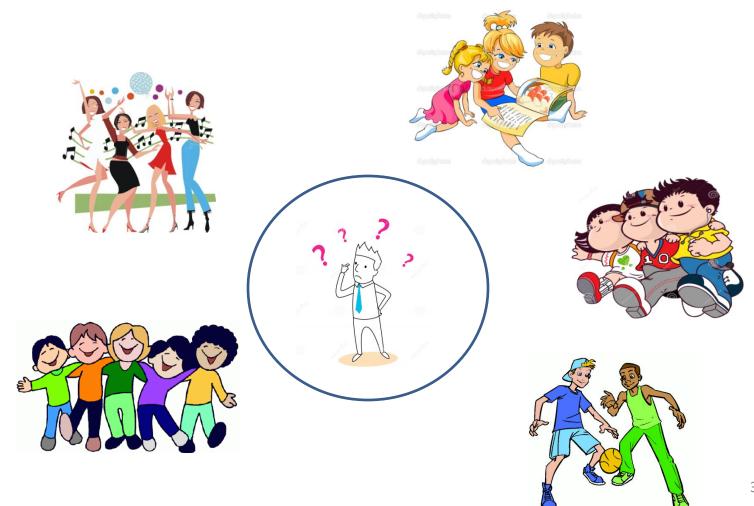
Algorithms: K Nearest Neighbors

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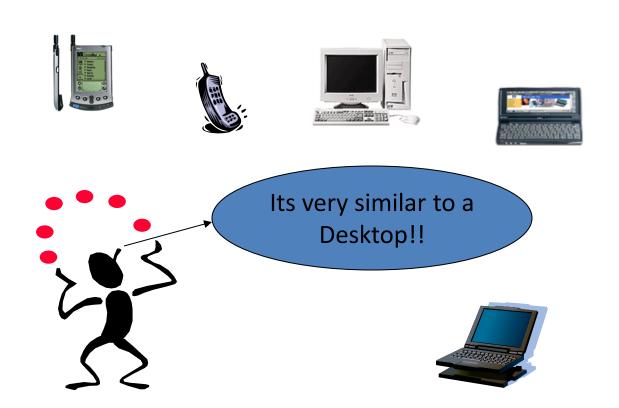


Simple Analogy...

 Tell me about your friends(who your neighbors are) and I will tell you who you are.



Instance-based Learning



KNN – Different names

- K-Nearest Neighbors
- Memory-Based Reasoning
- Example-Based Reasoning
- Instance-Based Learning
- Lazy Learning



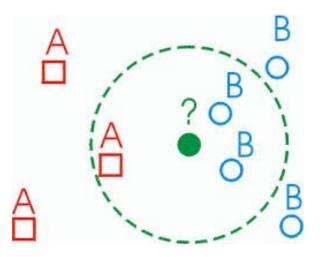
What is KNN?

- A powerful classification algorithm used in pattern recognition.
- K nearest neighbors stores all available cases and classifies new cases based on a similarity measure (e.g. distance function)
- One of the top data mining algorithms used today.
- A non-parametric lazy learning algorithm (An Instancebased Learning method).

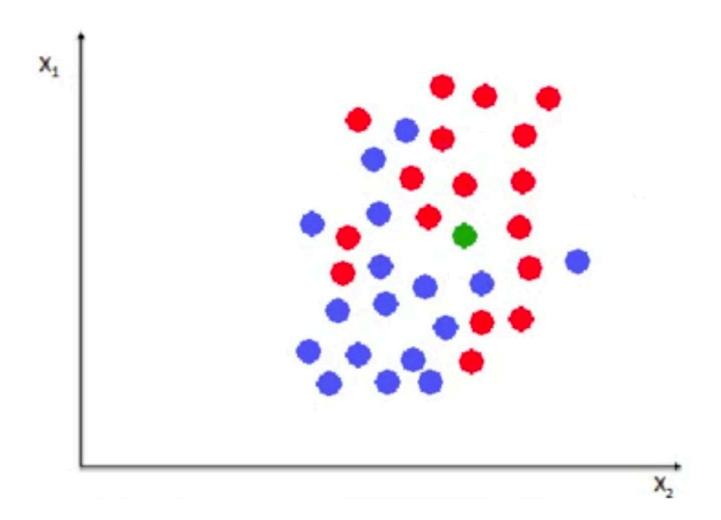


KNN: Classification Approach

- An object (a new instance) is classified by a majority votes for its neighbor classes.
- The object is assigned to the most common class amongst its K nearest neighbors.(measured by a distant function)

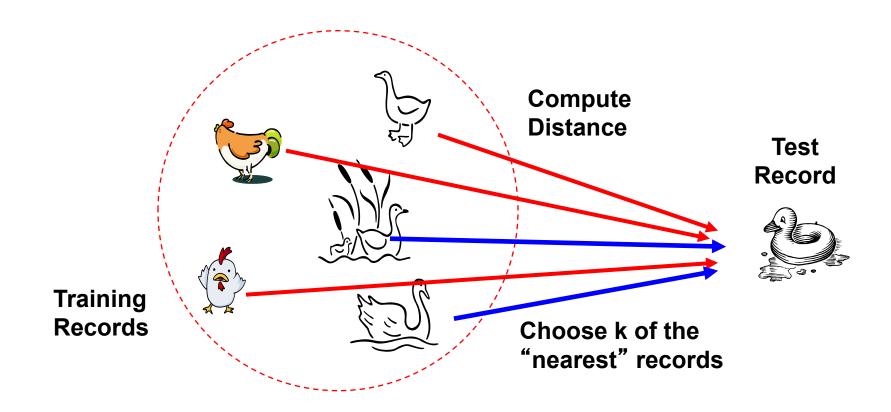






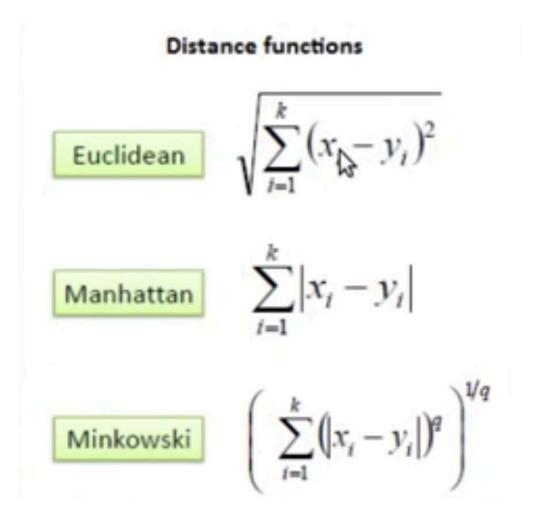


Distance Measure





Distance measure for Continuous Variables





Distance Between Neighbors

Calculate the distance between new example
(E) and all examples in the training set.

Euclidean distance between two examples.

$$-X = [x_1, x_2, x_3, ..., x_n]$$

$$-Y = [y_1, y_2, y_3, ..., y_n]$$

– The Euclidean distance between X and Y is defined as:

 $D(X,Y) = \sqrt{\sum_{i=1}^{n} (x_i - y_i)^2}$



K-Nearest Neighbor Algorithm

- All the instances correspond to points in an n-dimensional feature space.
- Each instance is represented with a set of numerical attributes.
- Each of the training data consists of a set of vectors and a class label associated with each vector.
- Classification is done by comparing feature vectors of different K nearest points.
- Select the K-nearest examples to E in the training set.
- Assign E to the most common class among its K-nearest neighbors.

3-KNN: Example(1)

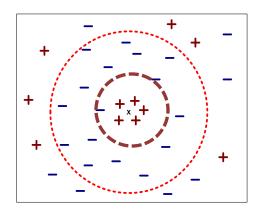
Customer	Age	Income	No. credit cards	Class
George	35	35K	3	No
Rachel	22	50K	2	Yes
Steve	63	200K	1	No
Tom	59	170K	1	No
Anne	25	40K	4	Yes
John	37	50K	2	YES

Distance from John
sqrt [(35-37) ² +(35-50) ² +(3- 2) ²]=15.16
sqrt [(22-37) ² +(50-50) ² +(2- 2) ²]=15
sqrt [(63-37) ² +(200-50) ² +(1- 2) ²]=152.23
sqrt [(59-37) ² +(170-50) ² +(1- 2) ²]=122
sqrt [(25-37) ² +(40-50) ² +(4- 2) ²]=15.74

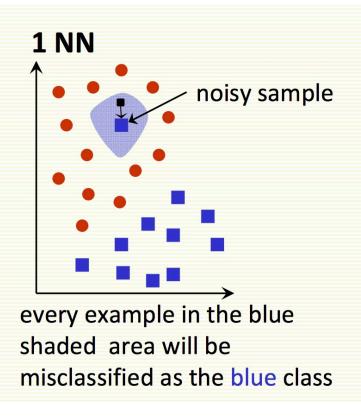


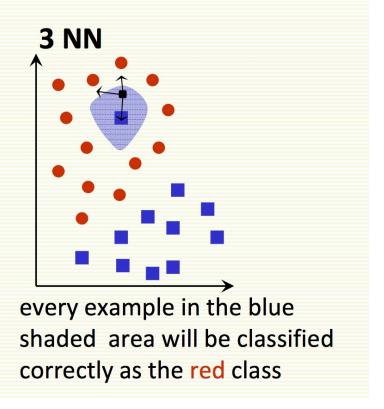
How to choose K?

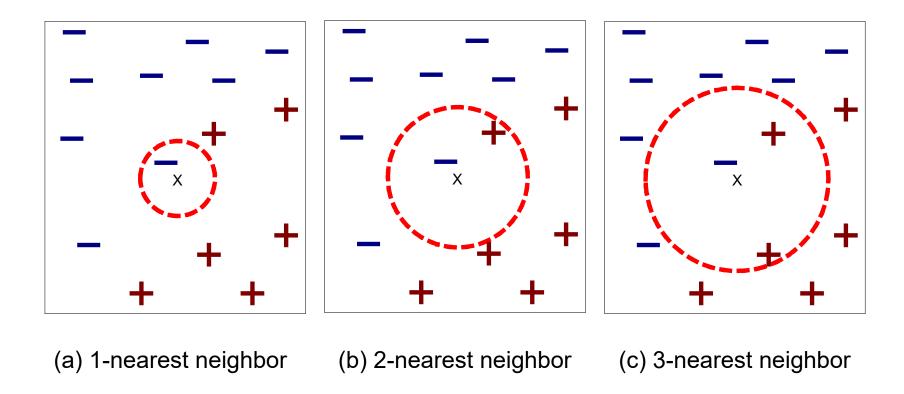
- If K is too small it is sensitive to noise points.
- Larger K works well. But too large K may include majority points from other classes.



Rule of thumb is K < sqrt(n), n is number of examples.







K-nearest neighbors of a record x are data points that have the k smallest distance to x

KNN Feature Weighting

 Scale each feature by its importance for classification

$$D(a,b) = \sqrt{\sum_{k} w_{k} (a_{k} - b_{k})^{2}}$$

- Can use our prior knowledge about which features are more important
- Can learn the weights $\mathbf{w_k}$ using cross-validation (to be covered later)



Feature Normalization

- Distance between neighbors could be dominated by some attributes with relatively large numbers.
 - e.g., income of customers in our previous example.

$$a_i = \frac{v_i - \min v_i}{\max v_i - \min v_i}$$

- Arises when two features are in different scales.
- Important to normalize those features.
 - Mapping values to numbers between 0 1.

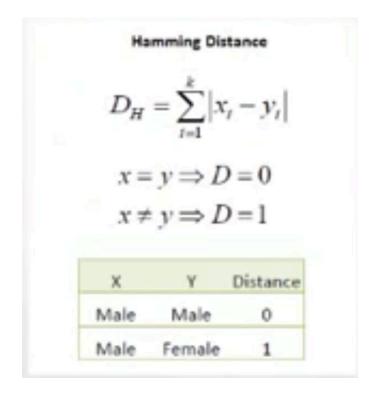


Nominal/Categorical Data

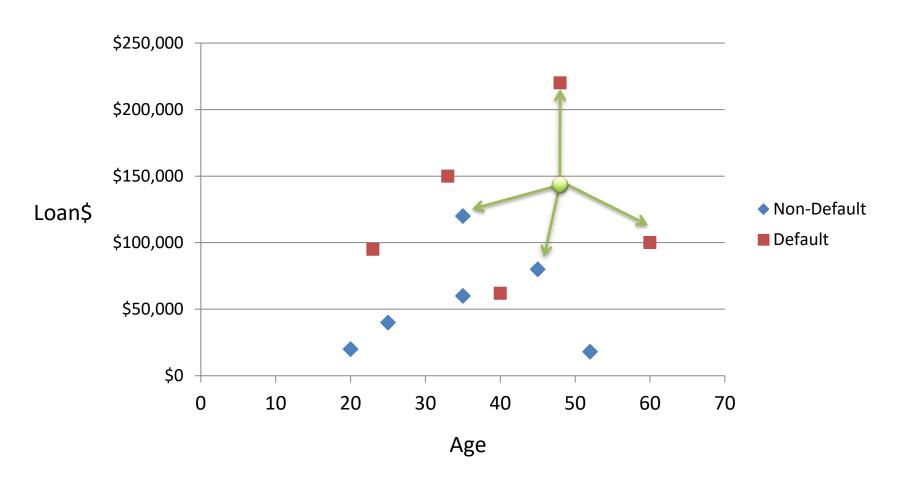
Distance works naturally with numerical attributes.

Binary value categorical data attributes can be regarded as 1

or 0.



KNN Classification



KNN Classification — Distance

Age	Loan	Default	Distance
25	\$40,000	N	102000
35	\$60,000	N	82000
45	\$80,000	N	62000
20	\$20,000	N	122000
35	\$120,000	N	22000
52	\$18,000	N	124000
23	\$95,000	Υ	47000
40	\$62,000	Υ	80000
60	\$100,000	Υ	42000
48	\$220,000	Υ	78000
33	\$150,000	Υ ←	8000
		<u> </u>	
48	\$142,000	Ŷ	

$$D = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$



KNN Classification — Standardized Distance

Age	Loan	Default	Distance
0.125	0.11	N	0.7652
0.375	0.21	N	0.5200
0.625	0.31	N ←	0.3160
0	0.01	N	0.9245
0.375	0.50	N	0.3428
0.8	0.00	N	0.6220
0.075	0.38	Υ	0.6669
0.5	0.22	Υ	0.4437
1	0.41	Υ	0.3650
0.7	1.00	Y	0.3861
0.325	0.65	Y	0.3771
0.7	0.61	¿ Ś	

$$X_{s} = \frac{X - Min}{Max - Min}$$



Strengths of KNN

- Very simple and intuitive.
- Can be applied to the data from any distribution.
- Good classification if the number of samples is large enough.

Weaknesses of KNN

- Takes more time to classify a new example.
 - need to calculate and compare distance from new example to all other examples.
- Choosing k may be tricky.
- Need large number of samples for accuracy.