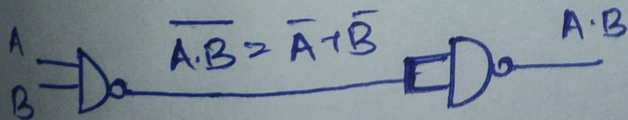
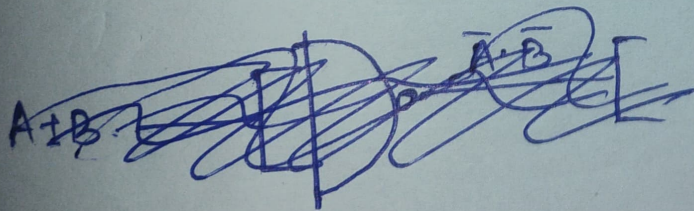
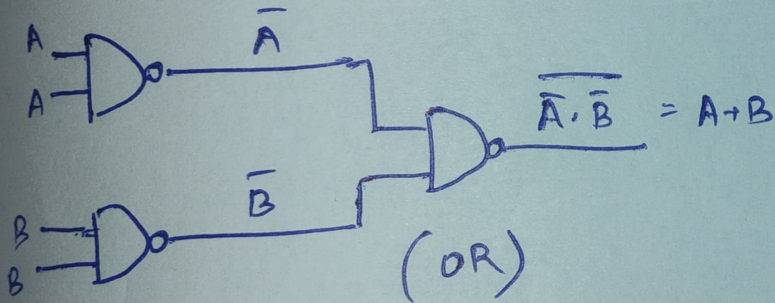


$A = 0$, Output = 1

$A = 1$, Output = 0

(NOT)



de Morgan,

$$\overline{A \cdot B} = \bar{A} + \bar{B}$$

$$\overline{A + B} = \bar{A} \cdot \bar{B}$$

Then,

$$\bar{A} \cdot \bar{B} = A + B$$

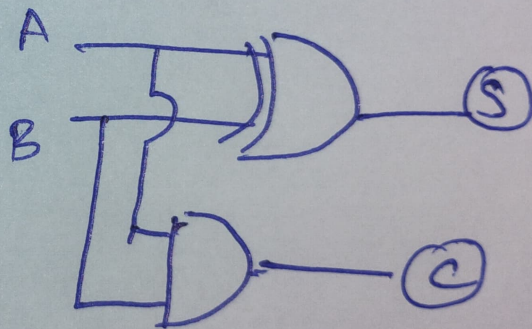
$$\overline{\bar{A} + \bar{B}} = A \cdot B$$

2. Half Adder

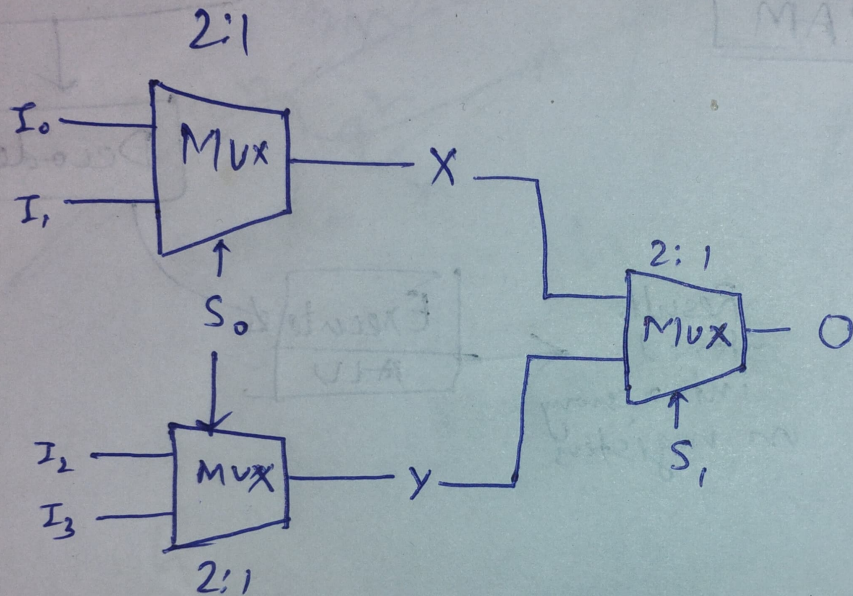
| <u>A</u> | <u>B</u> | <u>S</u> | <u>C</u> |
|----------|----------|----------|----------|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |

$$S = A \oplus B$$

$$C = A \cdot B$$



3.



To choose I_0 ,

$$S_0 = 0, S_1 = 0$$

To choose I_1 ,

$$S_0 = 1, S_1 = 0$$

To choose I_2

$$S_0 = 0, S_1 = 1$$

To choose I_3

$$S_0 = 1, S_1 = 1$$

$$X = \bar{S}_0 I_0 + S_0 I_1$$

$$O = \bar{S}_1 X + S_1 Y$$

$$Y = \bar{S}_0 I_2 + S_0 I_3$$

4. Two flip-flops are required

be the output of the FFs are S_1 and S_2

| S_1 | S_2 | |
|-------|-------|--------------------------------|
| 0 | 0 | $\rightarrow 0$ 1's |
| 0 | 1 | $\rightarrow 1$ 1's (together) |
| 1 | 0 | $\rightarrow 2$ 1's (together) |

$P = 1 \rightarrow$ when 3 trailing 1's are observed.

Two cycles $S_1 S_2$ and $S_{1\text{next}} S_{2\text{next}}$ are taken,

iff. $(S_1, S_2) \equiv (1, 0)$ and $(S_{1\text{next}}, S_{2\text{next}}) \equiv (1, 0)$

then, $P = 1$

i.e.

| S_1 | S_2 | $S_{1\text{next}}$ | $S_{2\text{next}}$ | P |
|-------|-------|--------------------|--------------------|-----|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 |

5.

| Q_1 | Q_0 | Q_1^* | Q_0^* |
|-------|-------|---------|---------|
| 0 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |

$$Q_1^* = Q_1 \oplus Q_0$$

$$Q_0^* = \overline{Q_0}$$