

CS 3310 HW #2

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1. int[] find (int[] arr, int left, int right, int min, max, int L, int R) {
    int minResult;
    if (left + 1 >= right)
        then minResult = Math.min(arr[left], min)
        if (arr[left] - min > max) {
            then max = arr[left] - min
            R = left
        }
    } else {
        int mid = (right + left) / 2
        minResult = find(arr, left, mid-1, min, max)
        minResult = find(arr, mid, right, minResult, max)
    }
    return minResult;
}

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2. int turningPoint (int[] arr, int left, int right) {
    int center = (right + left) / 2
    if (arr[center] > arr[center-1] && arr[center] > arr[center+1])
        then return center
    else if (arr[center] < arr[center+1])
        then turningPoint(arr, center+1, right)
    else if (arr[center] < arr[center-1])
        then turningPoint(arr, left, center)
    }
}

```

Best-Case:

$$\Omega(1)$$

Worst-Case:

$$T(n) = T(n/2) + c$$

$$= O(\log n)$$

Average Case

$$T(n) = T(n/2) + c$$

$$= O(\log n)$$


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3. a) int maxDiff (int[] arr) {
    Arrays.sort(arr); int sum1=0; int sum2=0;
    for (i=0; i<arr.length/2; i++) {
        sum1 += arr[i];
    }
    for (i=arr.length/2; i<arr.length; i++) {
        sum2 += arr[i];
    }
    return sum2 - sum1;
}

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b) int maxDiff(int[] arr) {
    int sum=0; int min=0; sum=0;
    for (int i=0; i<arr.length; i++) {
        sum += arr[i];
    }
    int avg = sum / arr.length;
    int lowSum=0, highSum=0;
    for (int i=0; i<arr.length; i++) {
        if (arr[i] >= avg)
            highSum += arr[i];
        else
            lowSum += arr[i];
    }
    return highSum - lowSum;
}

```



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4. boolean searchMatrix(int[][] matrix, int target) {
    int rowLow = 0, colLow = 0, rowHigh = length - 1, colHigh = matrix[0].length;
    while (rowLow < rowHigh) {
        int center = (rowHigh + rowLow) / 2;
        if (matrix[center][colLow] == target) {
            return true;
        }
        if (matrix[center][colLow] > target) {
            rowHigh = center - 1;
        } else if (matrix[center + 1][colLow] > target) {
            rowHigh = center;
            rowLow = center;
        } else {
            rowLow = center + 1;
        }
    }
    while (colLow <= colHigh) {
        int mid = (colHigh + colLow) / 2;
        if (matrix[rowLow][mid] == target) {
            return true;
        }
        if (matrix[rowLow][mid] > target) {
            colHigh = mid - 1;
        } else {
            colLow = mid + 1;
        }
    }
    return false;
}

```


5	2	5	7	12		1	0	2	7
4	1	4	2			5	9	3	4
5	6	3	8		x	6	1	2	8
1	6	7	9			1	2	8	5

$$n1 = (2+1+3+9)(1+9+2+5)$$

$$n2 =$$

$$n1 = (2+1)(1+9) = 30$$

$$n2 = (4+1)(1) = 5$$

$$n3 = 2(0-9) = -18$$

$$n4 = 1(5-1) = 4$$

$$n5 = (2+5)(9) = 63$$

$$n6 = (4-2)(1+0) = 2$$

$$n7 = (5-1)(5+9) = 56$$

$$n1 = (7+2)(2+4) = 63$$

$$n2 = (4+2)(2) = 12$$

$$n3 = 7(7-4) = 21$$

$$n4 = 2(3-2) = 2$$

$$n5 = (7+12)4 = 76$$

$$n6 = (4-7)(2+7) = -42$$

$$n7 = (12-2)(3+4) = 70$$

$$n1 = (5+6)(6+2) = 88$$

$$n2 = (1+6)(6) = 42$$

$$n3 = 5(1-2) = -5$$

$$n4 = 6(1-6) = -30$$

$$n5 = (5+6)2 = 22$$

$$n6 = (1-5)(6+1) = -28$$

$$n7 = (6-6)(1+2) = 0$$

$$n1 = (2+5)(3+8) = 84$$

$$n2 = (7+9)(2) = 32$$

$$n3 = 3(8-5) = 9$$

$$n4 = 9(8-2) = 54$$

$$n5 = (3+8)(5) = 55$$

$$n6 = (7-3)(2+8) = 64$$

$$n7 = (8-9)(8+5) = -13$$

$$30+4-63+56$$

$$5+4$$

$$-18+63$$

$$30-18+5+2$$

$$63+2-76+70$$

$$12+2$$

$$21+76$$

$$63+21+12-42$$

$$89-59$$

$$88-30-22+0$$

$$42-30$$

$$-5+22$$

$$88-5+12-28$$

$$84+54-55-13$$

$$32+54$$

$$9+55$$

$$89+9+32+69$$

$$27$$

$$9$$

$$45$$

$$9$$

$$59$$

$$14$$

$$97$$

$$30$$

$$\begin{array}{cc|cc}
 5 & 2 & 5 & 7 & 12 \\
 4 & 1 & & 4 & 2 \\
 5 & 6 & 3 & 8 & x \\
 1 & 6 & 7 & 9 &
 \end{array}
 \quad
 \begin{array}{cc|cc}
 1 & 0 & 2 & 7 \\
 5 & 9 & 3 & 8 \\
 6 & 1 & 2 & 8 \\
 1 & 2 & 8 & 5
 \end{array}$$

$$\begin{bmatrix} 2 & 5 \\ 4 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 \\ 5 & 9 \end{bmatrix}$$

$$m_1 = (2+1)(1+9) = 30$$

$$m_2 = (4+1)(1) = 5$$

$$m_3 = 2(0-9) = -18$$

$$m_4 = 1(5-1) = 4$$

$$m_5 = (2+5)(9) = 63$$

$$m_6 = (4-2)(1) = 2$$

$$\begin{bmatrix}
 27 & 45 & 59 & 97 \\
 9 & 9 & 14 & 30 \\
 36 & 17 & 70 & 64 \\
 12 & 43 & 86 & 125
 \end{bmatrix}$$