

Florida Polytechnic University

COP 4020

Assignment #5

Due Date: Saturday, April 09, 2022, by 11:59 pm. In your assignment, please be sure to explain all mentioned points CLEARLY. ***Submit your assignment in electronic format (scan it if hard to write on computer and submit only on canvas, do not email me).***

Total Points of Assignment = 68

Q1) (Total 15 Points)

Use the pumping lemma to show that this language is nonregular:

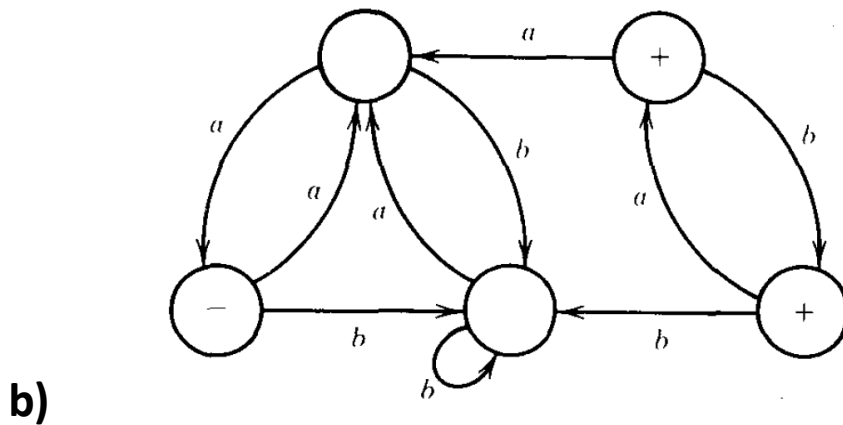
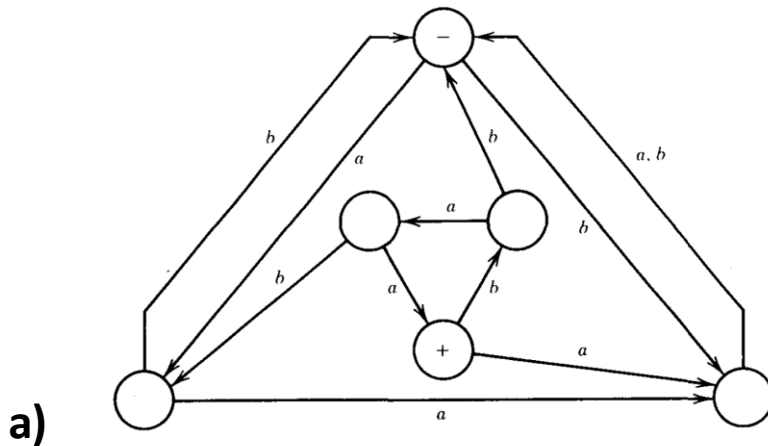
$$\{a^n b^n a^n\} = \{aba \ aabbaa \ aaabbbbaaa \ aaaabbbbbaaaa \dots\} \quad (5 \text{ Points})$$

$$\{a^n b a^n\} = \{aba \ aabaa \ aaabaaa \dots\} \quad (5 \text{ Points})$$

$$\{a^n b^{2n}\} = \{abb \ aabbbb \ aaabbbbbbb \dots\} \quad (5 \text{ Points})$$

Q2) (Total 10 Points)

By using blue paint, determine which of the following FA's accept any words:



Q3) (Total 18 Points)

Describe the language generated by the following context free grammar (CFG) in English and write regular expressions:

a)

$S \rightarrow SS$
 $S \rightarrow ZZZ$
 $Z \rightarrow bZ$
 $Z \rightarrow Zb$
 $Z \rightarrow a$

(3,3 Points)

b) $S \rightarrow aS$
 $S \rightarrow bb$ **(3,3 Points)**

c) $S \rightarrow XYX$
 $X \rightarrow aX$
 $X \rightarrow bX$
 $X \rightarrow \Lambda$
 $Y \rightarrow bbb$ **(3,3 Points)**

Q4) (Total 15 Points)

Find CFG for the following languages over the alphabet $\Sigma = \{a, b\}$:

- a) All words that have different first and last letters. **(5 Points)**
- b) All words in which the letter b is never tripled. **(5 Points)**
- c) All words that do not have substring ab. **(5 Points)**

Q5) (Total 10 Points)

Show that the CFG below is ambiguous by finding a word with two distinct syntax trees. Show both syntax trees.

a) $S \rightarrow Sbb$
 $S \rightarrow Sbbb$
 $S \rightarrow b$ **(5 Points)**

b) $S \rightarrow AA$
 $A \rightarrow AAA|a|bA|Ab$ **(5 Points)**

Wish You Best of Luck