

Segment Trees Lecture 1

Today's checklist

- 1. Requirement of Segment Trees
 - 2. Maximum element in a given Range
 - 3. Range Sum Query Mutable
 - 4. Range Frequency Queries



Proequites:

Recursion, Binary Trees, Implementation of Min Heap/ Martleap

What and Why?



User made Data Structure Range Quenies questions can be solved very officiently using Segment trees

$$arr = \begin{cases} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 1, & 4, & 2, & 8, & 6, & 4, & 9, & 3 \end{cases}$$

2rd - 6th index tak Ka maximum 3 9

from 1 to r if 9 want to get max Re than [T.C. = O(r-2)]

What and Why?



what if me have an array & me non multiple quaries on this array,

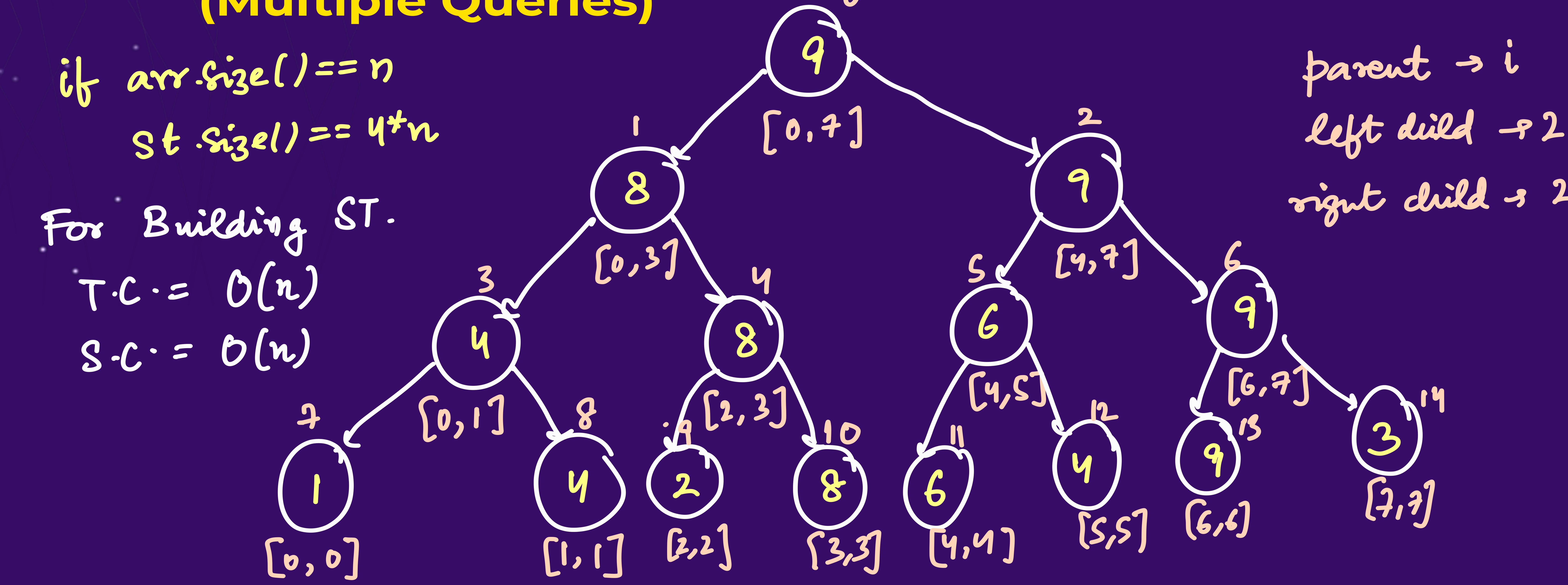
 $arr = \begin{cases} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 1, 4, 2, 8, 6, 4, 9, 3 \end{cases}$

21 11 7 22 72 23 73 24 84

Build Segment Tree



Q1: Find the Maximum element in a given Range. - [2, 7] (Multiple Queries)




left duild -92i+1 nat dull 3 2i+2





Q1: Find the Maximum element in a given Range.

```
vector<int> st;
void buildTree(int arr[], int i, int lo, int hi){
    if(lo==hi){ // base case
       st[i] = arr[lo];
        return;
   int mid = lo + (hi-lo)/2; // (lo+hi)/2
   buildTree(arr,2*i+1,lo,mid); // left subtree
    buildTree(arr,2*i+2,mid+1,hi); // right subtree
   st[i] = max(st[2*i+1], st[2*i+2]);
int main(){
    int arr[] = \{1,4,2,8,6,4,9,3\}; // 0 to 7
    int n = sizeof(arr)/4;
   st.resize(4*n);
    buildTree(arr,0,0,n-1);
```



Outside lie - FNT_MN

lo hi
4 (~< h)

Subset if [lo, hi] = [le, r]

if(lo=2 Ab hiz=r) return (ral)-, stlij

getMax

```
int getMax(int i, int lo, int hi, int& l, int& r){
   if(l>hi || r<lo) return INT_MIN;
   if(lo>=l && hi<=r) return st[i];
   int mid = lo + (hi-lo)/2; // (lo+hi)/2
   int leftMax = getMax(2*i+1,lo,mid,l,r);
   int rightMax = getMax(2*i+2,mid+1,hi,l,r);
   return max(leftMax,rightMax);
}</pre>
```

Homework:



Q: Find the Minimum element in a given Range. - of a given (Multiple Queries) (Almost Same)

What we did - some array - nueltiple quaries

Jet Min (L, Y) update (idx, val) construction

(Mabable)

Ques: Préfix 8nm:
$$T \cdot C \cdot = O(n+q)$$

S· $C \cdot = O(n)$



Q2: Range Sum Query - Mutable

arr =
$$\{1, 4, 2, 8, 6, 4, 9, 3\}$$

Sum from $[2,5] = \text{sum from } [0,5] - \text{sum from } [0,1]$
pre = $\{1, 5, 7, 15, 21, 25, 34, 37\}$
 $[d_{17}] = \text{pre}[r] - \text{pre}[l-1]$

[Leetcode 307]

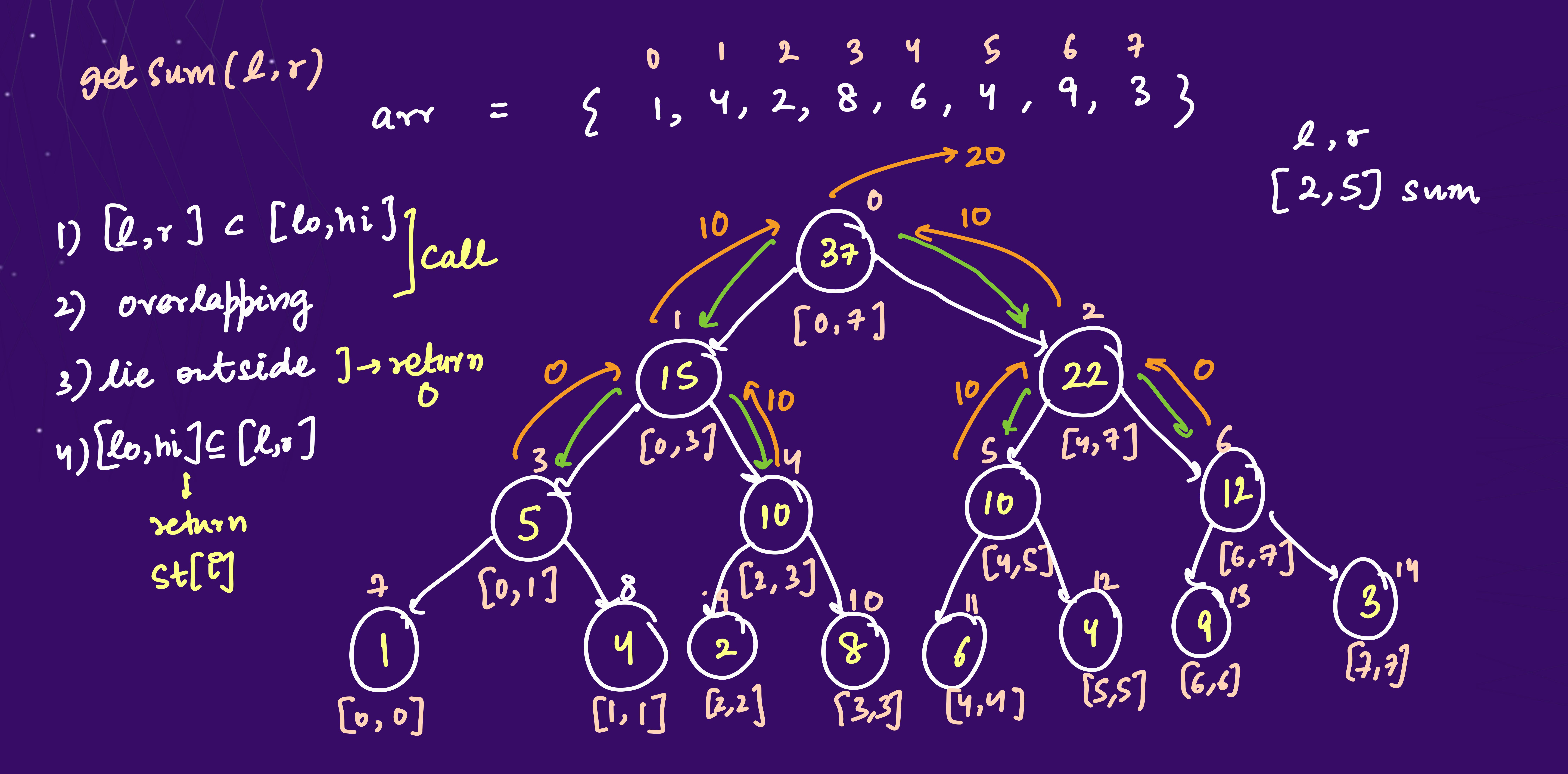
QUES:

$$num3 = \begin{cases} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 1, & 4, & 2, & 8, & 6, & 4, & 9, & 3 \end{cases}$$



Q2: Range Sum Query - Mutable____

$$o(1) = Sum(2,6)$$
 $arr = \{1,5,7,15,21,25,34,37\}$
 $o(1) = Sum(1,4)$
 $o(1) = Sum(0,5)$
 $o(1) = Sum(0,5)$
 $o(1) = update(2,10)$
 $o(n) = update(2,10)$
 $o(n$



 $arr = \{1, 4, 2, 8, 6, 4, 9, 3\}$ idx ral 1 1 1 (3,-2) if(idx=mid) go left 27
[0, 4] else go right

Build Tree

```
.vector<int> st;
int n;
NumArray(vector<int>& nums) {
   n = nums.size();
    st.resize(4*n);
    buildTree(nums,0,0,n-1);
void buildTree(vector<int>& nums, int i, int lo, int hi){
    if(lo==hi){
        st[i] = nums[hi];
        return;
    int mid = lo + (hi-lo)/2;
    buildTree(nums,2*i+1,lo,mid);
    buildTree(nums,2*i+2,mid+1,hi);
    st[i] = st[2*i+1] + st[2*i+2];
```

```
void updateVal(int i, int lo, int hi, int& index, int& val){
   if(lo==hi){
       st[i] = val;
       return;
   int mid = lo + (hi-lo)/2;
   if(index<=mid) updateVal(2*i+1,lo,mid,index,val);
   else updateVal(2*i+2,mid+1,hi,index,val);
   st[i] = st[2*i+1] + st[2*i+2];
void update(int index, int val) { // extra
   updateVal(0,0,n-1,index,val);
  int getSum(int i, int lo, int hi, int& l, int& r){
      if(l>hi || r<lo) return 0;
      if(lo>=1 && hi<=r) return st[i];
      int mid = lo + (hi-lo)/2; // (lo+hi)/2
      int leftSum = getSum(2*i+1,lo,mid,l,r);
      int rightSum = getSum(2*i+2,mid+1,hi,l,r);
       return leftSum + rightSum;
  int sumRange(int left, int right) {
      return getSum(0,0,n-1,left,right);
```

Ques: 2ach node of st will be a map.





Q3: Range Frequency Queries

arr =
$$\{2, 4, 2, 4, 6, 4, 2, 6\}$$

 $\{7, 7, 4, 6, 4, 2, 6\}$
 $\{1, 5, 4\} \rightarrow 3$
ele

[Leetcode 2080]

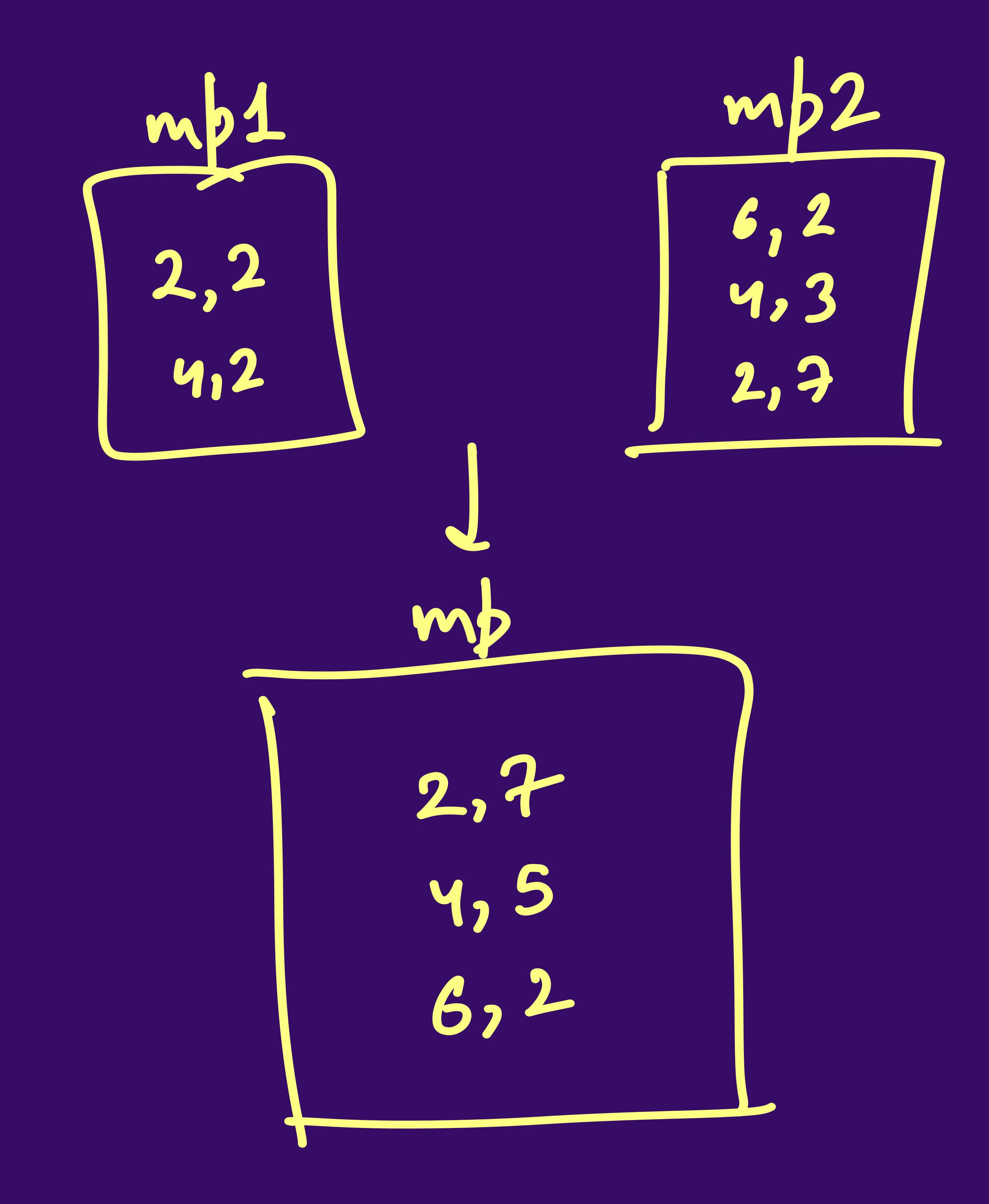




2,5
1

mp. insert (
$$\{2,5\}$$
);

mp[2] = 5



```
vector< unordered_map<int,int> > st;
int n;
unordered_map<int,int> addMaps(unordered_map<int,int>& mp1, unordered_map<int,int>& mp2){
   unordered_map<int,int> mp;
    for(auto x : mp1){
       mp.insert(x);
   for(auto x : mp2){
        int key = x.first, freq = x.second;
        if(mp.find(key)==mp.end()) // key not found in mp
            mp.insert(x);
       else mp[key] += freq;
    return mp;
```

```
void buildTree(vector<int>& arr, int i, int lo, int hi){
    if(lo==hi)
        st[i][arr[lo]] = 1;
                                                       int getFreq(int i, int lo, int hi, int& l, int& r, int& key){
        return;
                                                          if(l>hi | r<lo) return 0;
                                                           if(lo>=1 && hi<=r){
    int mid = lo + (hi-lo)/2;
                                                              if(st[i].find(key)==st[i].end()) return 0;
    buildTree(arr,2*i+1,lo,mid);
                                                              else return st[i][key];
    buildTree(arr,2*i+2,mid+1,hi);
                                                           int mid = lo + (hi-lo)/2; // (lo+hi)/2
    st[i] = addMaps(st[2*i+1],st[2*i+2]);
                                                           int leftAns = getFreq(2*i+1,lo,mid,l,r,key);
                                                           int rightAns = getFreq(2*i+2,mid+1,hi,l,r,key);
                                                           return leftAns + rightAns;
RangeFreqQuery(vector<int>& arr) {
    n = arr.size();
                                                       int query(int left, int right, int value) {
    st.resize(4*n);
                                                           return getFreq(0,0,n-1,left,right,value);
    buildTree(arr,0,0,n-1);
```



JHANK YOU