

# Supplementary Materials

## Compressed Sensing for Characterization of Tinnitus

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**T**his document contains a description of additional experiments to find a performant stimulus generation method and a discussion of sparsity in tinnitus signals. The code for all experiments is freely available at <https://github.com/alec-hoyland/tinnitus-project> and the data are available upon request.

### I. STIMULUS GENERATION

In the context of this paper, a stimulus generation method is a process that generates a random waveform that is:

- 1) auditorally-distinguishable
- 2) statistically uncorrelated, and
- 3) similar to tinnitus percepts.

Additionally, compressed sensing requires that the matrix of stimuli should satisfy the restricted isometry property, which many random matrices do with high probability (*e.g.* Gaussian random matrices) [?], [?].

#### A. Auditorally-Distinguishable Stimuli

We used mel-frequency binning to ensure that our stimuli were auditorally-distinguishable. The mel scale is a perceptual scale of pitches judged by listeners to be equal in distance from one to another (Fig. ??) [?].

The formula

$$m = 2595 \log_{10} \left( 1 + \frac{f}{700} \right) \quad (1)$$

converts  $f$  Hz to  $m$  mels.

Furthermore, to reduce the system complexity by more than 80x, we implement tonotopic binning, where the frequency scale is binned along 100 equally mel-spaced bins (Fig. ??).

### II. HYPERPARAMETER SWEEP

To determine a suitable stimulus generation method, we performed a hyperparameter sweep over hyperparameters of nine different stimulus generation methods. We used an *in-silico* model of the experiment, matching against an American Tinnitus Association tinnitus example, as in the human experiment.

The methods are as follows:

- 1) *Bernoulli*: A binned method in which each tonotopic bin has a probability  $p$  of being set to 0 dB otherwise it is set to -20 dB.
- 2) *Brimijoin*: A binned method inspired by [?]. Each bin is assigned an amplitude value chosen from a uniform distribution of discrete values on the interval  $[-20, 0]$ . We used 6 steps, which is consistent with the original paper.

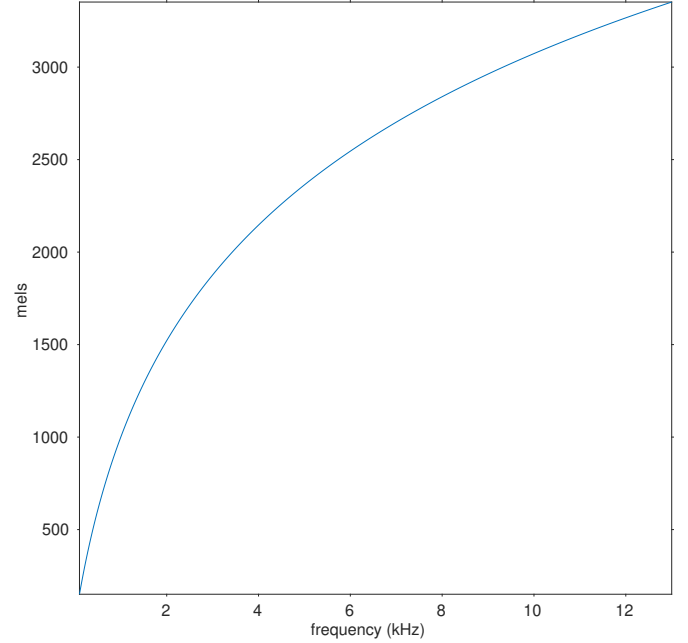


Fig. 1. The relationship between Hz and mels is logarithmic.

- 3) *Gaussian Noise No Bins*: The amplitude of each frequency was determined by Gaussian noise with known mean and variance, which are hyperparameters  $\mu$  and  $\sigma$ .
  - 4) *Gaussian Noise*: A binned method where the bin amplitudes were determined by a Gaussian random variable with known mean and variance, *e.g.*  $\mathcal{N}(\mu, \sigma)$ .
  - 5) *Gaussian Prior*: A binned method where the number of filled bins was set by  $\text{round}(\mathcal{N}(\mu, \sigma))$ , and that many bins were filled randomly at 0 dB (unfilled bins were set to -20 dB).
  - 6) *Power Distribution*: A binned method where the amplitude of each bin is drawn from a distribution matching the histogram of amplitudes of the American Tinnitus Association tinnitus examples from their website.
  - 7) *Uniform Noise No Bins*: The amplitude associated with each frequency is determined by a uniform random variable on the interval  $[-20, 0]$  dB.
  - 8) *Uniform Noise*: The amplitude associated with each tonotopic bin is determined by a uniform random variable on the interval  $[-20, 0]$  dB.
  - 9) *Uniform Prior*: The number of filled bins is determined by drawing an integer from the discrete interval  $[x_1, x_2] \in \mathbb{Z}^+$ . Then, that many bins are set to 0 dB, and all other bins are set to -20 dB.  $x_1$  and  $x_2$  are hyperparameters.
- 9 methods and 8 hyperparameters were varied in the hyper-

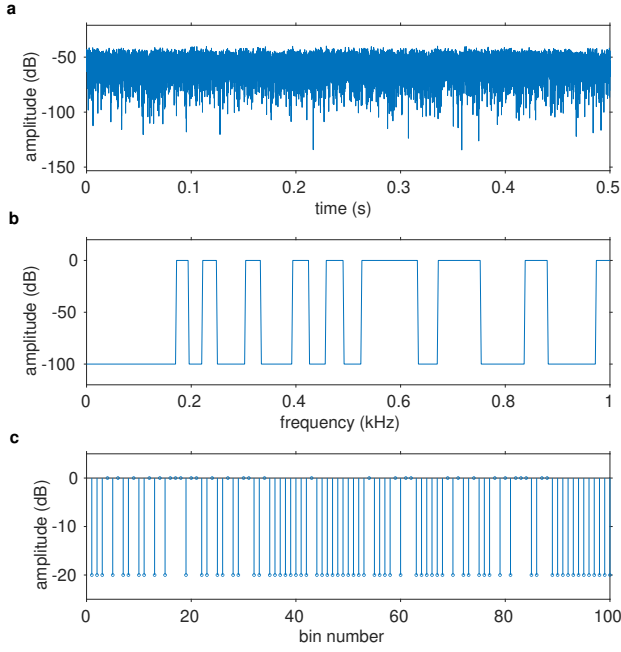


Fig. 2. Example stimulus. (a) shows the waveform of the stimulus, (b) the frequency spectrum from which the waveform was generated, and (c) the 100-dimensional bin representation.

parameter sweep grid search. Methods were evaluated *in-silico* using the model:

$$y = \text{sgn}(\Psi * \bar{x}) \quad (2)$$

where  $y \in \mathbb{R}^n$  is the binary response vector,  $\Psi \in \mathbb{R}^{n \times d}$  is the stimulus matrix, and  $\bar{x} \in \mathbb{R}^d$  is the true target signal (the spectrum of the ATA tinnitus example).

Each stimulus generation method, with different hyperparameters, was evaluated for target signals: buzzing, electric, roaring, screeching, static, and tea kettle.

#### UNITS FOR MAGNETIC PROPERTIES

Symbol	Quantity
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