

Urban exodus or rural shrinkage? Regional migration and attractiveness in a tight Dutch housing market

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ABSTRACT

In this paper, I address the impact of home-ownership and social renting rates on interregional migration in the Netherlands. I focus especially on their relation with natives' migration out of the larger and more popular Dutch urban regions. By applying a multilevel social relations model I am able to control simultaneously for (i) both region-specific effects of origin and destination, (ii) dyad (regional pair) specific effects, and (iii) the impact of the housing market structure in both the region of origin and the region of destination. I find positive and high elasticities of social renting (0.8) and homeownership (1.8) rates on out-migration, while homeownership rates have a smaller and negative impact (−0.5) on in-migration—pointing to the significant role the housing market has on the crowding out of natives in the larger urban regions. On top of that, I find that regional specific in- and out-migration flows are highly correlated (0.9) just as regional specific dyadic flows (0.8), showing each region's and dyad's ideosyncratic migration pattern. Finally, I show that the probabilistic model proposed is able to accurately predict migration flows both within and out-of-sample.

1. Introduction

In the recent decade cities have been proclaimed to be the overall “winners” within the regional socio-economic landscape (Glaeser, 2012). Indeed, there is an abundant empirical literature that finds that especially large metropolitan areas exhibit—on average—relatively more employment, more innovation and produce overall more added value (see, e.g., Balland et al., 2020). Most of this success of (large) cities can be attributed to positive regional and urban agglomeration economies (see for recent overviews of the size, scope and nature of these urban economies Melo et al., 2009; Duranton and Puga, 2020; Rosenthal and Strange, 2020).

Arguably, however, urban benefits do not accrue to everyone equally and recent empirical research has highlighted the negative sides of the proclaimed urban success. For example, there is ample empirical evidence of rising levels of economic segregation within cities (Tammaru et al., 2015), of suburbanization of poverty (Hochstenbach and Musterd, 2018), and crowding out of the housing market by short-term rentals (Koster et al., 2018) and by the increasing influx of high-skilled migrants to the most popular (inner) cities (Beckers and Boschman, 2019).

Indeed, many native residents of large and popular cities are moving out (cite ...)

Figure 1 illustrates this by showing out-migration rates of the urban region of Amsterdam for various age cohorts in the period 2011–2019.

To anticipate the results of this paper, I find strong negative effects of home-ownership rates on both in- and out-migration flows. Further, social renting rates also affect regional migration flows negatively, but only for out-migration. So, regions associated with ...

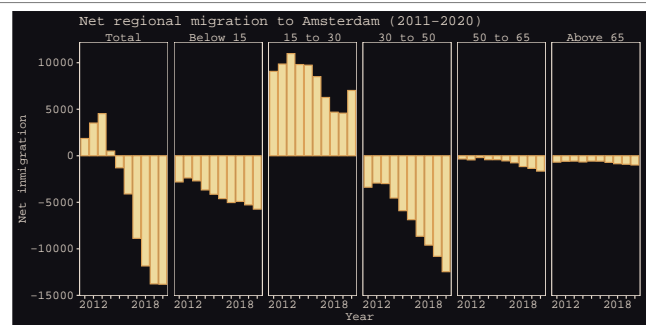


Figure 1: Net regional (domestic) migration into Amsterdam in the period 2011–2020 for various age cohorts (including total population in the most left-panel)

This paper reads as follows. The next section describes the data and focuses especially on the distribution of regional migration flows and housing market structure. Section 3 describes the modelling approach, where starting from traditional gravity model and using the descriptives of the migration flows, a Bayesian multilevel gravity model is constructed. Section 4 gives both the model results and interprets them by providing as well predictions within and out-of-sample. The last section concludes.

2. Literature

The current Dutch housing market is characterized by a low housing supply elasticity, high housing demand, and only a small segment (10%) that belongs to the private rental market (Michielsen et al., 2017). Because of the resulting large shortage of housing, many policy recommendations have been proposed, including plans for 700,000 new houses to be built in the coming decade. Unfortunately, the construction of a large amount of new dwellings is problematic in the

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Netherlands due to large and restrictive spatial constraints (Michielsen et al., 2019). Therefore, policy makers consider as well to change the housing structure, e.g., by converting rent controlled housing to home-ownership properties, to tackle at least the high housing prices by enlarging the home-ownership segment.

There is already a large amount of literature looking into the positive and negative effects of home-ownership—both from a private and from a social perspective (see for an overview Dietz and Haurin, 2003). It is argued that home-ownership leads to, e.g., better maintenance (of the own dwelling and the neighbourhood), more savings, higher education outcomes, higher individual labor supply, and even better health. One prominent negative effect of home-ownership is that it leads to less incentives to move residence because of higher moving costs vis-à-vis private renting.

This paper revisits the role of housing market structure as impediment for inter-municipality migration and specifically focuses on the role of home-ownership and social renting rates. In addition, it gives a framework to predict changes in the whole network of migration flows, when housing market structure change locally. To this end, I adopt a Bayesian multilevel gravity model which is not frequently encountered in the traditional gravity literature.¹ Traditional gravity modelling has the disadvantage that either municipality fixed effects of origins and destinations can be flows. This paper circumvents this disadvantage by adopting a multilevel incorporated or the municipalities' characteristics when not varying over approach with partial pooling², where the latter terms indicates that I do not impose fixed effects to control for origin and destination specific effects, but that I “draw” them from a distribution, hence the name partial pooling (where complete pooling states no group effects and no pooling fixed effects).

This papers adds two main elements to the literature. First, it does not only consider home-ownership but as well municipal social renting structure, which can be argued (see, e.g., Hughes and McCormick, 1981; Boyle and Shen, 1997; Boyle, 1998) to have a large effect on regional mobility as well as social renting rights are usually only valid locally (within municipality) and are lost when moving residence between municipalities.

Second, a partial pooling approach has another advantage, namely the municipal varying effects are completely probabilistic, making it feasible to predict both within and out-of-sample. In other words, with the results at hand I can predict migration flows between existing *and* hypothetical cities. The former might be used for looking at counterfactuals; for example, the changes in in-migration for all municipalities,

when one municipality changes its housing structure. The latter is useful when one wants to assess new migrations flows between one or even two new municipalities outside the sample.³

That housing market structure has a sizeable effect on migration decisions is empirically well-established, especially at the micro-level, where it is widely accepted that home-ownership has a negative effect on municipal mobility (Dietz and Haurin, 2003; Dohmen, 2005). For example, Palomares-Linares and van Ham (2018) find that home-ownership has a very strong immobility effect on internal migration in Spain during the period 2001–2011.

In the literature, less attention has been given to inter-city migration on the aggregate level with respect to the housing market as a specific barrier.⁴ For the UK, Congdon (2010) found within a multilevel gravity model that social rented housing had little effect on the attractivity of a region, although it had a small positive effect on preventing people from moving residence. For the Canadian case, Amirault et al. (2016) looked at the impact of home-ownership on migration flows within a gravity model using a Poisson pseudo maximum likelihood estimator and found an elasticity around -1 .

One of the main reasons to look into housing market structure and migration is that higher moving costs are detrimental to the aggregate labor market (Oswald, 1996, 1999). There is a large empirical literature (see, e.g., Munch et al., 2006, 2008; De Graaff and Van Leuvensteijn, 2013) looking at the impact of individual and aggregate home-ownership on labour market performance, where seemingly paradoxically at the aggregate level home-ownership is indeed harmful for labour market behaviour where at the individual level it is correlated with positive labour market performance.

This difference between individual and aggregate level is explained by sorting. Home-owners are indeed less mobile than private renters because of higher fixed and sunk moving costs which has a negative *aggregate* effect on labour market performance. However, home-owners are different from renters as they do *individually* better on the labour market (due to individual unobserved heterogeneity). So home-owners in countries with high home-ownership rates perform worse on the labour market vis-à-vis home-owners in countries with low home-ownership rates; but they still perform better than private renters. For social renters, the effect is different from private renters. On the individual level they are less mobile than renters at the free market as well, but their labor market performance is also worse than that of private renters (Hughes and McCormick, 1981; De Graaff et al., 2009).

¹That is, in the economic literature; a notable exception is Ranjan and Tobias (2007) in the economic trade literature. In the geographical literature this approach is more commonly adopted (see within a migration context Congdon, 2010; Congdon and Lloyd, 2012)

²There is a whole variety of names for these types of models, including hierarchical modeling, varying effects, mixed effects and shrinkage models. I use the more generic multilevel description as municipality and flows are by definition measured at a different level (scale) (see Gelman et al., 2013, for an indepth discussion).

³See for probabilistic predictions of international migration Azose and Raftery (2015).

⁴See Cushing and Poot (2004) for a historical overview of common themes within migration research.

3. Modeling framework

3.1. The traditional gravity model

In most disciplines, the workhorse model to study aggregate empirical migration flows has been the gravity model (see Anderson (2011) for a generic survey of the use of gravity models and Poot et al. (2016) for an overview of migration applications). I therefore start by adopting the basic gravity model specification pioneered by Tinbergen (1962), so:

$$\text{migrants}_{ij} = M_i^{\beta_1} M_j^{\beta_2} \text{dist}_{ij}^{\gamma}, \quad (1)$$

where migrants_{ij} are the number of migrants moving from i to j , M_i (M_j) denotes the ‘mass’ of i (j), and dist_{ij} the distance between i and j . Usually, the ‘mass’ variables are proxied by population, gross domestic product, density, etcetera. Moreover, the variable dist_{ij} may represent in general all sorts of frictions, not only physical distance.

Crucially, Anderson and Van Wincoop (2003) argue that origin and destination specific variables should be incorporated to take into account multilateral resistance terms. Most often, this is done by log-linearising model (1 and incorporating fixed effects for origins and destinations, as follows:

$$\log(\text{migrants}_{ij}) = o_i + d_j + \gamma \log(\text{dist}_{ij}) \quad (2)$$

Note that now all origin and destination specific variables are absorbed by the fixed effects o_i and d_j and that only variables affecting the frictions (dist_{ij}) can be incorporated, which could be cumbersome if one is especially interested in those variables.^{5,6} Figure 2 denotes the problem schematically in a generic dyadic type of network. Typically, one wants to model migration flows between i and j , whilst taken into account both the regional specific effects (o_i and d_j) and the regional variables (\mathbf{X}_i and \mathbf{X}_j) one is interested in, such as housing market, population structure or cultural variables.

Moreover, equation (2) is typically estimated with linear regression type of models, which is often very cumbersome given the large amount of zeros migrants flows. ‘Quick and dirty’ remedies as adding a small amount to the flow variable or removing all zeros have been proven to seriously bias the results (Linders and De Groot, 2006; Burger et al., 2009).

Therefore, I opt in the next subsection for a different strategy, with which I can tackle simultaneously the two disadvantages of above: incorporating both city varying effects and city specific variables and modelling the distribution of migrants flows as they are displayed in Figure 3—even when being zero.

⁵If there is another variable dimension—say, repeated observations over time—then this problem might be circumvented. However, this requires enough variation in the data as time-invariant variables can still not be taken into account.

⁶An often applied strategy to overcome this problem is to use differences between origin and destination specific variables. Take for example Δh_{ij} as the difference in home-ownership rates between i and j . A disadvantage of this approach is that the difference between 10% and 20% home-ownership rates and the difference between 80% and 90% home-ownership rates would be valued as the same.

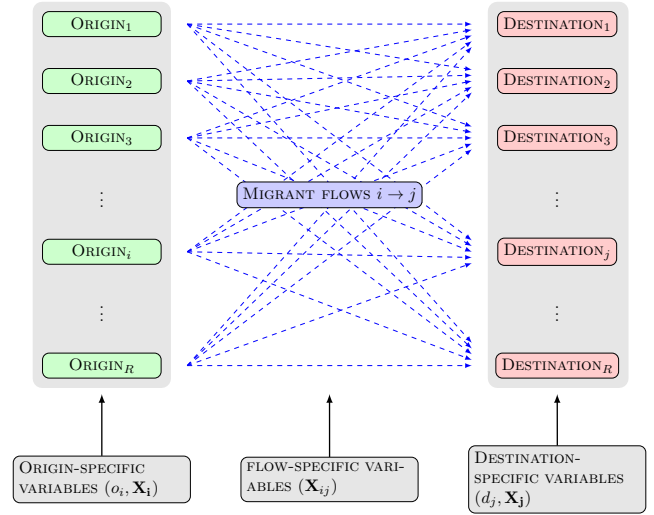


Figure 2: Decomposition of variables impacting migration flows from i to j ($\{i, j\} \in \{1, \dots, R\}$)

3.2. A multilevel social relations model for migrants flows

First, as municipal migrants flows are discrete, non-negative and relatively rare give the size of the population, theoretically the most appropriate way to go forward is to model migrant flows with a Poisson type of model. However, given that the sampling variance is much larger than the sampling mean of the migration flows (although not conditional on the covariates), we likely need to correct for overdispersion of heteroskedasticity (Silva and Tenreiro, 2006, states that heteroskedasticity (rather than the presence of too many zeros) is responsible for the main source of bias within gravity models.). An often used distribution to account for overdispersion is the Gamma-Poisson model (which is under re-parametrization similar to the perhaps better known negative binomial model). So, we use that for our outcome variable.

To account for the multiplicative nature of the theoretical model as in (1), I adopt a log link for the expected number of migrants λ_{ij} in the Gamma-Poisson model. Apart from the theoretical model, note that this log link ensures as well that the expected number of migrants is always positive. Further, I assume that $\log(\lambda_{ij})$ is a linear function of the municipal specific variables and the distance between i and j .

Finally, to adopt both municipality effects and variables I adopt a multilevel model with partial pooling. This entails that the municipal varying effects (unlike fixed effects) are now drawn from a, in this case Normal, distribution, where the parameters of this distribution are estimated as well (in the Bayesian literature they are known as well as hyper-parameters). Intuitively, this entails that municipalities are partially pooled indicating that (statistical) information between municipalities is shared. This is an attractive feature, as fixed effects assume no pooling. In that case, the model only learns from the information contained in that specific

municipality whereas with partial pooling it is ensured that outliers (very high or low effects) are effectively *shrunk* towards the mean. Indeed, this is a further extension of that best feature of linear regression: regression towards the mean.

The complete model now looks as follows:⁷

$$\text{Migrants}_{ij} \sim \text{Gamma-Poisson}(\lambda_{ij}, \tau) \quad (3a)$$

$$\begin{aligned} \log(\lambda_{ij}) = & \alpha + o_{\text{mun}[i]} + d_{\text{mun}[j]} + \\ & \beta_1 \log(\text{pop}_i) + \beta_2 \log(\text{pop}_j) + \\ & \beta_3 \log(\text{home}_i) + \beta_4 \log(\text{home}_j) + \\ & \beta_5 \log(\text{soc}_i) + \beta_6 \log(\text{soc}_j) + \\ & \beta_7 \log(\text{dist}_{ij}) \end{aligned} \quad (3b)$$

$$d_{\text{mun}} \sim \text{Normal}(0, \sigma_d) \quad (3c)$$

$$o_{\text{mun}} \sim \text{Normal}(0, \sigma_o) \quad (3d)$$

$$\beta_1, \dots, \beta_7 \sim \text{Normal}(0, 2) \quad (3e)$$

$$\alpha_o, \alpha_d \sim \text{Normal}(0, 2) \quad (3f)$$

$$\sigma_o, \sigma_d \sim \text{HalfCauchy}(0, 1) \quad (3g)$$

$$\tau \sim \text{Gamma}(0.01, 0.01) \quad (3h)$$

The first part (3a) models the outcome variable, being the number of migrants, using a Gamma-Poisson distribution (with parameter λ_{ij}) allowing for overdispersion by using an additional parameter τ . The being elasticities. Equations (3d) and (3c) constitute the linear part of the model is given by (3b) and states that the poisson outcome variable is on a log-scale and that most explanatory variables are on a log-scale as well, allowing for direct comparison of the parameters multilevel part, where parameters σ_o and σ_d measures the amount of pooling. If they go to zero, then the data exhibits complete pooling. If they become very large (go to infinity) there is no pooling (which is the fixed effects case). Equations (3e)–(3h) denote priors for all parameter involved. These priors are chosen that they are rather conservative. Namely, we know from previous empirical literature that the β -parameters typically are not lower than -2 or higher than 2 . But given the amount of data these priors are of little influence. The only structure I impose is that the standard deviations σ_o and σ_d are assumed to be non-negative with relatively probability in the their right tails. The Gamma prior for τ is a standard and as well a very conservative prior.

4. Data and methods

4.1. Data

I use inter-regional migration flows measured in individuals between all of the 40 Dutch COROP regions between 2012 and 2018. I use no information on within regional migration. So, I have 320 regional characteristics (or doubled when accounting for both origin and destination municipalities) and 10,902 aggregate migration flows ($7 \times (40 \times 40 - 40)$).

⁷I adopt here the model structure from McElreath (2020).

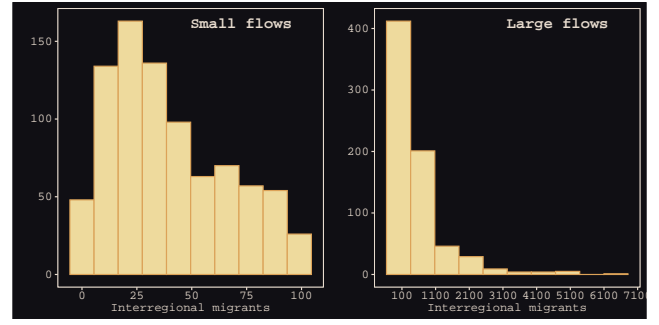


Figure 3: Histogram of inter-regional migrant flows. Left panel shows the histogram of small migrant flows ($0 \leq N < 100$) and the right panel shows the histogram of large migrant flows ($N \geq 100$). Note the different scale of the y-axes.

The histograms in Figure 3 show the distribution of migrant flows within my sample. The left panel deals with migrant flows below 100, the right panel with migrant flows of 100 and larger. Two main observations can be made.

First, there is a strong but consistent decay pattern in migration flow size in both panels, which points to a persistent underlying pattern. However, the right ‘tail’ in this distribution is rather thick.⁸ Thus, there are still observations quite far right in the distribution. Indeed, the sample mean is about 270, while the sample variance is around 290,000, leading to a strong presence of *overdispersion* (unconditional on other explanatory variables). Second, a small part of the dataset consists of zero observations. Although they do seem to be genuine observations and not caused by another process, I check in a robustness analysis whether the occurrence of zeros does need to be taken specifically into account.

Seven explanatory variables are added to the model. First, to account for spatial distance decay between origin i and destination j , distance between all regions are calculated as Euclidian distance between regional centroids (dist_{ij}). Secondly, as regional mass we use population size for both region of origin and region of destination (so pop_i and pop_j). Finally, for housing market structure we use variables indicating percentage of homeownership (home_i and home_j) and percentage of social renting (soc_i and soc_j), again in both regions of origin and destination. Social renting in the Netherlands includes all kinds of rent controlled housing but typically involves local housing corporations offering housing to lower income households, where eligibility is based on (local—within region) waiting lists.

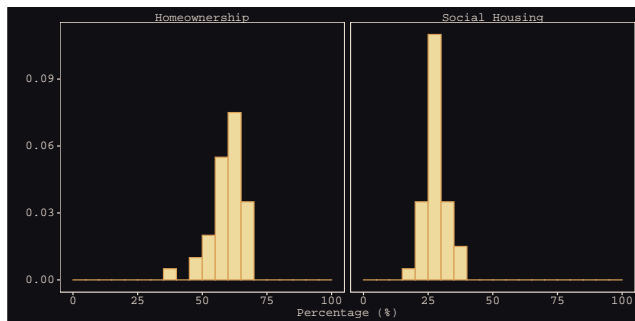
Figure 4 shows the distribution of social renting and homeownership across Dutch regions in 2018. Clearly, both home-ownership and social housing are prevalent across Dutch regions, with an average per city of 25% of social housing and around 60% of homeownership. Moreover, it is worthwhile to note that social renting is especially prevalent in the larger cities with a correlation of 0.46 between regional size and social renting (e.g., Amsterdam has about a 40% social renting rate). Also, more rural Dutch

⁸The largest migration flows are between the urban regions of Amsterdam and Utrecht and amount to about 6,555 migrants in 2018.

Table 1

This is a test caption.

b_dist	−1.345*** (0.001)	−1.385*** (0.001)	−1.686*** (0.001)	−1.628*** (0.024)
b_popb	0.827*** (0.001)	0.843*** (0.001)	0.516*** (0.031)	0.549*** (0.032)
b_popa	0.790*** (0.001)	0.770*** (0.001)	0.319*** (0.033)	0.318*** (0.033)
cons	4.793*** (0.001)	4.777*** (0.001)	4.595*** (0.176)	4.490*** (0.164)
b_sB		−1.474*** (0.007)	0.867*** (0.054)	0.867*** (0.054)
b_hB		−1.143*** (0.008)	0.169** (0.086)	0.166** (0.087)
b_sA		−1.821*** (0.007)	−0.245*** (0.055)	−0.259*** (0.054)
b_hA		−1.670*** (0.008)	1.575*** (0.088)	1.601*** (0.086)
sigma_y			0.125*** (0.046)	0.125*** (0.042)
sigma_gr.1			0.656*** (0.073)	0.673*** (0.082)
sigma_gr.2			0.466*** (0.053)	0.441*** (0.053)
Rho_1.3			0.803*** (0.060)	0.781*** (0.070)
sigma_d				0.385*** (0.009)
Rho_2.3				0.804*** (0.014)
PSIS_loo	849,398	793,476	384,369	123,396
R2	0.67	0.70	0.79	0.84

**Figure 4:** Histogram of social housing (left) and homeownership (right) percentages in COROP regions in 2018 (check)

regions exhibit much less social renting. Homeownership and city size correlate negatively (−0.63). Finally, there is a large negative correlation between social renting and homeownership (−0.88) across regions.

5. Results

6. Conclusions

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https://github.com/Thdegraaff/migration_gravity.

Acknowledgements

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