VISUALIZING UNITED STATE'S TRAFFIC FLOW

THARALD S. FONGAARD & JACOB PERRICONE
ADVISOR: PROFESSOR ALAIN KORNHAUSER

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Abstract

By analyzing trip generation in the United States, we will display key statistics in an informative graphic user interface. Specifically, given a node network of the entire nation and trip generation files, we will provide a means to determine the number of vehicles, people, and the average vehicle occupancy on each link at each time throughout the day.

Acknowledgements

Here are the acknowledgments. I'm sure you know what to do here...thanks, and thanks!

To The Hereditary Kingdom of Norway

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Chapter 1

Introduction

This is the introduction of my sample thesis. Let me just state that this is a very,

very limited introduction to LATEX, and I can not do justice to it through the next

few pages.

I recommend reading this .pdf file along with the .tex file open on the side so that

you can compare the pure ASCII text and the final result after compilation.

1.1 A Different Word Processing System

I highly recommend the booklet "The Not So Short Introduction to LATEX 2ε " which

is free and very well-written. It is available on:

http://tobi.oetiker.ch/lshort/lshort.pdf.

I refer you to the introduction there.

1

Chapter 2

Development of the Department of Operations Research and Financial Engineering

This Chapter has purposefully a very long title to illustrate how LaTeX $2_{\mathcal{E}}$ handles such long names. Now it is a good time to look on the table of contents and see how this Chapter and also Chapter 1 are listed. Notice that the number 1 in the phrase "and also Chapter 1" is automatically generated by using the command $\mathbf{ref\{ch:intro\}}$, because we labeled Chapter 1 'ch:intro' by using the command $\mathbf{label\{ch:intro\}}$ after the $\mathbf{labeled}$ Introduction declaration.

2.1 Initial Setup

A few things here to start. And here as well, since we need to fill in at least a line. Almost..., there we go!

Notice that I entered ellipses after the word 'Almost' above with the command \ldots, and not by simply typing three dots. Compare the result here: ... vs. ... ¹

¹Word does that too, but lousily!

Maybe some more words in a new paragraph. And more, and more, and more. Furthermore, additionally, in addition, and so on. Notice here that the word 'Furthermore' was broken into 'Fur-' and 'thermore' in order to fit the line—Word, as stupid as it is, would simply place the entire word on the next line, thus increasing the distance between words on the first line to fill up the entire line.

2.1.1 Additional Structure: The Use of Subsections

We are in a subsection now (two levels down from a Chapter). When we refer to X.Y.Z, we mean Chapter X, Section Y, and subsection Z. We declare a Chapter by the command $\hat G$ and so on.

The nice thing about LaTeX is that it takes care of the chapter, section, and subsection numbering automatically. If I were to add another subsection before this one the subsection number would change (increment by one). This section is 2.1.1 and I referred to it using the command \ref{label of this section}. I inserted a label right after the \subsection declaration by typing \label{label of this section}.

A subsubsection

Just for fun! Notice that no number is alloted for such a low level environment but it sometimes useful.

2.1.2 Another Subsection

And so on....

2.2 Mathematical Symbols

Let $X = \{X_n, n \in \mathbb{N}\}$ be a Markov chain with state space \mathcal{D} . Throughout this thesis, we use the notation

$$p_{ij} := \mathbb{P}\{X_{n+1} = j \mid X_n = i\}, \quad i, j \in \mathcal{D}$$
 (2.1)

for the transition probabilities of the Markov chain X. Furthermore, we denote by P the transition matrix, $P = [p_{ij}]_{i,j \in \mathcal{D}}$.

When we wrote (2.1) we implicitly assumed that the Markov chain X is time-homogeneous.

Let us also define Y,

$$Y = (Y_n)_{n=0,1,2,...}$$

to be another process. Notice that the second equation does not take a number on the right—this is the use of \begin{equation*} equation*.

Notice that the all the math characters, X, \mathcal{D} , and others such as α, β, γ are part of the text in LaTeX. On the contrary, Word includes such characters as foreign objects (usually images), which increases the size of the document file, sometimes makes them disappear, but most importantly are not as aesthetically pleasing as the resulting characters here.

2.3 Citing and Bibliography

When working with large documents you need an easy way to cite your references without having to go back to your list all the time to remember the names of the authors and the year of publication. Even more importantly, you need to have all your references listed in the end of the document in alphabetical order. Of course, they all need to be syntactically the same so that alone makes the manual entry of

references a big pain. Thankfully, LATEX takes care of that in a very easy and elegant way, using BibTeX.

I cite here a few books, papers, and technical reports, and please go to page 15 to see the resulting bibliography.

According to the books by Çinlar (1975), Bielecki and Rutkowski (2002), and Musiela and Rutkowski (1997) and the articles by Duffie and Gârleanu (2001), Blanco et al. (2005), and Cotton et al. (2004) we conclude absolutely nothing. However, in his report, Aas (2004) claims that otherwise. All these citations were entered by \cite{citation label}.

Notice the different citation style that follows: it is parenthetical, and observe that only one pair of parentheses is required (see Theorem 5.2 Antonov et al., 2005, pg. 32). This citation is entered by typing \cite[see Theorem 5.2][pg. 32]{AMM05} in the .tex file. (Here, the citation label corresponding to Antonov et al. (2005) is obviously AMM05.)

The citations are included in the file refs.bib under the folder Bibliography. You can modify it and make your own references. I highly recommend using JabRef for managing your bibliography entries, because it makes it a piece of cake to do a lot of dirty work. JabRef is free and it works as a Java Application.

Also notice that LaTeX, by default, includes in the Bibliography section only the references you actually cited throughout the text. If you want a source to appear in the Bibliography section without actually citing it anywhere in your text use the command \nocite{citation label}. For example here I type \nocite{B95} and you see no citation appear—however look at the fourth entry of the Bibliography. That cited book does not appear anywhere in this thesis, other than the Bibliography.

2.4 Referencing Figures and Tables

The very informative Figure 3.1 is on page 8. Both of these numbers were automatically generated—which is great when you add a new figure before the one you just inserted, because the numbering changes automatically for you. Use \ref{fig:dens} for the figure number and \pageref{fig:dens} for the page number where the figure is located. Here, fig:dens was the label of the figure (see actual .tex file for more information). Remember that LaTeX does not work like Word—the figures and tables are not always placed exactly where you want them, so avoid writing "according to the figure below...," and prefer writing "according to Figure [figure number]...," instead. The same things go unchanged for tables. Notice that when I talk about figures and tables in general, I do not need to capitalize them, however if I talk specifically about Figure 3.1 and Table 3.1, I'd better respect them and capitalize the 'f' and the 't.'

Since we're at it, notice that the quotes ', ', ", " are not inserted like in Word. For 'you need to use the 'key that is located above the Tab button. For 'you just press the 'key, exactly to the left of the Enter key. For double quotes just double the appropriate single quotes without leaving any space.

Chapter 3

Analysis of Problem

Time for some analysis, and probably graphs and tables. Thankfully LaTeX (and LaTeX 2ε) provides very nice environments for both.

3.1 Preliminary Analysis

Assume that the random variable D given $\tilde{p} = p$ is binomially distributed with parameters 50 and p (probability of success, in this case default). We also take the cumulative distribution function of \tilde{p} to be

$$F(\theta) = \mathbb{P}\{\tilde{p} \le \theta\} = \Phi\left(\frac{1}{\rho}\left(\sqrt{1-\rho^2}\,\Phi^{-1}(\theta) - \Phi^{-1}(\bar{p})\right)\right)$$

where Φ is the cumulative standard normal distribution function, ρ is the correlation coefficient between the idiosyncratic and market factors and \bar{p} is the mean default probability $(\bar{p} = \mathbb{E}\tilde{p})$. To calculate the density of \tilde{p} let

$$h(\theta, \rho, \bar{p}) := \frac{1}{\rho} \left(\sqrt{1 - \rho^2} \, \Phi^{-1}(\theta) - \Phi^{-1}(\bar{p}) \right),$$

$$\varphi(\theta) := \frac{d}{d\theta} \Phi(\theta) = \frac{1}{\sqrt{2\pi}} e^{-\theta^2/2},$$

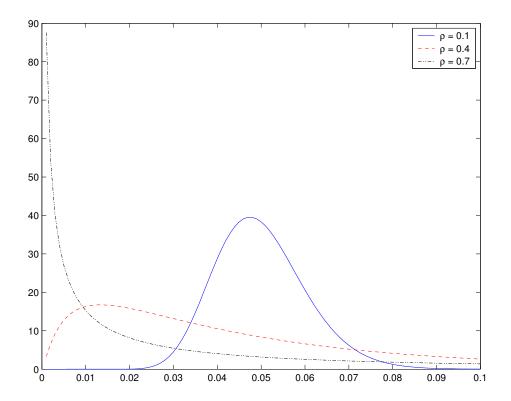


Figure 3.1: The density function f as given in (3.1) for three different ρ 's and $\bar{p} = 0.05$. (Plotted on [0, 0.1] for convenience.)

and notice that since Φ is a bijection we have

$$\Phi \circ \Phi^{-1}(\theta) = \Phi^{-1} \circ \Phi(\theta) = \theta,$$

for every $\theta \in \mathbb{R}$. Then, we have for the density of \tilde{p} ,

$$f(\theta, \rho, \bar{p}) = \frac{d}{d\theta} F(\theta) = \Phi'(h(\theta, \rho, \bar{p})) \frac{\partial}{\partial \theta} h(\theta, \rho, \bar{p})$$

$$= \varphi(h(\theta, \rho, \bar{p})) \frac{\sqrt{1 - \rho^2}}{\rho} \frac{d}{d\theta} \Phi^{-1}(\theta)$$

$$= \varphi(h(\theta, \rho, \bar{p})) \frac{\sqrt{1 - \rho^2}}{\rho} \frac{1}{\varphi(\Phi^{-1}(\theta))}, \tag{3.1}$$

for $\theta \in (0,1)$ and zero otherwise, since

$$\begin{split} \frac{d}{d\theta} \left(\Phi(\Phi^{-1}(\theta)) \right) &= \Phi'(\Phi^{-1}(\theta)) \frac{d}{d\theta} \Phi^{-1}(\theta) \Leftrightarrow \\ \frac{d}{d\theta} \theta &= \varphi(\Phi^{-1}(\theta)) \frac{d}{d\theta} \Phi^{-1}(\theta) \Leftrightarrow \\ \frac{d}{d\theta} \Phi^{-1}(\theta) &= \frac{1}{\varphi(\Phi^{-1}(\theta))}. \end{split}$$

The density of \tilde{p} is shown in Figure 3.1 for three different values of ρ and $\bar{p} = 0.05$. The effect of the correlation is to put more mass towards higher default probabilities as the correlation increases, thus resulting in larger number of defaults as the correlation increases.

Table 3.1: Values of the CDO Tranches.

			ρ	
		0.1	0.4	0.7
Equity	$C_E^{\star}(T)$	2.5712	2.8957	3.5642
Junior	$C_J^{\overline{\star}}(T)$	9.9289	9.6137	9.2120
Senior	$C_S^{\star}(T)$	35.0000	34.9905	34.7239
Sum	$C_E^{\star}(T) + C_J^{\star}(T) + C_S^{\star}(T)$	47.5000	47.5000	47.5001

Using the default values for the parameters as above we get the values for the tranches in Table 3.1.

Let's see one more result on Table 3.2. According to Frazier (2006)...

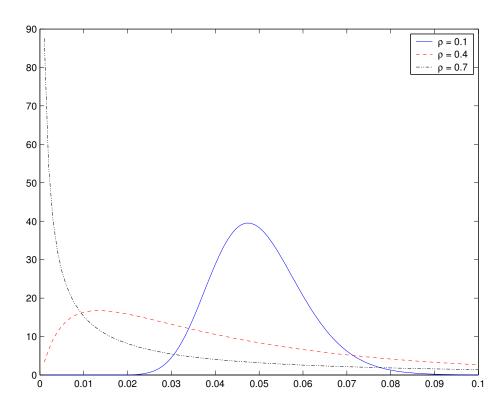


Figure 3.2: The density function f as given in (3.1) for three different ρ 's and $\bar{p}=0.05$. (Plotted on [0,0.1] for convenience.)

Table 3.2: These are the data.

DJ CDX Tranches:	0-3%	3-7%	7-10%	10-15%	15-30%	RMSE
Market mid spread	40.00%	312.5	122.5	42.5	12.5	
Bid/Ask Spread	2.00%	15.0	7	7	3	
Stochastic vol intensities	41.80%	308.9	116.2	44.9	2	1.68
Jump-diffusion intensities	46.90%	340.2	119.7	61.9	14.3	2.17
Pure-diffusion intensities	49.30%	442.9	94.9	16.8	0.4	5.34
Gaussian copula	46.80%	474.4	131.8	36.9	2.9	5.3
RFL Gaussian copula	48.60%	334.9	125.5	66.5	9.2	2.59
Double-t copula	45.10%	367	114.9	54.9	20	2.44

Source: Some source that I quote in the form Author (YYYY).

Appendix A

Code

```
tmp3 = [];
for i = (K_E + K_J +1):50
          tmp3(i- K_E - K_J) = (i - K_E - K_J) * binopdf(i,50,p);
end
C_J = K_J - sum(tmp2) +sum(tmp3)

C_S = K_S - sum(tmp3)

% Sanity check
C_E + C_J + C_S
```

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