

Classification of Biological Organisms from Images Using Advanced Mathematical Techniques

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Abstract

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1 Introduction

2 The Elliptic Fourier Transform

The Fourier transform is a way of finding constituent frequencies within a function on the real domain. The Fourier transform extends the concept of the Fourier series (which operates on a bounded interval) to the real domain.

2.1 The Fourier Series

The Fourier series is defined using the equations described below. It takes in a single repeating unit of a periodic function and allows us to generate an infinite sum which converges to the same function. This is useful because the resultant sum ends up depending on trigonometric functions.

Firstly we have a set of numbers, A_0 , A_n and B_n :

$$\begin{aligned} A_0 &= \frac{1}{P} \int_{-\frac{P}{2}}^{\frac{P}{2}} s(x) dx \\ A_n &= \frac{1}{P} \int_{-\frac{P}{2}}^{\frac{P}{2}} s(x) \cos\left(\frac{2\pi nx}{P}\right) dx \\ A_b &= \frac{1}{P} \int_{-\frac{P}{2}}^{\frac{P}{2}} s(x) \sin\left(\frac{2\pi nx}{P}\right) dx \end{aligned} \tag{1}$$

Here A_0 is a constant, and A_n and B_n are functions of n . In fact, since both the denominator of the fraction and the range of the integral for A_0 are the same, P , A_0 is simply the average around which the function oscillates.

These coefficients allow us to define the Fourier series:

$$s(x) \sim A_0 + \sum_{n=1}^{\infty} \left(A_n \cos\left(\frac{2\pi nx}{P}\right) + B_n \sin\left(\frac{2\pi nx}{P}\right) \right) \tag{2}$$

Here we use a \sim because this series doesn't always converge to the desired function, although in most cases it does.

3 Conclusion

Note: these are just example citations. [?, p. 150] [?] [?] [?] [?] .

4 Acknowledgements

5 Appendix

Note: These are unlikely to be in the final report, they are simply there as an example appendix for now.

main.cpp

elliptic_fourier.h

elliptic_fourier.cpp

drawing_area.h

drawing_area.cpp

6 Bibliography