

Prefix Sum

Lecture-34

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What is Prefix Sum?

arr =
$$\{1, 4, 5, 3, 2, 7, 6\}$$

pre = $\{1, 5, 10, 13, 15, 22, 28\}$

M-I: $T \cdot C \cdot = O(n^2) \rightarrow no \cdot d_5 \text{ ops} = 1 + 2 + 3 + 4 + \cdots \cdot h$

N-2: Single pass $\rightarrow T \cdot C \cdot O(n)$



Ques: Running sum of 1D Array

[Leetcode - 1480]

a, b, sun

nums =
$$[1,3,6,10]$$
 pre[b] - pre[a-1]

for (i=1 to i=n-1) {

| nums [i] = nums [i] + nums[i-1];

| o | 2 | 3 | 4 | 5 | 6 | 2 | 8

for &x : [9,1,8,6,5,2,4,3,10]

() [9,10,18,24,29,31,35,38,48]



Ques: Check if array can be partitioned into 2 continuous arrays of equal sum.

arr =
$$\{ 1, 2, 3, 4, 5, 6, 7, 8, 9 \}$$

or = $\{ 1, 2, 3, 4, 5, 6, 7, 8, 9 \}$

pre = $\{ 1, 3, 6, 10, 15, 21, 28, 36, 45 \}$

or to x == x+1 to n-1

pre[x] = pre[n-1] - pre[x+1-1]

2** pre[x] = pre[n-1]



Ques: Product of array except self [Leetcode - 238]

$$arr = \{1, 2, 3, 4\}$$

$$ans = \{24, 12, 9, 63\}$$

$$pre = \{1, 2, 6, 24\}$$

$$pre [i] = arr[i]^{+} pre [i-1]$$



Ques: Product of array except self [Leetcode - 238]

arr =
$$\{21, 2, 3, 43\}$$

pre = $\{21, 1, 2, 63\}$
suf = $\{24, 12, 4, 13\}$
ans = $\{24, 12, 8, 63\}$

Concept Anvolved: For Every Element -> product of all other elements = product of all other in left farit * product of all other in right part

Ques: Product of array except self [Leetcode - 238]

nums =
$$\{4, 2, 5, 3\}$$

pre = $\{1, 4, 8, 40\}$
suf = $\{30, 15, 3, 1\}$



$$p = nums[0]$$
 $p = nums[0]$
 $p = y 8 40$
 $suf[n-1] = 1$
 $p = nums[n-1]$
 $p = b 18 30$

Suffix Sum:

arr =
$$\{21, 2, 3, 43\}$$

pre = $\{21, 3, 6, 103\}$
suf = $\{24, 24, 12, 43\}$

Suffix Product:

arr =
$$\{21, 2, 3, 43\}$$

prep = $\{1, 2, 6, 243\}$
sufp = $\{24, 24, 12, 43\}$
ans = $\{24, 12, 8, 63\}$



Ques: Minimum Penalty for a shop [Leetcode - 2483]

Stmma C = 44NY

oth -> band

Penalty - 0, 1, 3 -> 3

st s band new dete

peralty-2

0+1+0+1=2

2^{ml} hour band kaldon

penalty-1

10 bye shop - yes

mbaje 7 th

12 boje -> n0

13 baje 3 yel 14 Jaje - close

Penalty = 01



Ques: Minimum Penalty for a shop [Leetcode - 2483]

After closing the shop > penalty = no of 4 after that how

penalty if we close the shop at nth hour

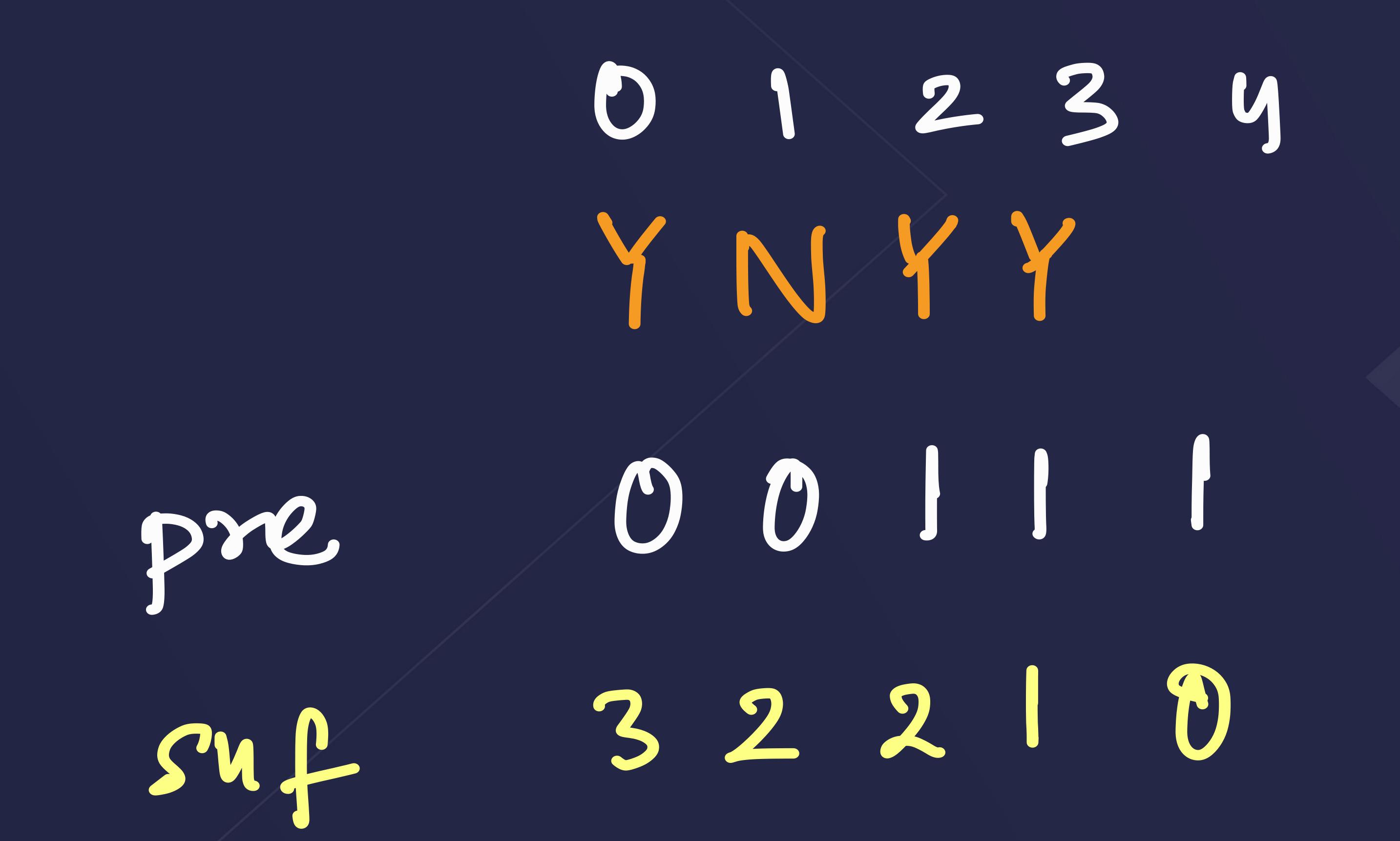
= no. of 'y' > no. of 'N' before nth hour

including & after

non hour

= Y Ka euffix sum + N ka brefix

```
SKILLS
```

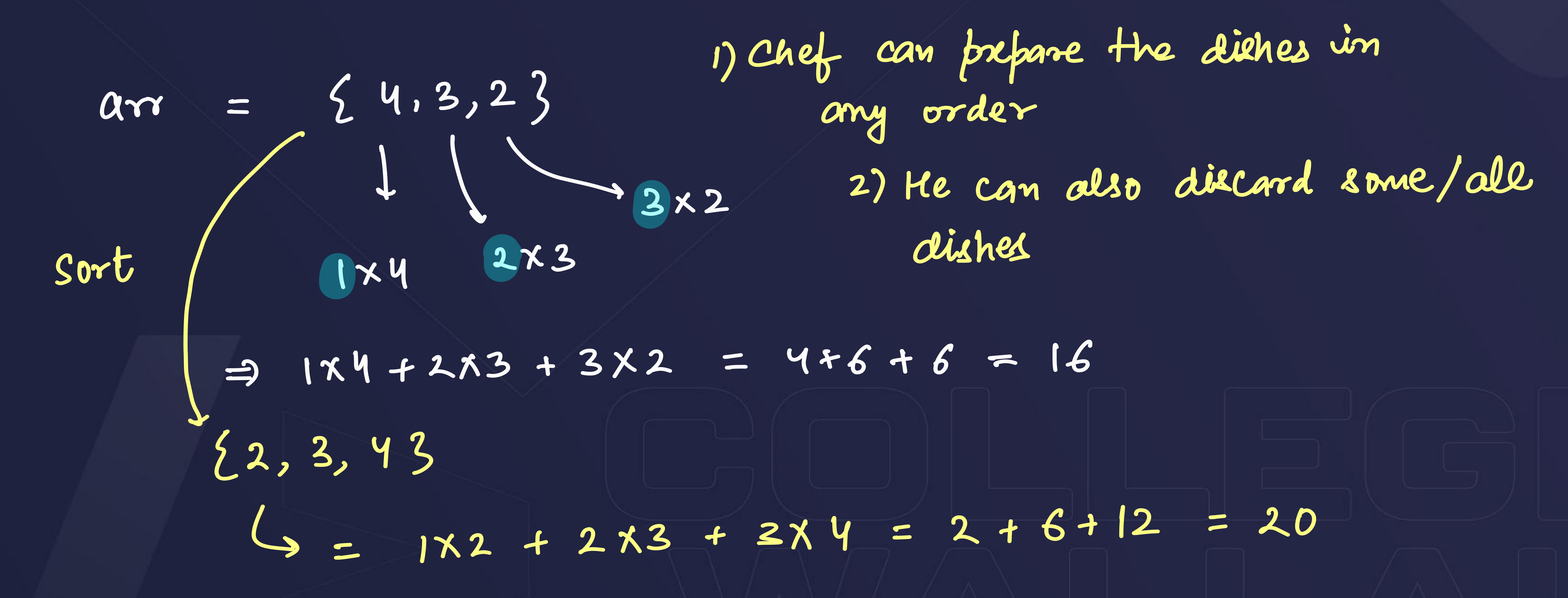






Leetcode – 1402

4 Sorting & Suffix Sum



$$arr = \{\xi-1, -8, 0, 5, -9\}$$

Sort (s arr = $\{\xi-1, -8, -1, 0, 5\}$

$$| \Rightarrow | 1 \times -9 + 2 \times -8 + 3 \times -1 + 4 \times 0 + 5 \times 5 | 0 \rangle$$

$$| \Rightarrow -9 - 16 - 3 + 0 + 2 / 5 | 0 \rangle$$

$$| \Rightarrow -3 \text{ (is bad)}$$

$$\Rightarrow 170 + 275 = 0 + 10 = 10 \text{ (is better)}$$

Leetcode - 1402

$$2-1,0,53$$

$$= 1x-1+2x0+3x5$$

$$= -1+0+15$$

$$= (14)$$

Leetcode - 1402

$$\{-8,-1,0,5\}$$

$$\Rightarrow -8\times1 + -1\times2 + 0\times3 + 5\times4 = -8-2 + 20 = 10$$

• All dishes with the satisfaction values must be taken be some of low dishes with negetive value can be taken.

$$2x+(-9,3,4,5)$$

$$3+(-9,3,4,5)$$

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$$3+($$

Sort (
$$arr = \{2-1, -8, 0, 5, -9\}$$

Suffix ($suffix$ $suff = \{2-13, -4, 4, 5, 5\}$
array $suff = \{2-13, -4, 4, 5, 5\}$



[Leetcode - 1402]



Ques: Longest subsequence with limited sum

```
nums = \{ 4, 5, 2, 13 \}

\{ \text{Sort } (0(n \log n)) \}

nums = \{ 1, 2, 4, 5 \}

\{ \text{prefix Sum } (0(n)) \}

nums = \{ 1, 3, 7, 12 \}
```

```
Den = $1434
```

```
[Leetcode - 2389] (!Pasy)
```

```
queries = \{3,10,213\} \rightarrow m

ans = \{2,3,43\} \rightarrow m
```

```
for(int i=0;i<m;i++){
   int len = 0;
   for(int j=0;j<n;j++){
      if(nums[j]>queries[i]) break;
      len++;
   }
   ans[i] = len;
}
```

[sorting, prefix cum, Binary Fearch]



Ques: Longest subsequence with limited sum Sorting & prefix rum [Leetcode - 2389]

 $nums = \{1, 3, 7, 12\}$

queries =
$$\{3,10,21\} \rightarrow m$$

ans = $\{3,10,21\} \rightarrow m$



Thank you!