

Circuit Theory and Electronics Fundamentals MEAer Example

Laboratory Report March 25, 2021

Contents

1	Introduction	1
2	Theoretical Analysis	2
3	Nodal method	2
4	Mesh method	3

1 Introduction

The objective of this laboratory is to study the behaviour of the circuit using nodal method and mesh method. The circuit contains both dependent and independent current and voltage source, I_b, I_d, V_c and V_a respectively. The circuit also has resistors with known resistance. The circuit can be seen in figure 1.

In Section 2, a theoretical analysis of the circuit is presented. In Section ??, the circuit is analysed by simulation, and the results are compared to the theoretical results obtained in Section 2. The conclusions of this study are outlined in Section ??.

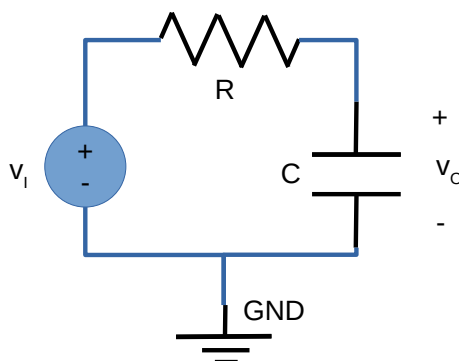


Figure 1: Dependent and Independent sources circuit.

2 Theoretical Analysis

This section, the circuit shown in Figure 1 is analysed theoretically, in terms of nodal and mesh method.

3 Nodal method

$$R_1 = 1.0216234171$$

$$R_2 = 3.0213296603$$

$$R_4 = 4.17287588373$$

$$R_5 = 3.07453996538$$

$$R_6 = 2.06761158432$$

$$R_7 = 7.0023872588$$

$$I_d = 1.00202530449$$

$$K_b = 1.00202530449$$

$$K_c = 8.38330387808$$

The circuit has 7 nodes, labeled as 1 to 7. Node 0 is chosen as ground ($V_0 = 0$). Using KCL for essential nodes (node 1, 4, 5, and 6), we have:

$$\text{Node 1: } \frac{V_1}{R_7} + \frac{V_2 - V_1}{R_6}$$

Using conductance, $G = \frac{1}{R}$, we get:

$$V_1 * G_7 + (V_2 - V_1) * G_6 \dots \dots \dots (1)$$

Node 4:

$$(V_3 - V_4) * G_1 - (V_4 - V_7) * G_3 + (V_5 - V_4) * G_2 \dots \dots \dots (2)$$

Node 5:

$$I_b = (V_5 - V_4) * G_2 \dots \dots \dots (3)$$

Node 6:

$$I_d - I_b = (V_6 - V_7) * G_5 \dots \dots \dots (4)$$

For node 7, $V_7 = V_c = K_c * I_c$

Using octave to find the nodes voltages we get:

$$V_1 = C_3$$

$$V_4 = \frac{G_3 * C_3 + I_b}{G_1 + G_3}$$

$$V_5 = \frac{G_2 * G_3 * C_3 + I_b * (G_1 + G_2 + G_3)}{G_2 * (G_1 + G_3)}$$

$$V_6 = C_3 + \frac{I_d}{G_5}$$

Substituting with the known values we have:

$$V_1 = 3.02$$

$$C_3 + 3.0745 = V_b$$

$$V_6 = 6.09$$

$$0.68 * C_3 + I_b = V_5$$

$$0.68(3.02) + I_b = V_5$$

$$V_5 = 2.05 + I_b$$

$$0.25(C_3 + I_b) = V_4$$

$$0.25(3.02 + I_b) = V_4$$

$$0.76 + 0.76 * I_b = V_4$$

$$\frac{-V_5 - V_4}{R_2} + I_b = -I_b$$

$$\frac{-2.05 - I_b * 0.76 - 0.76 * I_b}{2.01} = -I_b$$

$$-2.70 * I_b - 0.76 = -2.01 * I_b$$

$$0.69 * I_b = 0.76$$

$$I_b = -1.10 \text{ mA}$$

$$V_5 = 2.05 - 1.10$$

$$V_5 = 0.95v$$

$$V_4 = -0.076v$$

$$V_4 = 0.076v$$

$$V_6 = 6.09V$$

$$V_1 = 3.02v$$

4 Mesh method

Using KVL to find the currents in a circuit in Figure ??, we have:

Mesh 1:

$$I_1 = -I_b = -K_b * V_b \dots \dots \dots (1)$$

Mesh 2:

$$I_2 = -I_d \dots \dots \dots (2)$$

Mesh 3:

$$-I_3(R_7 + R_6 + R_4) + R_4 - I_4 = V_c \dots \dots \dots (3)$$

Mesh 4:

$$I_1 * R_3 + I_3 * R_4 - I_4(R_1 + R_3 + R_4) = -V_a$$

Using octave we get the values of currents as:

$$I_1 = -I_b$$

$$I_2 = I_d$$

$$V_3 = \frac{I_b * R - 3 * R_4 - R_4 * V_a + V_c (R_1 + R_3 + R_4)}{R_4^2 - (R_1 + R_3 + R_4) * (R_4 + R_6 + R_7)}$$

$$V_4 = \frac{I_b * R_3 * (R_4 + R_6 + R_7) + R_4 * V_c - V_a (R_4 + R_6 + R_7)}{R_4^2 - (R_1 + R_3 + R_4) (R_4 + R_6 + R_7)}$$