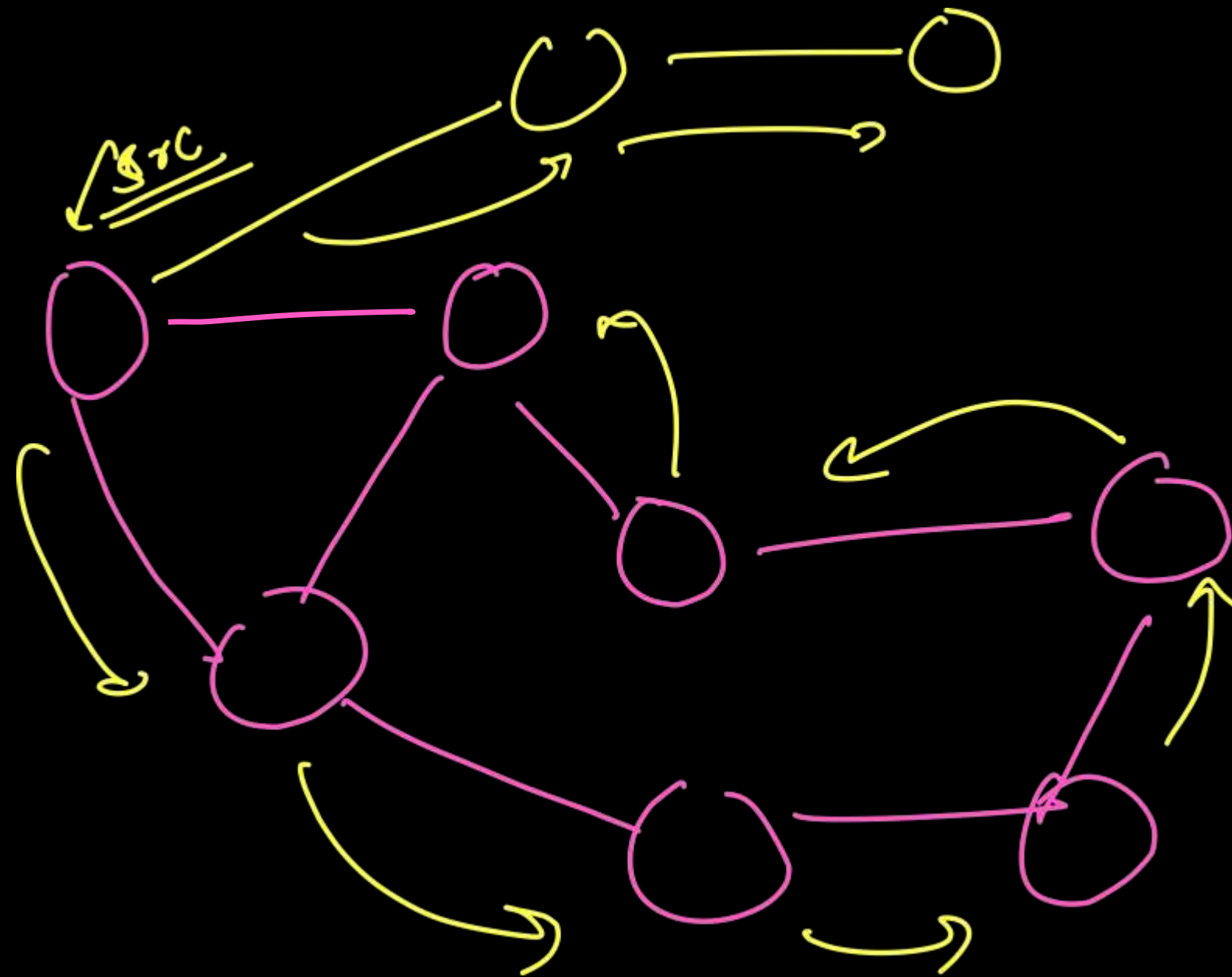
leetcode 947



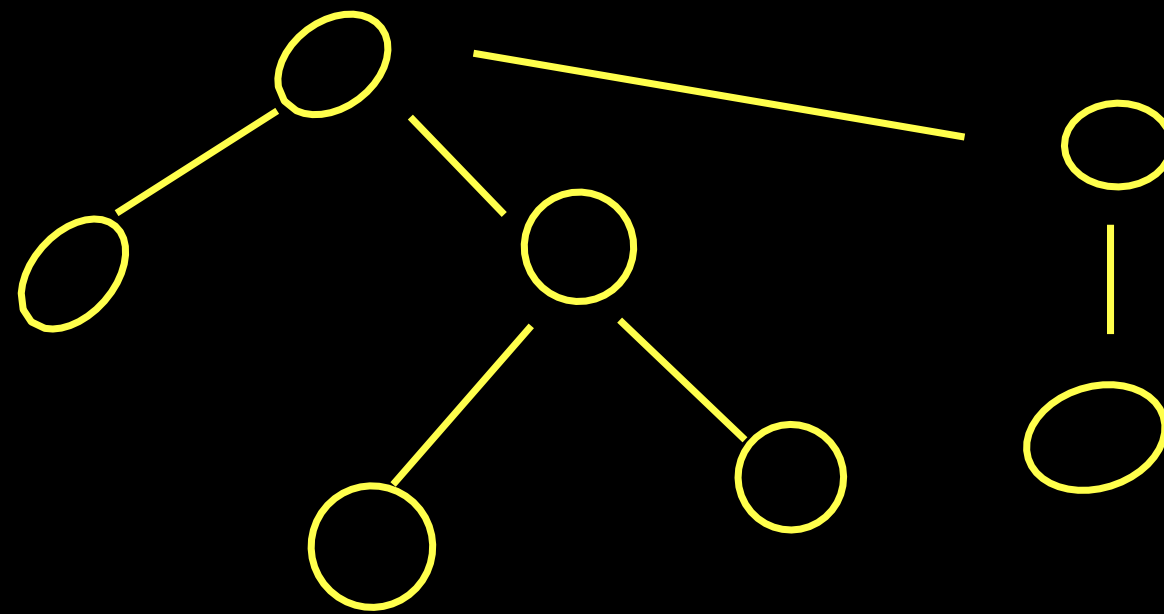


if 2 nodes share their row then they are in a same component or if 2 nodes share their column then they are in a same component

↪ Total nodes ————— no. of cc →

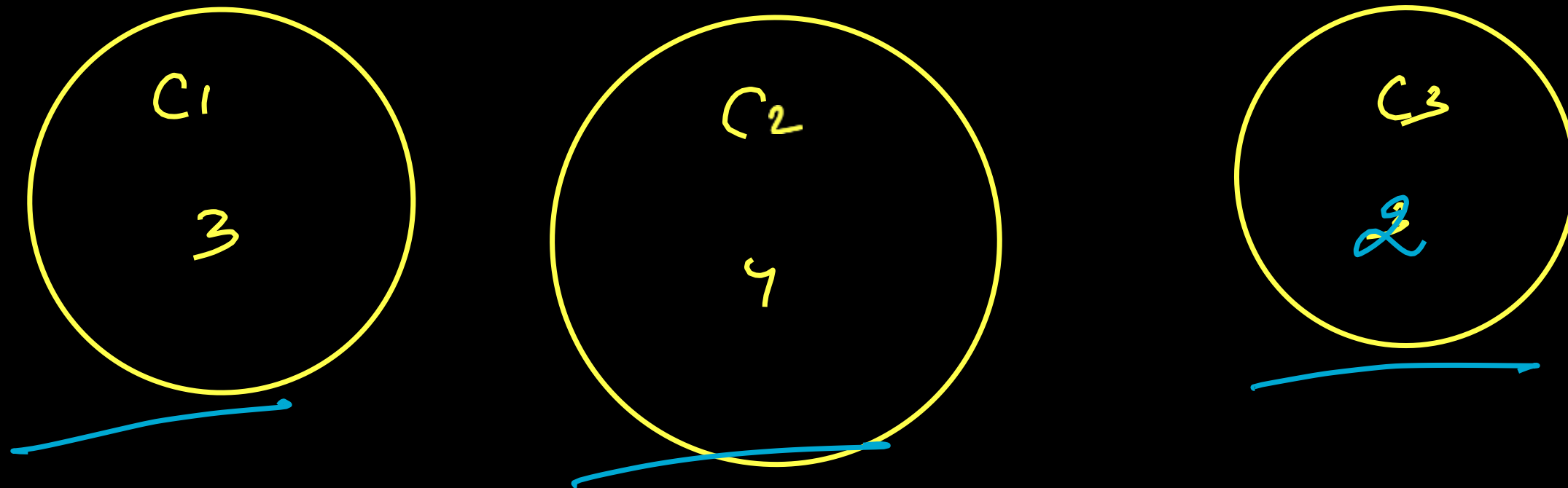


Defn req.



JOIN THE DARKSIDE

↳ Disconnected graph \Rightarrow edge list (DSO) \leftarrow sz of CC



$$3 \times 4 + 4 \times 2 + 3 \times 2$$

CC_1 CC_2 CC_3 " " " "

10^5

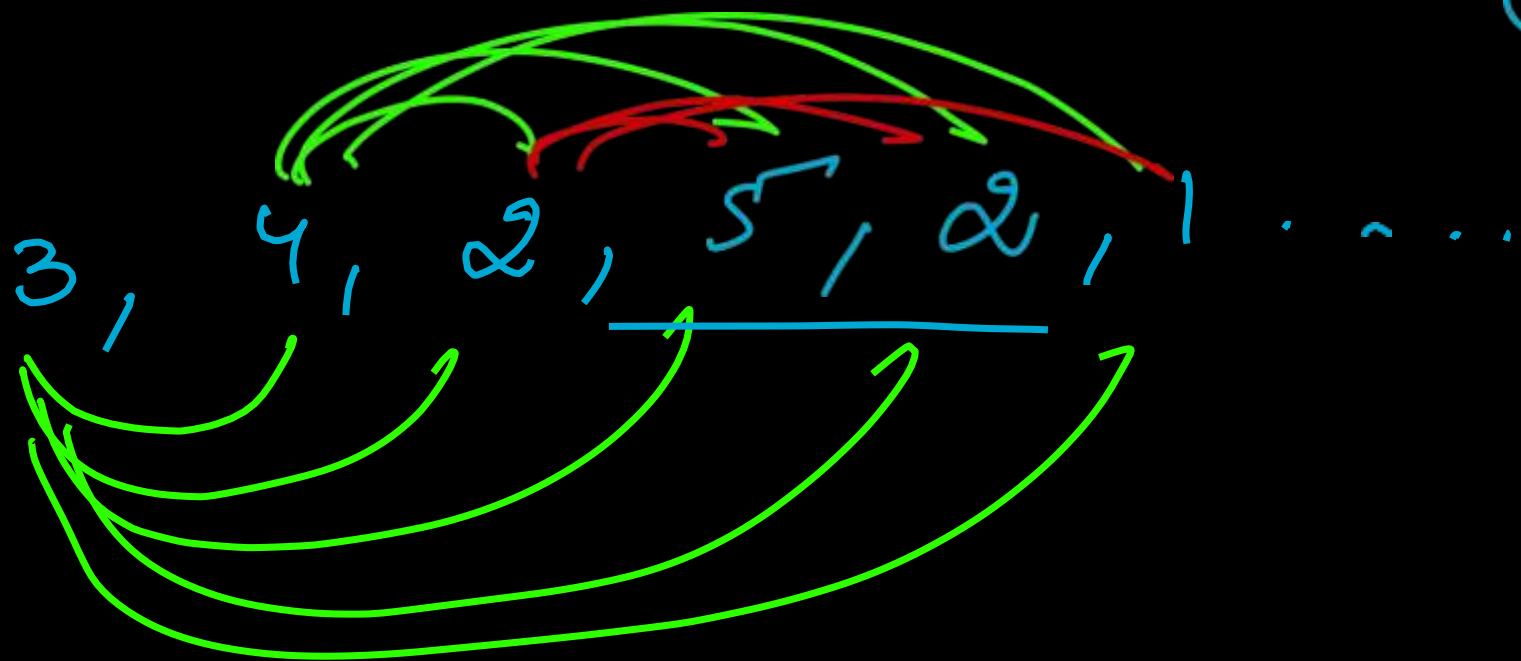
| | | | |
|---|---|---|--|
| 3 | 4 | 2 | |
|---|---|---|--|

n

n^2

df

Suff in sum



$$3 \times (4 + 2 + 5 + 2 + 1)$$

$$3 \times 4 + 3 \times 2 + 3 \times 5 + 3 \times 2 + 3 \times 1$$

$$+ 4 \times 2 + 4 \times 5 + 4 \times 2 + 4 \times 1$$

$$+ 2 \times 5 + 2 \times 2 + 2 \times 1$$

$$+ 5 \times 2 + 5 \times 1$$

$$+ 2 \times 1$$

→ $4(2 + 5 + 2 + 1)$
pairs



▶ **THANK YOU** ◀