Networks

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Contents

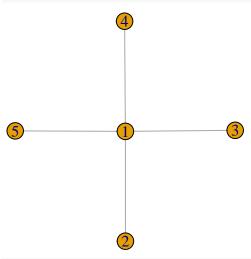
```
Toy networks
                                                          \mathbf{2}
 2
 3
                                                          4
 5
Real networks
                                                          6
 6
 9
library(igraph)
##
## Attaching package: 'igraph'
## The following objects are masked from 'package:stats':
##
##
    decompose, spectrum
## The following object is masked from 'package:base':
##
##
    union
library(tidyverse)
## Loading tidyverse: ggplot2
## Loading tidyverse: tibble
## Loading tidyverse: tidyr
## Loading tidyverse: readr
## Loading tidyverse: purrr
## Loading tidyverse: dplyr
## Conflicts with tidy packages ------
## as_data_frame(): dplyr, tibble, igraph
## compose():
            purrr, igraph
## crossing():
             tidyr, igraph
## filter():
            dplyr, stats
## groups():
             dplyr, igraph
## lag():
             dplyr, stats
## simplify():
            purrr, igraph
library(scales)
##
## Attaching package: 'scales'
## The following object is masked from 'package:purrr':
##
```

```
## discard
## The following objects are masked from 'package:readr':
##
## col_factor, col_numeric
theme_set(theme_bw())
```

Toy networks

Star network

```
# look at edge list and adjacency matrix
star <- graph.star(5, mode="undirected", center=1)
plot(star)</pre>
```



get.edgelist(star)

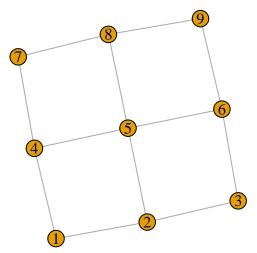
```
## [,1] [,2]
## [1,] 1 2
## [2,] 1 3
## [3,] 1 4
## [4,] 1 5
```

get.adjacency(star)

```
## 5 x 5 sparse Matrix of class "dgCMatrix"
##
## [1,] . 1 1 1 1
## [2,] 1 . . . .
## [3,] 1 . . . .
## [4,] 1 . . . .
## [5,] 1 . . . .
```

Lattice network

```
# look at edge list and adjacency matrix
grid <- graph.lattice(length=3, dim=2)
plot(grid)</pre>
```



get.edgelist(grid)

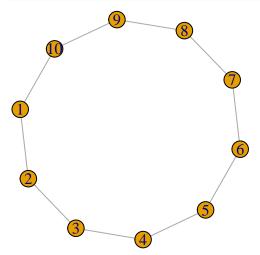
```
##
        [,1] [,2]
##
   [1,]
           1
## [2,]
           1
                4
## [3,]
           2
                3
##
  [4,]
           2
                5
##
  [5,]
           3
                6
## [6,]
           4
                5
## [7,]
           4
                7
## [8,]
           5
                6
## [9,]
           5
                8
## [10,]
           6
                9
## [11,]
           7
                8
## [12,]
```

get.adjacency(grid)

```
## 9 x 9 sparse Matrix of class "dgCMatrix"
##
## [1,] . 1 . 1 . . . . .
## [2,] 1 . 1 . 1 . . . .
## [3,] . 1 . . . 1 . . .
## [4,] 1 . . . 1 . 1 . .
## [5,] . 1 . 1 . 1 . 1 .
## [6,] . . 1 . 1 . . . 1
## [7,] . . . 1 . . . . 1
## [8,] . . . . 1 . 1 . .
```

Ring network

```
# look at edge list and adjacency matrix
grid <- graph.ring(10)
plot(grid)</pre>
```



get.edgelist(grid)

```
##
         [,1] [,2]
##
    [1,]
            1
##
   [2,]
            2
                 3
   [3,]
            3
                 4
##
##
   [4,]
            4
                 5
##
   [5,]
            5
                 6
   [6,]
            6
                 7
##
            7
##
   [7,]
                 8
##
   [8,]
            8
                 9
## [9,]
            9
                10
## [10,]
            1
                10
```

get.adjacency(grid)

```
## 10 x 10 sparse Matrix of class "dgCMatrix"
##
## [1,] . 1 . . . . . . . . . .
## [2,] 1 . 1 . . . . . . . .
## [3,] . 1 . 1 . . . . . . .
## [4,] . . 1 . 1 . . . . .
## [5,] . . . 1 . 1 . . . .
## [6,] . . . . 1 . 1 . . .
## [7,] . . . . . 1 . 1 . .
## [8,] . . . . . . 1 . 1 .
## [9,] . . . . . . . 1 . 1
```

Path length

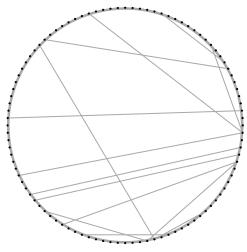
```
# look at all-pairs shortest path distances
shortest.paths(grid)
```

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
##
    [1,]
                 1
                            3
                                 4
                                      5
                                                      2
##
   [2,]
            1
                 0
                       1
                            2
                                 3
                                      4
                                            5
                                                 4
                                                      3
                                                            2
##
   [3,]
            2
                 1
                                 2
                                            4
                                                            3
                            1
            3
                 2
                                      2
                                           3
                                                            4
##
   [4,]
                                                 4
                                                      5
                       1
                            0
                                 1
                      2
                                                            5
##
   [5,]
            4
                 3
                            1
                                 0
                                      1
                                           2
            5
                 4
                      3
                            2
                                      0
                                                 2
                                                      3
                                                            4
##
   [6,]
                                 1
                                           1
##
   [7,]
            4
                 5
                      4
                            3
                                 2
                                      1
                                           0
                                                 1
                                                      2
                                                            3
   [8,]
            3
                 4
                      5
                            4
                                 3
                                      2
                                           1
                                                 0
                                                            2
##
                                                      1
## [9,]
            2
                 3
                      4
                            5
                                 4
                                      3
                                           2
                                                 1
                                                      0
                                                            1
            1
                 2
                      3
                            4
                                 5
                                      4
                                           3
                                                 2
                                                            0
## [10,]
                                                      1
```

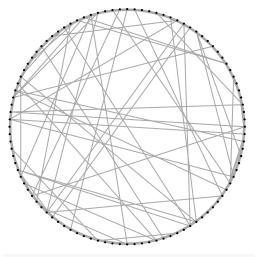
Watts-Strogatz

Plot a few watts-strogatz small world networks $\,$

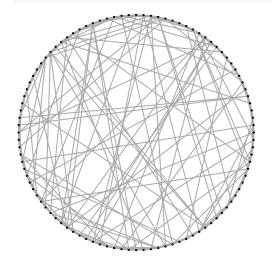
```
# mostly a ring
plot(watts.strogatz.game(1, 100, 5, 0.01), layout=layout.circle, vertex.size=1, vertex.label=NA)
```



```
# some rewiring
plot(watts.strogatz.game(1, 100, 5, 0.05), layout=layout.circle, vertex.size=1, vertex.label=NA)
```



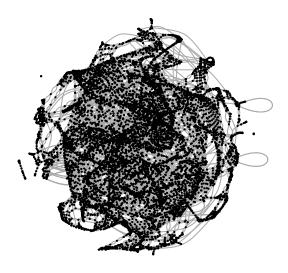
```
# lots of rewiring
plot(watts.strogatz.game(1, 100, 5, 0.10), layout=layout.circle, vertex.size=1, vertex.label=NA)
```



Real networks

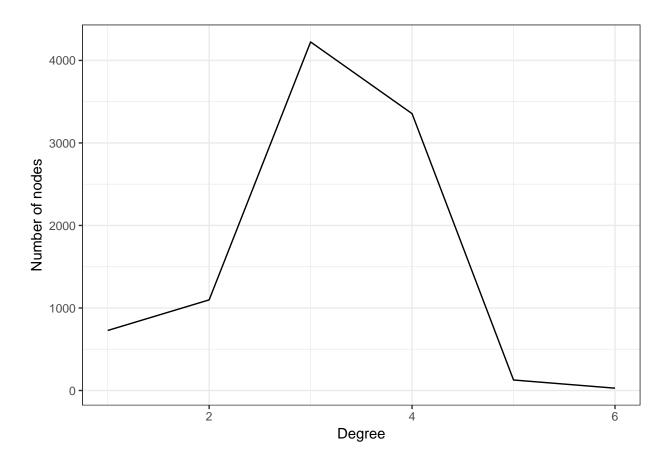
Washington DC road network

```
# read in edge list
dc_edges <- read.table('dc_road_network.tsv', sep="\t", header=F, col.names=c('src','dst'))
# convert to igraph object
dc_graph <- graph.data.frame(dc_edges, directed=F)
# plot hairball
plot(dc_graph, vertex.size=1, vertex.label=NA)</pre>
```



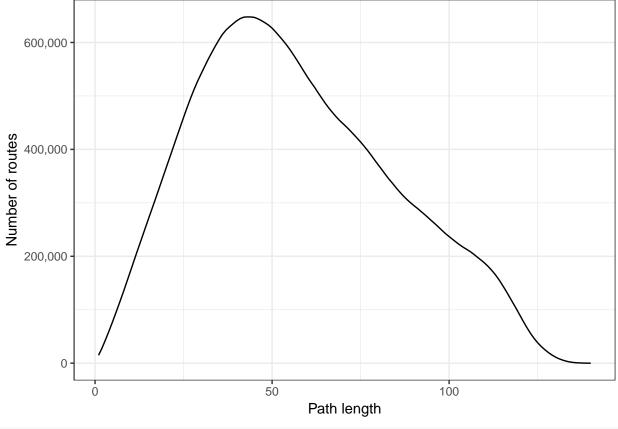
Degree distribution

```
# compute degree distribution
dc_degree_dist <- dc_edges %>%
  group_by(src) %>%
  summarize(degree=n()) %>%
  group_by(degree) %>%
  summarize(num_nodes=n())
ggplot(dc_degree_dist, aes(x = degree, y = num_nodes)) +
  geom_line() +
  xlab('Degree') +
  ylab('Number of nodes')
```



Path length

```
# plot distribution of path lengths
count <- path.length.hist(dc_graph)$res
plot_data <- data.frame(path_length = 1:length(count), count)
ggplot(plot_data, aes(x = path_length, y = count)) +
    geom_line() +
    xlab('Path length') +
    ylab('Number of routes') +
    scale_y_continuous(label = comma)</pre>
```



```
# compute mean path length
sum(1:length(count)*count)/sum(count)
```

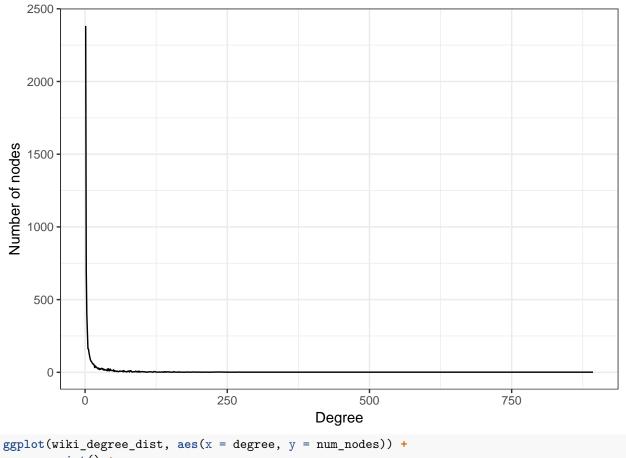
[1] 57.03254

Wikipedia voting network

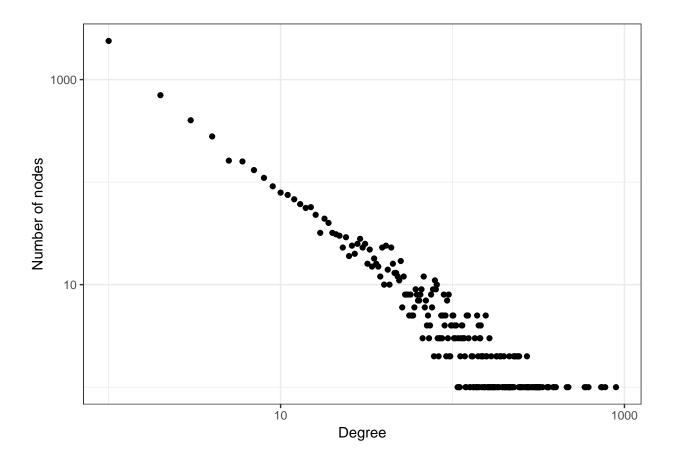
```
# read in edge list
wiki_edges <- read.table('wiki-Vote.txt', sep="\t", header=F, col.names=c('src','dst'))
wiki_graph <- graph.data.frame(wiki_edges, directed=T)</pre>
```

Degree distribution

```
wiki_degree_dist <- wiki_edges %>%
  group_by(src) %>%
  summarize(degree=n()) %>%
  group_by(degree) %>%
  summarize(num_nodes=n())
ggplot(wiki_degree_dist, aes(x = degree, y = num_nodes)) +
  geom_line() +
  xlab('Degree') +
  ylab('Number of nodes')
```

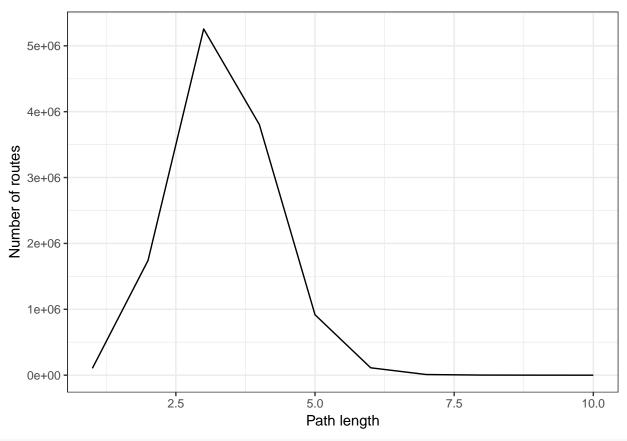


```
ggplot(wiki_degree_dist, aes(x = degree, y = num_nodes)) +
  geom_point() +
  xlab('Degree') +
  ylab('Number of nodes') +
  scale_y_log10() +
  scale_x_log10()
```



Path length

```
# plot distribution of path lengths
count <- path.length.hist(wiki_graph)$res
plot_data <- data.frame(path_length = 1:length(count), count)
ggplot(plot_data, aes(x = path_length, y = count)) +
   geom_line() +
   xlab('Path length') +
   ylab('Number of routes')</pre>
```



compute mean path length
sum(1:length(count)*count)/sum(count)

[1] 3.341011