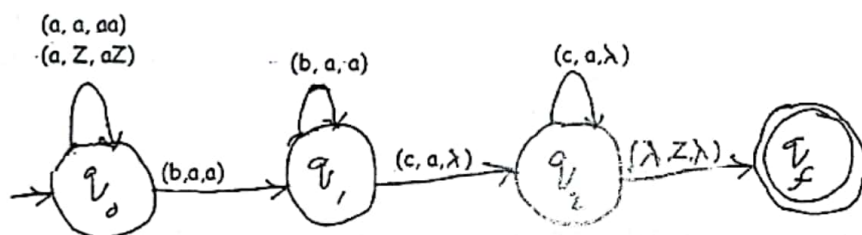


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(I) (6 points) Given the DFA for a language L, Give the DFA that accepts the complement and reverse of L.

	DFA that accepts the complement of L	DFA that accepts the reverse of L
<p>DFA accepting language L</p> <p>Accepted w: aa^*</p>	<p>Accepted w: $\lambda + b(a+b)^*$</p>	<p>Note that y can no longer be reached. Suggested new DFA:</p> <p>Accepted w: aa^*</p>

(II) (8 points) Given a PDA below



(i) Write the configuration sequence on input aabbcc starting with

$(q_0, aabbcc, Z) \vdash (q_0, abbcc, aZ) \vdash (q_0, bbcc, aaZ) \vdash$
 $(q_1, bcc, aaZ) \vdash (q_1, cc, aaZ) \vdash (q_2, c, aZ) \vdash (q_2, \lambda, Z) \vdash$
 (q_f, λ, Z)

(ii) Is the string aabbcc accepted?

Yes, The string aabbcc is accepted

(III) (6 points) Given the following Grammar,

- | | | |
|-----------------------|----------------------------|----------------------------|
| 1. $S \rightarrow AB$ | 2. $A \rightarrow aaA$ | 4. $B \rightarrow Bb$ |
| | 3. $A \rightarrow \lambda$ | 5. $B \rightarrow \lambda$ |

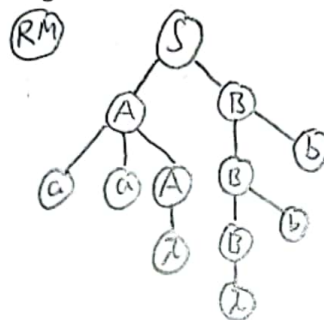
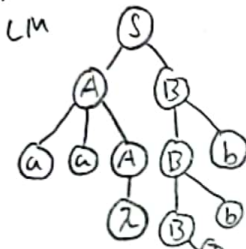
(i) Write a leftmost derivation sequence for deriving the string aabb

$$S \Rightarrow AB \Rightarrow aaAB \Rightarrow aaB \Rightarrow aaBb \Rightarrow aaBbb \Rightarrow aabb$$

(i) Write a rightmost derivation sequence for deriving the string aabb

$$S \Rightarrow AB \Rightarrow ABb \Rightarrow ABbb \Rightarrow Abb \Rightarrow aaAbb \Rightarrow aabb$$

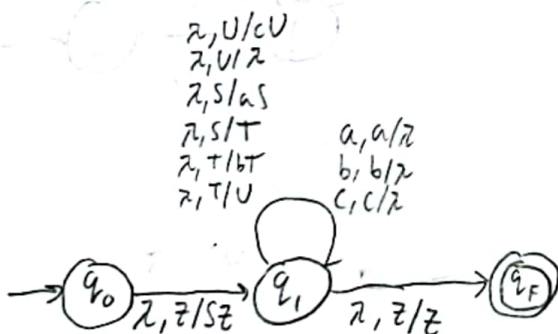
(iii) Give the derivation tree corresponding to the above derivations



(II) (10 points) Given a grammar:

- $$\begin{aligned} S &\rightarrow aS \mid T \\ T &\rightarrow bT \mid U \\ U &\rightarrow cU \mid \lambda \end{aligned}$$

(i) give an equivalent PDA transition diagram that accepts the same language.



(ii) give the configuration sequences on the string ab from the initial configuration to the accepting configuration.

$$\begin{aligned} (q_0, ab, z) &\vdash (q_1, ab, Sz) \vdash (q_1, ab, aSz) \vdash (q_1, b, Sz) \vdash (q_1, b, Tz) \vdash \\ &(q_1, b, bTz) \vdash (q_1, \lambda, Tz) \vdash (q_1, \lambda, Uz) \vdash (q_1, \lambda, z) \vdash (q_F, \lambda, z) \\ &\text{Accepted} \end{aligned}$$