

1

$$\text{Gcd}(41, 131)$$

$$131 = 3 \times 41 + 8$$

$$41 = 5 \times 8 + 1$$

$$8 = 8 \times 1 + 0$$

$$\text{Gcd}(41, 131) = 1$$

$$\text{Gcd} = 41x + 131y = 1$$

$$1 = 41 - 5 \times 8$$

$$1 = 41 - 5 \times (131 - 3 \times 41) = 16 \times 41 - 5 \times 131$$

$$16 \times 41 = 1 \pmod{131}$$

$$\text{Inverse} = 16$$

B

$$41x = 9 \pmod{131}$$

$$X = 16 \times 9 = 144$$

2

$$3^{100} = 1 \pmod{101}$$

$$(3^{100})^{14} = 1^{14} \pmod{101}$$

$$3^{1400} = 1 \pmod{101}$$

$$3^{1400} \times 3^3 = 1 \times 3^3 \pmod{101}$$

$$3^{1403} = 3^3 \pmod{101} = 27$$

3

$$1^2 = 1$$

$$2^2 = 0$$

$$3^2 = 1$$

$$4^2 = 0$$

$$5^2 = 1$$

Squares are 1 and 0

B

If a is even:

Even x even = even

Even mod 2 = 0

If a is odd

Odd x odd = odd

Odd mod 2 = 1