

(I) Give a formal definition with any notations for the following:

DFA as a 5 tuple, Language accepted by automaton, Regular language

(II) Given the alphabet as $\{0, 1\}$, write a DFA for the following three regular languages.

(Give the complete description of the DFA, and also as a transition graph)

(i) $L = \{w \mid w \text{ is a string of even length}\}$

(ii) $L = \{w \mid |w| \bmod 3 = 0\}$

(iii) $L = \{w \mid w \text{ contains the string } 001 \text{ as a substring}\}$

(iv) $L = \{w \mid w \text{ does not contain two consecutive } 1\text{'s}\}$

(III) Choose any DFA you made for Problem (II), describe the extended transition function on a string recursively using transitions one symbol at a time of following problems.

(i) A string (of length ≥ 4) that belongs to the language

(II) A string (of length ≥ 4) that does not belong to the language