Raw amplitude

$$\frac{e^{2}}{16\pi^{4}} 1 \int \frac{d^{d}p}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)\gamma^{\mu} \left(m + (k_{\sigma_{1}} + p_{\sigma_{1}})\gamma^{\sigma_{1}} \right) \left(m + p_{\sigma_{1}}\gamma^{\sigma_{2}} \right)\gamma^{\nu}}{\left(-m^{2} + (k_{\eta} + p_{\eta}) \left(k^{\eta} + p^{\eta} \right) \right) \left(-m^{2} + p_{\eta}p^{\eta} \right)} \right)$$

$$\tag{1}$$

Simplified numerator

$$\frac{e^2}{16\pi^4} 1 \int \frac{d^d p}{(2\pi)^4} \left(\frac{1}{(-m^2 + (k_\eta + p_\eta)(k^\eta + p^\eta))(-m^2 + p_\eta p^\eta)} \left(\epsilon_\nu(k) \bar{\epsilon}_\mu(k) m^2 \gamma^\mu \gamma^\nu + \epsilon_\nu(k) \bar{\epsilon}_\mu(k) m k_{\sigma_1} \gamma^\mu \gamma^{\sigma_1} \gamma^\nu \right. \\
\left. + \epsilon_\nu(k) \bar{\epsilon}_\mu(k) m p_{\sigma_1} \gamma^\mu \gamma^{\sigma_1} \gamma^\nu + \epsilon_\nu(k) \bar{\epsilon}_\mu(k) m p_{\sigma_1} \gamma^\mu \gamma^{\sigma_2} \gamma^\nu + \epsilon_\nu(k) \bar{\epsilon}_\mu(k) k_{\sigma_1} p_{\sigma_1} \gamma^\mu \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^\nu + \epsilon_\nu(k) \bar{\epsilon}_\mu(k) p_{\sigma_1} \gamma^\mu \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^\nu \right) \right)$$
(2)

Feynman parameterization

Here, we perform the following expansion:

$$\frac{1}{A_1} \cdots \frac{1}{A_n} = (n-1)! \int_0^1 dz_1 \int_0^{1-z_1} dz_2 \cdots \int_0^{1-z_1-z_{n-1}} dz_n \frac{1}{(z_1 A_1 + \dots + z_n A_n)^n}$$

We use this form because a single denominator raised to a power can be simplified with the Golden Integral.

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^dp}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\mu}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\nu}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\nu}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\nu$$

Expanded numerator

We split the numerator into additive terms, to process individually. The following is a list of such terms:

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1k^{\eta}p_{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$

$$(4)$$

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$
 (5)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}}{\left(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1k^{\eta}p_{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta}\right)^2} \right)$$
(6)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_2}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$
 (7)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)p_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_2}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1k^{\eta}p_{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$
(8)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_1}p_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1k^{\eta}p_{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$

$$(9)$$

Golden Integral

We resolve internal momentas with this transformation:

$$\int \frac{d^d q}{(2\pi)^d} \frac{(q^2)^a}{(q^2 + D)^b} = i \frac{\Gamma(b - a - \frac{1}{2}d)\Gamma(a + \frac{1}{2}d)}{(4\pi)^{d/2}\Gamma(b)\Gamma(\frac{1}{2}d)} D^{-(b - a - d/2)}$$

After this section, all internal momenta should disappear. We will now resolve each term in a queue. Each term may produce additional terms, which are pushed to the back of the queue and resolved later.

Evaluating internal momenta in this term (5 terms left)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$

$$(10)$$

Integrating over p Completing the square

$$A = z_1 + z_2 \tag{11}$$

$$B = 2z_1 k^{\eta} \tag{12}$$

$$C = -m^2 z_1 - m^2 z_2 + z_1 k_\eta k^\eta \tag{13}$$

After $p \to q_1$ substitutions

$$\frac{0.0625e^2}{\pi^4} \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(z_1+z_2)^{0.5} \left(-m^2z_1-m^2z_2-\frac{z_1^2k_{\eta}k^{\eta}}{4z_1+4z_2}+z_1k_{\eta}k^{\eta}+q_1\eta q_1^{\eta}\right)^2} \right)$$
(14)

Expanding numerator into 1 term(s)

$$\frac{0.0625e^2}{\pi^4} \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(z_1+z_2)^{0.5} \left(-m^2z_1-m^2z_2-\frac{z_1^2k_{\eta}k^{\eta}}{4z_1+4z_2}+z_1k_{\eta}k^{\eta}+q_{1\eta}q_1^{\eta}\right)^2} \right)$$
(15)

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^{2}\gamma^{\mu}\gamma^{\nu}}{(z_{1}+z_{2})^{0.5} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right) \tag{16}$$

Found 0 q-vector terms in the numerator. Apply golden integral

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(z_1+z_2)^{0.5}}\right)$$
(17)

Evaluating internal momenta in this term (5 terms left)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$
(18)

Integrating over p Completing the square

$$A = z_1 + z_2 \tag{19}$$

$$B = 2z_1 k^{\eta} \tag{20}$$

$$C = -m^2 z_1 - m^2 z_2 + z_1 k_\eta k^\eta \tag{21}$$

After $p \to q_1$ substitutions

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}}{(z_1+z_2)^{0.5} \left(-m^2z_1-m^2z_2-\frac{z_1^2k_{\eta}k^{\eta}}{4z_1+4z_2}+z_1k_{\eta}k^{\eta}+q_{1\eta}q_1^{\eta}\right)^2} \right) \tag{22}$$

Expanding numerator into 1 term(s)

$$\frac{0.0625e^2}{\pi^4} \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}}{(z_1+z_2)^{0.5} \left(-m^2z_1-m^2z_2-\frac{z_1^2k_{\eta}k^{\eta}}{4z_1+4z_2}+z_1k_{\eta}k^{\eta}+q_{1\eta}q_1^{\eta}\right)^2} \right) \tag{23}$$

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{(z_{1}+z_{2})^{0.5} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(24)

Found 0 q-vector terms in the numerator. Apply golden integral

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}}{(z_1+z_2)^{0.5}} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\nu} \right)$$
(25)

Evaluating internal momenta in this term (5 terms left)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k) \bar{\epsilon}_{\mu}(k) m p_{\sigma_1} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\nu}}{(-m^2 z_1 - m^2 z_2 + z_1 k_{\eta} k^{\eta} + z_1 k_{\eta} p^{\eta} + z_1 p_{\eta} p^{\eta} + z_2 p_{\eta} p^{\eta})^2} \right)$$
(26)

Integrating over p Completing the square

$$A = z_1 + z_2 \tag{27}$$

$$B = 2z_1 k^{\eta} \tag{28}$$

$$C = -m^2 z_1 - m^2 z_2 + z_1 k_\eta k^\eta \tag{29}$$

After $p \to q_1$ substitutions

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m\left(z_{1}\left(z_{1}+z_{2}\right)^{0.5}k_{\sigma_{1}}-2\left(z_{1}+z_{2}\right)q_{1}_{\sigma_{1}}\right)\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{2\left(z_{1}+z_{2}\right)^{2.0}\left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1}\eta q_{1}^{\eta}\right)^{2}} \right)$$
(30)

Expanding numerator into 3 term(s)

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}q_{1}\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1}\eta q_{1}^{\eta}\right)^{2}} \right)$$
(31)

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{2}q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(32)

$$\frac{0.0625e^{2}}{\pi^{4}} 1 \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\overline{\epsilon}_{\mu}(k)mz_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{2(z_{1}+z_{2})^{1.5}\left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$

$$(33)$$

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$

$$(34)$$

Found 1 q-vector terms in the numerator. Term vanishes due to Ward identity

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{2}q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(35)

Found 1 q-vector terms in the numerator. Term vanishes due to Ward identity

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}}{2\left(z_{1}+z_{2}\right)^{1.5}\left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$

$$(36)$$

Found 0 q-vector terms in the numerator. Apply golden integral

$$\frac{1249999896.56489i}{\pi^2}e^21\int_0^1 dz_1\int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}\right)$$
(37)

Evaluating internal momenta in this term (5 terms left)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mp_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_2}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$
(38)

Integrating over p Completing the square

$$A = z_1 + z_2 \tag{39}$$

$$B = 2z_1 k^{\eta} \tag{40}$$

$$C = -m^2 z_1 - m^2 z_2 + z_1 k_\eta k^\eta \tag{41}$$

After $p \to q_1$ substitutions

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m\left(z_{1}\left(z_{1}+z_{2}\right)^{0.5}k_{\sigma_{1}}-2\left(z_{1}+z_{2}\right)q_{1}_{\sigma_{1}}\right)\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu}}{2\left(z_{1}+z_{2}\right)^{2.0}\left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(42)

Expanding numerator into 3 term(s)

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}q_{1}\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1}\eta q_{1}^{\eta}\right)^{2}} \right)$$
(43)

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{2}q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(44)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_2}\gamma^{\nu}}{2(z_1+z_2)^{1.5} \left(-m^2z_1 - m^2z_2 - \frac{z_1^2k_{\eta}k^{\eta}}{4z_1+4z_2} + z_1k_{\eta}k^{\eta} + q_{1\eta}q_1^{\eta} \right)^2} \right)$$
(45)

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}q_{1}\sigma_{1}\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1}\eta q_{1}^{\eta}\right)^{2}} \right)$$
(46)

Found 1 q-vector terms in the numerator. Term vanishes due to Ward identity

Integrating this term:

$$\frac{0.0625e^2}{\pi^4} \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_2 q_1 \sigma_1 \gamma^{\mu} \gamma^{\sigma_2} \gamma^{\nu}}{(z_1+z_2)^{2.0} \left(-m^2 z_1 - m^2 z_2 - \frac{z_1^2 k_{\eta} k^{\eta}}{4z_1 + 4z_2} + z_1 k_{\eta} k^{\eta} + q_1 \eta q_1^{\eta} \right)^2} \right) \tag{47}$$

Found 1 q-vector terms in the numerator. Term vanishes due to Ward identity

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu}}{2\left(z_{1}+z_{2}\right)^{1.5}\left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$

$$(48)$$

Found 0 q-vector terms in the numerator. Apply golden integral

$$\frac{1249999896.56489i}{\pi^2}e^21\int_0^1 dz_1\int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}}\gamma^{\mu}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(49)

Evaluating internal momenta in this term (5 terms left)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)p_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$
(50)

Integrating over p Completing the square

$$A = z_1 + z_2 \tag{51}$$

$$B = 2z_1 k^{\eta} \tag{52}$$

$$C = -m^2 z_1 - m^2 z_2 + z_1 k_\eta k^\eta \tag{53}$$

After $p \to q_1$ substitutions

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k) \left(z_{1} \left(z_{1}+z_{2} \right)^{0.5} k_{\sigma_{1}} - 2 \left(z_{1}+z_{2} \right) q_{1\sigma_{1}} \right)^{2} \gamma^{\mu} \gamma^{\sigma_{1}} \gamma^{\sigma_{2}} \gamma^{\nu}}{4 \left(z_{1}+z_{2} \right)^{3.5} \left(-m^{2}z_{1} - m^{2}z_{2} - \frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}} + z_{1}k_{\eta}k^{\eta} + q_{1\eta}q_{1}^{\eta} \right)^{2}} \right)$$
(54)

Expanding numerator into 3 term(s)

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{1.5} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(55)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1^2 k_{\sigma_1} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu}}{4(z_1+z_2)^{2.5} \left(-m^2 z_1 - m^2 z_2 - \frac{z_1^2 k_{\eta} k^{\eta}}{4z_1 + 4z_2} + z_1 k_{\eta} k^{\eta} + q_{1\eta} q_1^{\eta}\right)^2} \right)$$
(56)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1 k_{\sigma_1} q_{1\sigma_1} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu}}{(z_1+z_2)^{2.0} \left(-m^2 z_1 - m^2 z_2 - \frac{z_1^2 k_{\eta} k^{\eta}}{4z_1 + 4z_2} + z_1 k_{\eta} k^{\eta} + q_{1\eta} q_1^{\eta} \right)^2} \right)$$
(57)

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{1.5} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(58)

Found 0 q-vector terms in the numerator. Apply golden integral $\,$

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_1}\gamma^{\mu}}{(z_1+z_2)^{1.5}} \gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu} \right)$$
(59)

Integrating this term:

$$\frac{0.0625e^2}{\pi^4} \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1^2 k_{\sigma_1} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu}}{4(z_1+z_2)^{2.5} \left(-m^2 z_1 - m^2 z_2 - \frac{z_1^2 k_{\eta} k^{\eta}}{4z_1 + 4z_2} + z_1 k_{\eta} k^{\eta} + q_{1\eta} q_1^{\eta} \right)^2} \right)$$
(60)

Found 0 q-vector terms in the numerator. Apply golden integral

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1^2 k_{\sigma_1}}{4(z_1+z_2)^{2.5}} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu} \right)$$
(61)

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{1}k_{\sigma_{1}}q_{1}_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1} - m^{2}z_{2} - \frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}} + z_{1}k_{\eta}k^{\eta} + q_{1\eta}q_{1}^{\eta} \right)^{2}} \right)$$
(62)

Found 1 q-vector terms in the numerator. Term vanishes due to Ward identity

Evaluating internal momenta in this term (6 terms left)

$$\frac{0.0625e^2}{\pi^4} 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d p}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_1}p_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}}{(-m^2z_1 - m^2z_2 + z_1k_{\eta}k^{\eta} + z_1k_{\eta}p^{\eta} + z_1p_{\eta}p^{\eta} + z_2p_{\eta}p^{\eta})^2} \right)$$
(63)

Integrating over p Completing the square

$$A = z_1 + z_2 \tag{64}$$

$$B = 2z_1 k^{\eta} \tag{65}$$

$$C = -m^2 z_1 - m^2 z_2 + z_1 k_\eta k^\eta \tag{66}$$

After $p \to q_1$ substitutions

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k) \left(z_{1}(z_{1}+z_{2})^{0.5}k_{\sigma_{1}}-2(z_{1}+z_{2})q_{1}_{\sigma_{1}}\right)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{2(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(67)

Expanding numerator into 3 term(s)

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{2(z_{1}+z_{2})^{1.5} \left(-m^{2}z_{1} - m^{2}z_{2} - \frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}} + z_{1}k_{\eta}k^{\eta} + q_{1\eta}q_{1}^{\eta} \right)^{2}} \right)$$
(68)

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{1}k_{\sigma_{1}}q_{1}_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(69)

$$\frac{0.0625e^2}{\pi^4} \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \int \frac{d^d q_1}{(2\pi)^4} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_2 k_{\sigma_1} q_{1\sigma_1} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu}}{(z_1+z_2)^{2.0} \left(-m^2 z_1 - m^2 z_2 - \frac{z_1^2 k_{\eta} k^{\eta}}{4z_1 + 4z_2} + z_1 k_{\eta} k^{\eta} + q_{1\eta} q_1^{\eta} \right)^2} \right)$$
(70)

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{2(z_{1}+z_{2})^{1.5}\left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(71)

Found 0 q-vector terms in the numerator. Apply golden integral

$$\frac{1249999896.56489i}{\pi^2}e^{2}1\int_{0}^{1}dz_1\int_{0}^{-z_1+1}dz_2\left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(72)

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{1}k_{\sigma_{1}}q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(73)

Found 1 q-vector terms in the numerator. Term vanishes due to Ward identity

Integrating this term:

$$\frac{0.0625e^{2}}{\pi^{4}} \int_{0}^{1} dz_{1} \int_{0}^{-z_{1}+1} dz_{2} \int \frac{d^{d}q_{1}}{(2\pi)^{4}} \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{2}k_{\sigma_{1}}q_{1}_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}}{(z_{1}+z_{2})^{2.0} \left(-m^{2}z_{1}-m^{2}z_{2}-\frac{z_{1}^{2}k_{\eta}k^{\eta}}{4z_{1}+4z_{2}}+z_{1}k_{\eta}k^{\eta}+q_{1\eta}q_{1}^{\eta}\right)^{2}} \right)$$
(74)

Found 1 q-vector terms in the numerator. Term vanishes due to Ward identity Evaluating internal momenta in this term (6 terms left)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(z_1+z_2)^{0.5}} \right)$$
 (75)

Evaluating internal momenta in this term (5 terms left)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}}{(z_1+z_2)^{0.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} \right)$$
 (76)

Evaluating internal momenta in this term (4 terms left)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} \right)$$

$$(77)$$

Evaluating internal momenta in this term (3 terms left)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu} \gamma^{\sigma_2} \gamma^{\nu} \right)$$
(78)

Evaluating internal momenta in this term (2 terms left)

$$\frac{1249999896.56489i}{\pi^2}e^21\int_0^1 dz_1\int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_1}\gamma^{\mu}}{(z_1+z_2)^{1.5}}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(79)

Evaluating internal momenta in this term (1 terms left)

$$\frac{1249999896.56489i}{\pi^2}e^{2}1\int_{0}^{1}dz_1\int_{0}^{-z_1+1}dz_2\left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1^2k_{\sigma_1}}{4(z_1+z_2)^{2.5}}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(80)

Evaluating internal momenta in this term (0 terms left)

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu} \right)$$
(81)

Final amplitudes after momenta integration

$$\frac{1249999896.56489i}{\pi^2}e^21\int_0^1 dz_1\int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(z_1+z_2)^{0.5}}\right)$$
(82)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}}{(z_1+z_2)^{0.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} \right)$$
(83)

$$\frac{1249999896.56489i}{\pi^2}e^21\int_0^1 dz_1\int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}\right)$$
(84)

$$\frac{1249999896.56489i}{\pi^2}e^{2}1\int_{0}^{1}dz_1\int_{0}^{-z_1+1}dz_2\left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}}\gamma^{\mu}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(85)

$$\frac{1249999896.56489i}{\pi^2}e^21\int_{0}^{1}dz_1\int_{0}^{-z_1+1}dz_2\left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_1}\gamma^{\mu}}{(z_1+z_2)^{1.5}}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(86)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1^2 k_{\sigma_1}}{4(z_1+z_2)^{2.5}} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu} \right)$$
(87)

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_{0}^{1} dz_1 \int_{0}^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu} \right)$$
(88)

Integrating cutoffs

Here we integrate all t-variables, which represent the upper and lower cutoffs.

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(z_1+z_2)^{0.5}} \right)$$
(89)

Denominator only

1 (90)

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}}{(z_1+z_2)^{0.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} \right)$$

$$(91)$$

Denominator only

1

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} \right)$$

$$(93)$$

Denominator only

1

(94)

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu} \gamma^{\sigma_2} \gamma^{\nu} \right)$$

$$(95)$$

Denominator only

1

(96)

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_1}\gamma^{\mu}}{(z_1+z_2)^{1.5}} \gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu} \right)$$

$$(97)$$

Denominator only

1

(98)

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1^2 k_{\sigma_1}}{4(z_1+z_2)^{2.5}} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu} \right)$$

$$(99)$$

Denominator only

1

(100)

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^21\int_0^1 dz_1\int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right)$$

$$(101)$$

(102)

Denominator only

1

Integrating z-variables

Here we integrate all z-variables, the Feynman parameters.

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^2\gamma^{\mu}\gamma^{\nu}}{(z_1+z_2)^{0.5}} \right)$$
(103)

Integrating wrt z_2 ...

$$-2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^{2}\sqrt{z_{1}}\gamma^{\mu}\gamma^{\nu} + 2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m^{2}\gamma^{\mu}\gamma^{\nu} \tag{104}$$

Integrating wrt z_1 ...

$$\frac{2m^2}{3}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)\gamma^{\mu}\gamma^{\nu} \tag{105}$$

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_{2}^{1} dz_1 \int_{2}^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_1}}{(z_1+z_2)^{0.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} \right)$$
(106)

Integrating wrt z_2 ...

$$-2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m\sqrt{z_{1}}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu} + 2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mk_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu} \tag{107}$$

Integrating wrt z_1 ...

$$\frac{2m}{3}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu} \tag{108}$$

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu} \right)$$

$$(109)$$

Integrating wrt z_2 ...

$$-\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m\sqrt{z_{1}}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}$$

$$\tag{110}$$

Integrating wrt z_1 ...

$$-\frac{m}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu} \tag{111}$$

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu}\gamma^{\sigma_2}\gamma^{\nu} \right)$$
(112)

Integrating wrt z_2 ...

$$-\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)m\sqrt{z_{1}}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)mz_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu} \tag{113}$$

Integrating wrt z_1 ...

$$-\frac{m}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{2}}\gamma^{\nu} \tag{114}$$

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^21\int_0^1 dz_1\int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_1}\gamma^{\mu}}{(z_1+z_2)^{1.5}}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(115)

Integrating wrt z_2 ...

$$-2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} + \frac{2q_{1\sigma_{1}}}{\sqrt{z_{1}}}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} \tag{116}$$

Integrating wrt z_1 ...

$$2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} \tag{117}$$

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1^2 k_{\sigma_1}}{4(z_1+z_2)^{2.5}} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu} \right)$$
(118)

Integrating wrt $z_2...$

$$\frac{1}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)\sqrt{z_{1}}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} - \frac{1}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{1}^{2}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} \tag{119}$$

Integrating wrt z_1 ...

$$\frac{1}{18}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} \tag{120}$$

Integrating this term

$$\frac{1249999896.56489i}{\pi^2}e^2 \int_0^1 dz_1 \int_0^{-z_1+1} dz_2 \left(-\frac{\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_1k_{\sigma_1}}{2(z_1+z_2)^{1.5}} \gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu} \right)$$
(121)

Integrating wrt $z_2...$

$$-\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)\sqrt{z_{1}}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} + \epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)z_{1}k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}$$

$$\tag{122}$$

Integrating wrt $z_1...$

$$-\frac{1}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu} \tag{123}$$

Final amplitudes after z-variable integration

$$\frac{1249999896.56489i}{\pi^2} e^2 1 \left(\frac{2m^2}{3} \epsilon_{\nu}(k) \bar{\epsilon}_{\mu}(k) \gamma^{\mu} \gamma^{\nu} \right)$$
 (124)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \left(\frac{2m}{3}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}\right)$$
(125)

$$\frac{1249999896.56489i}{\pi^2}e^21\left(-\frac{m}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\nu}\right)$$
(126)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \left(-\frac{m}{6} \epsilon_{\nu}(k) \bar{\epsilon}_{\mu}(k) k_{\sigma_1} \gamma^{\mu} \gamma^{\sigma_2} \gamma^{\nu} \right)$$
 (127)

$$\frac{1249999896.56489i}{\pi^2}e^21\left(2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right) \tag{128}$$

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \left(\frac{1}{18}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_1}\gamma^{\mu}\gamma^{\sigma_1}\gamma^{\sigma_2}\gamma^{\nu}\right)$$
(129)

$$\frac{1249999896.56489i}{\pi^2}e^2 1 \left(-\frac{1}{6} \epsilon_{\nu}(k) \bar{\epsilon}_{\mu}(k) k_{\sigma_1} \gamma^{\mu} \gamma^{\sigma_1} \gamma^{\sigma_2} \gamma^{\nu} \right) \tag{130}$$

Evaluating spins and gamma matrices

TODO jk do it yourself you slags, here's the sum, have fun. Don't forget to take traces/multiply by -1 for internal fermion loops.

$$\frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(\frac{2m^{2}}{3}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)\gamma^{\mu}\gamma^{\nu}\right) + \frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(\frac{2m}{3}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}\right) + \frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(-\frac{m}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\nu}\right) + \frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}\right) + \frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(2\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)q_{1\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}\right) + \frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(-\frac{1}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}\right) + \frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(-\frac{1}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}\right) + \frac{1249999896.56489i}{\pi^{2}}e^{2}1\left(-\frac{1}{6}\epsilon_{\nu}(k)\bar{\epsilon}_{\mu}(k)k_{\sigma_{1}}\gamma^{\mu}\gamma^{\sigma_{1}}\gamma^{\sigma_{2}}\gamma^{\nu}\right)$$