

1. (4 points) Let S_1 and S_2 be the standard Vigenère and Permutation ciphers, respectively, with $\mathcal{P} = (\mathbb{Z}_{26})^5$ (so the block length of each is $m = 5$). Consider the product cipher $S_1 \times S_2$. Consider the keycode $k_1 = \text{latex}$ in Vigenère Cipher, and the key k_2 in Permutation Cipher given by

1	2	3	4	5
4	5	2	1	3

Find the decryption $d_{(k_1, k_2)}(\text{IEAEDURMZXALZTM})$ in $S_1 \times S_2$. Write your plaintext with spaces.

2. (3 points) Find a Vigenère keycode k'_1 such that $d_{(k_2, k'_1)}(\text{IEAEDURMZXALZTM})$ in $S_2 \times S_1$ is the same plaintext you obtained in previous problem.
3. (4 points) Let M be the Multiplicative Cipher and S be the Shift Cipher. For the encryption rule $e_{(9, 15)}(x)$ in $M \times S$, find the corresponding encryption rule $e_{(c, d)}(x)$ in $S \times M$. In other words, find the value of c and d such that $e_{(c, d)}(x)$ in $S \times M$ is equal to $e_{(9, 15)}(x)$ in $M \times S$.
4. (9 points) Find the solution for problem 4 of the problem set 5. You should also write the intermediate results (i.e., the rows A, B, D, E, F, G, H, and J from Figure 1).