

**VISVESVARAYA TECHNOLOGICAL  
UNIVERSITY**

“JnanaSangama”, Belgaum -590014, Karnataka.



**LAB REPORT  
on**

**Artificial Intelligence (23CS5PCAIN)**

*Submitted by*

**Aaryan Prakash (1BM23CS006)**

*in partial fulfillment for the award of the degree of*  
**BACHELOR OF ENGINEERING**  
*in*  
**COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING**

(Autonomous Institution under VTU)

**BENGALURU-560019**

**Sep-2024 to Jan-2025**

**B.M.S. College of Engineering,**  
**Bull Temple Road, Bangalore 560019**  
(Affiliated To Visvesvaraya Technological University, Belgaum)  
**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Aaryan Prakash (1BM23CS006)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

<b>Prof. Swathi Sridharan</b> Assistant Professor Department of CSE, BMSCE	<b>Dr. Kavitha Sooda</b> Professor & HOD Department of CSE, BMSCE
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**Github Link:**

<https://github.com/TheAaryanPrakash/AI-Lab/tree/main>



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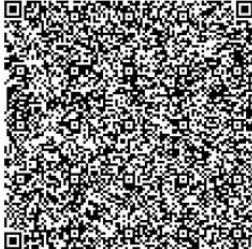
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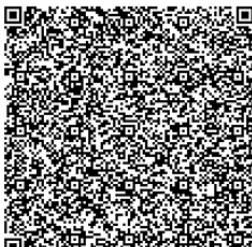
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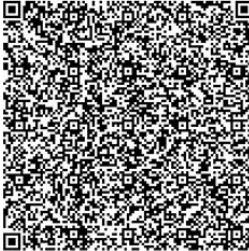
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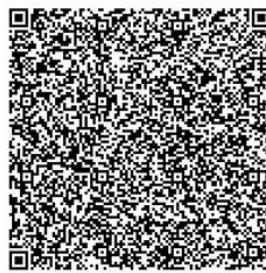
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## Program 1

Implement Tic – Tac – Toe Game  
Implement vacuum cleaner agent

### Algorithm:

20/05/25 Lab 1: Tic Tac Toe

Breadcrumbs

Constraints:

Human ← 'X'  
AI ← 'O'  
Empty ← ''

function create-board():  
 Return 3x3 list filled with empty

function print-board(board):  
 for each row in board:  
 print elements of row separated by '|'  
 print '---'

function check-win(board):  
 for i = 0 to 2:  
 if board[0][0] == board[1][1] == board[2][2] == Empty  
 return board[0][0] // Row Win  
 if board[0][0] == board[0][1] == board[0][2] == Empty  
 return board[0][0] // Column Win  
 if board[0][0] == board[1][1] == board[2][2] == Empty  
 return board[0][0] // Diagonal Win  
 if board[0][2] == board[1][1] == board[2][0] == Empty  
 return board[0][2] // Diagonal Win  
 return None

function is-board-full(board):  
 for each row in board:  
 for each cell in row:  
 if cell == empty:  
 return False  
 return True

function get-available-moves (board):

    moves ← empty list

    for i from 0 to 2:

        for j from 0 to 2:

            if board[i][j] == Empty:

                append (i, j) to moves

    return moves

function minimax (board, depth, is-maximizing):

    winner ← check-board (board)

    if winner == A2

        return 1

    if winner == Human:

        return -1

else if is-board-full (board):

    return 0

if is-maximizing:

    best-score ← -inf

    for each (i, j) in get-available-moves (board):

        board[i][j] ← A2

        score ← minimax (board, depth + 1, False)

        board[i][j] ← Empty

        best-score = max (score, best-score)

    return best-score

else:

    best-score ← inf

    for each (i, j) in get-available-moves (board):

        board[i][j] ← Human

        score ← minimax (board, depth + 1, True)

        board[i][j] ← Empty

        best-score = min (score, best-score)

    return best-score

```

function best-move (board):
    best-score ← -inf
    move ← None
    for each (i,j) in get-available-moves (board):
        board[i][j] ← AI
        score ← minimize (board, 0, False)
        board[i][j] ← Empty
        if score > best-score:
            best-score ← score
            move ← (i,j)
    return move

```

```

function play-game():
    board ← create-board()
    print-board (board)

    while True:
        while Done:
            print "Enter Row" → row
            print "Enter Column" → column
            if board[row][column] == empty:
                board[row][column] ← Human
                break; Done
            else "Cell is occupied"
        print-board (board)

```

```

winner ← check-winner (board)
if winner is not None:
    print winner + " Wins"
    break
if is-board-full (board):
    print "Draw"
    break

```

```

move = local_move(board)
if board is not None:
    board[move[0]][move[1]] = 'X'
print_board(board)

```

```

winner = check_winner(board)
if winner is not None:
    print(winner + " wins")
    break
if is_board_full(board):
    print("Draw")
    break

```

Main:

```
call play_game()
```

Output



Enter Row: 0

Enter Col: 0



Enter Row: 1

Enter Col: 1



Enter Row: 2

Enter Col: 2



X Wins!

## Code:

```

def print_board(board):
    print("\n")
    for i in range(3):
        print(" | ".join(board[i*3:(i+1)*3]))
        if i < 2:
            print("-" * 10)
    print("\n")

```

```

def check_winner(board, player):
    win_conditions = [
        [0, 1, 2], [3, 4, 5], [6, 7, 8],

```

```

[0, 3, 6], [1, 4, 7], [2, 5, 8],
[0, 4, 8], [2, 4, 6]
]
for combo in win_conditions:
    count=0
    for pos in combo:
        if board[pos]==player:
            count+=1
    if count==3:
        return True
    return False

board = [" "] * 9
current_player = "X"
print_board(board)

while True:
    while True:
        pos = int(input(f"Player {current_player}, enter your move (1-9): ")) - 1
        if 0 <= pos <= 8 and board[pos] == " ":
            board[pos] = current_player
            break
        else:
            print("Invalid move. Try again.")

    print_board(board)

    if check_winner(board, current_player):
        print(f"Player {current_player} wins!")
        break
    if " " not in board:
        print("It's a draw!")
        break

# Switch players
current_player = "O" if current_player == "X" else "X"

```

```
X |   |
-----| 0 |
-----O |   | X

Player X, enter your move (1-9): 1

X |   |
-----|  |
-----|  |
-----|  |

Player 0, enter your move (1-9): 5

X |   |
-----| 0 |
-----|  |
-----|  |

Player X, enter your move (1-9): 9

X |   |
-----| 0 |
-----|  | X
```

```
Player 0, enter your move (1-9): 7

X |   |
-----| 0 |
-----O |   | X

Player X, enter your move (1-9): 3

X |   | X
-----
| 0 |
-----
O |   | X

Player 0, enter your move (1-9): 2

X | 0 | X
-----
| 0 |
-----
O |   | X

Player X, enter your move (1-9): 6

X | 0 | X
-----
| 0 | X
-----
O |   | X

Player X wins!
```

## Vacuum Cleaner

31.2.25 Lab 3: Vacuum Cleaner

Brundocode

```
rooms = { "A": "Dirty",  
          "B": "Dirty" }
```

vac\_loc = "A"

```
def suck():  
    print("Sucking dirt at room " + vac_loc)  
    rooms[vac_loc] = "clean"
```

```
def move():  
    global vac_loc  
    if (vac_loc == 'A'):  
        print("move to B")  
        vac_loc = 'B'  
    else:  
        print("move to A")  
        vac_loc = 'A'
```

while 'Dirty' in rooms.values():  
 if rooms[vac\_loc] == 'Dirty':  
 suck()  
 else:  
 move()



Output

Sucking dirt at room A

Moving to B

Sucking dirt at room B

```
import random  
rooms=[1,1,1,1]  
botpos=(int(input("Enter Initial Position"))-1)  
cleanedpos=[]  
cost=0
```

```
def movebot(pos):
```

```
    while True:
```

```

n= random.randint(0,3)
if n != pos and n not in cleanedpos:
    pos = n
    break
return pos

while True:
    print(str(rooms))
    print(botpos+1)

    if rooms[botpos]==1:

        rooms[botpos]=0
        cleanedpos.append(botpos)
        cost+=1
        if len(cleanedpos) == 4:
            break
        botpos=movebot(botpos)

    elif rooms[botpos]==0:
        cleanedpos.append(botpos)
        if len(cleanedpos) == 4:
            break
        botpos = movebot(botpos)

print("cost="+str(cost))

```

```

Enter Initial Position2
[1, 1, 1, 1]
2
[1, 0, 1, 1]
3
[1, 0, 0, 1]
1
[0, 0, 0, 1]
4
cost=4

```

## Program 2

Implement 8 puzzle problems using Depth First Search (DFS)  
Implement Iterative deepening search algorithm

[a] 2 = Lab 2: 8 Puzzle

Pseudocode

```
function get Manhattan Distance (state)
    distance = 0
    for each tile in state:
        if tile is not 0:
            target-position = get Target Position (tile)
            current-position = get Current Position (state, tile)
            distance += abs(target-position-row - current-position-row) +
            abs(target-position-col - current-position-col)
    return distance
```

```
function getMisplacedTiles (state):
    misplaced = 0
    for each blk in state:
        if blk is not in its target-
            position:
                misplaced += 1
    return misplaced
```

```
function A Star Search (startState, goalState, heuristicType):
    openList = priorityQueue()
    closedList = set()
    startNode = createNode (startState, null, 0)
    openList.push (startNode)
    while openList is not empty:
        current-node = openList.pop ()
        if current-node.state == goalState:
            return reconstructPath (current Node)
        closedList.add (current-node.state)
```

for each move in validMoves (currentNode, state):  
childState = applyMove (currentNode, state)  
childState = applyMove (currentNode, state, move)  
if childState in closedList:  
    continue

g = currentNode.g + 1  
if heuristicType == "misplacedTiles":  
    h = getMisplacedTiles (childState)  
else if heuristicType == "manhattan":  
    h = getManhattanDistance (childState)  
f = g + h  
childNode = createNode (childState, currentNode, g, f)  
openList.push (childNode)

return null

function reconstructPath (node):

path = []  
while node is not null:  
    path.append (node.state)  
    node = node.parent  
return reverse (path)

Data part

(1, 2, 3)

(4, 5, 6)

(0, 7, 8)

(1, 2, 3)

(4, 5, 6)

(7, 0, 8)

(1, 2, 3)  
 (4, 5, 6)  
 (7, 8, 9)

Decision tree

1	2	3	$g=0, h=2, f=2$
4	5	6	
-	7	8	

1	2	3	1	2	3	$g=1, h=1, f=4$
-	5	6	4	5	6	
4	7	8	7	-	8	

$$g=1, h=3, f=4$$

1	2	3	1	2	3
4	-	6	4	5	6
7	5	8	7	8	-

$$h=3, g=1, f=4$$

$$h=1, g=1, f=2$$

import time

```
def find_possible_moves(state):
    index = state.index('_')
    moves = {
        0: [1, 3],
        1: [0, 2, 4],
        2: [1, 5],
        3: [0, 4, 6],
        4: [1, 3, 5, 7],
        5: [2, 4, 8],
        6: [3, 7],
        7: [6, 8, 4],
        8: [5, 7],
    }
    return moves.get(index, [])
```

```
def dfs(initial_state, goal_state, max_depth=50):
    stack = [(initial_state, [], 0)]
    visited = {tuple(initial_state)}
    states_explored = 0
```

```

printed_depths = set()

while stack:
    current_state, path, depth = stack.pop()

    if depth > max_depth:
        continue

    if depth not in printed_depths:
        print(f"\n--- Depth {depth} ---")
        printed_depths.add(depth)

    states_explored += 1
    print(f"State # {states_explored}: {current_state}")

    if current_state == goal_state:
        print(f"\n Goal reached at depth {depth} after exploring {states_explored} states.\n")
        return path, states_explored

    possible_moves_indices = find_possible_moves(current_state)

    for move_index in reversed(possible_moves_indices): # Reverse for DFS order
        next_state = list(current_state)
        blank_index = next_state.index('_')
        next_state[blank_index], next_state[move_index] = next_state[move_index],
        next_state[blank_index]

        if tuple(next_state) not in visited:
            visited.add(tuple(next_state))
            stack.append((next_state, path + [next_state], depth + 1))

    print(f"\n Goal state not reachable within depth {max_depth}. Explored {states_explored} states.\n")
    return None, states_explored

# ----- TEST -----
initial_state = [1, 2, 3,
                 4, 8, '_',
                 7, 6, 5]

goal_state = [1, 2, 3,
              4, 5, 6,
              7, 8, '_']

# Measure execution time
start_time = time.time()

```

```

solution_path, explored = dfs(initial_state, goal_state, max_depth=50)
end_time = time.time()

if solution_path is None:
    print("No solution found.")
else:
    print("Solution path:")
    for step, state in enumerate(solution_path, start=1):
        print(f"Step {step}: {state}")

print("\nExecution time: {:.6f} seconds".format(end_time - start_time))
print("Total states explored:", explored)

--- Depth 0 ---
State #1: [1, 2, 3, 4, 8, '_', 7, 6, 5]

--- Depth 1 ---
State #2: [1, 2, '_', 4, 8, 3, 7, 6, 5]

--- Depth 2 ---
State #3: [1, '_', 2, 4, 8, 3, 7, 6, 5]

--- Depth 3 ---
State #4: ['_', 1, 2, 4, 8, 3, 7, 6, 5]

--- Depth 4 ---
State #5: [4, 1, 2, '_', 8, 3, 7, 6, 5]

--- Depth 5 ---
State #6: [4, 1, 2, 8, '_', 3, 7, 6, 5]

--- Depth 6 ---
State #7: [4, '_', 2, 8, 1, 3, 7, 6, 5]

--- Depth 7 ---
State #8: ['_', 4, 2, 8, 1, 3, 7, 6, 5]

--- Depth 8 ---
State #9: [8, 4, 2, '_', 1, 3, 7, 6, 5]

```

```
--- Depth 9 ---
State #10: [8, 4, 2, 1, '_', 3, 7, 6, 5]

--- Depth 10 ---
State #11: [8, '_', 2, 1, 4, 3, 7, 6, 5]

--- Depth 11 ---
State #12: ['_', 8, 2, 1, 4, 3, 7, 6, 5]

--- Depth 12 ---
State #13: [1, 8, 2, '_', 4, 3, 7, 6, 5]

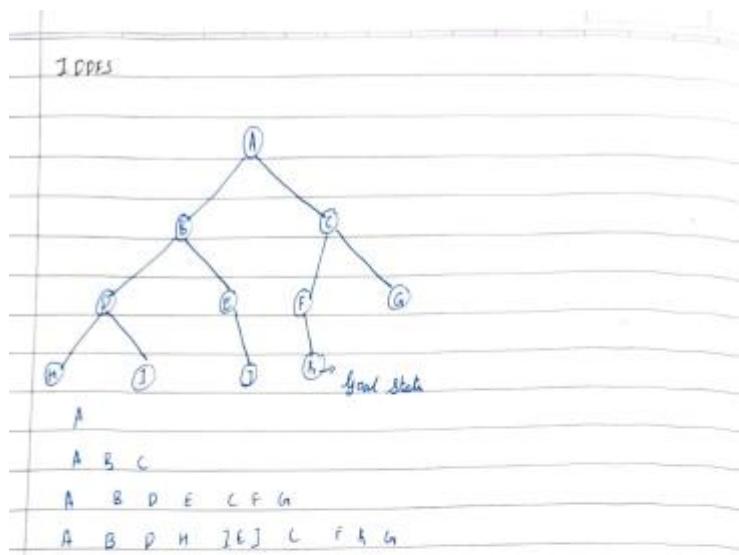
--- Depth 13 ---
State #14: [1, 8, 2, 7, 4, 3, '_', 6, 5]

--- Depth 14 ---
State #15: [1, 8, 2, 7, 4, 3, 6, '_', 5]

--- Depth 15 ---
State #16: [1, 8, 2, 7, 4, 3, 6, 5, '_']

--- Depth 16 ---
State #17: [1, 8, 2, 7, 4, '_', 6, 5, 3]
```

## IDDFS



def IDDFS (root, goal, graph, max\_depth):

def dls (node, depth, path):

if node == goal:

return path

if depth == 0

return None

for child in graph.get(node, []):

result = dls (child, depth - 1, path + [child])

if result:

return result

for l in range (max\_depth + 1):

result = dls (root, l, [root])

if result:

return result

return None



import time

# ----- MOVE GENERATOR -----

def find\_possible\_moves(state):

index = state.index('\_')

if index == 0:

return [1, 3]

elif index == 1:

return [0, 2, 4]

elif index == 2:

```

        return [1, 5]
    elif index == 3:
        return [0, 4, 6]
    elif index == 4:
        return [1, 3, 5, 7]
    elif index == 5:
        return [2, 4, 8]
    elif index == 6:
        return [3, 7]
    elif index == 7:
        return [4, 6, 8]
    elif index == 8:
        return [5, 7]
    return []

# ----- DEPTH LIMITED SEARCH -----
def depth_limited_dfs(state, goal_state, limit, path, visited):
    if state == goal_state:
        return path

    if limit <= 0:
        return None

    visited.add(tuple(state))

    for move_index in find_possible_moves(state):
        next_state = list(state)
        blank_index = next_state.index('_')
        next_state[blank_index], next_state[move_index] = next_state[move_index], next_state[blank_index]

        if tuple(next_state) not in visited:
            result = depth_limited_dfs(next_state, goal_state, limit - 1, path + [next_state], visited)
            if result is not None:
                return result
    return None

# ----- ITERATIVE DEEPENING DFS -----
def iddfs(initial_state, goal_state, max_depth=30):
    for depth in range(max_depth):
        print(f"Searching at depth limit = {depth}")
        visited = set()
        result = depth_limited_dfs(initial_state, goal_state, depth, [initial_state], visited)
        if result is not None:
            return result, depth
    return None, max_depth

```

```

# ----- TEST -----
initial_state = [1, 2, 3,
                 4, 8, '_',
                 7, 6, 5]

goal_state  =[1, 2, 3,
              4, 5, 6,
              7, 8, '_']

# Measure execution time
start_time = time.time()
solution_path, depth_reached = iddfs(initial_state, goal_state, max_depth=30)
end_time = time.time()

if solution_path is None:
    print("Goal state is not reachable within given depth limit.")
else:
    print("\n\nSolution path found:")
    for step, state in enumerate(solution_path, start=0):
        print(f"Step {step}: {state}")

print("\nExecution time: {:.6f} seconds".format(end_time - start_time))
print("Depth reached:", depth_reached)

Searching at depth limit = 0
Searching at depth limit = 1
Searching at depth limit = 2
Searching at depth limit = 3
Searching at depth limit = 4
Searching at depth limit = 5

Solution path found:
Step 0: [1, 2, 3, 4, 8, '_', 7, 6, 5]
Step 1: [1, 2, 3, 4, 8, 5, 7, 6, '_']
Step 2: [1, 2, 3, 4, 8, 5, 7, '_', 6]
Step 3: [1, 2, 3, 4, '_', 5, 7, 8, 6]
Step 4: [1, 2, 3, 4, 5, '_', 7, 8, 6]
Step 5: [1, 2, 3, 4, 5, 6, 7, 8, '_']

Execution time: 0.000194 seconds
Depth reached: 5

==== Code Execution Successful ====

```

## Program 3

Implement A\* search algorithm

Lab 3: 8-Puzzle (using A\* Algorithm)

Basic code

```
function A-star (start-state, goal-state):
    create open = priority queue (ordered by f = g + h)
    create closed = empty set

    g(start-state) = 0
    h(start-state) = heuristic (start-state)          // heuristic f = calculated + g
    f (start-state) = g (start-state) + h (start-state)      // Manhattan distance

    insert (f (start-state), g (start-state), start-state, path = {} ) into open

    while OPEN is not empty:
        (f, g, current-state, path) = remove state with lowest f from open

        if current-state = goal-state:
            return path + [current-state]

        add current-state to closed

        for each neighbour in get-neighbours (current-state):
            if neighbour not in closed:
                g(neighbour) = g + 1
                h(neighbour) = heuristic (neighbour)
                f (neighbour) = g (neighbour) + h (neighbour)

                insert (f (neighbour), g (neighbour), neighbour, path +
                        [current-state]) into OPEN

    return no-solution
```



1 2 3  
4 5 6  
7 - 8

↓ 8

1 2 3  
4 5 6  
7 8 -

### Observations

Solving the 8 Puzzle using different methods use different times:

Solving the same input in all 4 methods:

Input: 1 2 3  
4 8 -  
7 6 5

Time:

→ DFS: 1.178773 seconds      Worst

States Explored: 20,787

→ BFS: 0.003539 seconds

States Explored: 59

→ IDDFS: 0.000262 seconds

Depth Reached: 5

→ A-Star: 0.000044 seconds      Best

```
import heapq
import time
```

```
# Heuristic: Manhattan Distance
```

```
def heuristic(state, goal):
```

```
    distance = 0
```

```
    for i in range(1, 9): # tile numbers 1 to 8
```

```
        x1, y1 = divmod(state.index(i), 3)
```

```
        x2, y2 = divmod(goal.index(i), 3)
```

```
        distance += abs(x1 - x2) + abs(y1 - y2)
```

```
    return distance
```

```

# Get neighbors by sliding blank (0) up/down/left/right
def get_neighbors(state):
    neighbors = []
    i = state.index(0) # position of blank
    x, y = divmod(i, 3)
    moves = [(-1,0), (1,0), (0,-1), (0,1)]

    for dx, dy in moves:
        new_x, new_y = x + dx, y + dy
        if 0 <= new_x < 3 and 0 <= new_y < 3:
            j = new_x * 3 + new_y
            new_state = list(state)
            new_state[i], new_state[j] = new_state[j], new_state[i]
            neighbors.append(tuple(new_state))
    return neighbors

# A* Search for 8-puzzle
def astar(start, goal):
    open_set = []
    heapq.heappush(open_set, (heuristic(start, goal), 0, start))

    came_from = {}
    g_score = {start: 0}

    while open_set:
        _, cost, current = heapq.heappop(open_set)

        if current == goal:
            # Reconstruct path
            path = []
            while current in came_from:
                path.append(current)
                current = came_from[current]
            path.append(start)
            return path[::-1]

        for neighbor in get_neighbors(current):
            tentative_g = g_score[current] + 1
            if neighbor not in g_score or tentative_g < g_score[neighbor]:
                came_from[neighbor] = current
                g_score[neighbor] = tentative_g
                f_score = tentative_g + heuristic(neighbor, goal)
                heapq.heappush(open_set, (f_score, tentative_g, neighbor))

    return None # no solution

# ----- TEST -----

```

```

start = (1, 2, 3,
        4, 8, 0,
        7, 6, 5)

goal = (1, 2, 3,
        4, 5, 6,
        7, 8, 0)

# Measure execution time
start_time = time.time()
path = astar(start, goal)
end_time = time.time()

if path:
    print("Steps to solve ({} moves):".format(len(path)-1))
    for state in path:
        for i in range(0, 9, 3):
            print(state[i:i+3])
        print()
else:
    print("No solution found")

print("Execution time: {:.6f} seconds".format(end_time - start_time))

```

```
Steps to solve (5 moves):
```

```
(1, 2, 3)
```

```
(4, 8, 0)
```

```
(7, 6, 5)
```

```
(1, 2, 3)
```

```
(4, 8, 5)
```

```
(7, 6, 0)
```

```
(1, 2, 3)
```

```
(4, 8, 5)
```

```
(7, 0, 6)
```

```
(1, 2, 3)
```

```
(4, 0, 5)
```

```
(7, 8, 6)
```

```
(1, 2, 3)
```

```
(4, 5, 0)
```

```
(7, 8, 6)
```

```
(1, 2, 3)
```

```
(4, 5, 6)
```

```
(7, 8, 0)
```

```
Execution time: 0.000111 seconds
```

## Program 4

Implement Hill Climbing search algorithm to solve N-Queens problem

21/01/2025 Week 4: Hill Climbing Algorithm

function Hill-Climbing (problem) returns local minimum state

~~REMOVED~~

current = make-Nodes (problem, initial state)

loop do

neighbour = highest valued neighbour of current

if neighbour.value < current.value then return current.state  
current = neighbour

ex: 4 Queens

			Q
		Q	
	Q		
Q			

→ Neighbours of  $x_0 = 3, x_1 = 1, x_2 = 2, x_3 = 0$  ( $\text{cost} = 2$ )

- $x_0 = 2, x_1 = 3, x_2 = 2, x_3 = 0$  ( $\text{cost} = 1$ ) → Choose this
- $x_0 = 0, x_1 = 1, x_2 = 3, x_3 = 0$  ( $\text{cost} = 1$ ) ∴ best cost
- $x_0 = 0, x_1 = 1, x_2 = 2, x_3 = 3$  ( $\text{cost} = 6$ )
- $x_0 = 3, x_1 = 2, x_2 = 1, x_3 = 0$  ( $\text{cost} = 6$ )
- $x_0 = 3, x_1 = 0, x_2 = 2, x_3 = 1$  ( $\text{cost} = 1$ )
- $x_0 = 3, x_1 = 1, x_2 = 0, x_3 = 2$  ( $\text{cost} = 1$ )

→ Neighbours of  $x_0 = 1, x_1 = 3, x_2 = 2, x_3 = 0$  ( $\text{cost} = 1$ )

- $x_0 = 3, x_1 = 1, x_2 = 2, x_3 = 0$  ( $\text{cost} = 1$ )
- $x_0 = 2, x_1 = 3, x_2 = 1, x_3 = 0$  ( $\text{cost} = 2$ )
- $x_0 = 0, x_1 = 3, x_2 = 2, x_3 = 1$  ( $\text{cost} = 4$ )
- $x_0 = 1, x_1 = 2, x_2 = 3, x_3 = 0$  ( $\text{cost} = 2$ )
- $x_0 = 1, x_1 = 0, x_2 = 2, x_3 = 3$  ( $\text{cost} = 2$ )
- $x_0 = 1, x_1 = 3, x_2 = 0, x_3 = 2$  ( $\text{cost} = 0$ ) → Choose this

→ Reached local maximum at step 2, state  $[1, 0, 2, 3], h = 2$

```
import random
import math
```

```
def compute_cost(state):
```

"""Count diagonal conflicts for a permutation-state (one queen per row & column)."""

conflicts = 0

n = len(state)

for i in range(n):

for j in range(i + 1, n):

```

        if abs(state[i] - state[j]) == abs(i - j):
            conflicts += 1
    return conflicts

def random_permutation(n):
    arr = list(range(n))
    random.shuffle(arr)
    return arr

def neighbors_by_swaps(state):
    """All neighbors obtained by swapping two columns (keeps permutation property)."""
    n = len(state)
    for i in range(n - 1):
        for j in range(i + 1, n):
            nb = state.copy()
            nb[i], nb[j] = nb[j], nb[i]
            yield nb

def hill_climb_with_restarts(n, max_restarts=None):
    """Hill climbing on permutations with random restart on plateau (no revisits)."""
    visited = set()
    total_states = math.factorial(n)
    restarts = 0

    while True:
        # pick a random unvisited start permutation
        if len(visited) >= total_states:
            raise RuntimeError("All states visited — giving up (no solution found.)")

        state = random_permutation(n)
        while tuple(state) in visited:
            state = random_permutation(n)
            visited.add(tuple(state))

        # climb from this start
        while True:
            cost = compute_cost(state)
            if cost == 0:
                return state, restarts

            # find best neighbor (swap-based neighbors)
            best_neighbor = None
            best_cost = float("inf")
            for nb in neighbors_by_swaps(state):
                c = compute_cost(nb)
                if c < best_cost:
                    best_cost = c

```

```

best_neighbor = nb

# if strictly better, move; otherwise it's a plateau/local optimum -> restart
if best_cost < cost:
    state = best_neighbor
    visited.add(tuple(state))
else:
    # plateau or local optimum -> restart
    restarts += 1
    if max_restarts is not None and restarts >= max_restarts:
        raise RuntimeError(f"Stopped after {restarts} restarts (no solution found).")
    break # go pick a new unvisited start

def format_board(state):
    n = len(state)
    lines = []
    for r in range(n):
        lines.append(" ".join("Q" if state[c] == r else "-" for c in range(n)))
    return "\n".join(lines)

if __name__ == "__main__":
    n = 4
    solution, restarts = hill_climb_with_restarts(n)
    print("Found solution:", solution)
    print(format_board(solution))

Found solution: [2, 0, 3, 1]
- Q -
- - - Q
Q - - -
- - Q -

```

## Program 5

Simulated Annealing to Solve 8-Queens problem

Simulated Annealing

```

current <- initial state
neighbor <- random
T <- oo
while T > 0
    next <- neighbor (current)
    ΔE <- current.cost - next.cost
    if ΔE > 0 then
        current <- next
    else
        current <- next with probability  $P = e^{-\Delta E/T}$ 
    decrease T
return current

```

5-Queens Trace

Initial  $\Rightarrow (0, 1, 2, 3, 4) \rightarrow h=10$   
 $\cdot (1, 1, 2, 3, 4) \rightarrow h=7$   
 $\cdot (1, 0, 2, 3, 4) \rightarrow h=4$   
 $\cdot (1, 0, 0, 3, 4) \rightarrow h=3$   
 $\cdot (1, 2, 0, 3, 4) \rightarrow h=2$  (Best Solution)

Reached local maxima at step 4  
State:  $[1, 2, 0, 3, 4]$ ,  $h=2$

6-Queens Trace

Initial  $\Rightarrow (0, 1, 2, 3, 4, 5) \rightarrow h=15$   
 $\cdot (1, 1, 2, 3, 4, 5) \rightarrow h=11$   
 $\cdot (1, 0, 2, 3, 4, 5) \rightarrow h=7$   
 $\cdot (1, 0, 0, 3, 4, 5) \rightarrow h=5$   
 $\cdot (1, 0, 0, 2, 4, 5) \rightarrow h=3$   
 $\cdot (5, 0, 0, 3, 4, 2) \rightarrow h=2$  (Best Solution)

Reached local maxima at step 5  
State:  $[5, 0, 0, 3, 4, 2]$ ,  $h=2$

8/10

```
import random
import math
```

```
def cost(state):
```

```

attacks = 0
n = len(state)
for i in range(n):
    for j in range(i + 1, n):
        if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
            attacks += 1
return attacks

def get_neighbor(state):

    neighbor = state[:]
    i, j = random.sample(range(len(state)), 2)
    neighbor[i], neighbor[j] = neighbor[j], neighbor[i]
    return neighbor

def simulated_annealing(n=8, max_iter=10000, temp=100.0, cooling=0.95):

    current = list(range(n))
    random.shuffle(current)
    current_cost = cost(current)

    temperature = temp
    cooling_rate = cooling

    best = current[:]
    best_cost = current_cost

    for _ in range(max_iter):
        if temperature <= 0 or best_cost == 0:
            break

        neighbor = get_neighbor(current)
        neighbor_cost = cost(neighbor)
        delta = current_cost - neighbor_cost

        if delta > 0 or random.random() < math.exp(delta / temperature):
            current, current_cost = neighbor, neighbor_cost
            if neighbor_cost < best_cost:
                best, best_cost = neighbor[:], neighbor_cost

        temperature *= cooling_rate

    return best, best_cost

def print_board(state):

```

```
n = len(state)
for row in range(n):
    line = " ".join("Q" if state[col] == row else "." for col in range(n))
    print(line)
print()
```

```
n = 8
solution, cost_val = simulated_annealing(n, max_iter=20000)
print("Best position found:", solution)
print(f'Number of non-attacking pairs: {n*(n-1)//2 - cost_val}')
print("\nBoard:")
print_board(solution)
```

Best position found: [6, 3, 1, 7, 5, 0, 2, 4]  
Number of non-attacking pairs: 28

Board:

```
. . . . . Q . .
. . Q . . . .
. . . . . . Q .
. Q . . . .
. . . . . . . Q
. . . . Q . . .
Q . . . . . .
. . . Q . . . .
```

==== Code Execution Successful ====

## Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

15/10/2025 Lab 5: Implement Augmented Propositional Logic

B. Create a knowledge base using propositional logic and query entail the knowledge base

→ Algorithm T7-entails-user-input()

Input:

KB-sentences ← list of propositional sentences from user  
query ← query sentence from user

Brace:

Symbol ← all unique propositional symbols appearing in KB-sentences;  
return T7-check-all(KB-sentences, query, symbols, empty model)      query

→ Function T7-check-all(KB, x, symbols, model)

if symbols is empty then  
    if PL-true!(KB, model) then  
        return PL-true!(x, model)

else  
    return true

else  
    p ← first(symbols)  
    rest ← symbols - {p}

model·true = model ∨ (p=true)

model·false = model ∨ (p=false)

return (T7-check-all(KB, x, rest, model·true) AND  
      T7-check-all(KB, x, rest, model·false))

```

→ function PL-True? (sentence-set, model)
    for each sentence S in sentence-set do
        if S evaluate to True under model
            return True
    return False

```

i Consider a knowledge base KB that contains the following propositional logic sentences

$$S_1 \rightarrow P$$

$$P \rightarrow \neg R$$

$$S_2 \vee R$$

i Construct a truth table that shows the truth value of each sentence in KB and indicate the models in which the KB is true

P	S <sub>1</sub>	R	$S_1 \rightarrow P$	$P \rightarrow \neg R$	$S_2 \vee R$	KB True
T	T	T	T	F	T	F
T	T	F	T	T	T	F
T	F	T	T	F	T	F
T	F	F	T	T	F	F
F	T	T	F	T	T	F
F	T	F	F	T	T	F
F	F	T	T	F	T	T
F	F	F	T	T	F	F

ii Does KB entail R

In all models where KB is true, R = T

∴ KB entails R

iii Does KB entail  $R \rightarrow P$

TTT	$R \rightarrow P$
TTF	F
FFT	F

} Both false  $\Rightarrow$  KB does not entail  $R \rightarrow P$

iv Does KB entail  $S_1 \rightarrow R$

TTT	$S_1 \rightarrow R$
TTF	T
FFT	T

} Always true  $\Rightarrow$  KB entails  $S_1 \rightarrow R$

A			B			C			AVL			BV -> L			KB			$\alpha$		
A	B	C	F	F	T	F	F	T	F	F	T	F	F	F	F	F	F	F	F	
F	F	F	T	T	F	F	T	F	F	F	T	F	F	F	F	F	F	F		
F	F	T	F	F	T	F	F	T	F	F	T	①	①	①	①	①	①	①		
F	T	F	T	T	F	T	T	F	F	T	T	②	②	②	②	②	②	②		
F	T	T	F	F	T	T	F	F	F	F	T	F	F	F	F	F	F	F		
T	F	F	T	T	F	F	T	F	F	F	T	③	③	③	③	③	③	③		
T	F	T	F	F	T	T	F	T	F	F	T	④	④	④	④	④	④	④		
T	T	F	T	T	T	F	T	T	F	F	T	⑤	⑤	⑤	⑤	⑤	⑤	⑤		
T	T	T	T	T	T	T	T	T	T	T	T	⑥	⑥	⑥	⑥	⑥	⑥	⑥		

$\therefore KB \text{ entails } \alpha \text{ (T, T, T, T, T, T)}$

```

import itertools

def evaluate_formula(formula, truth_assignment):
    eval_formula = formula
    for symbol, value in truth_assignment.items():
        eval_formula = eval_formula.replace(symbol, str(value))
    return eval(eval_formula)

def generate_truth_table(variables):
    return list(itertools.product([False, True], repeat=len(variables)))

def is_entailed(KB_formula, alpha_formula, variables):
    truth_combinations = generate_truth_table(variables)
    print(f"{''.join(variables)} | KB Result | Alpha Result")
    print("-" * (len(variables) * 2 + 15))
    for combination in truth_combinations:
        truth_assignment = dict(zip(variables, combination))
        KB_value = evaluate_formula(KB_formula, truth_assignment)
        alpha_value = evaluate_formula(alpha_formula, truth_assignment)
        result_str = " ".join(["T" if value else "F" for value in combination])
        print(f"{result_str} | {'T' if KB_value else 'F'} | {'T' if alpha_value else 'F'}")
    if KB_value and not alpha_value:
        return False
    return True

```

```

KB = "(A or C) and (B or not C)"
alpha = "A or B"
variables = ['A', 'B', 'C']

if is_entailed(KB, alpha, variables):
    print("\nThe knowledge base entails alpha.")
else:
    print("\nThe knowledge base does not entail alpha.")

```

A	B	C	KB Result	Alpha Result
F	F	F	F	F
F	F	T	F	F
F	T	F	F	T
F	T	T	T	T
T	F	F	T	T
T	F	T	F	T
T	T	F	T	T
T	T	T	T	T

The knowledge base entails alpha.

## Program 7

Implement unification in first order logic

24/10/25 Unification of FOL

i  $P(f(x), g(y), z)$   
 $P(f(g(z)), g(f(a)), f(a))$   
 Find  $\theta$  (MGu)

ii  $O(x, P(u))$   
 $O(Fy), y)$

iii  $H(x, g(x))$   
 $H(g(y), g(g(z)))$

i  $x = g(z), y = f(a)$  Possible ✓

ii  $x = F(y), y = f(x)$  Not possible ✓

iii  $x = g(y)$  Possible ✓  
 $x = g(z)$   
 $\Rightarrow y = z$

i Compare  $f(x)$  and  $f(g(x))$   
 $\theta_1 = \{x \mapsto g(x)\}$   
 $\rightarrow g(y) \in g(f(a))$   
 $\theta_2 = \{y \mapsto f(a)\}$   
 $\rightarrow u \in f(a)$   
 $\theta_3 = \{u \mapsto f(a)\}$

$\Rightarrow \theta = \{x \mapsto g(x), y \mapsto f(a), u \mapsto f(a)\}$

Apply  $\theta$  to both predicates

$P(f(x), g(y), u) \stackrel{\theta}{=} P(f(g(z)), g(f(a)), f(a))$   $\models$   
 $\therefore$  Both are identical.

2 Comparing  $x$  and  $f(y)$

$$x = \text{fly}$$

$$f(x) \approx y$$

$$f(x) = y$$

$$\text{Now, } x : f(f(y)) = y$$

$\hookrightarrow$  cycles, not straightforward

3 Comparing  $x \approx g(y)$

$$x = g(y)$$

Comparing  $g(x)$  and  $g(g(z))$

$$x = g(z)$$

$$g(x) = g(g(z))$$

$$g(g(y)) \approx g(g(z))$$

can be unified

when  $y = z$

$$x = g(y)$$

$$y = z$$

$$x = g(z)$$

$$y = z$$

Thus, MUV is

$$\emptyset = \{x \approx g(z), y/z\}$$

\* Substitute

$$H(x, g(x)) / \{x \approx g(z), y/z\} = H(g(z), g(g(z)))$$

$$H(g(y), g(g(z))) \approx g(z) = H(g(z)) = g(g(z))$$

Thus, successful unification.

*Afterwards*  
*unification*  $\Rightarrow$  *Tic Tac Toe*  
*AB prior*

## Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

12/11/2025 Forward Reasoning Algorithm

function FOL-KB-Ask(KB, x) returns a substitution or false

inputs: KB, x

local variable: new

repeat until new is empty

new  $\leftarrow \{\}$

for each rule in KB do

$(p_1 \wedge p_2 \dots \wedge p_n \Rightarrow q) \in \text{Standardise-Variabiles}(\text{rule})$

for each  $\theta$  such that  $\text{SUBST}(\theta, p_1 \wedge p_2 \dots \wedge p_n) = \text{SUBST}(\theta, q)$

$q' \in \text{SUBST}(\theta, q)$

if  $q'$  does not unify with sentence in KB

add  $q'$  to new

$\emptyset \in \text{unify}(q', x)$

if  $\emptyset$  is not fail return  $\emptyset$

add new to KB

return KB

Output

Query: Mortal (Arnold)

Initial facts: { 'Human (Arnold)' }

Total facts: { 'Human (Arnold)', 'Mortal (Arnold)' }

import re

```
def match_pattern(pattern, fact):
```

```
    """
```

Checks if a fact matches a rule pattern using regex-style variable substitution.

Variables are lowercase words like p, q, x, r etc.

Returns a dict of substitutions or None if not matched.

```
    """
```

```
# Extract predicate name and arguments
```

```
pattern_pred, pattern_args = re.match(r'(\w+)
```

```
', pattern).groups()
```

```
fact_pred, fact_args = re.match(r'(\w+)
```

```
', fact).groups()
```

```

if pattern_pred != fact_pred:
    return None # predicate mismatch

pattern_args = [a.strip() for a in pattern_args.split(",")]
fact_args = [a.strip() for a in fact_args.split(",")]

if len(pattern_args) != len(fact_args):
    return None

subst = {}
for p_arg, f_arg in zip(pattern_args, fact_args):
    if re.fullmatch(r'[a-z]\w*', p_arg): # variable
        subst[p_arg] = f_arg
    elif p_arg != f_arg: # constants mismatch
        return None
return subst

def apply_substitution(expr, subst):
    """Replaces all variable names in expr using the given substitution dict."""
    for var, val in subst.items():
        expr = re.sub(rf"\b{var}\b", val, expr)
    return expr

# ----- Knowledge Base -----
rules = [
    (["American(p)", "Weapon(q)", "Sells(p,q,r)", "Hostile(r)"], "Criminal(p)"),
    (["Missile(x)"], "Weapon(x)"),
    (["Enemy(x, America)"], "Hostile(x)"),
    (["Missile(x)", "Owns(A, x)"], "Sells(Robert, x, A)")
]
facts = {
    "American(Robert)",
    "Enemy(A, America)",
    "Owns(A, T1)",
    "Missile(T1)"
}
goal = "Criminal(Robert)"

def forward_chain(rules, facts, goal):
    added = True
    while added:

```

```

added = False
for premises, conclusion in rules:
    possible_substs = []
    for p in premises:
        for f in facts:
            subst = match_pattern(p, f)
            if subst:
                possible_substs.append(subst)
                break
            else:
                break
        else:
            break
    else:
        combined = {}
        for s in possible_substs:
            combined.update(s)

    new_fact = apply_substitution(conclusion, combined)

    if new_fact not in facts:
        facts.add(new_fact)
        print(f"Inferred: {new_fact}")
        added = True
    if new_fact == goal:
        return True
return goal in facts

```

```
print("Goal achieved:", forward_chain(rules, facts, goal))
```

```

Inferred: Weapon(T1)
Inferred: Hostile(A)
Inferred: Sells(Robert, T1, A)
Inferred: Criminal(Robert)
Goal achieved: True

```

## Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution

Comment:  $\neg \neg A \equiv A$

// Eliminate implications and disjunctions

for each subformula in F:

if subformula is  $(A \rightarrow B)$ :

replace with  $\neg A \vee B$

if subformula is  $(A \vee B)$ :

replace with  $((\neg A \vee B) \wedge (A \vee \neg B))$

// Move negation inwards

while there exists a negation applied to a compound formula

apply de Morgan's law

$\neg(A \wedge B) \equiv (\neg A \vee \neg B)$

$\neg(A \vee B) \equiv (\neg A \wedge \neg B)$

push  $\neg$  through quantifiers

$\forall x \neg P(x) \equiv \exists x \neg P(x)$

$\exists x \neg P(x) \equiv \forall x \neg P(x)$

remove double negation:

$\neg(\neg A) \equiv A$

// Standardize variables

for each quantified variable  $x$  in F:

if variable name repeats:

rename it to a unique variable

// Skolemize

for each  $\exists x$  in F:

if  $\exists x$  is inside  $\forall y_1 \forall y_2 \dots \forall y_n$ :

Replace  $x$  with a new skolem function  $f(y_1, y_2, \dots, y_n)$

else:

replace  $x$  with new skolem constant

remove  $\exists$  quantifier

II Drop Universal Quantifiers

remove all  $\forall$  quantifiers

II Distribute  $\vee$  over  $\wedge$

repeat until no distribution is possible:

apply rules:

$$(A \vee (B \wedge C)) \rightarrow ((A \vee B) \wedge (A \vee C))$$

$$((A \wedge B) \vee C) \rightarrow ((A \vee C) \wedge (B \vee C))$$

II Simplify

remove duplicate literals in clauses

remove tautological clauses (where  $A$  and  $\neg A$  appear together)

return F

Output

$$\text{function } (A \rightarrow (B \vee C)) \wedge \neg (D \rightarrow E)$$

$$\text{Output: } (\neg A \vee B \vee C) \wedge D \wedge \neg E$$

from copy import deepcopy

```
def print_step(title, content):
    print(f"\n{'='*45}\n{title}\n{'='*45}")
    if isinstance(content, list):
        for i, c in enumerate(content, 1):
            print(f"{i}. {c}")
    else:
        print(content)
```

```
KB = [
    ["\neg Food(x)", "Likes(John,x)"],
    ["Food(Apple)"],
    ["Food(Vegetable)"],
    ["\neg Eats(x,y)", "Killed(x)", "Food(y)"],
    ["Eats(Anil,Peanuts)"],
    ["Alive(Anil)"],
    ["\neg Alive(x)", "\neg Killed(x)"],
    ["Killed(x)", "Alive(x)"]
]
```

```
QUERY = ["Likes(John,Peanuts)"]
```

```

def negate(literal):
    if literal.startswith("¬"):
        return literal[1:]
    return "¬" + literal

def substitute(clause, subs):
    new_clause = []
    for lit in clause:
        for var, val in subs.items():
            lit = lit.replace(var, val)
        new_clause.append(lit)
    return new_clause

def unify(lit1, lit2):
    """Small unifier for patterns like Food(x) and Food(Apple)."""
    if "(" not in lit1 or "(" not in lit2:
        return None
    pred1, args1 = lit1.split("(")
    pred2, args2 = lit2.split("(")
    args1 = args1[:-1].split(",")
    args2 = args2[:-1].split ","
    if pred1 != pred2 or len(args1) != len(args2):
        return None
    subs = {}
    for a, b in zip(args1, args2):
        if a == b:
            continue
        if a.islower():
            subs[a] = b
        elif b.islower():
            subs[b] = a
        else:
            return None
    return subs

def resolve(ci, cj):
    """Return list of (resolvent, substitution, pair)."""
    resolvents = []
    for li in ci:
        for lj in cj:
            if li == negate(lj):
                new_clause = [x for x in ci if x != li] + [x for x in cj if x != lj]
                resolvents.append((list(set(new_clause)), {}, (li, lj)))
            else:
                # same predicate, opposite sign
                if li.startswith("¬") and not lj.startswith("¬") and li[1:].split("(")[0] == lj.split("(")[0]:

```

```

subs = unify(li[1:], lj)
if subs:
    new_clause = substitute([x for x in ci if x != li] + [x for x in cj if x != lj], subs)
    resolvents.append((list(set(new_clause)), subs, (li, lj)))
elif lj.startswith("¬") and not li.startswith("¬") and lj[1:].split("(")[0] == li.split("(")[0]:
    subs = unify(lj[1:], li)
    if subs:
        new_clause = substitute([x for x in ci if x != li] + [x for x in cj if x != lj], subs)
        resolvents.append((list(set(new_clause)), subs, (li, lj)))
return resolvents

def resolution(kb, query):
    clauses = deepcopy(kb)
    negated_query = [negate(q) for q in query]
    clauses.append(negated_query)
    print_step("Initial Clauses", clauses)

    steps = []
    new = []
    while True:
        pairs = [(clauses[i], clauses[j]) for i in range(len(clauses))
                  for j in range(i + 1, len(clauses))]
        for (ci, cj) in pairs:
            for r, subs, pair in resolve(ci, cj):
                if not r:
                    steps.append({
                        "parents": (ci, cj),
                        "resolvent": r,
                        "subs": subs
                    })
                    print_tree(steps)
                    print("\n\☒ Empty clause derived — query proven.")
                    return True
                if r not in clauses and r not in new:
                    new.append(r)
                    steps.append({
                        "parents": (ci, cj),
                        "resolvent": r,
                        "subs": subs
                    })
        if all(r in clauses for r in new):
            print_step("No New Clauses", "Query cannot be proven ✗")
            print_tree(steps)
            return False
        clauses.extend(new)

def print_tree(steps):

```

```

print("\n" + "*45)
print("Resolution Proof Trace")
print("*45)
for i, s in enumerate(steps, 1):
    p1, p2 = s["parents"]
    r = s["resolvent"]
    subs = s["subs"]
    subs_text = f" Substitution: {subs}" if subs else ""
    print(f" Resolve {p1} and {p2}")
    if subs_text:
        print(subs_text)
    if r:
        print(f" => {r}")
    else:
        print(" => {} (empty clause)")
    print("-"*45)

def main():
    print_step("Knowledge Base in CNF", KB)
    print_step("Negated Query", [negate(q) for q in QUERY])
    proven = resolution(KB, QUERY)
    if proven:
        print("\n✓ Query Proven by Resolution: John likes peanuts.")
    else:
        print("\n✗ Query cannot be proven from KB.")

if __name__ == "__main__":
    main()
Unifying: P(f(x).g(y).y) and P(f(g(z)).g(f(a)).f(a))
=> Substitution: x : g(z), y : f(a)

Unifying: Q(x,f(x)) and Q(f(y).y)
=> Not unifiable.

Unifying: H(x,g(x)) and H(g(y).g(g(z)))
=> Substitution: x : g(y), y : z

==== Code Execution Successful ====

```

## Program 10

### Implement Alpha-Beta Pruning

12/01/2022 Alpha-Beta Pruning

```

function Alpha-Beta-Search (state) returns an action
    v ← Max-Value (state, -∞, ∞)
    return the action in Actions (state) with value v

function Max-Value (state, α, β) returns a utility value
    if Terminal-Test (state) then return UINFTY (state)
    v ← -∞
    for each a in Actions (state) do
        v ← Max (v, Min-Value (RESULT (state, a), α, β))
        if v ≥ β then return v
        α ← Max (α, v)
    return v

function Min-Value (state, α, β) returns a utility value
    if Terminal-Test (state) then return UINFTY (state)
    v ← +∞
    for each a in Actions (state) do
        v ← Min (v, Max-Value (RESULT (state, a), α, β))
        if v ≤ α then return v
        β ← min (β, v)
    return v

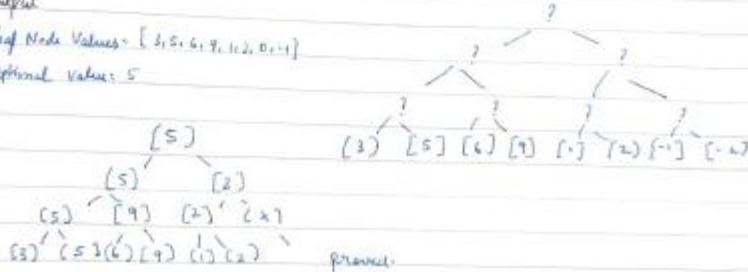
```

A/B action v

Output

Leaf Node Values: [3, 5, 6, 9, 10, 2, 0, 1]

Optional Value: 5



# Simplified Tic-Tac-Toe with Unification + Alpha-Beta  
# No parsing layer, direct symbolic unification and minimax

```

def unify(a, b):
    """Very simple unification for small terms like ('line', [X,O,X])"""
    if a == b:
        return {}
    if isinstance(a, str) and a.islower(): # variable
        return {a: b}
    if isinstance(b, str) and b.islower():
        return {b: a}
    if isinstance(a, tuple) and isinstance(b, tuple):
        if a[0] != b[0] or len(a[1]) != len(b[1]):
            return None

```

```

subs = {}
for x, y in zip(a[1], b[1]):
    s = unify(x, y)
    if s is None:
        return None
    subs.update(s)
return subs
return None

# Winning triples (rows, cols, diagonals)
WIN_TRIPLES = [(0,1,2),(3,4,5),(6,7,8),(0,3,6),(1,4,7),(2,5,8),(0,4,8),(2,4,6)]

def winner(board):
    pattern = ('line', ['X','X','X'])
    for i,j,k in WIN_TRIPLES:
        term = ('line', [board[i], board[j], board[k]])
        if unify(term, pattern):
            return 'X'
        if unify(term, ('line',['O','O','O'])):
            return 'O'
    return None

def is_full(board): return all(c != '_' for c in board)

def evaluate(board):
    w = winner(board)
    if w == 'X': return 1
    if w == 'O': return -1
    if is_full(board): return 0
    return None

def alpha_beta(board, player, alpha=-float('inf'), beta=float('inf')):
    val = evaluate(board)
    if val is not None:
        return val, None

    moves = [i for i,c in enumerate(board) if c == '_']
    best_move = None
    if player == 'X':
        max_eval = -float('inf')
        for m in moves:
            new_board = board[:]
            new_board[m] = 'X'
            eval_, _ = alpha_beta(new_board, 'O', alpha, beta)
            if eval_ > max_eval:
                max_eval, best_move = eval_, m

```

```

        alpha = max(alpha, eval_)
        if beta <= alpha: break
    return max_eval, best_move
else:
    min_eval = float('inf')
    for m in moves:
        new_board = board[:]
        new_board[m] = 'O'
        eval_, _ = alpha_beta(new_board, 'X', alpha, beta)
        if eval_ < min_eval:
            min_eval, best_move = eval_, m
    beta = min(beta, eval_)
    if beta <= alpha: break
return min_eval, best_move

def print_board(b):
    for i in range(0,9,3):
        print(''.join(b[i:i+3]))
    print()

# --- Example usage ---
board = ['_']*9
score, move = alpha_beta(board, 'X')
print("Best first move for X:", move)
board[move] = 'X'
print_board(board)

```

```

Best first move for X: 0
X _ _
- - -
- - -

```