

# TMSCA MIDDLE SCHOOL MATHEMATICS TEST #2 © NOVEMBER 1, 2014

### **GENERAL DIRECTIONS**

- 1. About this test:
  - A. You will be given 40 minutes to take this test.
  - B. There are 50 problems on this test.
- 2. All answers must be written on the answer sheet/Scantron form/Chatsworth card provided. If you are using an answer sheet be sure to use **BLOCK CAPITAL LETTERS**. Clean erasures are necessary for accurate grading.
- 3. If using a scantron answer form be sure to correctly denote the number of problems not attempted.
- 4. You may write anywhere on the test itself. You must write only answers on the answer sheet.
- 5. You may use additional scratch paper provided by the contest director.
- 6. All problems have **ONE** and **ONLY ONE** correct [BEST] answer. There is a penalty for all incorrect answers.
- 7. Calculators **MAY NOT** be used on this test.
- 8. All problems answered correctly are worth **FIVE** points. **TWO** points will be deducted for all problems answered incorrectly. No points will be added or subtracted for problems not answered.
- 9. In case of ties, percent accuracy will be used as a tie breaker.

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### 2014-2015 TMSCA Middle School Mathematics Test #2

$$4. \ 1,760 \div 4 \div 11 =$$

5. Simplify: 
$$4 - (3 + 2)^2 + 1^5 =$$

6. Let n equal the sum of all the prime factors of 120. Find the value of  $n^2$ .

B. -20

7. 
$$$24.55 =$$
 \_\_\_\_\_ nickels + 32 dimes

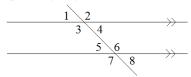
8. Which of the following is not a rational number?

A. 
$$\sqrt{5}$$

C. 123.
$$\overline{7}$$

E. 
$$\sqrt{169}$$

9. Using the picture below, name a pair of corresponding angles.



10. The point (23, -17) lies in which Quadrant?

11. Jeffry has at most \$360 in his bank account. Which inequality statement models Jeffry's bank account?

A. 
$$J < 360$$

B. 
$$J > 360$$

C. 
$$J \le 360$$

$$\mathrm{D}.\,J \geq 360$$

E. 
$$J = 360$$

12. Let *m* equal the GCF of 14 and 21. Let *n* equal the LCM of 21 and 24. Find the prime factorization of the sum of *m* and *n*.

A. 
$$3 \cdot 7^2 \cdot 13$$

B. 
$$5^2 \cdot 7$$

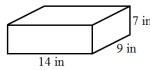
C. 
$$3 \cdot 5 \cdot 13$$

D. 
$$5 \cdot 7^2 \cdot 11$$

E. 
$$2^3 \cdot 3 \cdot 7$$

- 15. What is the unit rate of 56 apples costing \$12.88?
- A. \$0.31 per apple
- B. \$0.17 per apple
- C. \$0.18 per apple
- D. \$0.27 per apple
- E. \$0.23 per apple

16. What is the volume of the rectangular prism below?



- A. 574 in<sup>3</sup>
- B. 882 in<sup>3</sup>
- C. 1,764 in<sup>3</sup>
- D. 644 in<sup>3</sup>
- E.  $776 \text{ in}^2$

- $17.\ 199 + 231 =$  (Roman numeral)
- A. CDXXX
- B. DCXXX
- C. CCCCXXX
- D. CMVVV
- E. CMXXX

- 18. Change the number 73,000,000,000,000 into scientific notation.
- A.  $73 \times 10^{12}$
- B.  $7.3 \times 10^{12}$
- C.  $0.73 \times 10^{13}$
- D.  $7.3 \times 10^{13}$
- E.  $7.3 \times 10^{-12}$

19. Solve:

A.  $x < \frac{14}{3}$ 

- 4 + 3x 9 < 20 1
  - B.  $x > \frac{32}{3}$
- C. x < 8
- D. x > 6
- E. *x* < -6

- 20. 1.5 pints = \_\_\_\_ cups
- A. 6

B. 3

C. 4

D. 5

E. 7

21. Using the stem-and-leaf plot below, find the range of the values.

 $\frac{1}{9}$  key: 4|9=49

- 3 1 1 1 1 1
- 449999999

A. 49

B. 31

C. 29

D. 39

E. 25

- $22. 1 + 2 + 3 + 4 + \dots + 12 + 13 + 14 = \underline{\hspace{1cm}}$
- A. 104
- B. 105
- C. 106
- D. 107
- E. 102

- 23. 1,920 acres = \_\_\_\_\_ square miles
- A. 3

B. 2.5

C. 2

- D. 1.5
- E. 4.5

- 24. What is the 6<sup>th</sup> triangular number?
- A. 21

B. 28

C. 15

D. 18

E. 36

- 25. The supplement of a 13.79° is equal to \_\_\_\_\_\_°.
- A. 193.79
- B. 76.21
- C. 71.21
- D. 166.21
- E. 167.21
- 26. Each letter of the words *MANIAC MATHEMATICIAN* is separately written on a tile and placed in a box. What is the probability of reaching in the box and drawing an *M*?
- A.  $\frac{3}{12}$

B.  $\frac{1}{4}$ 

C.  $\frac{5}{19}$ 

D.  $\frac{1}{5}$ 

- E.  $\frac{3}{19}$
- 27. If  $\pi = 3$ , the circumference of a circle with a diameter of 17 inches is equal to \_\_\_\_\_ inches.
- A. 51

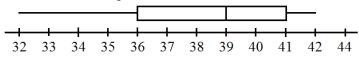
B. 20

- C. 25.5
- D. 867
- E. 216.75

28.  $\overline{AB}$  has endpoints A(16, 4) and B(-8, -22). What are the coordinates of point C is the midpoint of  $\overline{AB}$ ?

- A. (4, -9)
- B. (12, -13)
- C. (8, -18)
- D. (8, -13)
- E. (-4, -13)

29. Identify the first-quartile in the box-and-whisker plot below.



A. 32

B. 36

C. 39

D. 41

E. 42

30. If g(x) = 4x - 3, find the value of g(-7).

A. -6

- B. -14
- C. -25
- D. -28
- E. -31

31. What is the sum of the eight terms in the sequence -6, -2, 2, ..., 22?

A. 48

B. 72

C. 56

D. 64

E. 84

32. What is the maximum number of erasers that cost \$0.37 each that Taha can buy with a \$20 bill?

A. 56

B. 55

C. 54

D. 53

E. 52

33. Multiply: (3m-2)(2m+7)

- A.  $6m^2 14$
- B.  $6m^2 17m 5$
- C.  $6m^2 6m 14$
- D.  $6m^2 + 6m + 14$
- E.  $6m^2 + 17m 14$

34. Which equation below is an example of a direct variation equation?

- A. y = 3x 1
- B. 3x + 2y = 9
- C. y = 12x
- D. 11x = 6y 4
- E. y 1 = 7(x + 1)

35. During baseball season, Sue swung at 120 pitches and made contact with 36. What percent of the swings did Sue make contact with?

- A. 30%
- B. 35%
- C. 25%
- D. 40%
- E. 36%

36. Simplify: -7<sup>0</sup>

A. -7

B. 0

C. -1

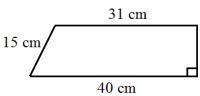
D. 1

E. 7

37. How much simple interest will there be depositing \$400 at 5% for 3 years?

- A. \$60.00
- B. \$600.00
- C. \$6.00
- D. \$66.00
- E. \$660.00

38. The area of the trapezoid below is equal to \_\_\_\_\_ cm<sup>2</sup>.



- A. 852
- B. 620
- C. 426
- D. 532.5
- E. 1,065

39. What is the sum of the coordinates of the midpoint that lies between the points (10, -12) and (16, 8)?

A. 30

B. 11

C. 46

D. 17

E. 9

- 40. Which of the following is an example of an exponential function?
- A.  $f(x) = 12x^{10}$
- B.  $f(x) = 3x^2 + 4x$  C. f(x) = 4x 8
- D.  $f(x) = 4(x)^7$
- E.  $f(x) = 3^x$

- 41. What is the y-intercept of the linear equation 3x 7y = 42?
- A. 14

- D. 49

- E. -39
- 42.  $\{2, 4, 6, 8, 10, 12, 14\} \cap \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15\}$  has \_\_\_\_ elements.
- A. 7

B. 23

C. 29

- E. 15
- 43. Alisha has a \$50 bill. She buys items that cost \$17.26, \$15.33, \$9.97 and \$2.78. If there is no tax, how much change will Alisha receive from her \$50 bill?
- A. \$5.32
- B. \$7.19
- C. \$2.81
- D. \$2.78
- E. \$4.66
- 44. Daisy scored a 92, 84 and 86 on her first three tests. What must she score on the next test to have an average of 90?
- A. 95

B. 96

C. 97

D. 98

E. 99

- 45. What is the range of the relation  $\{(3, 4), (7, -9), (10, -2), (-12, 7)\}$ ?
- A. {16}
- B. {-12, 3, 7, 10}
- C. {22, 16}
- D. {-9, -2, 4, 7}
- E. {7, -2, 8, -5}
- 46. Which of the following is the equation of a circle with its center located at (-5, 9) with a diameter of 8 units?
- A.  $(x+5)^2 + (y-9)^2 = 64$  B.  $(x+5)^2 + (y-9)^2 = 16$  C.  $(x-5)^2 + (y+9)^2 = 8$  D.  $x^2 + y^2 = 8$  E.  $x^2 + y^2 = 64$

- A. 44

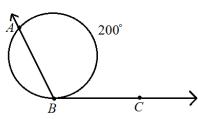
B. 41

C. 39

D. 37

E. 32

48. In the picture below, major arc AB =  $200^{\circ}$ . What is the measure of  $\angle ABC$ ?



- A. 100°
- B. 400°
- $C.200^{\circ}$
- D. 160°
- E. 80°

- 49. Simplify:  $\sqrt{24}$
- A.  $3\sqrt{8}$
- B.  $6\sqrt{2}$
- C.  $8\sqrt{3}$
- D.  $2\sqrt{6}$
- E.  $6\sqrt{4}$

50. Find the value of x in the picture below.



- A.  $8\sqrt{2}$
- B. 4

- C.  $4\sqrt{2}$
- D.  $8\sqrt{3}$
- E.  $4\sqrt{3}$

# 2014-2015 TMSCA Middle School Mathematics Test #2 Answer Key

1. D	18. D	35. A
2. A	19. C	36. C
3. E	20. B	37. A
4. C	21. D	38. C
5. B	22. B	39. B
6. D	23. A	40. E
7. B	24. A	41. B
8. A	25. D	42. A
9. E	26. E	43. E
10. D	27. A	44. D
11. C	28. A	45. D
12. B	29. B	46. B
13. A	30. E	47. D
14. E	31. D	48. A
15. E	32. C	49. D
16. B	33. E	50. C
17. A	34. C	

## 2014-2015 TMSCA Middle School Mathematics Test #2 Selected Answers

- 8. A rational number is one which, as a decimal, is either a terminating decimal or a repeating decimal. From what we are given, 4.6 is a terminating decimal, 123.  $\overline{7}$  is a repeating decimal,  $\frac{1}{4} = 0..25$  and is terminating,  $\sqrt{169} = 13$  and a terminating decimal.  $\sqrt{5} = 2.23607...$ , which is a non-terminating, non-repeating decimal. Therefore,  $\sqrt{5}$  is not a rational number.
- 23. Since 1 square mile = 640 acres,  $\frac{1920}{640}$  = 3 and 1,920 acres = 3 square miles.
- 24. The  $n^{\text{th}}$  triangular number can be found using the formula  $\frac{n(n+1)}{2}$ . So, we get  $\frac{6(7)}{2} = 21$ .
- 30. If g(x) = 4x 3, then g(-7) = 4(-7) 3 = -28 3 = -31. So, g(-7) = -31.
- 37. Simple interest can be found using the formula, I = prt, where p is the principle amount, r is the rate and t is time, in years. We are given \$400 at 5% for 3 years, so I = (400)(0.05)(3) = \$60.00.
- 41. To find the y-intercept of a function, substitute 0 in for x and solve for y. We are given, 3x 7y = 42, so substituting 0 in for x we get 3(0) 7y = 42. The simplifies to -7y = 42 and we solve this one-step equation to get y = -6, which is the y-intercept.
- 45. The range of a function is the set of y-values from the ordered pairs. We are given the relation  $\{(3, 4), (7, -9), (10, -2), (-12, 7)\}$ , so therefore the range of the relation is  $\{-9, -2, 4, 7\}$ , when listed least to greatest.