

Ans 3. Let the array of drops be D
with elements $d_1, d_2, d_3, \dots, d_n$

Also, let S_{ij} represent the
subarray d_i, d_{i+1}, \dots, d_j .

Thus $D = S_{1n}$ (n is the length of D)
& $d_i = S_{ii}$

a) Subproblem Description

- Let $F(S_{ij})$ represent the set of possible ways to combine the drops according to the problem rules.
- Let $F_0(S_{ij})$ be the optimal (required) solution from the set $F(S_{ij})$

a) Subproblem Description

$F_0(S_{ij})$ can be reduced to finding $F_0(S_{ip})$ and $F_0(S_{(p+1)j})$ for some $i \leq p \leq j$
s.t. combining them gives $F_0(S_{ij})$

b) Recurrence Relation:

$$F_0(S_{ij}) = \begin{cases} 0 & ; j-i=0 \\ d_i^2 + d_j^2 & ; j-i=1 \\ \max_{i \leq k \leq j} \left[F_0(S_{ik}) + F_0(S_{(k+1)j}) + \left(\sum_{n=i}^k d_n \right)^2 + \left(\sum_{n=k+1}^j d_n \right)^2 \right] & ; j-i > 1 \end{cases}$$