

Step 4

$$\begin{array}{ccccc}
 & S^0 \wedge S^0 & \xrightarrow{\text{id}_{\text{Sets}_*|S^0, S^0}^{\otimes, -1}} & S^0 \otimes_{\text{Sets}_*} S^0 & \xrightarrow{\text{id}_{\mathbb{1}/\text{Sets}_*}^{\otimes, -1} \wedge \text{id}_{S^0}} \\
 & \nearrow \lambda_{S^0}^{\text{Sets}_*, -1} & & & \\
 S^0 & \xrightarrow{\quad} & \lambda_{S^0}'^{-1} & \xrightarrow{\quad} & \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} S^0 \\
 & \downarrow \text{id}_{S^0} \wedge [x] & (1) & \downarrow \text{id}_{S^0} \otimes_{\text{Sets}_*} [x] & \\
 & & & & (4) \\
 & \downarrow & (5) & \downarrow & \\
 & S^0 \wedge X & \xrightarrow{\text{id}_{\text{Sets}_*|S^0, X}^{\otimes, -1}} & S^0 \otimes_{\text{Sets}_*} X & \xrightarrow{\text{id}_{\mathbb{1}/\text{Sets}_*}^{\otimes, -1} \wedge \text{id}_X} \\
 & \nearrow \lambda_X^{\text{Sets}_*, -1} & (2) & & \\
 X & \xrightarrow{\quad} & \lambda_X'^{-1} & \xrightarrow{\quad} & \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} X \\
 & \downarrow [x] & & & \downarrow \text{id}_{\mathbb{1}_{\text{Sets}_*}} \wedge [x]
 \end{array}$$

Diagram illustrating Step 4 of a proof, showing a commutative diagram with objects and morphisms.

The diagram consists of the following objects and morphisms:

- Top Row:**
 - $S^0 \wedge S^0 \xrightarrow{\text{id}_{\text{Sets}_*|S^0, S^0}^{\otimes, -1}} S^0 \otimes_{\text{Sets}_*} S^0 \xrightarrow{\text{id}_{\mathbb{1}/\text{Sets}_*}^{\otimes, -1} \wedge \text{id}_{S^0}} \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} S^0$
- Left Column:**
 - $S^0 \xrightarrow{\lambda_{S^0}^{\text{Sets}_*, -1}} S^0 \wedge S^0$
 - $S^0 \xrightarrow{[x]} X$
- Bottom Row:**
 - $S^0 \wedge X \xrightarrow{\text{id}_{\text{Sets}_*|S^0, X}^{\otimes, -1}} S^0 \otimes_{\text{Sets}_*} X \xrightarrow{\text{id}_{\mathbb{1}/\text{Sets}_*}^{\otimes, -1} \wedge \text{id}_X} \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} X$
- Right Column:**
 - $\mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} S^0 \xrightarrow{\text{id}_{\mathbb{1}_{\text{Sets}_*}} \wedge [x]} \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} X$
- Horizontal Morphisms:**
 - $S^0 \xrightarrow{\lambda_{S^0}'^{-1}} \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} S^0$ (labeled (1))
 - $S^0 \wedge X \xrightarrow{\lambda_X^{\text{Sets}_*, -1}} S^0 \otimes_{\text{Sets}_*} X$ (labeled (2))
 - $X \xrightarrow{\lambda_X'^{-1}} \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} X$
- Vertical Morphisms:**
 - $S^0 \wedge S^0 \xrightarrow{\text{id}_{S^0} \wedge [x]} S^0 \wedge X$ (labeled (3))
 - $S^0 \otimes_{\text{Sets}_*} S^0 \xrightarrow{\text{id}_{S^0} \otimes_{\text{Sets}_*} [x]} S^0 \otimes_{\text{Sets}_*} X$ (labeled (4))
 - $S^0 \otimes_{\text{Sets}_*} X \xrightarrow{\text{id}_{\mathbb{1}/\text{Sets}_*}^{\otimes, -1} \wedge \text{id}_X} \mathbb{1}_{\text{Sets}_*} \otimes_{\text{Sets}_*} X$ (labeled (5))