

INTRODUCTION TO CRYPTOGRAPHY – QUIZ 4

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Quiz

- (2 points) An involutory key in a permutation cipher is a permutation π such that $\pi^{-1}=\pi$. In other words, $\pi(i)=j \Leftrightarrow \pi(j)=i$. For $m=3$, there are four involutory keys. Find them.

-> Consider $p = (1\ 2\ 3)$

Involuntary keys (π) include :

- $\begin{pmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \end{pmatrix}$
- $\begin{pmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \end{pmatrix}$
- $\begin{pmatrix} 1 & 2 & 3 \\ 1 & 3 & 2 \end{pmatrix}$
- $\begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{pmatrix}$

Eg: CAT encrypted using $\pi = \begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{pmatrix}$ -> TAC

Now π (TAC) -> CAT

- (4 points) For the key $K = \begin{pmatrix} 3 & 2 \\ 5 & 7 \end{pmatrix}$ in Hill Cipher, find K^{-1} .

-> $K = \begin{pmatrix} 3 & 2 \\ 5 & 7 \end{pmatrix}$ is a 2x2 matrix, therefore inverse of such matrix -> $K^{-1} = (1/\det|k|) \begin{pmatrix} 7 & -2 \\ -5 & 3 \end{pmatrix}$

$$|K| = 21 - 10 = 11$$

$$1/|K| = 11^{-1} = 19$$

$$K^{-1} = (19) \begin{pmatrix} 7 & -2 \\ -5 & 3 \end{pmatrix} = \begin{pmatrix} 133 & -38 \\ -95 & 57 \end{pmatrix} = \begin{pmatrix} 3 & -12 \\ -17 & 5 \end{pmatrix} = \begin{pmatrix} 3 & 14 \\ 9 & 5 \end{pmatrix}$$

$$\text{Therefore, } K^{-1} = \begin{pmatrix} 3 & 14 \\ 9 & 5 \end{pmatrix}$$

- (6 points) By using the Hill cipher with the key K as given in the previous problem, decrypt:

WZNLQM

-> W Z N L Q M

 22 25 13 11 16 12

$$(22 \quad 25) \begin{pmatrix} 3 & 14 \\ 9 & 5 \end{pmatrix} = (5 \quad 17)$$

$$(13 \quad 11) \begin{pmatrix} 3 & 14 \\ 9 & 5 \end{pmatrix} = (8 \quad 3)$$

$$(16 \quad 12) \begin{pmatrix} 3 & 14 \\ 9 & 5 \end{pmatrix} = (0 \quad 24)$$

5	17	8	3	0	24
F	R	I	D	A	Y

Therefore, decrypted text = friday

4. (2 points) Suppose that a key stream is generated for a stream cipher by using the following linear recurrence $z_{i+2} = z_i + z_{i+1} \bmod 2$ for $i \geq 1$. For the initial vector $(z_1, z_2) = (1, 1)$ find the first six bits of the key stream.

->

$$z_{i+2} = z_i + z_{i+1}$$

$$z_1 = 1, z_2 = 1$$

$$z_3 = z_{1+2} = z_1 + z_{1+1} = z_1 + z_2 = 1+1 = 2 \bmod 2 = 0$$

$$z_4 = z_{2+2} = z_2 + z_{2+1} = z_2 + z_3 = 1+0 = 1 \bmod 2 = 1$$

$$z_5 = z_{3+2} = z_3 + z_{3+1} = z_3 + z_4 = 0+1 = 1 \bmod 2 = 1$$

$$z_6 = z_{4+2} = z_4 + z_{4+1} = z_4 + z_5 = 1+1 = 2 \bmod 2 = 0$$

Therefore, the first 6 bits of the key stream are : 1,1,0,1,1,0

5. (2 points) Find the period of the key stream generated by linear recurrence and initial vector as given in the previous problem.

-> Key stream's period is given by $2^m - 1$ where m is the initial key length. The initial key length in the previous question is m=2, therefore

$$\text{Period} = 2^2 - 1 = 4 - 1 = 3$$

6. (4 points) By using auto key cipher with the key k = 7, decrypt:

LBF B

-> Auto key = 7

L	B	F	B
11	1	5	1
$11-7=4$	$1-4=-3=23$	$5-23=-18=8$	$1-8=-7=19$
4	23	8	19
E	X	I	T

Plaintext = exit