

Congratulations! You passed!

Grade received 100% To pass 80% or higher

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1. The solution to the differential equation $\dot{p}(t) = \hat{\omega} \times p(t) = [\hat{\omega}]p(t)$ is $p(t) = e^{t\hat{\omega}}p(0)$, where $p(0)$ is the initial vector and $p(t)$ is the vector after it has been rotated at the angular velocity $\hat{\omega}$ for time $t = \theta$ (where $\hat{\omega}\theta$ are the exponential coordinates). You can think of $R = e^{t\hat{\omega}}$ as the rotation operation that moves $p(0)$ to $p(t) = p(\theta)$.
 1 / 1 point

Which of the following statements is correct? Select all that apply.

☒ $R_{ab} = R_{ab}e^{t\hat{\omega}}$ represents the orientation of a new frame $\{b\}$ relative to $\{a\}$ after the frame $\{b\}$ has been rotated by θ about an axis u represented in the $\{b\}$ frame as \hat{u} .

☒ Correct. Multiplication of the rotation operation on the right corresponds to u being interpreted in the frame of the second subscript, $\{b\}$.

☐ $R_{ab} = R_{ab}e^{t\hat{\omega}}$ represents the orientation of a new frame $\{b\}$ relative to $\{a\}$ after the frame $\{b\}$ has been rotated by θ about an axis u represented in the $\{a\}$ frame as \hat{u} .

☐ $R_{ab} = e^{t\hat{\omega}}R_{ab}$ represents the orientation of a new frame $\{b\}$ relative to $\{a\}$ after the frame $\{b\}$ has been rotated by θ about an axis u represented in the $\{b\}$ frame as \hat{u} .

☒ $R_{ab} = e^{t\hat{\omega}}R_{ab}$ represents the orientation of a new frame $\{b\}$ relative to $\{a\}$ after the frame $\{b\}$ has been rotated by θ about an axis u represented in the $\{a\}$ frame as \hat{u} .

☒ Correct. Multiplication of the rotation operation on the left corresponds to u being interpreted in the frame of the first subscript, $\{a\}$.

2. The simple closed-form solution to the infinite series for the matrix exponential when the matrix is an element of $\mathfrak{so}(3)$ (a skew-symmetric 3x3 matrix) is called what?
 1 / 1 point

☐ Riemann's formula.

☒ Rodrigues' formula.

☐ Robertson's formula.

☒ Correct.

3. The matrix exponential and the matrix log relate a rotation matrix (an element of $SO(3)$) and the skew-symmetric representation of the exponential coordinates (elements of $\mathfrak{so}(3)$), which can also be thought of as the $\mathfrak{so}(3)$ representation of the angular velocity, followed for unit time. Which of the following statements is correct? Select all that apply.
 1 / 1 point

☒ $\exp: \mathfrak{so}(3) \rightarrow SO(3)$

☒ Correct. The matrix exponential "integrates" the skew-symmetric $\mathfrak{so}(3)$ representation of an angular velocity for unit time to yield the rotation matrix describing the orientation achieved after rotating from an initial orientation described by the identity matrix.

☐ $\exp: SO(3) \rightarrow \mathfrak{so}(3)$

☐ $\log: \mathfrak{so}(3) \rightarrow SO(3)$

☒ $\log: SO(3) \rightarrow \mathfrak{so}(3)$

☒ Correct. The matrix logarithm of a rotation matrix R gives the angular velocity that must be followed for unit time, starting from a frame represented as the identity matrix, to rotate to R . It "differentiates" the net rotational displacement to find the angular velocity that must be followed for unit time.