

Statistics 3—assignment---session 17

Problem 1

Step 1: State the null hypothesis: $H_0: \mu=100$

Step 2: State the alternate hypothesis: $H_1: \neq 100$

Step 3: State your alpha level. We'll use 0.05 for this example. As this is a two-tailed test, split the alpha into two.

$$0.05/2=0.025$$

Step 4: Find the z-score associated with your alpha level. You're looking for the area in one tail only. A z-score for 0.75(1-0.025=0.975) is 1.96. As this is a two-tailed test, you would also be considering the left tail (z=1.96)

$$Z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$$

Step 5: Find the test statistic using this formula:

$$z=(108-100)/(15/\sqrt{36})=0.08$$

Step 6: If Step 5 is less than -1.96 or greater than 1.96 (Step 3), reject the null hypothesis. In this case, it is lesser than 1.96, so you cannot reject the null hypothesis.

Problem 2

For this analysis, let P_1 = the proportion of Republican voters in the first state

P_2 = the proportion of Republican voters in the second state

p_1 = the proportion of Republican voters in the sample from the first state

p_2 = the proportion of Republican voters in the sample from the second state.

The number of voters sampled from the first state (n_1) = 100

the number of voters sampled from the second state (n_2) = 100.

The solution involves four steps.

- $n_1 P_1 = 100 * 0.52 = 52$
- $n_1(1 - P_1) = 100 * 0.48 = 48$
- $n_2 P_2 = 100 * 0.47 = 47$

- $n_2(1 - P_2) = 100 * 0.53 = 53$
- the mean of the difference in sample proportions: $E(p_1 - p_2) = P_1 - P_2 = 0.52 - 0.47 = 0.05$.
- the standard deviation of the difference.

$$\begin{aligned}\sigma_d &= \sqrt{\{ [P_1(1 - P_1) / n_1] + [P_2(1 - P_2) / n_2] \}} \\ \sigma_d &= \sqrt{\{ [(0.52)(0.48) / 100] + [(0.47)(0.53) / 100] \}} \\ \sigma_d &= \sqrt{(0.002496 + 0.002491)} = \sqrt{0.004987} = 0.0706\end{aligned}$$

- This problem requires to find the probability that p_1 is less than p_2 . This is equivalent to finding the probability that $p_1 - p_2$ is less than zero. To find this probability, we need to transform the random variable ($p_1 - p_2$) into a z-score. That transformation appears below.

$$z_{p_1 - p_2} = (x - \mu_{p_1 - p_2}) / \sigma_d = (0 - 0.05) / 0.0706 = -0.7082$$

the probability of a z-score being -0.7082 or less is 0.24.

Therefore, the probability that the survey will show a greater percentage of Republican voters in the second state than in the first state is 0.24.

Problem 3

My score = 1100

Mean = 1026

Standard deviation = 209

$$z = (x - \mu) / \sigma = (1100 - 1026) / 209 = .3541$$

$$1 - .3541 = 0.6368$$

By 63% scores are less than 1100.

So by 63% did well than an average test taker