BoGL Syntax

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We generally adopt the Haskell rules for lexical syntax. In particular, *name* is used for function and parameter names and stands for alphanumeric strings starting with a lowercase letter. Similarly, *Name* is used for symbols (which are basically nullary constructors) and stands for alphanumeric strings starting with an uppercase letter. It is also used for the names of games. The nonterminal *int* stands for integer constants. Comments are also handled as in Haskell.

A game definition consists of a name, two mandatory type definitions for the board and player inputs, any number of additional type definitions, followed by any number of value and function definitions. The board definition determines the board dimensions and the type of values that can appear on a board.

Games and Type Definitions

```
game ::= game Name board input typedef^* valuedef^* (game definition)
board ::= type Board = Array (int,int) of type (board type)
input ::= type Input = type (input type)
typedef ::= type Name = type (type definition)
```

Value definitions (for values and functions) require a signature declaring their type plus an equation for defining the value. If a value is parameterized, that is, if it is followed by a parameter list, it represents a function.

A board definition (for a variable *name* with declared type Board) is equivalent to an array definition and may contain a number of definitions for individual positions (given by pairs of integers) and for sets of positions, which can be given by using a variable for either or both coordinates. The semantics of a definition such as board! (x,2) = Empty is to set all fields in the second row to Empty.

Value Definitions

```
valuedef ::= signature equation
                                              (value definition)
signature ::= name : type
                                              (type signature)
equation ::= name = expr
                                              (value equation)
                name\ parlist = expr
                                              (function equation)
                boarddef*
                                              (board definition)
boarddef ::= name ! (pos, pos) = expr
                                              (board equation)
     pos ::= int \mid name
                                              (board positions)
  parlist ::=
                (par_1, \ldots, par_k)
                                              (parameter\ list,\ k \geq 1)
     par ::= name | parlist
                                              (parameter)
```

The type system builds on a collection of basic types, which include predefined numbers and booleans as well as the type Symbol, which is the type for all symbol values (*Name*). The special type Input is a synonym for the type of information that is gathered from the user in each move during an execution of the game.

An enumeration type is given by a set of symbols, and an extended type adds to a base type one or

more symbols, which are values and can be thought of nullary data constructors. For example, the Haskell type Maybe Int can be represented by the extended type Int & {Nothing}. Extended types facilitate the extension of types by values for representing "special" situations. For example, Player & {Empty} is a type typically used in a board type definition.

A tuple type can contain extended types, and a plain type is either a tuple type or an extended type. The language has first-order function types whose argument and result types can be any plain type.

Types

```
\begin{array}{llll} \textit{btype} & ::= & \mathsf{Bool} \mid \mathsf{Int} \mid \mathsf{Symbol} \mid \mathsf{Input} & \textit{(base type)} \\ \textit{etype} & ::= & \{\mathit{Name}_1, \ldots, \mathit{Name}_k\} & \textit{(enumeration type)} \\ \textit{xtype} & ::= & \textit{btype} \mid \textit{xtype} \& \textit{etype} & \textit{(extended type)} \\ \textit{ttype} & ::= & (\textit{xtype}_1, \ldots, \textit{xtype}_k) & \textit{(tuple type}, k \geq 2) \\ \textit{ptype} & ::= & \textit{xtype} \mid \textit{ttype} & \textit{(plain type)} \\ \textit{ftype} & ::= & \textit{ptype} -> \textit{ptype} & \textit{(function type)} \\ \textit{type} & ::= & \textit{ptype} \mid \textit{ftype} & \textit{(type)} \\ \end{array}
```

Atomic expressions are either basic integer values or symbols. True and False are symbols of type Bool, all other symbols have either the type Symbol or the type of the type definition they occur in. For example, the type definition type Player = $\{A,B\}$ that occurs in the BoGL prelude defines A and B to be symbols of type Player. Note that the case for infix application includes the Haskell notation for array lookup board! (x,y).

Expressions

```
expr ::= int
                                              (integer)
            Name
                                              (symbol)
            name
                                              (variable)
                                              (parenthesized expression)
            (expr)
            (expr_1, \ldots, expr_k)
                                              (tuple, k \geq 2)
            name(expr_1, \ldots, expr_k)
                                              (function application)
            expr binop expr
                                              (infix application)
            let name = expr in expr
                                              (local definition)
                                              (conditional)
            if expr then expr else expr
            while expr do expr
                                              (while loop)
binop ::= + | - | == | ! | ...
                                              (binary operation)
```