Week 8 GLM Practical Notes

```
library(tidyverse)
## Warning: package 'tidyverse' was built under R version 4.0.5
## -- Attaching packages ----- tidyverse 1.3.1 --
## v ggplot2 3.3.5
                    v purrr 0.3.4
## v tibble 3.1.0 v dplyr 1.0.5
## v tidyr 1.1.3 v stringr 1.4.0
## v readr 1.4.0 v forcats 0.5.1
## Warning: package 'ggplot2' was built under R version 4.0.5
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
      select
library(GGally)
## Warning: package 'GGally' was built under R version 4.0.5
## Registered S3 method overwritten by 'GGally':
    method from
   +.gg
         ggplot2
library(patchwork)
## Warning: package 'patchwork' was built under R version 4.0.5
## Attaching package: 'patchwork'
## The following object is masked from 'package:MASS':
##
##
      area
```

```
library(rsq)
```

Warning: package 'rsq' was built under R version 4.0.5

```
pub <- read.csv("Data/pub.csv")
# Setting female and married as factors
pub <- pub %>%
  mutate(across(2:3, as.factor))
```

Exploratory analysis

Summary

First, a basic summary of the data. We look for any possible indication of data errors.

```
summary(pub)
```

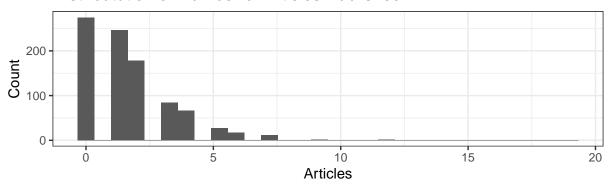
```
##
      articles
                   female married
                                       kids
                                                     prestige
##
  Min. : 0.000
                   0:494 0:309
                                         :0.0000
                                  Min.
                                                       :0.755
  1st Qu.: 0.000
                   1:421 1:606
                                  1st Qu.:0.0000
                                                  1st Qu.:2.260
## Median : 1.000
                                  Median :0.0000
                                                  Median :3.150
                                  Mean :0.4951
## Mean
        : 1.693
                                                  Mean :3.103
## 3rd Qu.: 2.000
                                  3rd Qu.:1.0000
                                                  3rd Qu.:3.920
                                                  Max.
## Max.
         :19.000
                                  Max. :3.0000
                                                        :4.620
##
       mentor
## Min.
         : 0.000
## 1st Qu.: 3.000
## Median: 6.000
## Mean : 8.767
## 3rd Qu.:12.000
## Max.
          :77.000
```

There are some values that appear to be quite high for mentor and articles, but when we look at the overall distribution we see that it is very skewed and so these values are probably not a cause for concern at the moment.

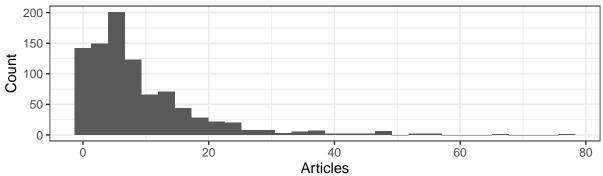
```
y = "Count")
articles_histogram / mentor_histogram
```

```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

Distributution of Number of Articles Published



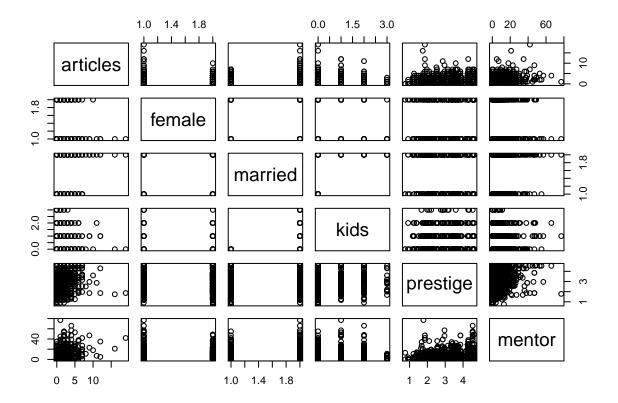
Distributution of Number of Articles Published by Mentor



Pairs plot

A quick look at all the possible associations between the variables:

pairs(pub)

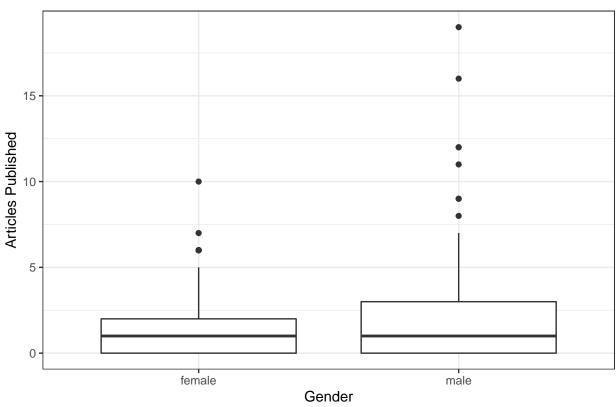


There seems to be more articles/wider spread for males than females. More articles for married than unmarried. Fewer kids more articles. There seems to be some positive relationship between prestige and articles but not extremely strong. The relationship between mentor and articles is somewhat unclear.

There are obvious relationships between some of the explanatory variables. Marriage means higher numbers of kids. The prestige of the program is positively correlated with the output of the mentor.

Boxplots

Male/Female



We see that the median number of publications is similar for men and women but that there is a larger dispersion for the number of articles produced by men.

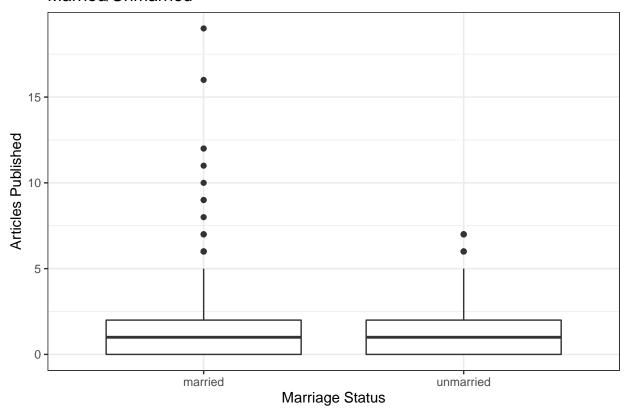
```
mean_articles_f <- pub %>%
  group_by(female) %>%
  summarise(mean = mean(articles)) %>%
  mutate(mean = signif(mean,3))
mean_articles_f

## # A tibble: 2 x 2
## female mean
## <fct> <dbl>
## 1 0     1.88
## 2 1     1.47
```

The mean number of articles is lower for women however.

```
y = "Articles Published")
married_boxplot
```

Married/Unmarried



Larger spread for people who are married but again similar median.

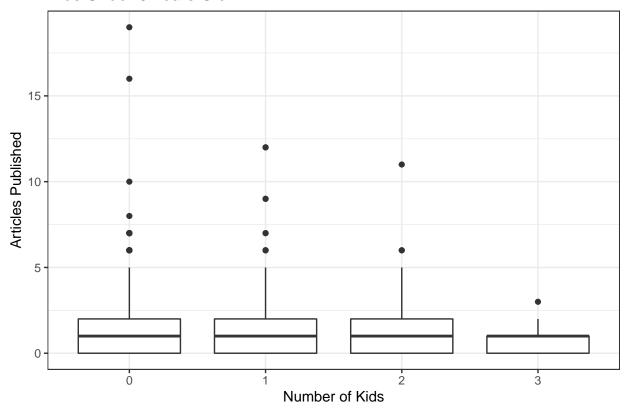
```
mean_articles_married <- pub %>%
  group_by(married) %>%
  summarise(mean = mean(articles)) %>%
  mutate(mean = signif(mean,3))

mean_articles_married
```

Married people have a higher mean output, but the difference is smaller.

```
kids_boxplot <- pub %>%
ggplot() +
geom_boxplot(aes(x = as.factor(kids), y = articles)) +
```

Kids Under 6 Years Old



Larger spread of articles for individuals with fewer children. $\,$

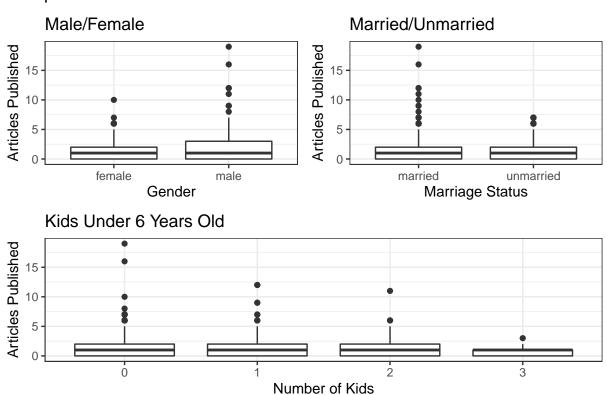
```
mean_articles_kids <- pub %>%
  group_by(kids) %>%
  summarise(mean = mean(articles)) %>%
  mutate(mean = signif(mean,3))

mean_articles_kids
```

```
## # A tibble: 4 x 2
## kids mean
## <int> <dbl>
## 1 0 1.72
## 2 1 1.76
## 3 2 1.54
## 4 3 0.812
```

```
(female_boxplot + married_boxplot) / kids_boxplot +
plot_annotation(
   title = "Comparison Over Factor Levels of Articles Published"
)
```

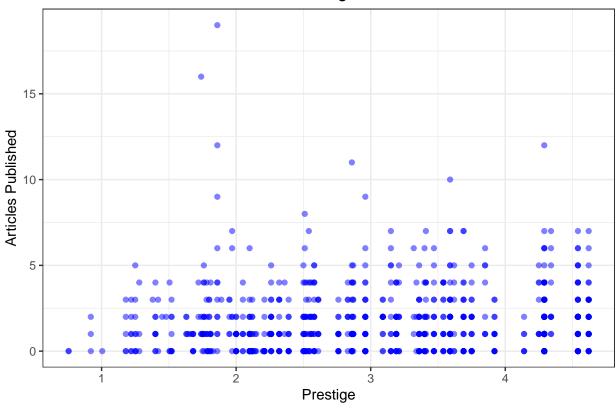
Comparison Over Factor Levels of Articles Published



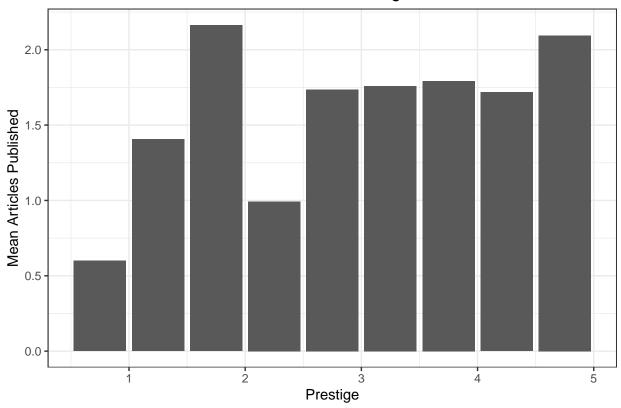
Highest output from individuals with one child, then the number of articles drops off. Since the relationship between number of kids and articles is not monotonic, it is probably best to treat the number of children as a factor.

```
pub$kids <- as.factor(pub$kids)</pre>
```

Number of Articles Published vs Prestige

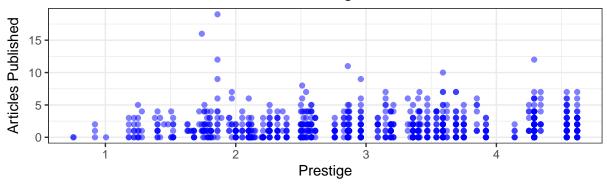


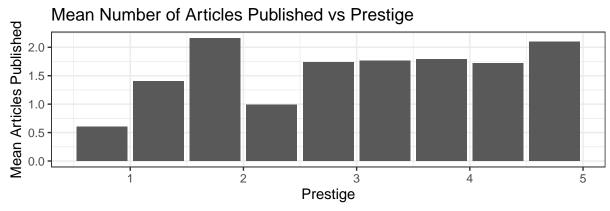
Mean Number of Articles Published vs Prestige



prestige_points / prestige_colplot

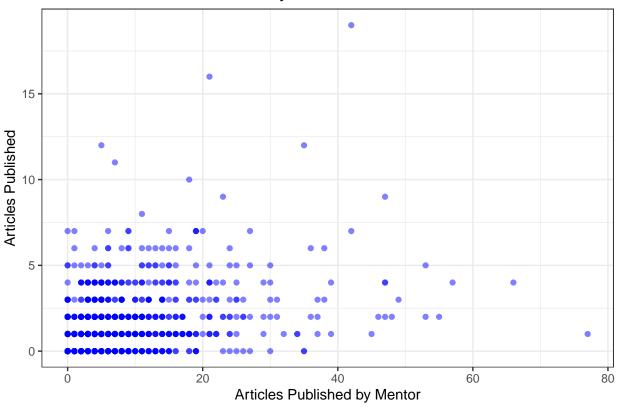
Number of Articles Published vs Prestige



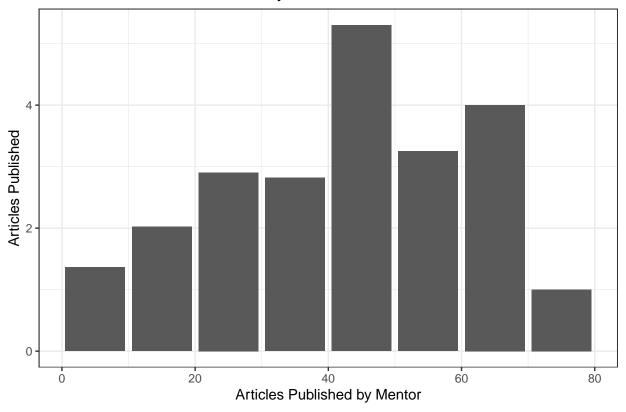


Grouping prestige into 0.5 unit increments and taking the mean we see that the mean number of publications seems to increase slightly with prestige.

Number of Articles Published by Mentor vs Number of Articles Published

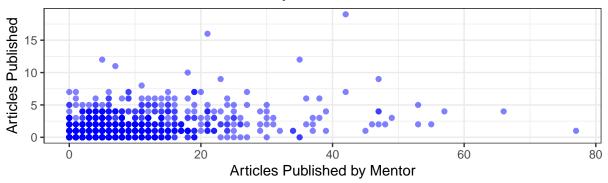


Number of Articles Published by Mentor vs Mean Number of Articles Publish

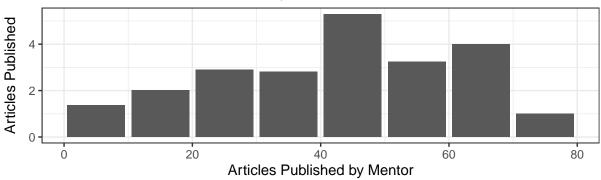


mentor_points / mentor_colplot

Number of Articles Published by Mentor vs Number of Articles Published



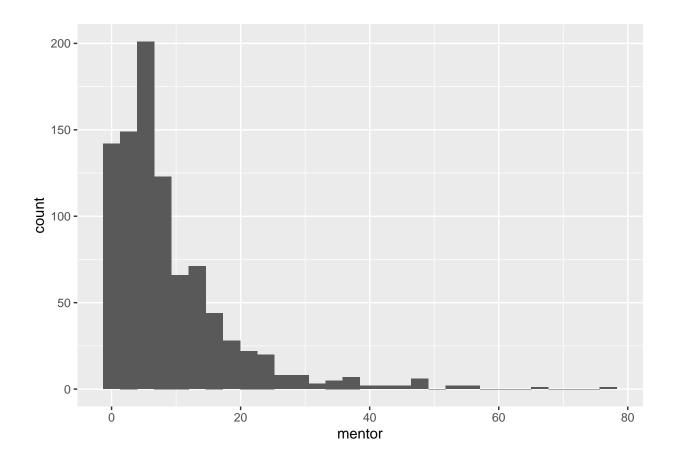
Number of Articles Published by Mentor vs Mean Number of Articles Publis



Grouping the number of articles published by mentors into intervals of 10 articles, there appears to be some positive relationship between the mean number of articles produced by PhD candidates and output of their mentors but the relationship is not particularly clear. There is also very sparse data at the end of the series.

```
pub %>%
  ggplot(aes(x = mentor)) +
  geom_histogram()
```

'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



Model Fitting

```
pub.glm <- glm(articles ~ 1 + female + married + kids + prestige + mentor +</pre>
                female*(married + kids + prestige + mentor),
              data = pub,
              family = poisson)
summary(pub.glm)
##
## Call:
## glm(formula = articles ~ 1 + female + married + kids + prestige +
      mentor + female * (married + kids + prestige + mentor), family = poisson,
##
##
      data = pub)
##
## Deviance Residuals:
##
                    Median
                                3Q
      Min
               1Q
                                        Max
## -3.7415 -1.5570 -0.3722 0.5641
                                     5.3047
##
## Coefficients:
##
                   Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                   0.513401 0.136150
                                       3.771 0.000163 ***
## female1
```

```
## married1
                     0.093216
                                0.090495
                                           1.030 0.302981
## kids1
                                          -2.181 0.029183 *
                    -0.187308
                                0.085881
## kids2
                    -0.272641
                                0.103798
                                          -2.627 0.008623 **
## kids3
                    -0.829794
                                          -2.816 0.004864 **
                                0.294683
## prestige
                    -0.041905
                                0.034074
                                          -1.230 0.218774
## mentor
                     0.025854
                                0.002289
                                          11.297 < 2e-16 ***
                                           0.700 0.484077
## female1:married1
                     0.088610
                                0.126630
## female1:kids1
                     0.028791
                                0.155220
                                           0.185 0.852851
## female1:kids2
                    -0.231699
                                0.233793
                                          -0.991 0.321663
## female1:kids3
                     0.308019
                                1.044513
                                           0.295 0.768076
## female1:prestige 0.133147
                                0.055437
                                           2.402 0.016317 *
                                0.004936
## female1:mentor
                    -0.001124
                                          -0.228 0.819832
##
                   0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 1817.4 on 914
                                      degrees of freedom
## Residual deviance: 1625.6 on 901 degrees of freedom
## AIC: 3321.4
##
## Number of Fisher Scoring iterations: 5
```

Being female significant negative effect, as expected. Being married has a slight positive effect but it is not statistically significant; although it looked on the exploratory plots that there might be a difference, the means were quite similar so this seems to make sense. Having children has a statistically significant negative effect, as we would expect given the plots. Somewhat surprisingly, prestige does not have a statistically significant effect in the model, but the output of the mentor has a slight positive effect.

None of the interactions appear significant apart from female1:prestige which has a slight positive effect.

AIC model selection

```
## Start: AIC=3487.15
## articles ~ 1
##
##
              Df Deviance
                              AIC
                   1669.5 3341.3
## + mentor
               1
                    1794.4 3466.1
## + female
               1
## + prestige
               1
                   1806.6 3478.3
## + kids
               3
                   1806.1 3481.8
## + married
               1
                   1814.6 3486.3
```

```
## <none>
          1817.4 3487.1
##
## Step: AIC=3341.29
## articles ~ mentor
##
             Df Deviance
                            AIC
## + female
            1 1657.0 3330.7
              3 1658.6 3336.4
## + kids
## <none>
                  1669.5 3341.3
## + married 1
                1667.6 3341.4
## + prestige 1 1669.3 3343.1
## Step: AIC=3330.74
## articles ~ mentor + female
##
##
                  Df Deviance
                                AIC
## + kids
                   3 1638.9 3318.6
## <none>
                       1657.0 3330.7
## + married
                     1656.7 3332.4
                   1
                     1656.8 3332.6
## + prestige
                   1
## + female:mentor 1
                       1657.0 3332.7
## Step: AIC=3318.64
## articles ~ mentor + female + kids
##
                  Df Deviance
## + married
                   1 1633.3 3315.1
                       1638.9 3318.6
## <none>
                      1638.8 3320.5
## + female:mentor 1
                       1638.8 3320.6
## + prestige
                   1
## + female:kids
                   3
                      1637.6 3323.3
##
## Step: AIC=3315.07
## articles ~ mentor + female + kids + married
##
                   Df Deviance
##
                                 AIC
## <none>
                       1633.3 3315.1
## + female:married 1
                      1633.1 3316.8
## + prestige
                    1
                       1633.1 3316.8
## + female:mentor
                    1 1633.2 3317.0
## + female:kids
                    3 1632.0 3319.8
##
## Call: glm(formula = articles ~ mentor + female + kids + married, family = poisson,
##
      data = pub)
## Coefficients:
## (Intercept)
                    mentor
                               female1
                                              kids1
                                                           kids2
                                                                       kids3
                   0.02557
                              -0.22597
                                         -0.18031
##
      0.34765
                                                        -0.32775
                                                                     -0.82152
##
     married1
##
      0.14812
## Degrees of Freedom: 914 Total (i.e. Null); 908 Residual
## Null Deviance:
                      1817
```

```
## Residual Deviance: 1633 AIC: 3315
```

Using forward selection we get the formula: articles \sim mentor + female + kids + married.

```
stepAIC(pub.glm,
       scope = list(lower = pub.glm.null, upper = pub.glm),
       data = pub,
       direction = "backward")
## Start: AIC=3321.36
## articles ~ 1 + female + married + kids + prestige + mentor +
      female * (married + kids + prestige + mentor)
##
                    Df Deviance
##
                                  AIC
## - female:kids
                     3 1626.9 3316.6
## - female:mentor
                     1
                       1625.7 3319.4
## - female:married 1 1626.1 3319.9
## <none>
                         1625.6 3321.4
## - female:prestige 1
                         1631.4 3325.2
##
## Step: AIC=3316.64
## articles ~ female + married + kids + prestige + mentor + female:married +
##
      female:prestige + female:mentor
##
##
                    Df Deviance
## - female:mentor
                     1 1627.0 3314.8
## - female:married
                       1627.3 3315.0
                     1
                         1626.9 3316.6
## <none>
## - female:prestige 1 1632.8 3320.6
                     3
                        1649.0 3332.7
## - kids
##
## Step: AIC=3314.79
## articles ~ female + married + kids + prestige + mentor + female:married +
##
      female:prestige
##
##
                    Df Deviance
                                  AIC
## - female:married
                     1 1627.4 3313.2
## <none>
                         1627.0 3314.8
## - female:prestige 1
                         1632.9 3318.6
## - kids
                     3
                        1649.3 3331.0
## - mentor
                       1757.2 3442.9
                     1
## Step: AIC=3313.18
## articles ~ female + married + kids + prestige + mentor + female:prestige
##
##
                    Df Deviance
                                  AIC
## <none>
                         1627.4 3313.2
                       1632.2 3316.0
## - married
                     1
                       1633.1 3316.8
## - female:prestige 1
                        1651.0 3330.8
## - kids
                     3
## - mentor
                   1 1757.5 3441.2
```

```
## Call: glm(formula = articles ~ female + married + kids + prestige +
##
      mentor + female:prestige, family = poisson, data = pub)
##
## Coefficients:
##
        (Intercept)
                             female1
                                               married1
                                                                    kids1
           0.47391
                            -0.63170
                                              0.13862
                                                                 -0.18735
##
                                              prestige
             kids2
                                                                   mentor
##
                               kids3
           -0.32483
                            -0.82756
                                              -0.03619
                                                                  0.02542
##
## female1:prestige
##
           0.12655
##
## Degrees of Freedom: 914 Total (i.e. Null); 906 Residual
## Null Deviance:
                       1817
## Residual Deviance: 1627 AIC: 3313
Using backward selection, the formula selected is:
articles ~ female + married + kids + prestige + mentor + female:prestige.
stepAIC(pub.glm.null,
       scope = list(lower = pub.glm.null, upper = pub.glm),
       data = pub,
       direction = "both")
## Start: AIC=3487.15
## articles ~ 1
##
##
             Df Deviance
                            AIC
## + mentor
              1 1669.5 3341.3
## + female
              1
                 1794.4 3466.1
## + prestige 1
                 1806.6 3478.3
## + kids
              3
                 1806.1 3481.8
## + married 1 1814.6 3486.3
## <none>
                  1817.4 3487.1
##
## Step: AIC=3341.29
## articles ~ mentor
##
##
             Df Deviance
                            AIC
            1 1657.0 3330.7
## + female
## + kids
              3 1658.6 3336.4
                  1669.5 3341.3
## <none>
## + married 1 1667.6 3341.4
## + prestige 1
                  1669.3 3343.1
## - mentor
              1
                  1817.4 3487.1
##
## Step: AIC=3330.74
## articles ~ mentor + female
##
##
                  Df Deviance
                                  AIC
## + kids
                   3 1638.9 3318.6
## <none>
                        1657.0 3330.7
## + married
                      1656.7 3332.4
                   1 1656.8 3332.6
## + prestige
```

```
## + female:mentor 1 1657.0 3332.7
## - female 1 1669.5 3341.3
## - mentor
                  1 1794.4 3466.1
##
## Step: AIC=3318.64
## articles ~ mentor + female + kids
##
##
                  Df Deviance
                                AIC
## + married
                   1 1633.3 3315.1
## <none>
                      1638.9 3318.6
## + female:mentor 1 1638.8 3320.5
                  1 1638.8 3320.6
## + prestige
## + female:kids
                      1637.6 3323.3
                   3
## - kids
                   3 1657.0 3330.7
## - female
                  1 1658.6 3336.4
## - mentor
                  1
                      1775.9 3453.6
##
## Step: AIC=3315.07
## articles ~ mentor + female + kids + married
##
                   Df Deviance
                                 AIC
## <none>
                       1633.3 3315.1
## + female:married 1 1633.1 3316.8
## + prestige
                   1 1633.1 3316.8
## + female:mentor 1 1633.2 3317.0
## - married 1 1638.9 3318.6
## + female:kids
                    3 1632.0 3319.8
## - female
                   1 1650.5 3330.3
                    3 1656.7 3332.4
## - kids
                   1 1772.5 3452.2
## - mentor
##
## Call: glm(formula = articles ~ mentor + female + kids + married, family = poisson,
##
      data = pub)
##
## Coefficients:
## (Intercept)
                   mentor
                              female1
                                             kids1
                                                          kids2
                                                                       kids3
                              -0.22597
                   0.02557
                                           -0.18031
##
      0.34765
                                                       -0.32775
                                                                    -0.82152
##
     married1
      0.14812
##
## Degrees of Freedom: 914 Total (i.e. Null); 908 Residual
## Null Deviance:
                       1817
## Residual Deviance: 1633 AIC: 3315
So the question, how do we select between these models?
Test for inclusion of prestige
pub.glm.noprestige <- glm(articles ~ 1 + female + married + kids + mentor,</pre>
```

pub.glm.prestige <- glm(articles ~ 1 + female + married + kids + mentor + prestige,</pre>

data = pub,

data = pub,

family = poisson)

```
family = poisson)
dof <- pub.glm.prestige$rank - pub.glm.noprestige$rank
lrt <- deviance (pub.glm.noprestige) - deviance(pub.glm.prestige)
pval <- 1 - pchisq(lrt,dof)
cbind(lrt,dof,pval)</pre>
```

```
## lrt dof pval
## [1,] 0.2325111 1 0.6296681
```

Just including prestige is not significant.

```
## lrt dof pval
## [1,] 5.893019 2 0.05252273
```

The hypothesis test suggests that there is a significant effect for including both prestige and female at the 10% significance level.

Let us include the prestige and female*prestige term since it has a borderline significant effect which we may want to examine in our analysis.

Marriage may not be significant, so let us test for it:

```
## lrt dof pval
## [1,] 5.571698 1 0.01825305
```

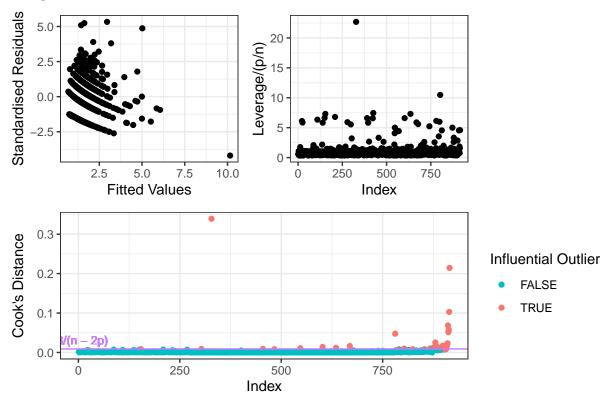
Final model:

Diagnostics

Here are the diagnostic plots for the model: standardised residuals, leverage and Cook's distances.

```
# Number of coefficients in the model
p <- pub.glm.selected$rank</pre>
# Number of observations
n <- nrow(model.frame(pub.glm.selected))</pre>
r_standard_plot <- data.frame(fitted_values = fitted(pub.glm.selected),</pre>
           r_standard = rstandard(pub.glm.selected)) %>%
  ggplot(aes(x = fitted_values, y = r_standard)) +
  geom point() +
  theme bw() +
  labs(x = "Fitted Values", y = "Standardised Residuals")
influence_plot <- data.frame(influence = influence(pub.glm.selected)$hat/(p/n),</pre>
           index = 1:length(influence(pub.glm.selected)$hat)) %>%
  ggplot(aes(x = index, y = influence)) +
  geom_point() +
  theme_bw() +
  labs(x = "Index", y = "Leverage/(p/n)")
cooks bound \leftarrow 8 / (n - 2 * p)
cooks_distance_plot <- data.frame(cooks_distance = cooks.distance(pub.glm.selected),</pre>
                                   index = 1:n) %>%
  # Select slightly below the bound to be influential outliers in the plot too
  mutate(influential_outlier = cooks_distance >= cooks_bound - 0.001) %>%
  ggplot() +
  geom_point(aes(x = index, y = cooks_distance, colour = influential_outlier)) +
  geom_hline(aes(yintercept = cooks_bound), colour = "#C77CFF") +
  geom_text(aes(x = 10, y = cooks_bound, label = "8/(n - 2p)", vjust = -0.5),
            size = 3, colour = "#C77CFF") +
  theme_bw() +
  scale_colour_manual(name = "Influential Outlier", values = c("#00BFC4","#F8766D")) +
  labs(x = "Index", y = "Cook's Distance")
(r_standard_plot + influence_plot) / cooks_distance_plot +
  plot_annotation(
    title = "Diagnostic Plots for the Selected Model"
```

Diagnostic Plots for the Selected Model



If we remove the "influential outliers", this causes some changes to the analysis:

```
# These are the indices of the points which are above the bound for Cook's distance which(cooks.distance(pub.glm.selected) > 8/(n-2*p))
```

```
## 328 455 547 602 635 669 781 803 867 871 878 879 880 883 887 890 892 893 895 896 ## 328 455 547 602 635 669 781 803 867 871 878 879 880 883 887 890 892 893 895 896 ## 898 899 900 903 904 907 908 909 910 911 912 913 914 915 ## 898 899 900 903 904 907 908 909 910 911 912 913 914 915
```

```
##
## Call: glm(formula = articles ~ 1 + female + married + kids + prestige +
## mentor + female * (married + kids + prestige + mentor), family = poisson,
```

```
##
      data = pub2)
##
## Coefficients:
       (Intercept)
                                              married1
##
                            female1
                                                                   kids1
##
          0.172387
                           -0.297644
                                              0.084918
                                                               -0.156762
##
             kids2
                               kids3
                                              prestige
                                                                 mentor
##
         -0.233044
                           -1.315832
                                              0.017901
                                                                0.027858
                     female1:kids1
                                         female1:kids2
## female1:married1
                                                           female1:kids3
##
          0.065173
                            0.039737
                                             -0.355084
                                                                0.878977
                      female1:mentor
## female1:prestige
##
          0.049186
                           -0.005856
##
## Degrees of Freedom: 880 Total (i.e. Null); 867 Residual
## Null Deviance:
                       1429
## Residual Deviance: 1298 AIC: 2872
```

Looking to see if there is any difference in automatic model selection:

```
## Start: AIC=2976.58
## articles ~ 1
##
             Df Deviance
##
                           AIC
## + mentor 1 1332.5 2882.1
## + prestige 1 1411.8 2961.5
## + kids
              3 1413.5 2967.1
## + female
              1 1419.8 2969.4
## <none>
                 1429.0 2976.6
## + married 1 1428.5 2978.1
##
## Step: AIC=2882.11
## articles ~ mentor
##
             Df Deviance
##
                          AIC
## + kids
              3 1318.0 2873.6
## + female
              1 1326.9 2878.6
## <none>
                 1332.5 2882.1
## + prestige 1
                  1330.7 2882.3
## + married
                 1331.9 2883.5
             1
##
## Step: AIC=2873.57
## articles ~ mentor + kids
##
##
             Df Deviance
                           AIC
## + female 1 1307.5 2865.2
```

```
## + married 1 1313.6 2871.2
                 1318.0 2873.6
## <none>
## + prestige 1 1316.2 2873.8
##
## Step: AIC=2865.16
## articles ~ mentor + kids + female
##
##
                  Df Deviance
                                AIC
## + married
                  1 1304.6 2864.2
## <none>
                      1307.5 2865.2
## + prestige
                  1
                     1306.0 2865.7
## + female:mentor 1
                      1306.8 2866.4
## + female:kids
                   3
                      1304.4 2868.1
##
## Step: AIC=2864.21
## articles ~ mentor + kids + female + married
##
##
                   Df Deviance
                                 AIC
                       1304.6 2864.2
## <none>
                      1302.8 2864.4
## + prestige
## + female:mentor 1 1303.8 2865.4
## + female:married 1 1304.4 2866.0
## + female:kids
                   3 1301.4 2867.1
##
## Call: glm(formula = articles ~ mentor + kids + female + married, family = poisson,
      data = pub2)
##
## Coefficients:
## (Intercept)
                                 kids1
                                              kids2
                                                          kids3
                                                                    female1
                   mentor
      0.22852
                   0.02677
                              -0.15225
                                           -0.30705
##
                                                       -1.23641
                                                                    -0.17462
##
     married1
      0.11554
##
##
## Degrees of Freedom: 880 Total (i.e. Null); 874 Residual
## Null Deviance:
                      1429
## Residual Deviance: 1305 AIC: 2864
stepAIC(pub.glm2,
       scope = list(lower = pub.glm2.null, upper = pub.glm2),
       data = pub2,
       direction = "backward")
## Start: AIC=2871.91
## articles ~ 1 + female + married + kids + prestige + mentor +
##
      female * (married + kids + prestige + mentor)
##
                    Df Deviance AIC
##
                     3 1301.1 2868.7
## - female:kids
## - female:married
                   1 1298.5 2870.1
## - female:prestige 1 1299.0 2870.6
## - female:mentor 1 1299.3 2870.9
## <none>
                        1298.3 2871.9
```

```
##
## Step: AIC=2868.74
## articles ~ female + married + kids + prestige + mentor + female:married +
      female:prestige + female:mentor
##
##
                   Df Deviance
## - female:married 1 1301.2 2866.9
## - female:prestige 1 1301.8 2867.4
## - female:mentor 1 1302.5 2868.1
## <none>
                        1301.1 2868.7
## - kids
                    3 1322.2 2883.8
##
## Step: AIC=2866.86
## articles ~ female + married + kids + prestige + mentor + female:prestige +
      female:mentor
##
##
                   Df Deviance
                                  AIC
## - female:prestige 1 1301.9 2865.5
## - female:mentor
                    1 1302.6 2866.2
                        1301.2 2866.9
## <none>
## - married
                   1 1304.3 2867.9
## - kids
                    3 1323.1 2882.7
##
## Step: AIC=2865.5
## articles ~ female + married + kids + prestige + mentor + female:mentor
##
                 Df Deviance
                                AIC
## - female:mentor 1 1302.8 2864.4
                 1 1303.8 2865.4
## - prestige
                      1301.9 2865.5
## <none>
                 1 1305.2 2866.8
## - married
## - kids
                  3 1323.7 2881.3
##
## Step: AIC=2864.41
## articles ~ female + married + kids + prestige + mentor
            Df Deviance
                           AIC
## - prestige 1 1304.6 2864.2
## <none>
                 1302.8 2864.4
## - married 1 1306.0 2865.7
## - female 1 1311.5 2871.1
              3 1325.0 2880.7
## - kids
## - mentor
             1 1380.7 2940.3
##
## Step: AIC=2864.21
## articles ~ female + married + kids + mentor
##
##
            Df Deviance
                          AIC
## <none>
                1304.6 2864.2
## - married 1
               1307.5 2865.2
## - female 1 1313.6 2871.2
## - kids 3 1326.9 2880.5
## - mentor 1 1397.0 2954.6
```

```
##
## Call: glm(formula = articles ~ female + married + kids + mentor, family = poisson,
       data = pub2)
##
##
## Coefficients:
   (Intercept)
##
                    female1
                                married1
                                                 kids1
                                                              kids2
                                                                            kids3
       0.22852
                   -0.17462
                                 0.11554
                                              -0.15225
                                                            -0.30705
                                                                         -1.23641
##
##
        mentor
##
       0.02677
##
## Degrees of Freedom: 880 Total (i.e. Null); 874 Residual
## Null Deviance:
                        1429
## Residual Deviance: 1305 AIC: 2864
```

I do not think that there is a good justification for removing influential outliers from the analysis. I cannot think of a good reason that the information would be incorrectly recorded other than a few minor counting errors.

Model quality

This is a Poisson model so a goodness of fit test can be appropriate, however the counts are quite small. The deviance is given by $D(y) \sim \chi^2(n-p)$ under \mathcal{H}_0 . Here n = 915 and p = 92

```
# Goodness of fit for the model without outliers excluded
deviance(pub.glm.prestige)

## [1] 1627.437

dim(pub)[1] - pub.glm.prestige$rank

## [1] 906

qchisq(0.95,dim(pub)[1] - pub.glm.prestige$rank)

## [1] 977.1359

# Goodness of fit for the model with outliers excluded
deviance(pub.glm2)

## [1] 1298.294

dim(pub2)[1] - pub.glm2$rank

## [1] 867

qchisq(0.95,dim(pub2)[1] - pub.glm2$rank)

## [1] 936.6119
```

This is not a good fit. With outliers removed it is still not a good fit.

Here we are looking at the R_{KL}^2 value:

```
rsq(pub.glm.selected,type = "kl")
## [1] 0.104527
rsq(pub.glm2,type = "kl")
## [1] 0.09144423
```

Without removing the data the R_{KL}^2 is better for the first model. It is quite close to 0, so the model really does not capture a lot of the variation in the data.

Interpretation

Confidence intervals at 95% level:

```
##
                                        upper exp_estimate exp_lower exp_upper
                    estimate
                               lower
## female1
                     -0.6320 -0.9850 -0.2780
                                                     0.532
                                                               0.373
                                                                          0.757
                                                     1.150
## married1
                      0.1390 0.0146 0.2630
                                                               1.010
                                                                          1.300
## kids1
                     -0.1870 -0.3260 -0.0486
                                                     0.829
                                                               0.722
                                                                          0.953
                     -0.3250 -0.5030 -0.1470
                                                     0.723
                                                               0.605
## kids2
                                                                          0.864
## kids3
                     -0.8280 -1.3800 -0.2750
                                                     0.437
                                                               0.252
                                                                          0.759
## mentor
                      0.0254 0.0215 0.0294
                                                     1.030
                                                               1.020
                                                                          1.030
## prestige
                     -0.0362 -0.1020 0.0294
                                                     0.964
                                                               0.903
                                                                          1.030
## female1:prestige 0.1270 0.0221 0.2310
                                                     1.130
                                                               1.020
                                                                          1.260
##
                            rownames
## female1
                             female1
## married1
                            married1
## kids1
                               kids1
```

```
## kids2 kids2
## kids3 kids3
## mentor mentor
## prestige prestige
## female1:prestige female1:prestige
```

Estimating ϕ

Estimate for $p\hat{h}i$:

```
phi_hat <- 1/(dim(pub)[1] - pub.glm.prestige$rank) *
  sum((pub$articles - pub.glm.selected$fitted.values)^2/pub.glm.selected$fitted.values)</pre>
```

The data is actually overdispersed. This implies that the standard errors were too small and that the CI's were too narrow. We can adjust the estimated variances by multiplying by a factor of $\hat{\phi}$, giving the following confidence intervals:

```
##
                   estimate
                              lower
                                        upper exp_estimate exp_lower exp_upper
## female1
                                                                          0.856
                    -0.6320 -1.1100 -0.156000
                                                     0.532
                                                               0.330
## married1
                    0.1390 -0.0283 0.306000
                                                     1.150
                                                               0.972
                                                                         1.360
## kids1
                    -0.1870 -0.3740 -0.000719
                                                     0.829
                                                               0.688
                                                                         0.999
## kids2
                    -0.3250 -0.5650 -0.085000
                                                     0.723
                                                               0.569
                                                                         0.918
## kids3
                    -0.8280 -1.5700 -0.084900
                                                     0.437
                                                               0.208
                                                                         0.919
## mentor
                    0.0254 0.0201 0.030700
                                                     1.030
                                                               1.020
                                                                         1.030
## prestige
                    -0.0362 -0.1240 0.052000
                                                     0.964
                                                               0.883
                                                                         1.050
## female1:prestige 0.1270 -0.0140 0.267000
                                                     1.130
                                                               0.986
                                                                         1.310
##
                           rownames
## female1
                            female1
## married1
                           married1
## kids1
                              kids1
## kids2
                              kids2
## kids3
                              kids3
## mentor
                             mentor
## prestige
                           prestige
```

female1:prestige female1:prestige

This has some implications for the results of our analysis.