



AI VIET NAM

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# CNN Training

## How to increase training accuracy?

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# Objectives

## Activation and Initialization

Glorot initialization (2010)

$$W \sim \mathcal{N}\left(0, \frac{1}{n_j}\right)$$

$n_j$  is #inputs in layer  $j$

Assuming activation functions are linear

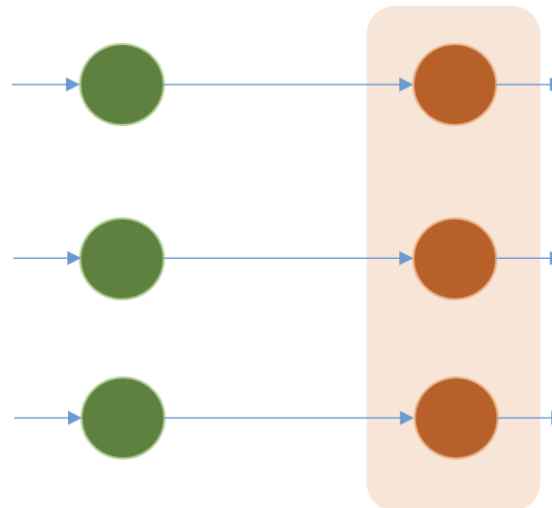
He initialization (2015)

Taking activation function into account

Adapt to ReLU activation

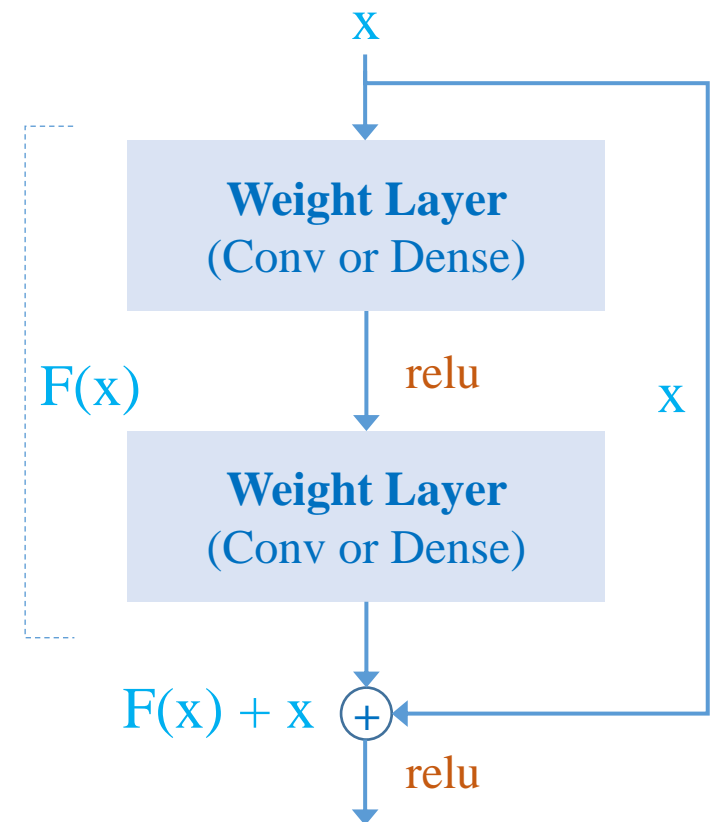
$$W \sim \mathcal{N}\left(0, \frac{2}{n_j}\right)$$

## Data and Feature Normalization



Batch Normalization

## Skip Connections



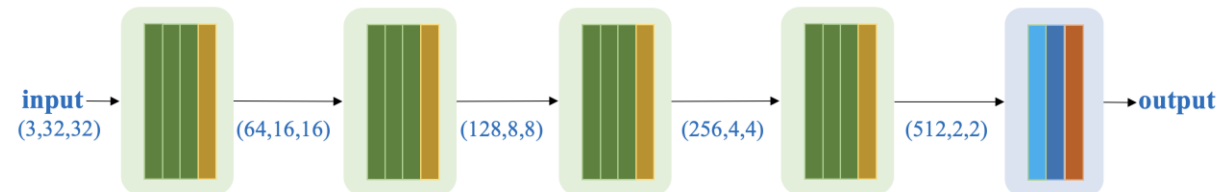
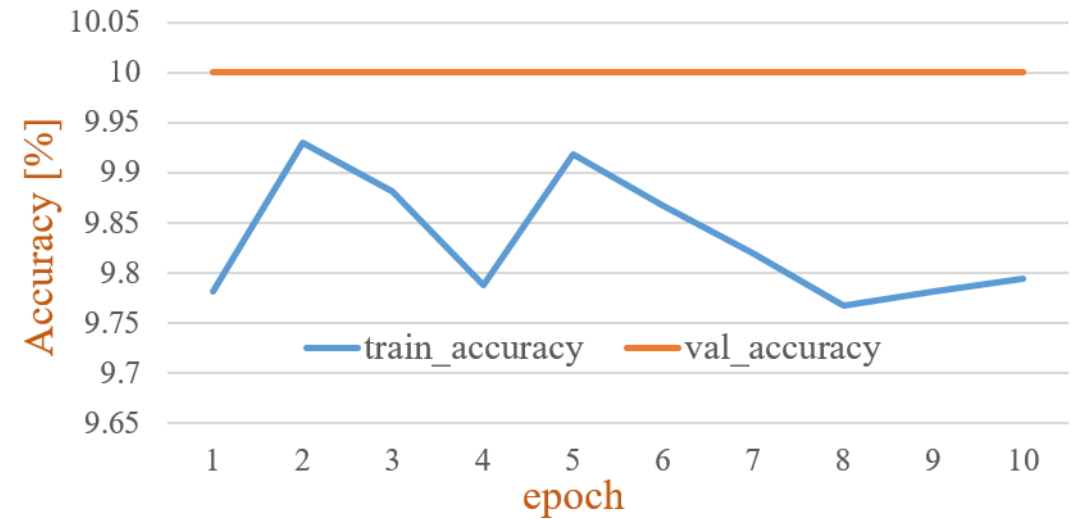
# Outline

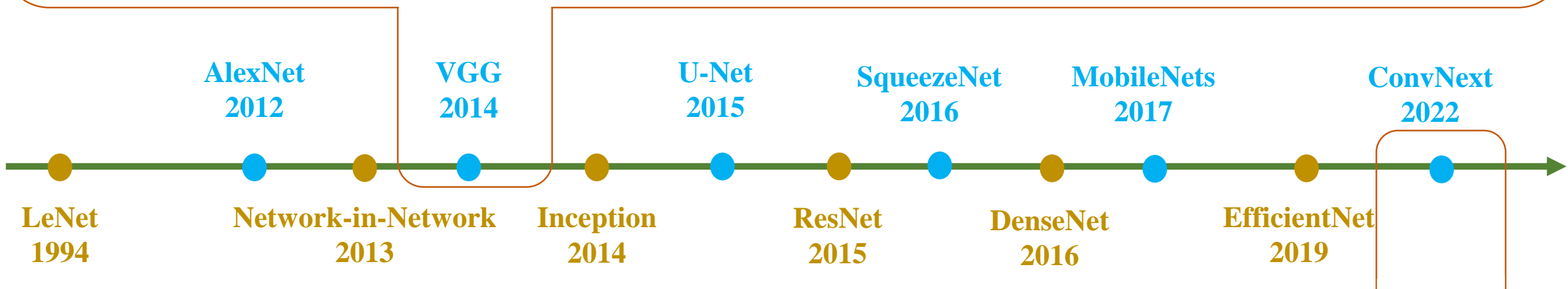
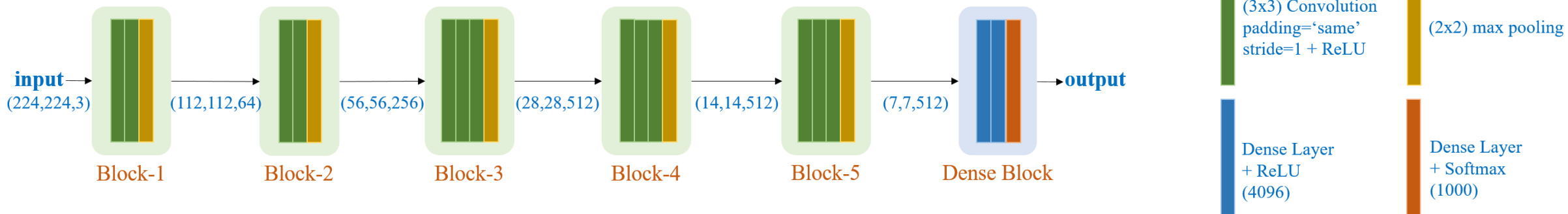
## SECTION 1

### Setting-up Context

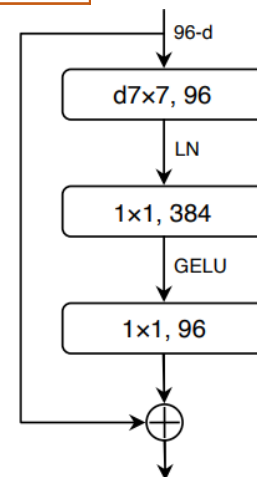
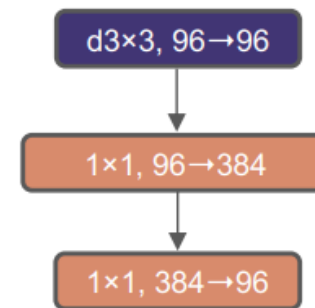
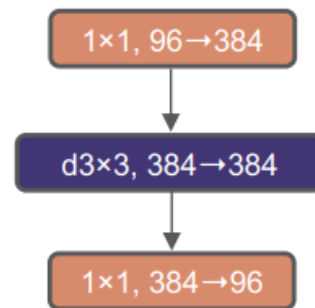
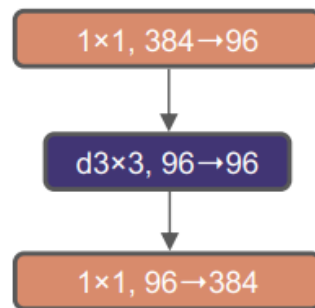
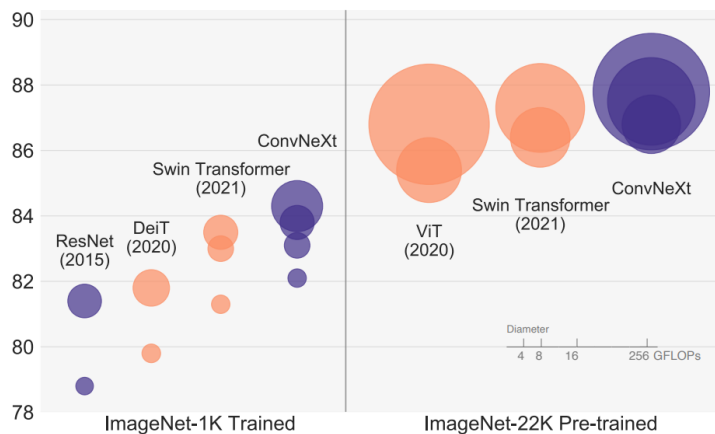
## SECTION 2

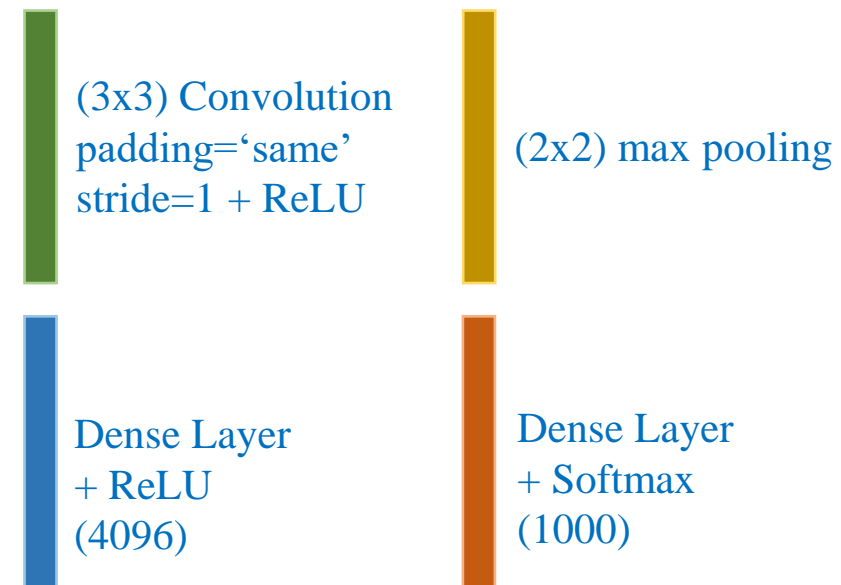
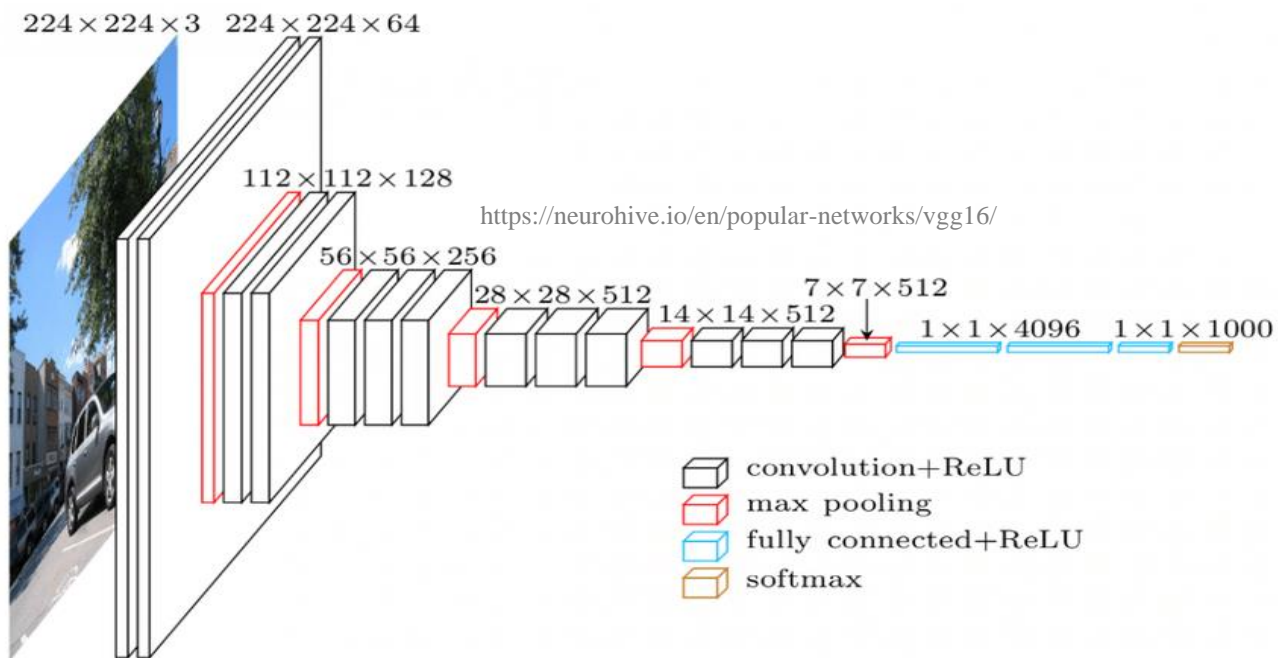
### Solutions for the Context





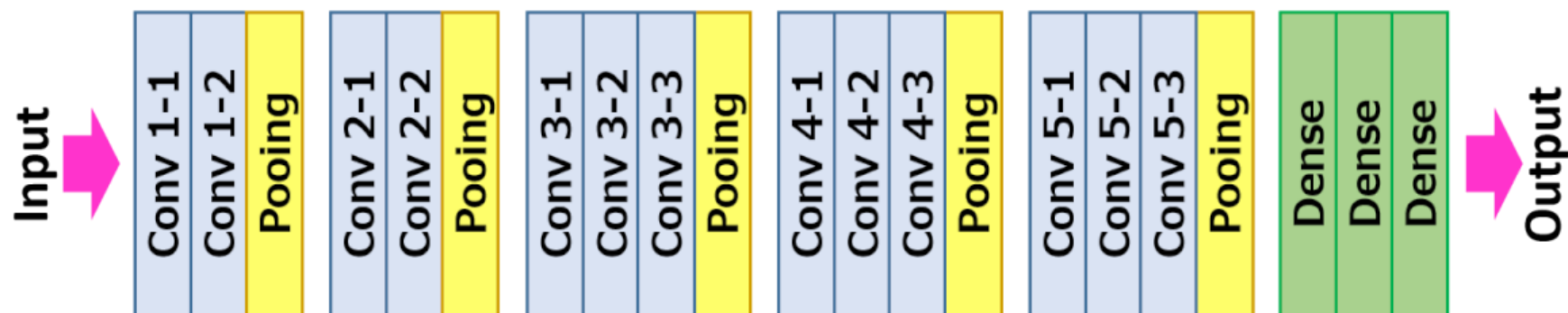
ImageNet-1K Acc.



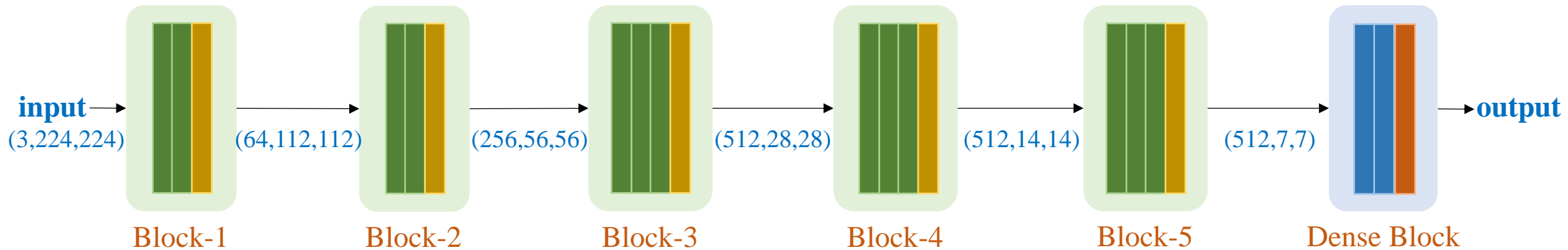


# VGG16

## VGG-16



## ❖ VGG16 for ImageNet



(3x3) Convolution  
padding='same'  
stride=1 + ReLU



(2x2) max pooling



Dense Layer  
+ ReLU  
(4096)



Dense Layer  
+ Softmax  
(1000)

```
# Define the blocks
```

```
block1 = nn.Sequential(  
    nn.Conv2d(3, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(64, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.MaxPool2d(kernel_size=2, stride=2),  
)  
block2 = nn.Sequential(  
    nn.Conv2d(64, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(128, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.MaxPool2d(kernel_size=2, stride=2),  
)  
block3 = nn.Sequential(  
    nn.Conv2d(128, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.MaxPool2d(kernel_size=2, stride=2),  
)  
block4 = nn.Sequential(  
    nn.Conv2d(256, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.MaxPool2d(kernel_size=2, stride=2),  
)  
block5 = nn.Sequential(  
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),  
    nn.MaxPool2d(kernel_size=2, stride=2),  
)
```

```
# Classifier
```

```
classifier = nn.Sequential(  
    nn.Flatten(),  
    nn.Linear(512*7*7, 4096), nn.ReLU(inplace=True),  
    nn.Linear(4096, 4096), nn.ReLU(inplace=True),  
    nn.Linear(4096, 1000),  
)
```

```
# Combine all blocks into one model
```

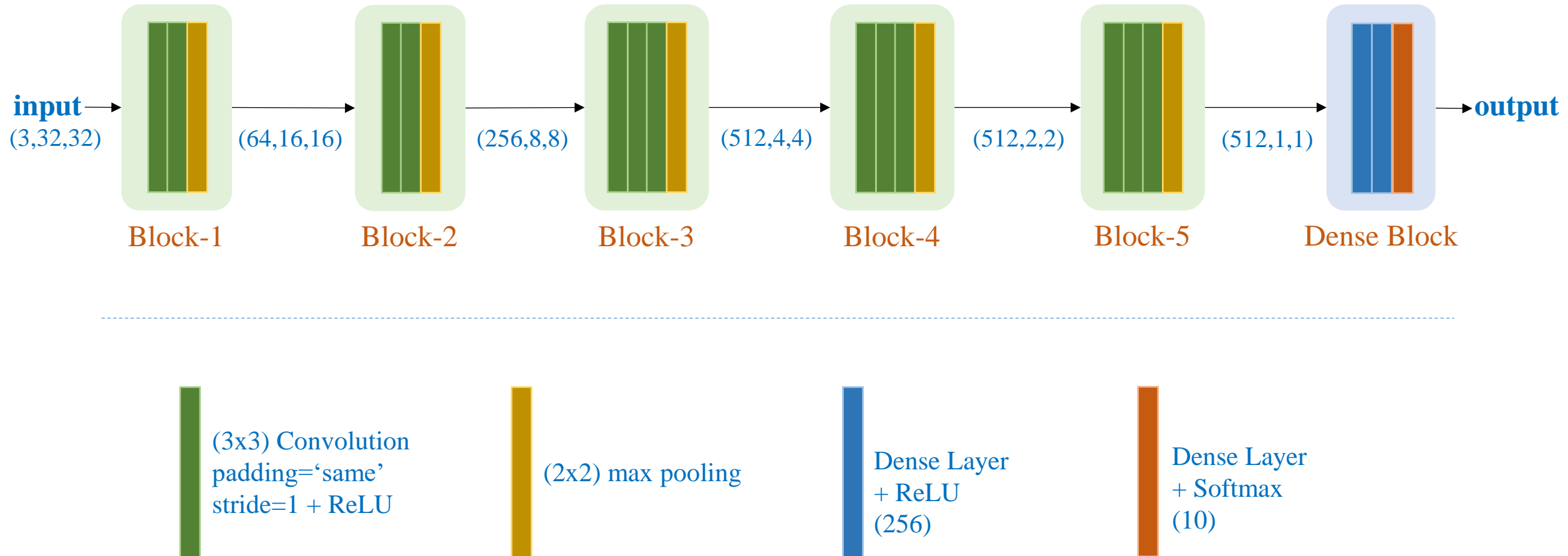
```
class VGG16(nn.Module):  
    def __init__(self):  
        super(VGG16, self).__init__()  
        self.block1 = block1  
        self.block2 = block2  
        self.block3 = block3  
        self.block4 = block4  
        self.block5 = block5  
        self.classifier = classifier  
  
    def forward(self, x):  
        x = self.block1(x)  
        x = self.block2(x)  
        x = self.block3(x)  
        x = self.block4(x)  
        x = self.block5(x)  
        x = self.classifier(x)  
        return x
```

```
# Instantiate the model
```

```
model = VGG16()
```

# CNN Architectures

## ❖ VGG16-like for Cifar-10





```
# Define the blocks
```

```
block1 = nn.Sequential(
    nn.Conv2d(3, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(64, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block2 = nn.Sequential(
    nn.Conv2d(64, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(128, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block3 = nn.Sequential(
    nn.Conv2d(128, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block4 = nn.Sequential(
    nn.Conv2d(256, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block5 = nn.Sequential(
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
```

```
# Classifier
```

```
classifier = nn.Sequential(
    nn.Flatten(),
    nn.Linear(512*1*1, 256), nn.ReLU(inplace=True),
    nn.Linear(256, 256), nn.ReLU(inplace=True),
    nn.Linear(256, 10),
)
```

```
# Combine all blocks into one model
```

```
class VGG16(nn.Module):
    def __init__(self):
        super(VGG16, self).__init__()
        self.block1 = block1
        self.block2 = block2
        self.block3 = block3
        self.block4 = block4
        self.block5 = block5
        self.classifier = classifier
```

```
    def forward(self, x):
        x = self.block1(x)
        x = self.block2(x)
        x = self.block3(x)
        x = self.block4(x)
        x = self.block5(x)
        x = self.classifier(x)
        return x
```

```
# Instantiate the model
```

```
model = VGG16()
```

# Image Data

## Fashion-MNIST dataset

Grayscale images

Resolution=28x28

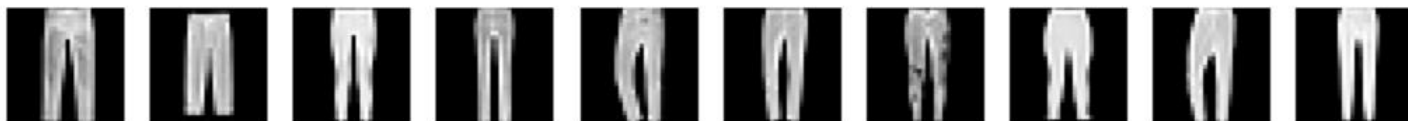
Training set: 60000 samples

Testing set: 10000 samples

T-shirt



Trouser



Pullover



Dress



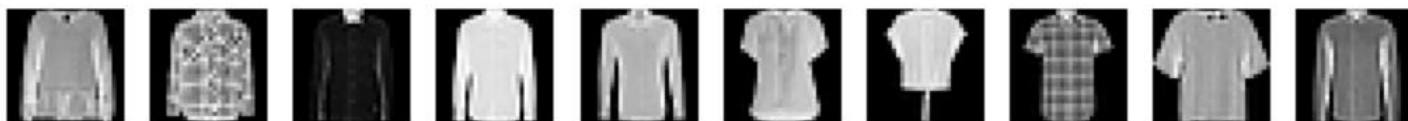
Coat



Sandal



Shirt



Sneaker



Bag

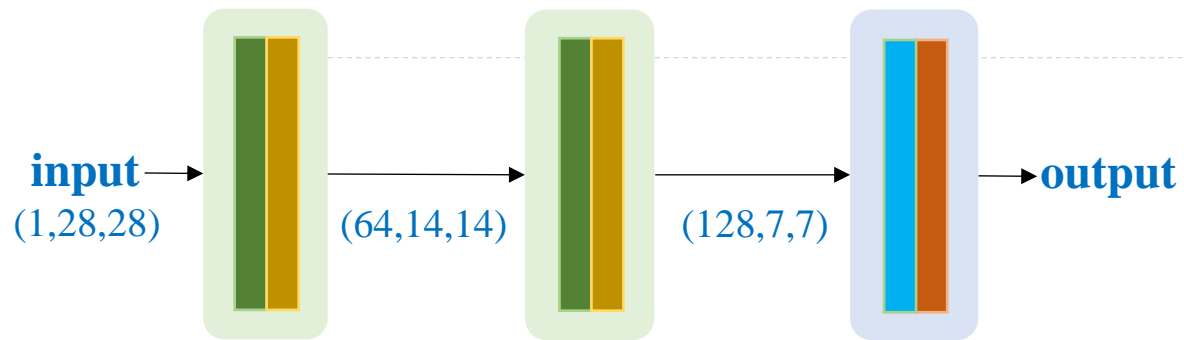


Ankle  
Boot



# Network Training

## ❖ Fashion-MNIST dataset

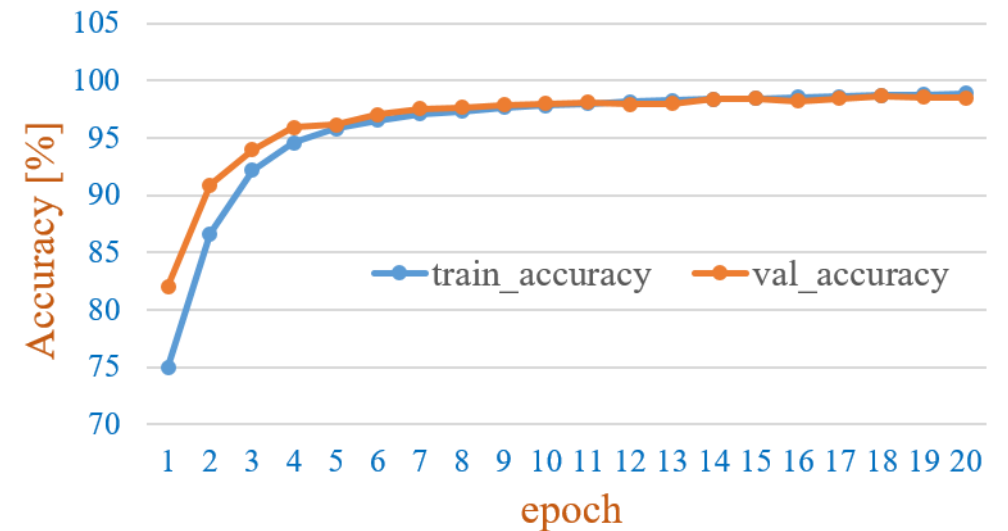
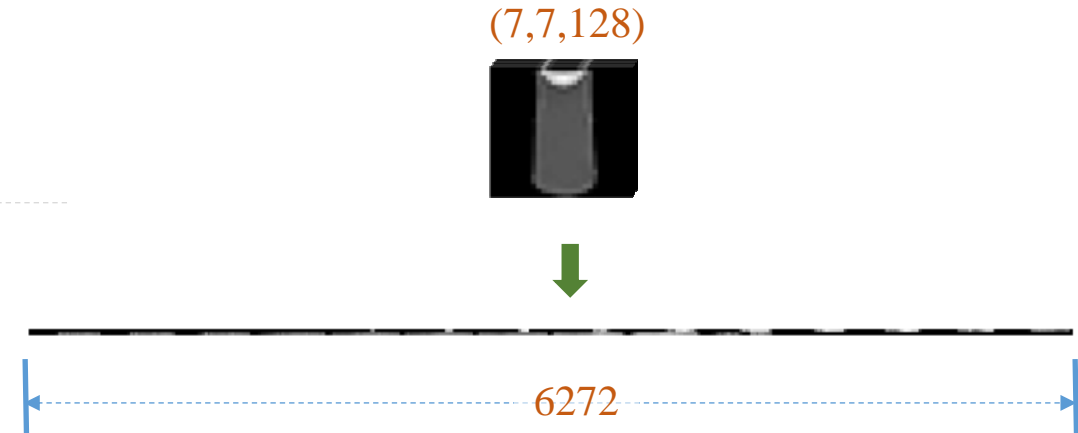


(3x3) Convolution  
padding='same'  
stride=1 + Sigmoid

(2x2) max pooling

Flatten

Dense Layer-10  
+ Softmax





## ❖ Fashion-MNIST dataset

### X-data format

(batch, channel, height, width)

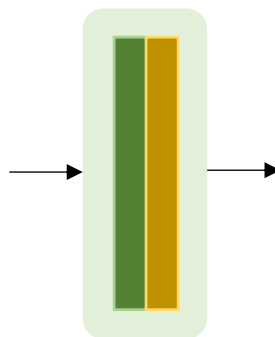
### Data normalization [0,1]

(3x3) Convolution with 64 filters,  
stride=1, padding='same'  
+ Sigmoid activation  
+ glorot\_uniform initialization

Adam optimizer and Cross-entropy loss

(3x3) Convolution  
padding='same'  
stride=1 + Sigmoid

(2x2) max pooling



```
# Data
transform = Compose([transforms.ToTensor()])
train_set = FashionMNIST(root='data',
                           train=True,
                           download=True,
                           transform=transform)

trainloader = DataLoader(train_set,
                          batch_size=256,
                          shuffle=True,
                          num_workers=4)
```

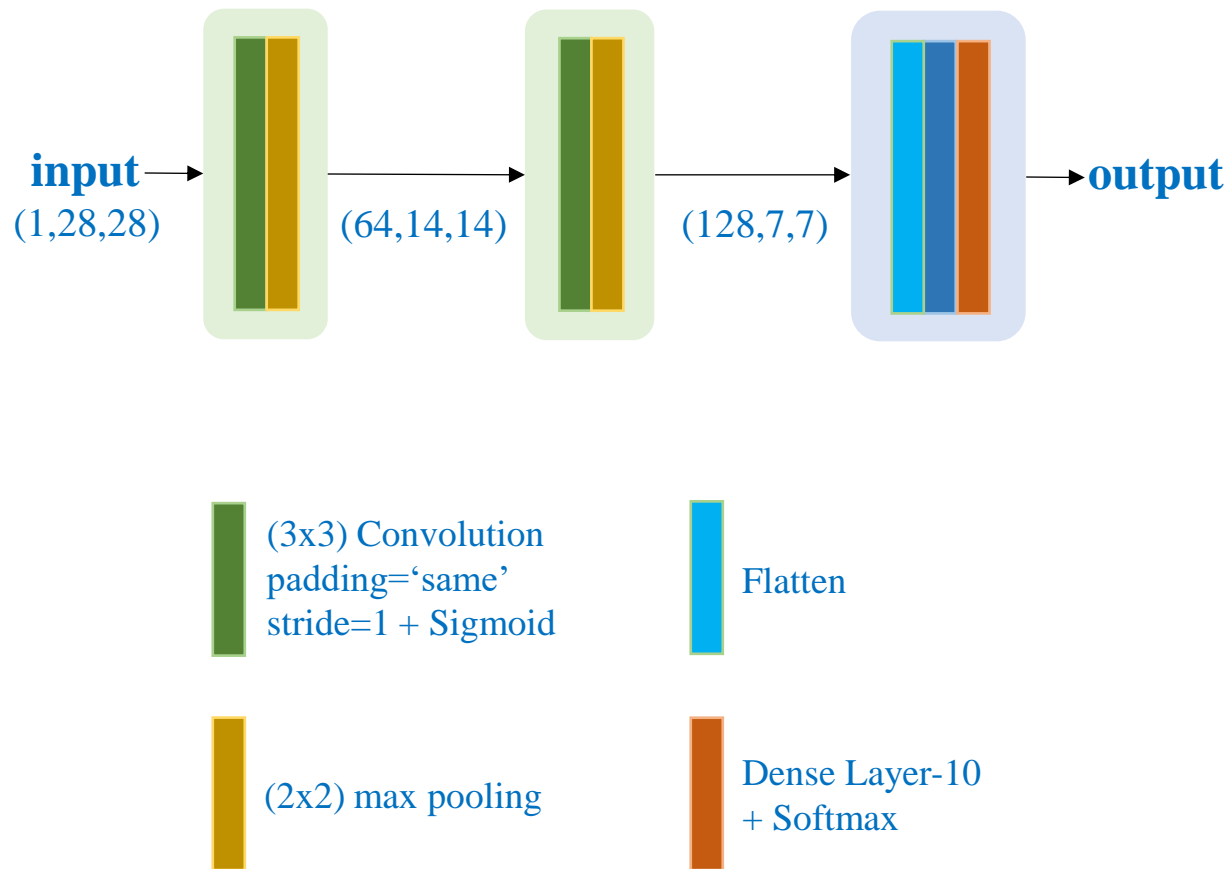
```
import torch.nn as nn
import torch.nn.init as init

block = nn.Sequential(nn.Conv2d(1, 64, 3,
                                 stride=1,
                                 padding='same'),
                       nn.Sigmoid(),
                       nn.MaxPool2d(2, 2))

for m in block:
    if isinstance(m, nn.Conv2d):
        init.xavier_uniform_(m.weight)
        if m.bias is not None:
            init.zeros_(m.bias)

# Loss and optimizer
criterion = nn.CrossEntropyLoss()
optimizer = Adam(model.parameters(), lr=1e-3)
```

## ❖ Fashion-MNIST dataset



```
# Declare layers
conv_layer1 = nn.Sequential(
    nn.Conv2d(1, 64, 3, stride=1, padding='same'),
    nn.Sigmoid(),
    nn.MaxPool2d(2, 2)
)
conv_layer2 = nn.Sequential(
    nn.Conv2d(64, 128, 3, stride=1, padding='same'),
    nn.Sigmoid(),
    nn.MaxPool2d(2, 2)
)

flatten = nn.Flatten()
fc_layer1 = nn.Sequential(
    nn.Linear(128*7*7, 512),
    nn.Sigmoid()
)
fc_layer2 = nn.Linear(512, 10)

# Given data x
x = conv_layer1(x)
x = conv_layer2(x)
x = flatten(x)
x = fc_layer1(x)
x = fc_layer2(x)
```



# Network Training

**Cifar-10 dataset**  
(more complex dataset)

Color images

Resolution=32x32

Training set: 50000 samples

Testing set: 10000 samples

airplane



automobile



bird



cat



deer



dog



frog



horse



ship

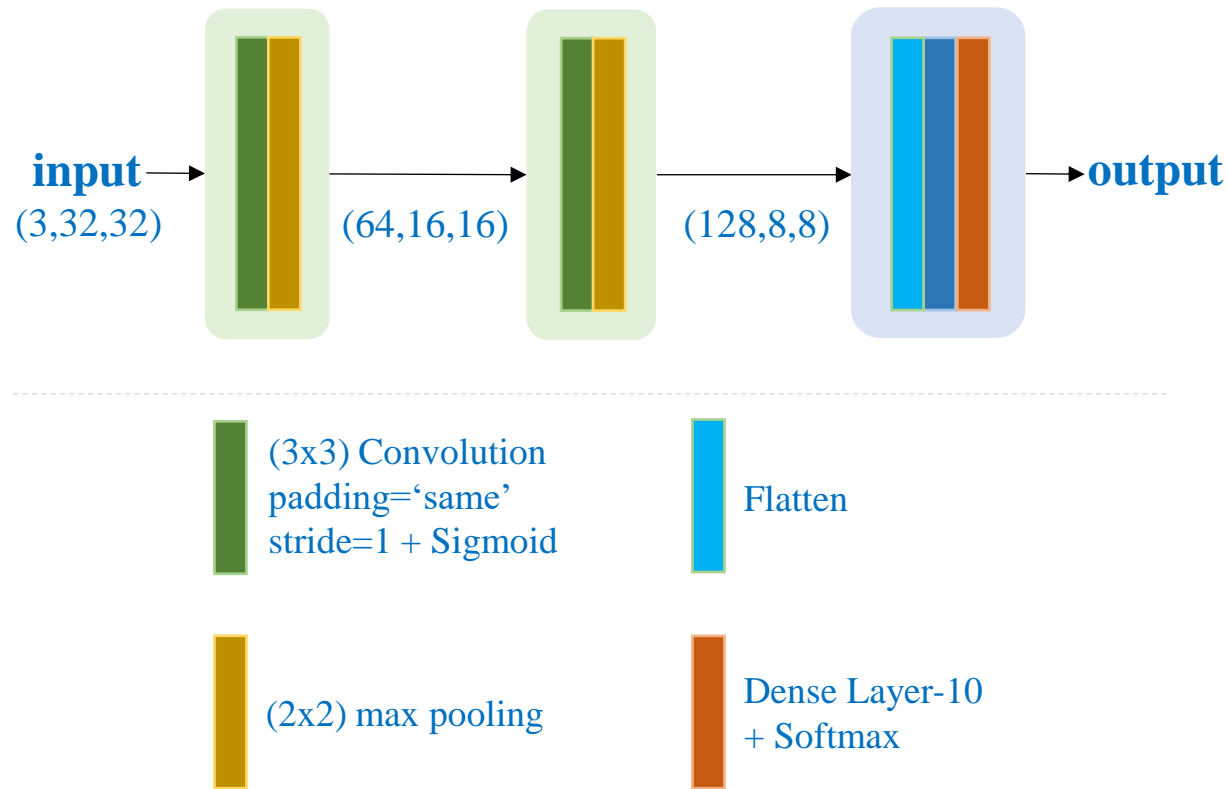


truck



# Network Training

## ❖ Cifar-10 dataset



Data normalization [0,1]

Glorot uniform initialization

Adam optimizer with lr=1e-3

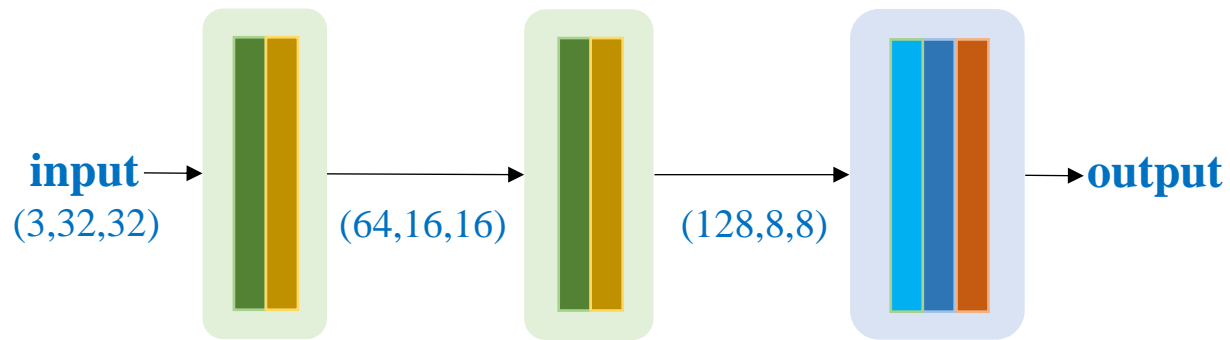
```
conv_layer1 = nn.Sequential(
    nn.Conv2d(1, 64, 3, stride=1, padding='same'),
    nn.Sigmoid(),
    nn.MaxPool2d(2, 2)
)
conv_layer2 = nn.Sequential(
    nn.Conv2d(64, 128, 3, stride=1, padding='same'),
    nn.Sigmoid(),
    nn.MaxPool2d(2, 2)
)

flatten = nn.Flatten()
fc_layer1 = nn.Sequential(
    nn.Linear(128*8*8, 512),
    nn.Sigmoid()
)
fc_layer2 = nn.Linear(512, 10)

# Given data x
x = conv_layer1(x)
x = conv_layer2(x)
x = flatten(x)
x = fc_layer1(x)
x = fc_layer2(x)
```

# Network Training

## ❖ Cifar-10 dataset



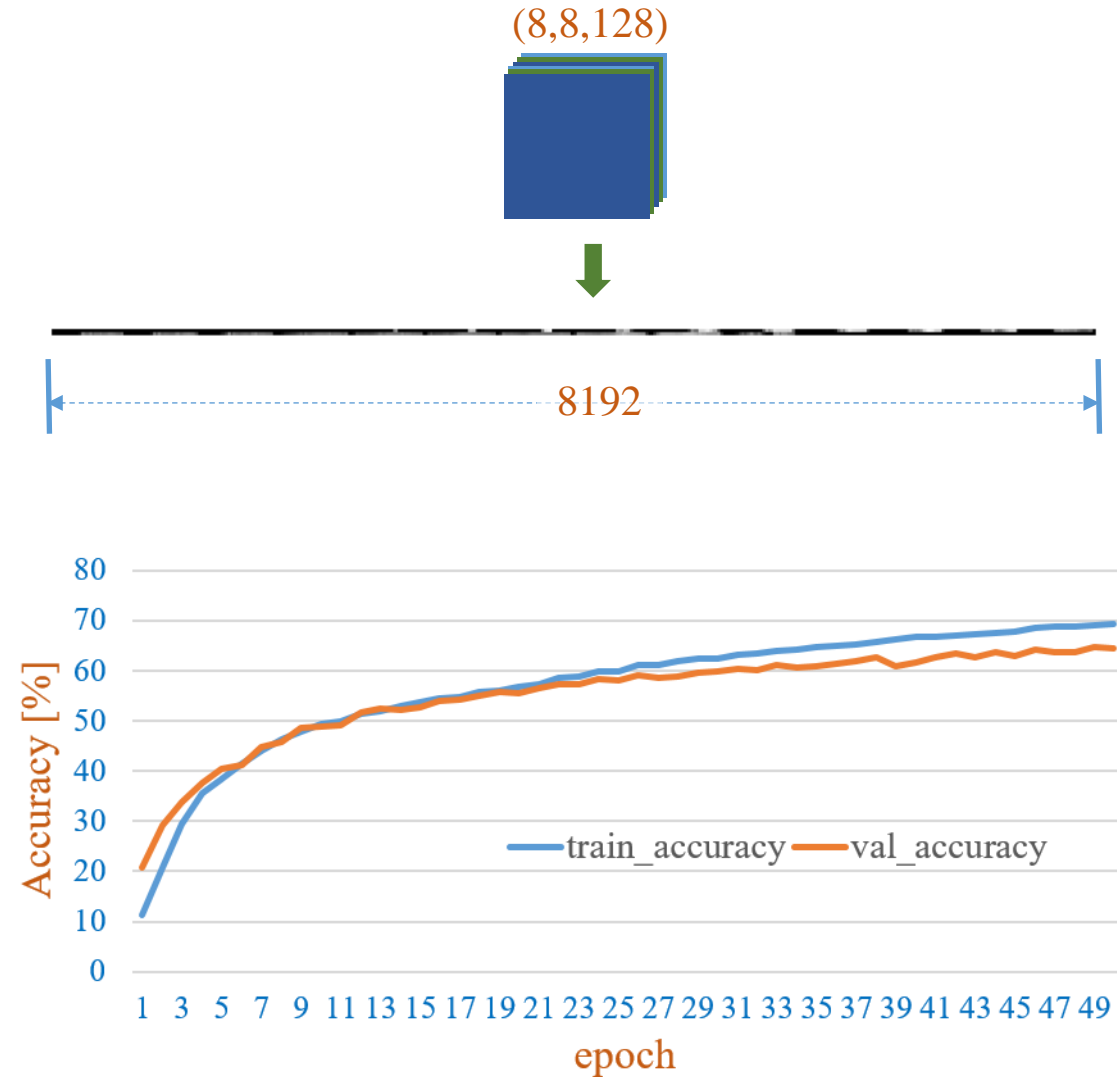
(3x3) Convolution  
padding='same'  
stride=1 + Sigmoid

(2x2) max pooling

Flatten

Dense Layer-10  
+ Softmax

Accuracy: 69.3% - Val\_accuracy: 64.5%

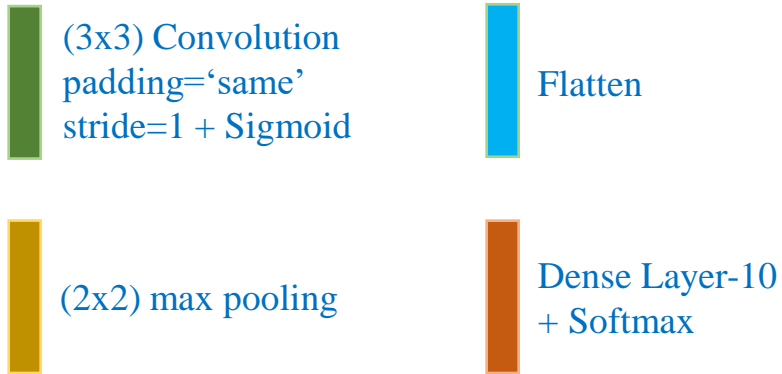




# Network Training

## ❖ Cifar-10 dataset:

### ❖ Adding more layers

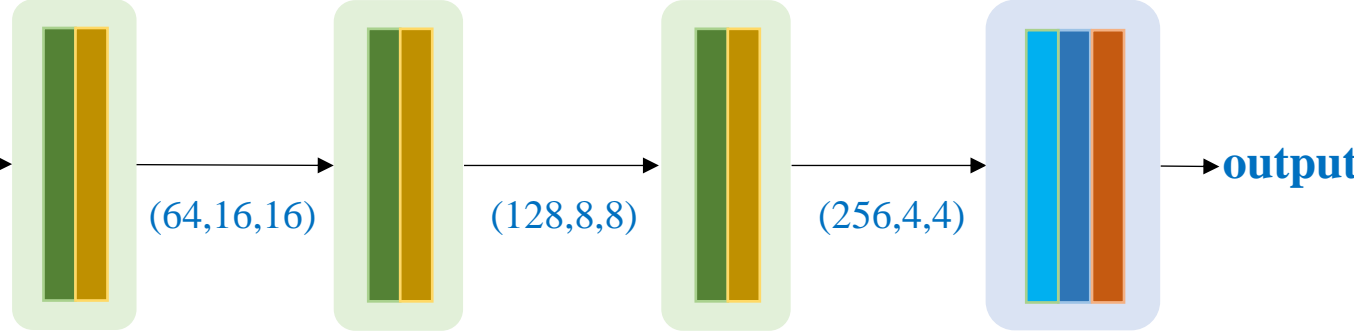


Data normalization [0,1]

Glorot uniform initialization

Adam optimizer with lr=1e-3

input  
(3,32,32)

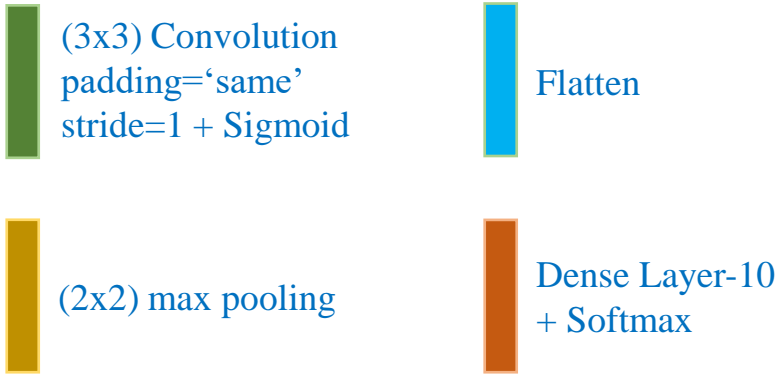
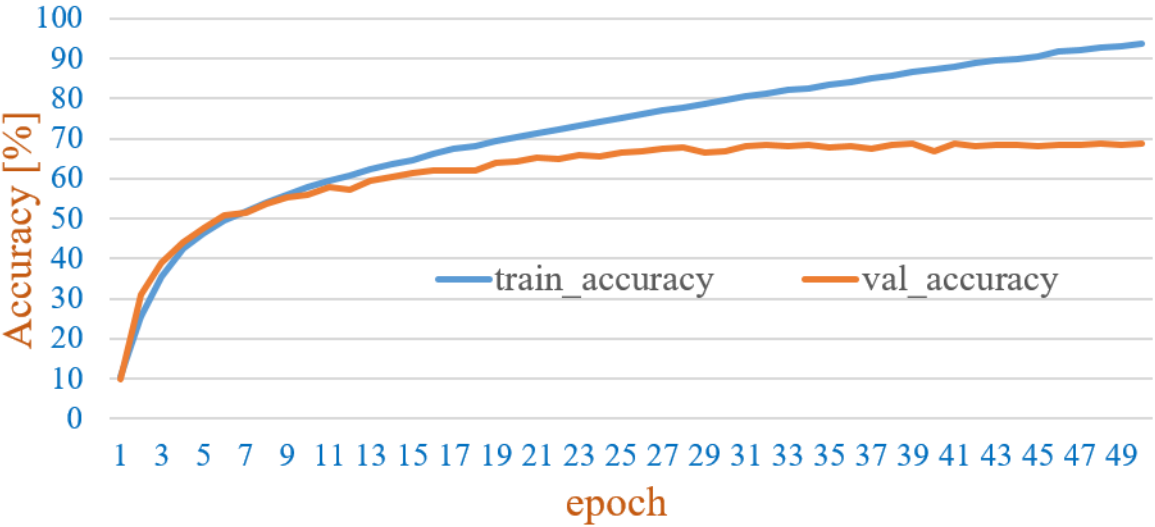
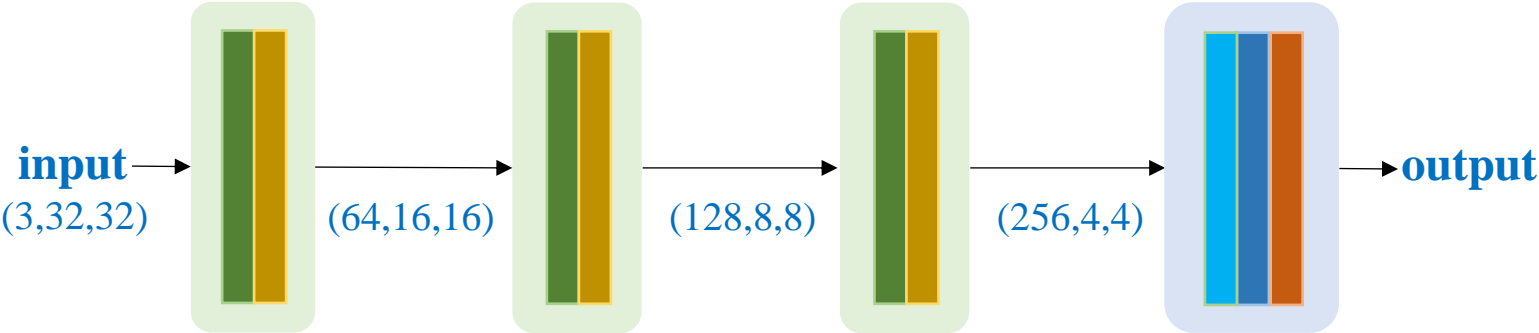


```
conv_layer1 = nn.Sequential(  
    nn.Conv2d(3, 64, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
conv_layer2 = nn.Sequential(  
    nn.Conv2d(64, 128, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
conv_layer3 = nn.Sequential(  
    nn.Conv2d(128, 256, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
  
flatten = nn.Flatten()  
fc_layer1 = nn.Sequential(  
    nn.Linear(256*4*4, 512),  
    nn.Sigmoid()  
)  
  
fc_layer2 = nn.Linear(512, n_classes)
```

## ❖ Cifar-10 dataset:

### ❖ Adding more layers

Good news: Network accuracy increases about 25%



Accuracy: 93.8% - Val\_accuracy: 68.7%

# Network Training

Cifar-10 dataset:

❖ Keep adding more layers

(3x3) Convolution  
padding='same'  
stride=1 + Sigmoid

Flatten

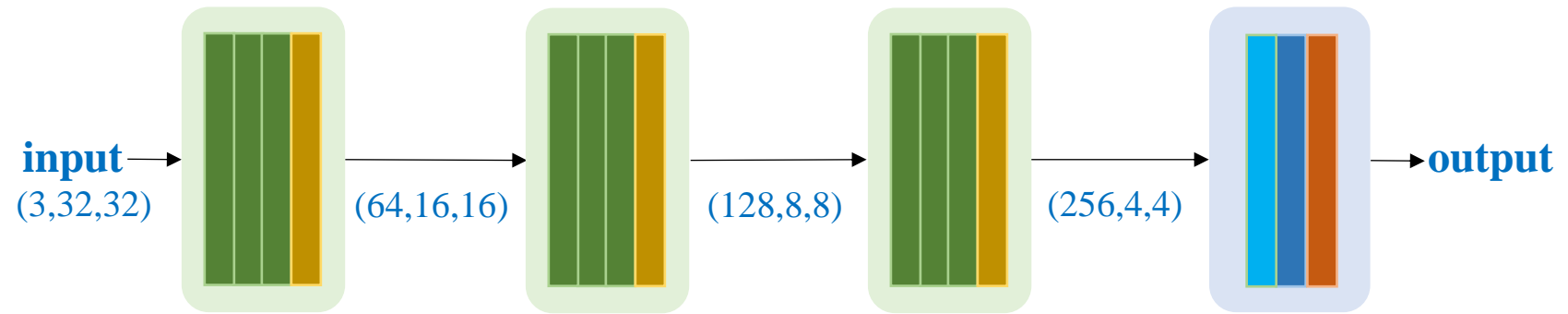
(2x2) max pooling

Dense Layer-10  
+ Softmax

Data normalization [0,1]

Glorot uniform initialization

Adam optimizer with lr=1e-3



```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.Sigmoid(),
                             nn.MaxPool2d(2, 2))

conv_layer4 = nn.Sequential(nn.Conv2d(64, 128, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer5 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer6 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.Sigmoid(),
                             nn.MaxPool2d(2, 2))

conv_layer7 = nn.Sequential(nn.Conv2d(128, 256, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer8 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer9 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.Sigmoid(),
                             nn.MaxPool2d(2, 2))

flatten = nn.Flatten()

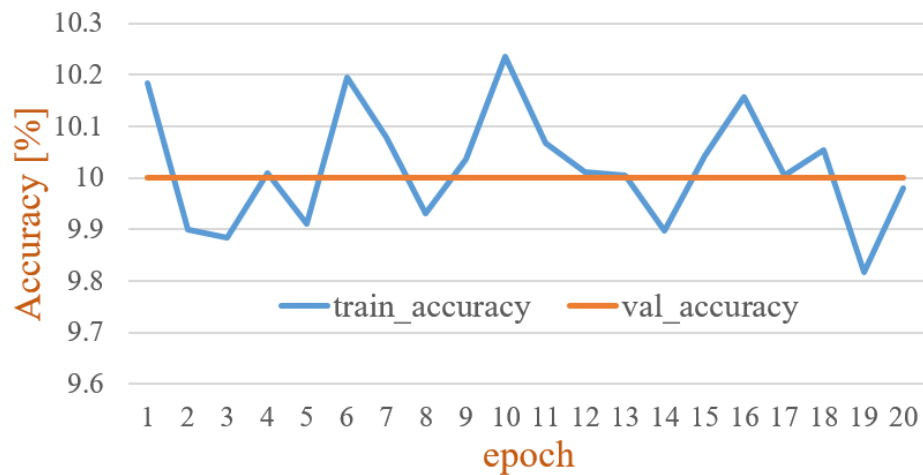
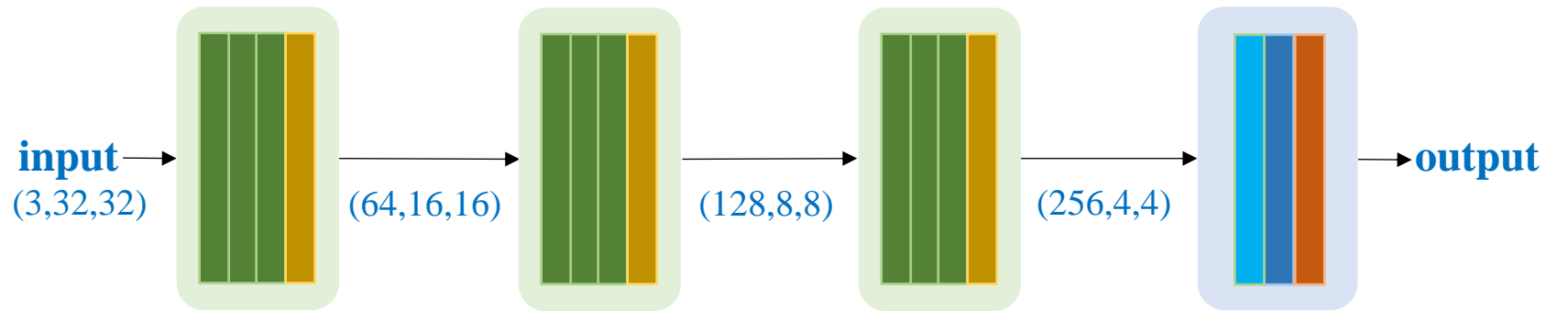
fc_layer1 = nn.Sequential(nn.Linear(256*4*4, 512), nn.Sigmoid())
fc_layer2 = nn.Linear(512, 10)
```

# Network Training

## ❖ Cifar-10 dataset:

❖ Keep adding more layers

The network does not learn



(3x3) Convolution  
padding='same'  
stride=1 + Sigmoid

(2x2) max pooling

Flatten

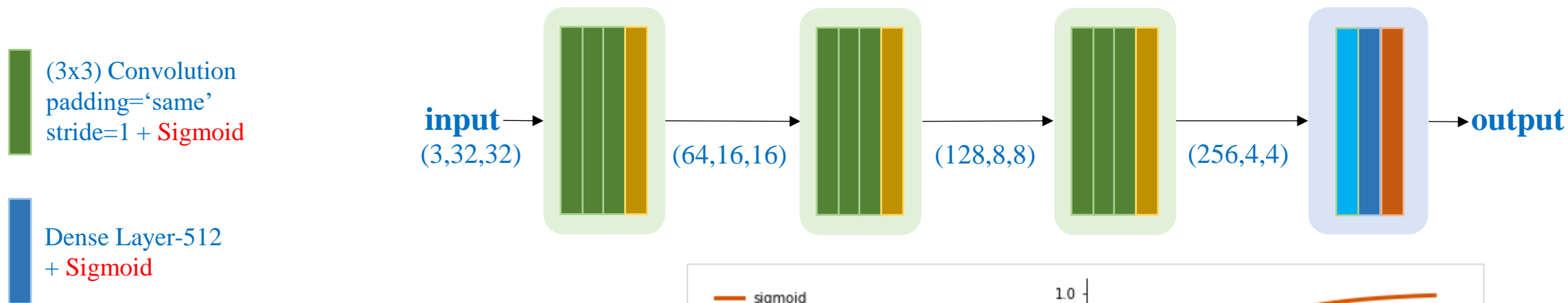
Dense Layer-10  
+ Softmax

Dense Layer-512  
+ Sigmoid

# Network Training

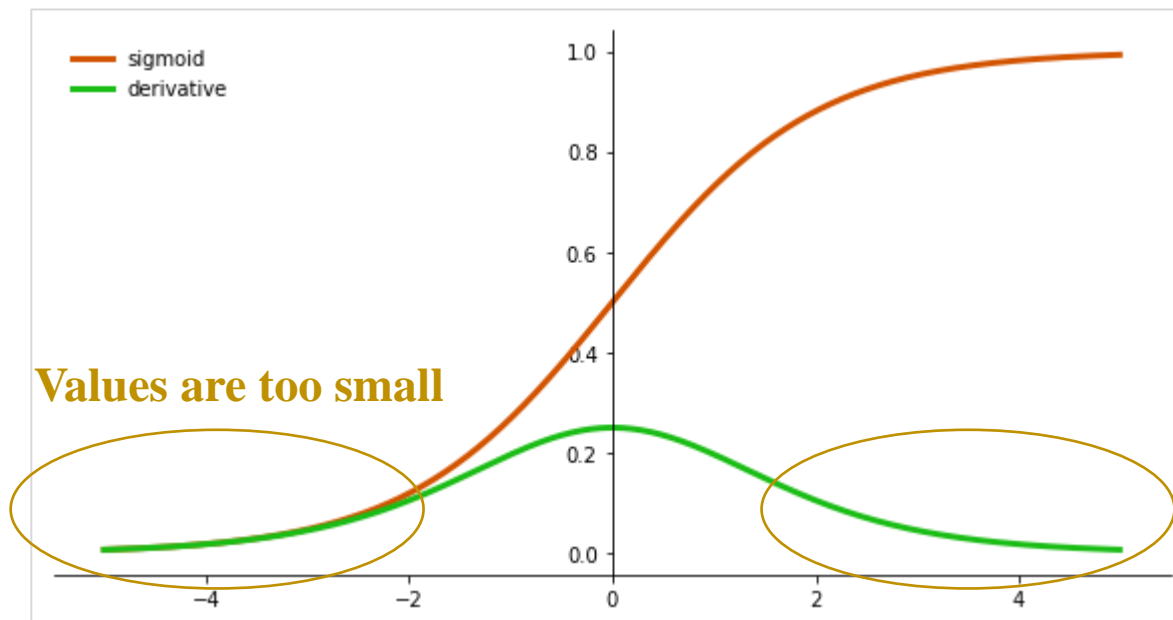
## ❖ Cifar-10 dataset:

### ❖ Keep adding more layers



$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

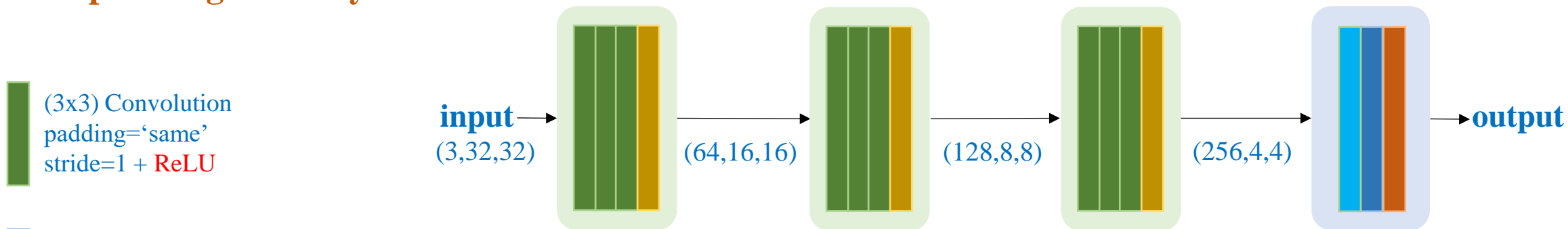
Vanishing Problem



# Network Training

## ❖ Cifar-10 dataset:

### ❖ Keep adding more layers

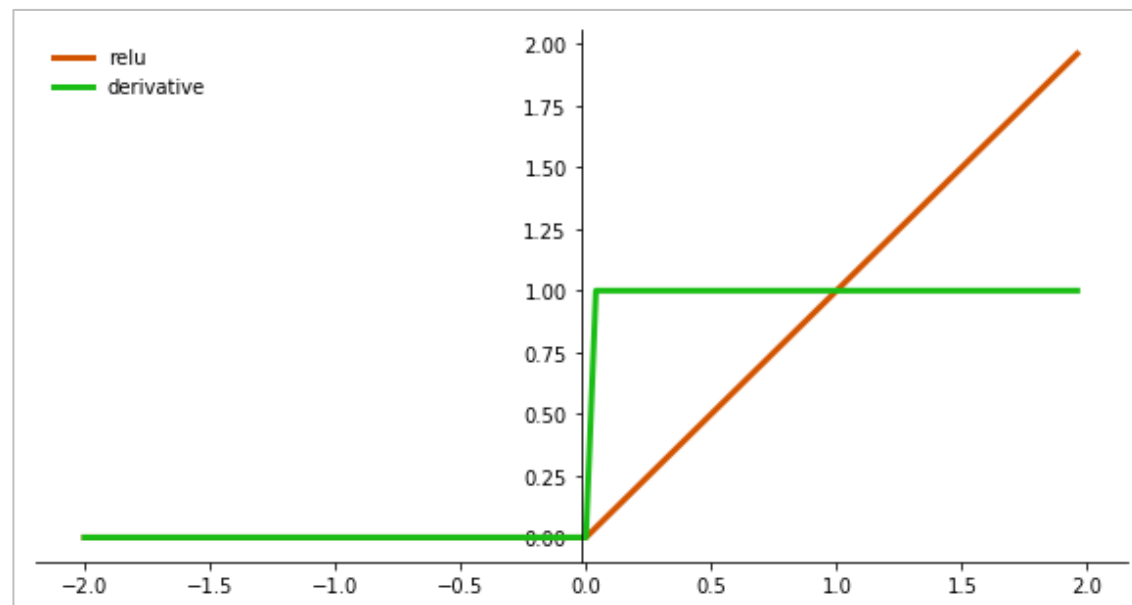


$$\text{ReLU}(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

```
nn.Conv2D(...), nn.Sigmoid()
```



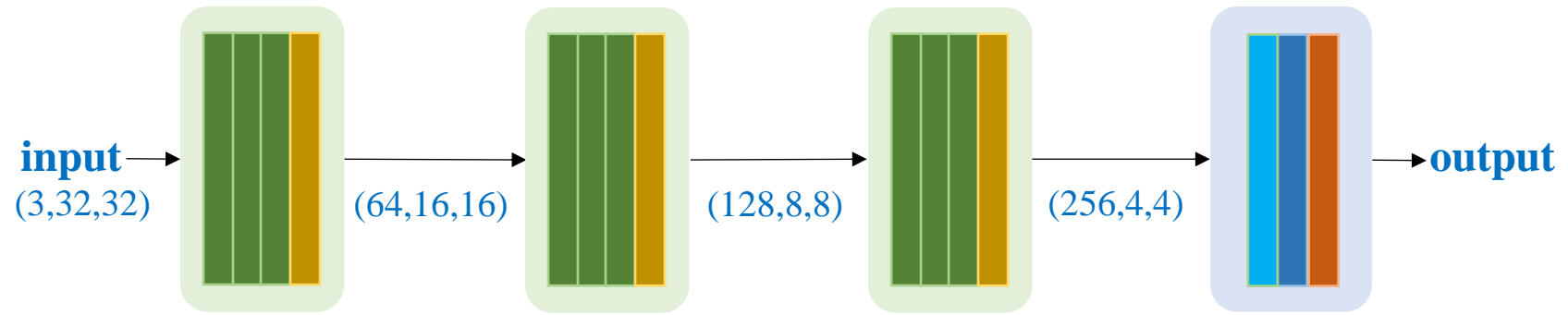
```
nn.Conv2D(...), nn.ReLU()
```



# Network Training

❖ **Cifar-10 dataset:**

❖ **Use ReLU**



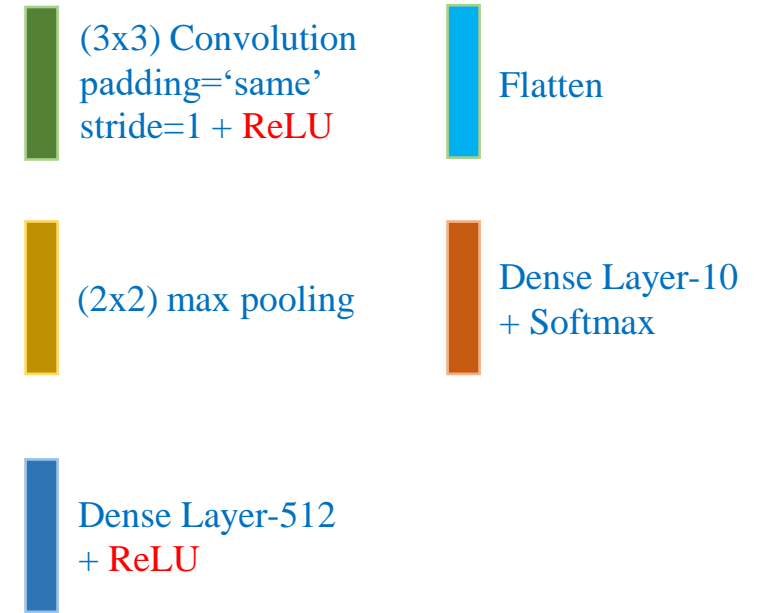
```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))

conv_layer4 = nn.Sequential(nn.Conv2d(64, 128, 3, stride=1, padding='same'), nn.ReLU())
conv_layer5 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU())
conv_layer6 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))

conv_layer7 = nn.Sequential(nn.Conv2d(128, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer8 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer9 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))

flatten = nn.Flatten()

fc_layer1 = nn.Sequential(nn.Linear(256*4*4, 512), nn.ReLU())
fc_layer2 = nn.Linear(512, 10)
```



Data normalization [0,1]

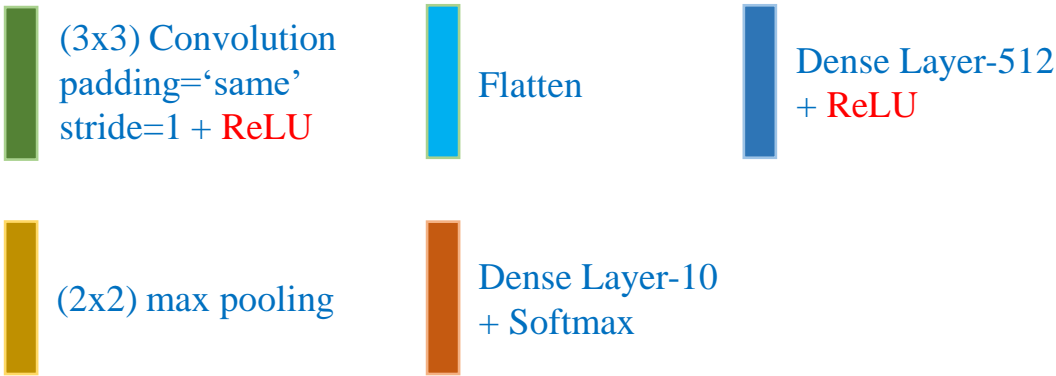
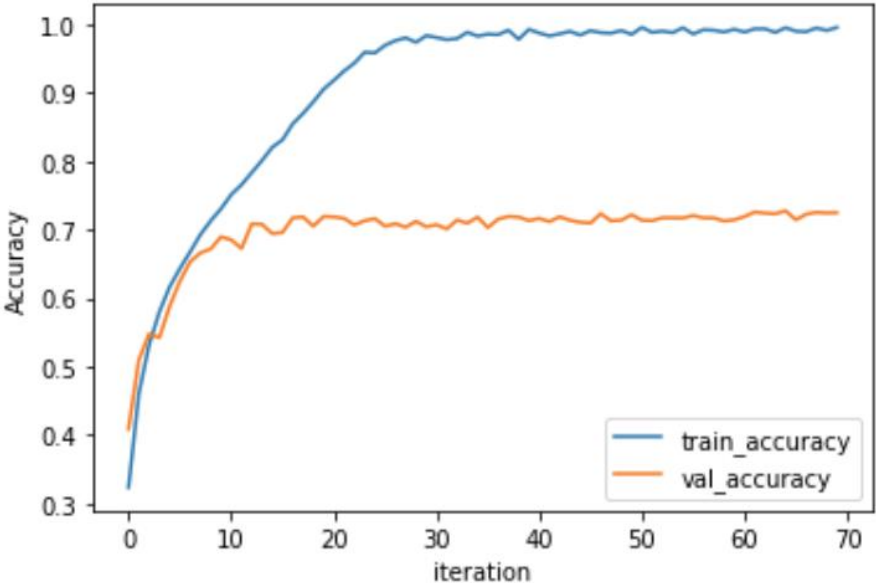
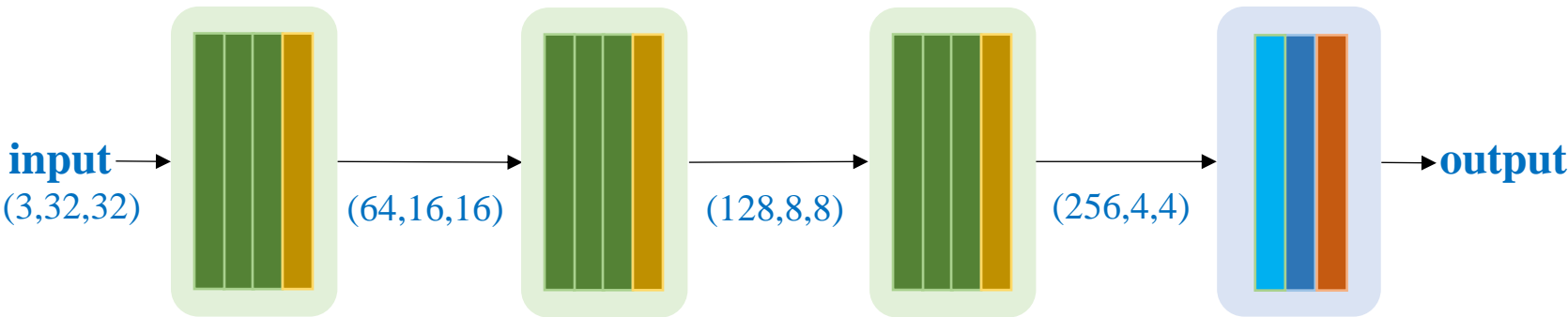
Glorot uniform initialization

Adam optimizer with lr=1e-3

# Network Training

- ❖ **Cifar-10 dataset:**
  - ❖ Use ReLU

Training Accuracy reaches up to 99%

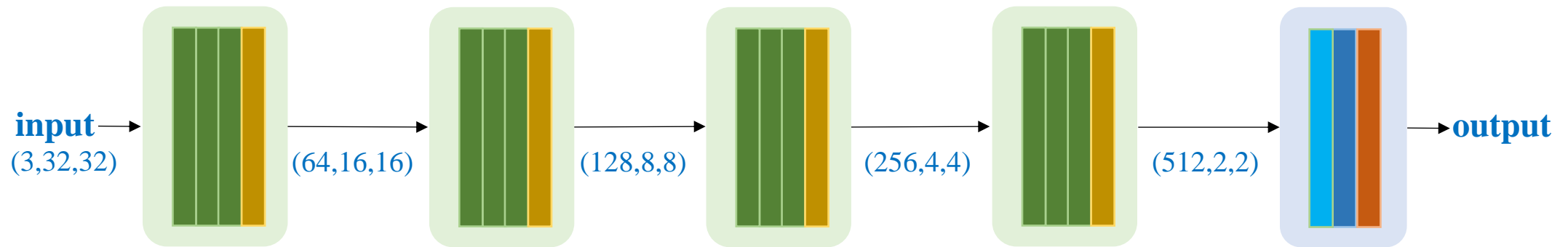


Adding more layers; Hope reach to 100%



# Network Training

## ❖ Use ReLU and add more layers



Data normalization [0,1]

Glorot uniform initialization

Adam optimizer with lr=1e-3

(3x3) Convolution  
padding='same'  
stride=1 + ReLU

(2x2) max pooling

Flatten

Dense Layer-10  
+ Softmax

Dense Layer-512  
+ ReLU

# Implementation

```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))

conv_layer4 = nn.Sequential(nn.Conv2d(64, 128, 3, stride=1, padding='same'), nn.ReLU())
conv_layer5 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU(),)
conv_layer6 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))

conv_layer7 = nn.Sequential(nn.Conv2d(128, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer8 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer9 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))

conv_layer10 = nn.Sequential(nn.Conv2d(256, 512, 3, stride=1, padding='same'), nn.ReLU())
conv_layer11 = nn.Sequential(nn.Conv2d(512, 512, 3, stride=1, padding='same'), nn.ReLU())
conv_layer12 = nn.Sequential(nn.Conv2d(512, 512, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))

flatten = nn.Flatten()

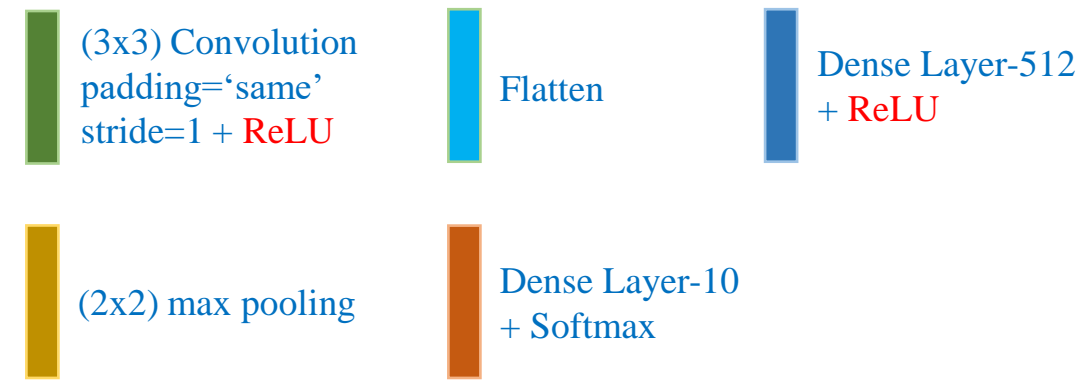
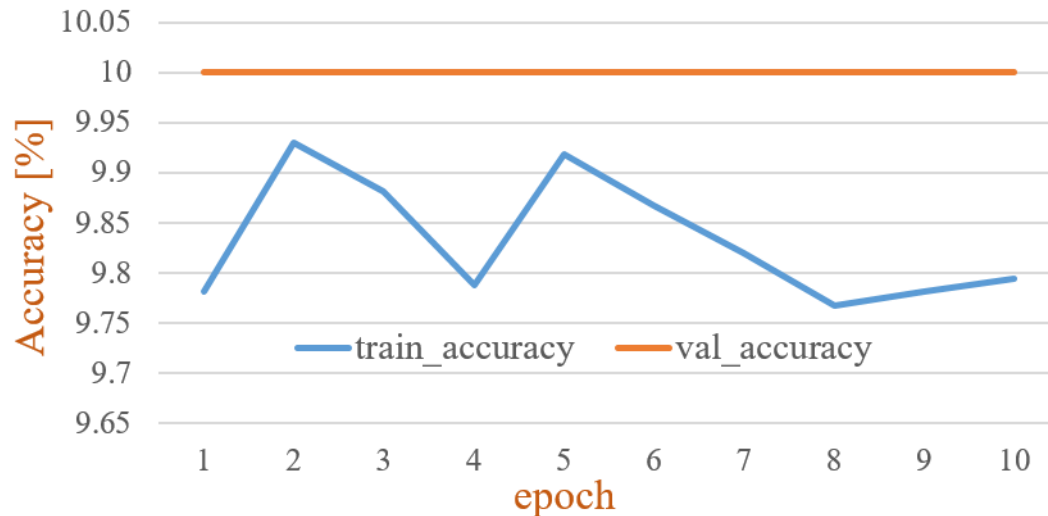
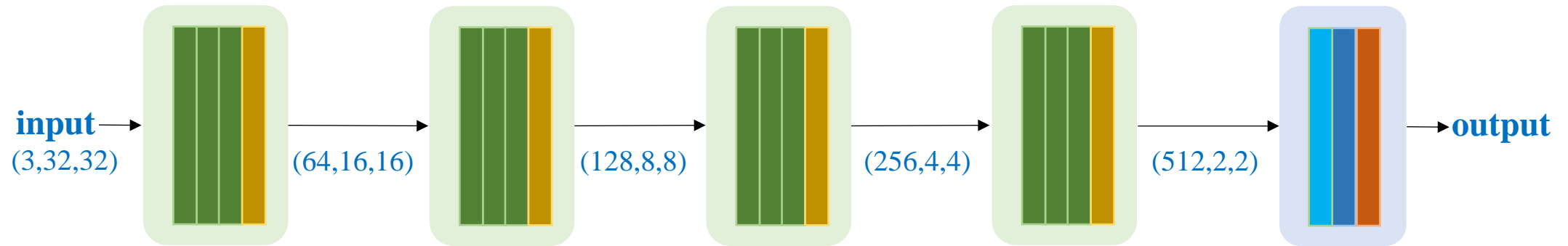
fc_layer1 = nn.Sequential(nn.Linear(512 * 2 * 2, 512), nn.ReLU())
fc_layer2 = nn.Linear(512, 10)
```

```
def initialize_weights(self):
    for m in self.modules():
        if isinstance(m, nn.Conv2d):
            init.xavier_uniform_(m.weight)
            if m.bias is not None:
                init.zeros_(m.bias)
        elif isinstance(m, nn.Linear):
            init.xavier_uniform_(m.weight)
            if m.bias is not None:
                init.zeros_(m.bias)

def forward(self, x):
    x = self.conv_layer1(x)
    x = self.conv_layer2(x)
    x = self.conv_layer3(x)
    x = self.conv_layer4(x)
    x = self.conv_layer5(x)
    x = self.conv_layer6(x)
    x = self.conv_layer7(x)
    x = self.conv_layer8(x)
    x = self.conv_layer9(x)
    x = self.conv_layer10(x)
    x = self.conv_layer11(x)
    x = self.conv_layer12(x)
    x = self.flatten(x)
    x = self.fc_layer1(x)
    out = self.fc_layer2(x)
    return out
```

# Network Training

## ❖ Use ReLU and add more layers

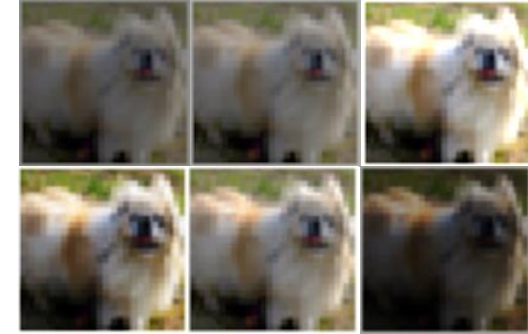
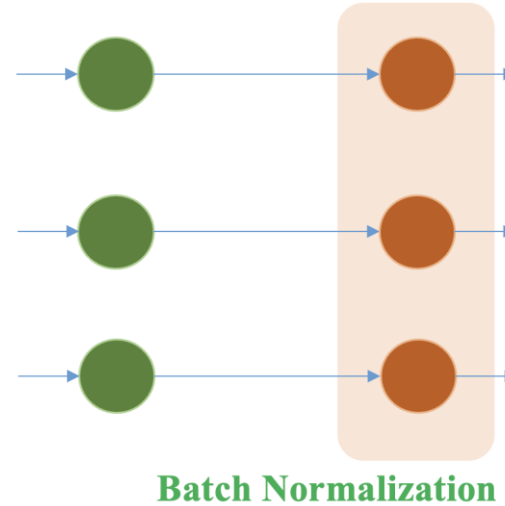


Network does not learn again

# Outline

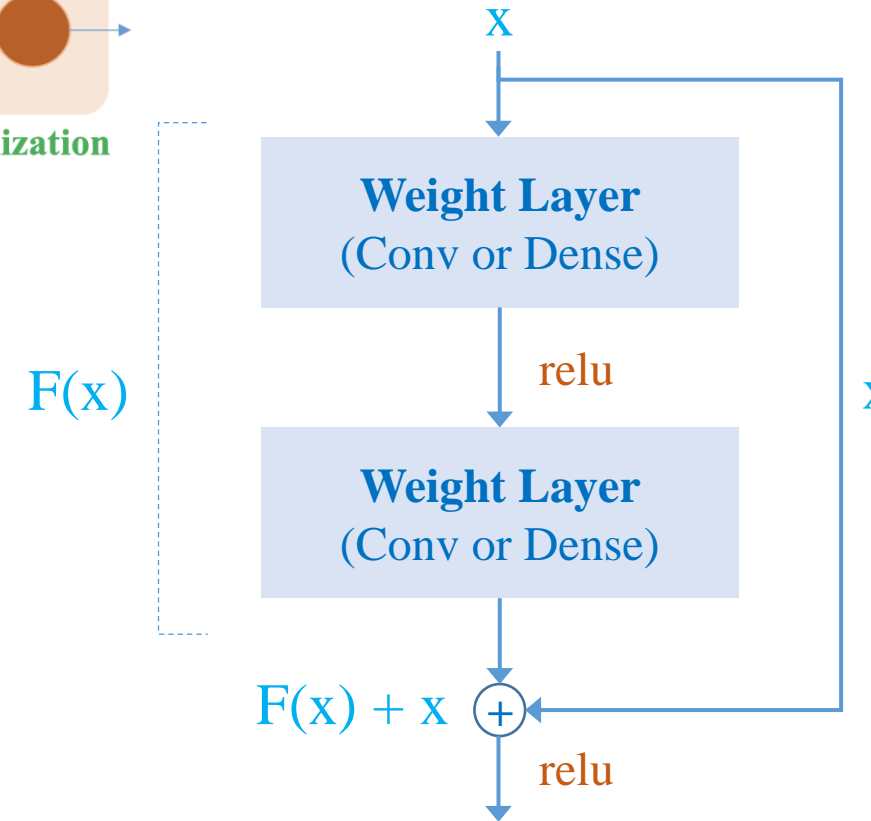
## SECTION 1

### Setting-up Context



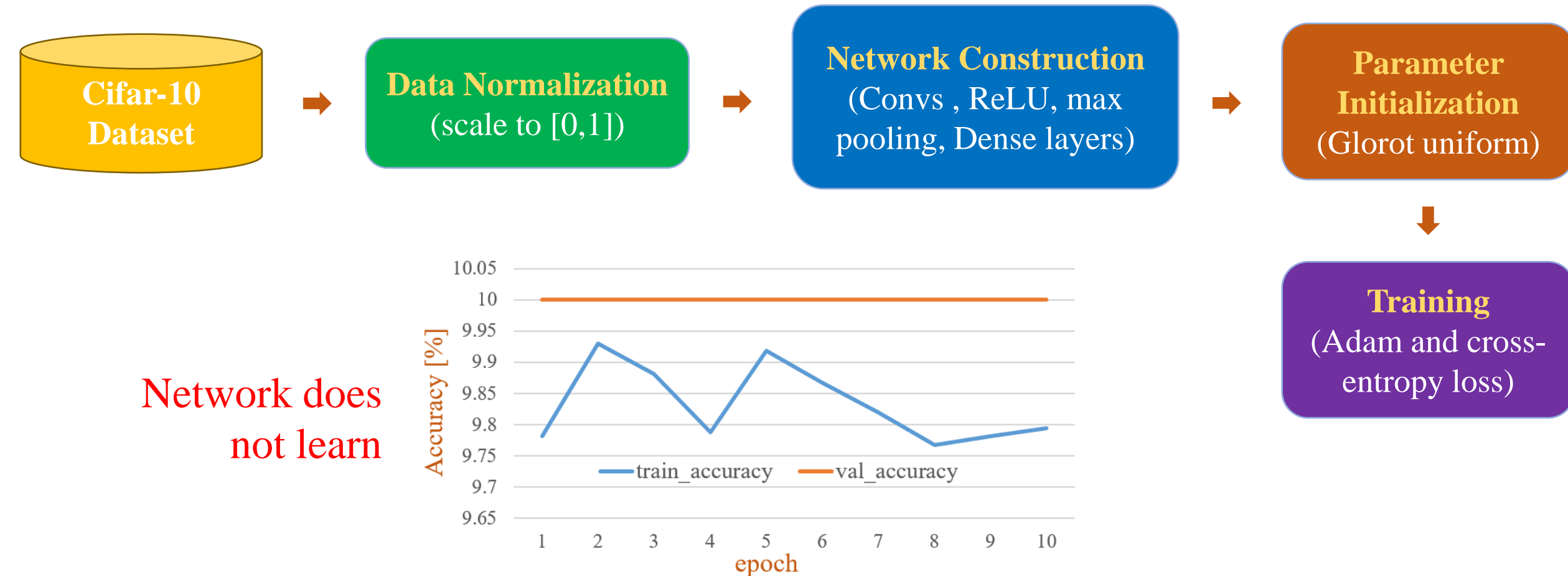
## SECTION 2

### Solutions for the Context

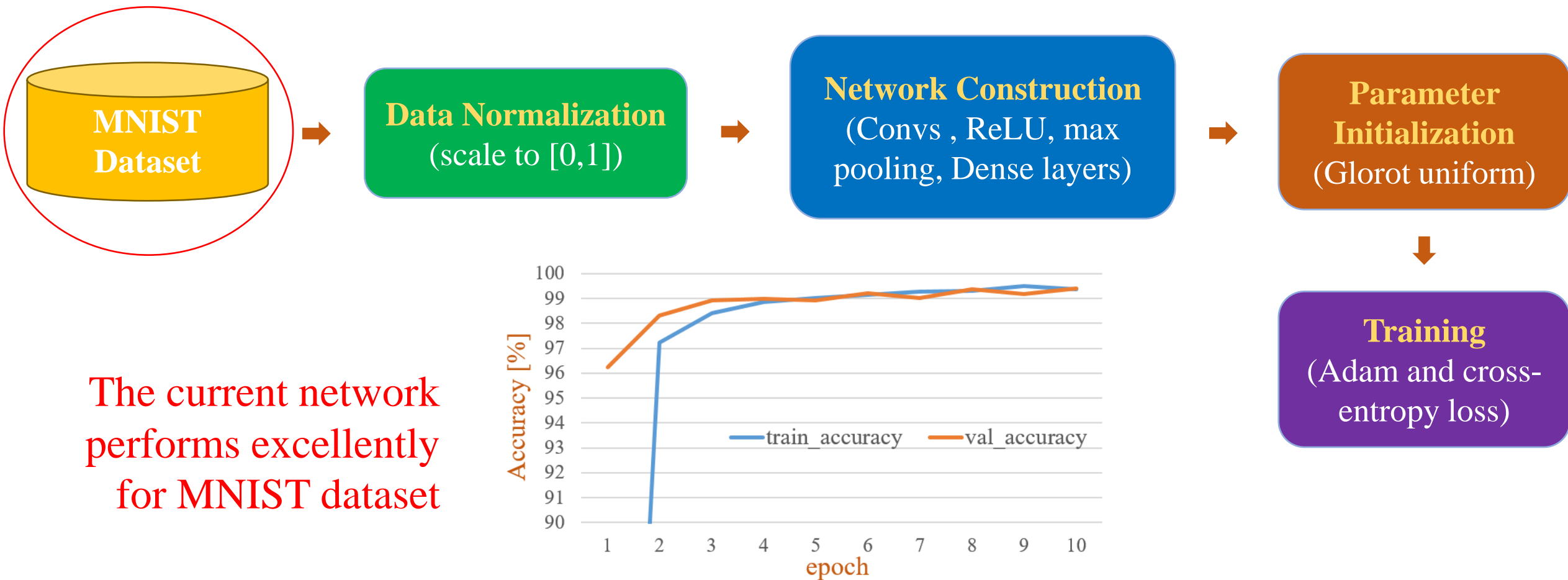


# Network Training

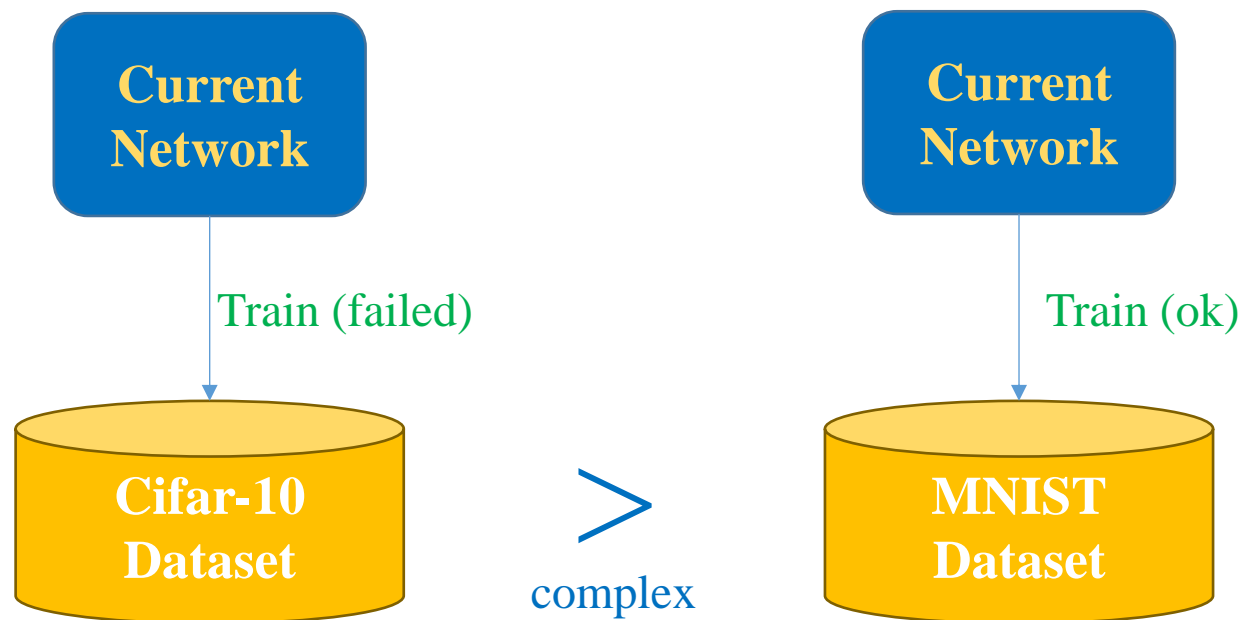
## ❖ Summary of the current network



## ❖ Solution 1: Observation

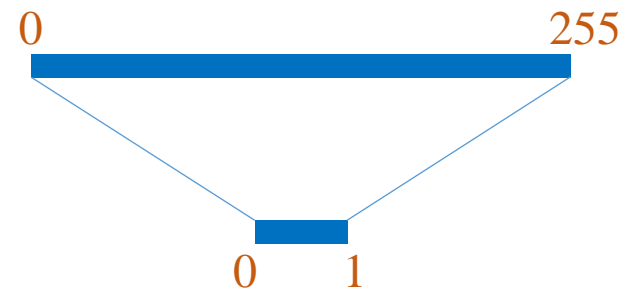


## ❖ Solution 1: Idea



How to reduce the complexity of the Cifar-10 dataset

**Data Normalization**  
(scale to [0,1])



**Data Normalization**  
(convert to 0-mean and 1-deviation)

$X =$



$$X = \frac{X - \mu}{\sigma}$$

$$\mu = \frac{1}{n} \sum_i X_i$$

$$\sigma = \sqrt{\frac{1}{n} \sum_i (X_i - \mu)^2}$$

## ❖ Solution 1: Idea

$$\bar{X} = \frac{X - \mu}{\sigma}$$

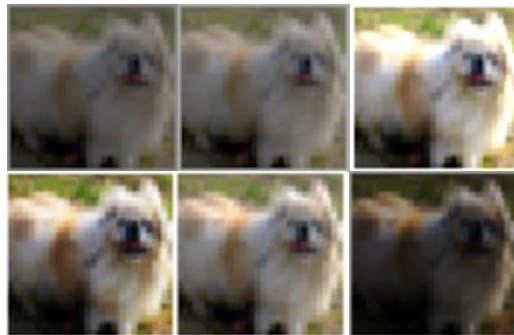
$$\mu = \frac{1}{n} \sum_i X_i$$

$$\sigma = \sqrt{\frac{1}{n} \sum_i (X_i - \mu)^2}$$

This normalization helps network to be invariant to linear transformation

$$Y = aX + b$$

$$\bar{Y} = \frac{Y - \mu_Y}{\sigma_Y} = \bar{X}$$



$$Y = aX + b$$

$$\begin{aligned} \bar{Y} &= \frac{Y - \mu_Y}{\sigma_Y} = \frac{(aX + b) - \frac{1}{n} \sum_i (aX_i + b)}{\sqrt{\frac{1}{n} \sum_i \left( (aX_i + b) - \frac{1}{n} \sum_j (aX_j + b) \right)^2}} \\ &= \frac{aX - \frac{1}{n} \sum_i aX_i}{\sqrt{\frac{1}{n} \sum_i \left( aX_i - \frac{1}{n} \sum_j aX_j \right)^2}} \\ &= \frac{X - \frac{1}{n} \sum_i X_i}{\sqrt{\frac{1}{n} \sum_i \left( X_i - \frac{1}{n} \sum_j X_j \right)^2}} = \frac{X - \mu_X}{\sqrt{\frac{1}{n} \sum_i (X_i - \mu_X)^2}} = \bar{X} \end{aligned}$$



# Network Training

## Solution 1: 0-mean and unit-deviation normalization

**Data Normalization**  
(convert to 0-mean  
and 1-deviation)

$$X = \frac{X - \mu_d}{\sigma_d}$$

$\mu_d$  is the mean of dataset

$\sigma_d$  is the deviation for the whole dataset

```
# Load dataset with only the ToTensor transform
compute_transform = transforms.Compose([transforms.ToTensor()])
dataset = torchvision.datasets.CIFAR10(root='data', train=True,
                                       transform=compute_transform,
                                       download=True)

loader = torch.utils.data.DataLoader(dataset, batch_size=1024,
                                       shuffle=False, num_workers=4)

mean = 0.0
for images, _ in loader:
    batch_samples = images.size(0) # Batch size
    images = images.view(batch_samples, images.size(1), -1)
    mean += images.mean(2).sum(0)
mean = mean / len(loader.dataset)

variance = 0.0
for images, _ in loader:
    batch_samples = images.size(0)
    images = images.view(batch_samples, images.size(1), -1)
    variance += ((images - mean.unsqueeze(1))**2).sum([0,2])
std = torch.sqrt(variance / (len(loader.dataset)*32*32))

# Data
transform = Compose([ToTensor(),
                     Normalize(mean, std)])
train_set = CIFAR10(root='data', train=True,
                    download=True, transform=transform)
trainloader = DataLoader(train_set, batch_size=256,
                         shuffle=True, num_workers=4)
```

## ❖ Solution 1: 0-mean and unit-deviation normalization

**Data Normalization**  
(convert to 0-mean  
and 1-deviation)

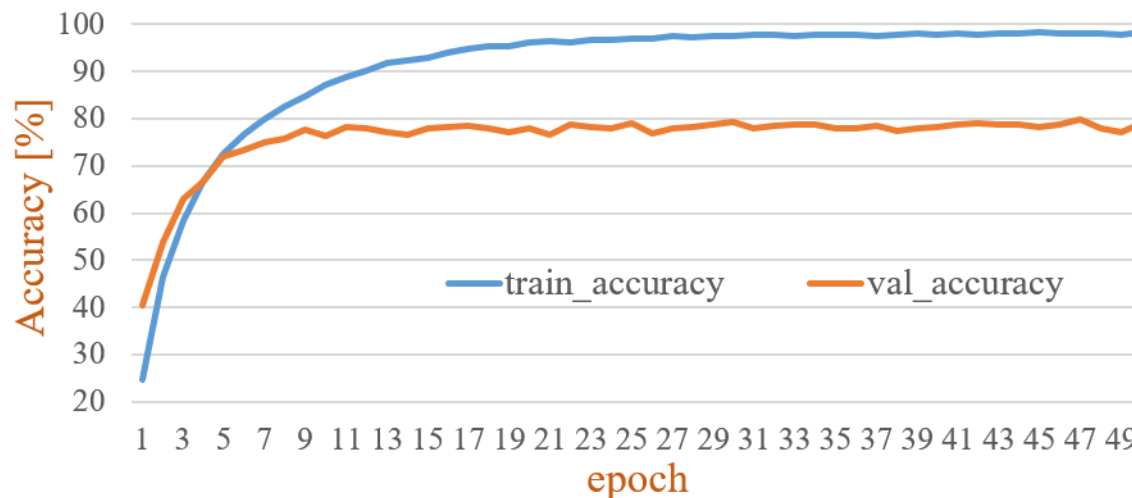
$$X = \frac{X - \mu_d}{\sigma_d}$$

$\mu_d$  is the mean of dataset

$\sigma_d$  is the deviation for the whole dataset

Normalize each channel separately

```
transform = Compose([ToTensor(),  
                      Normalize([0.4914, 0.4822, 0.4465],  
                                [0.2470, 0.2435, 0.2616])])  
train_set = CIFAR10(root='data', train=True,  
                    download=True, transform=transform)
```

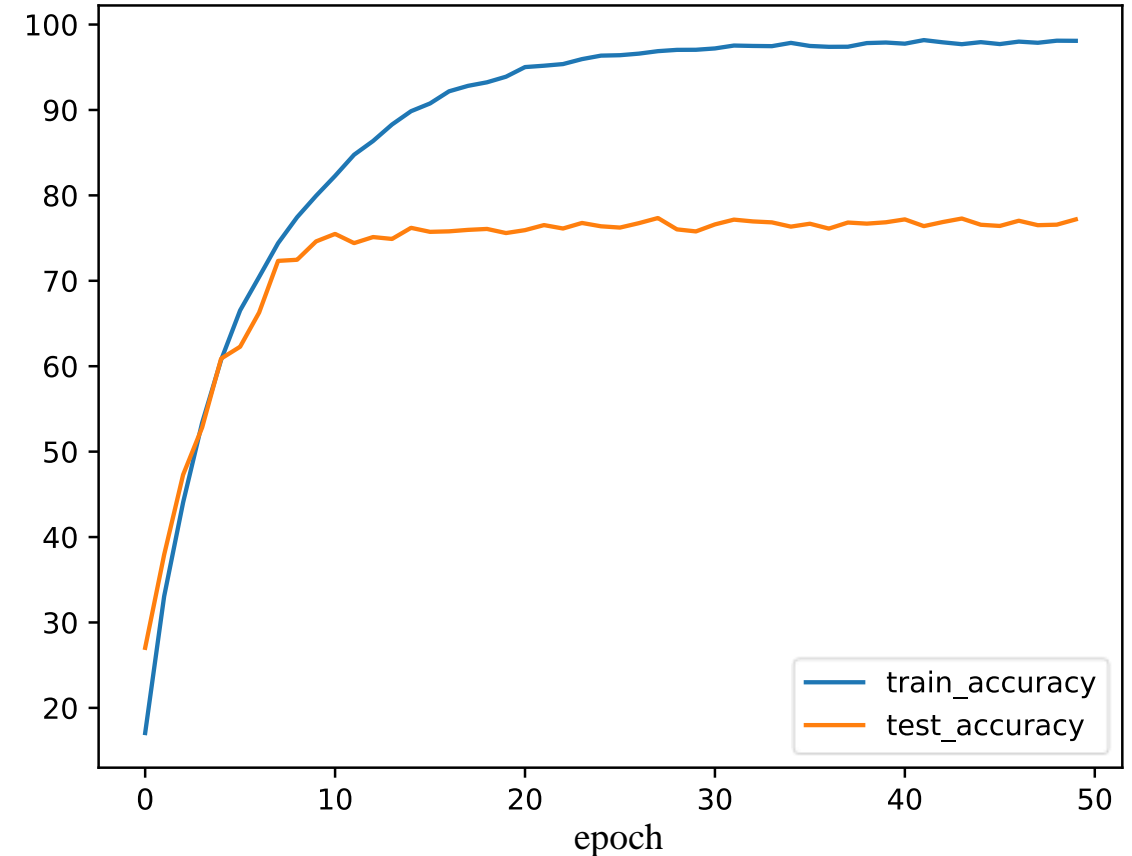
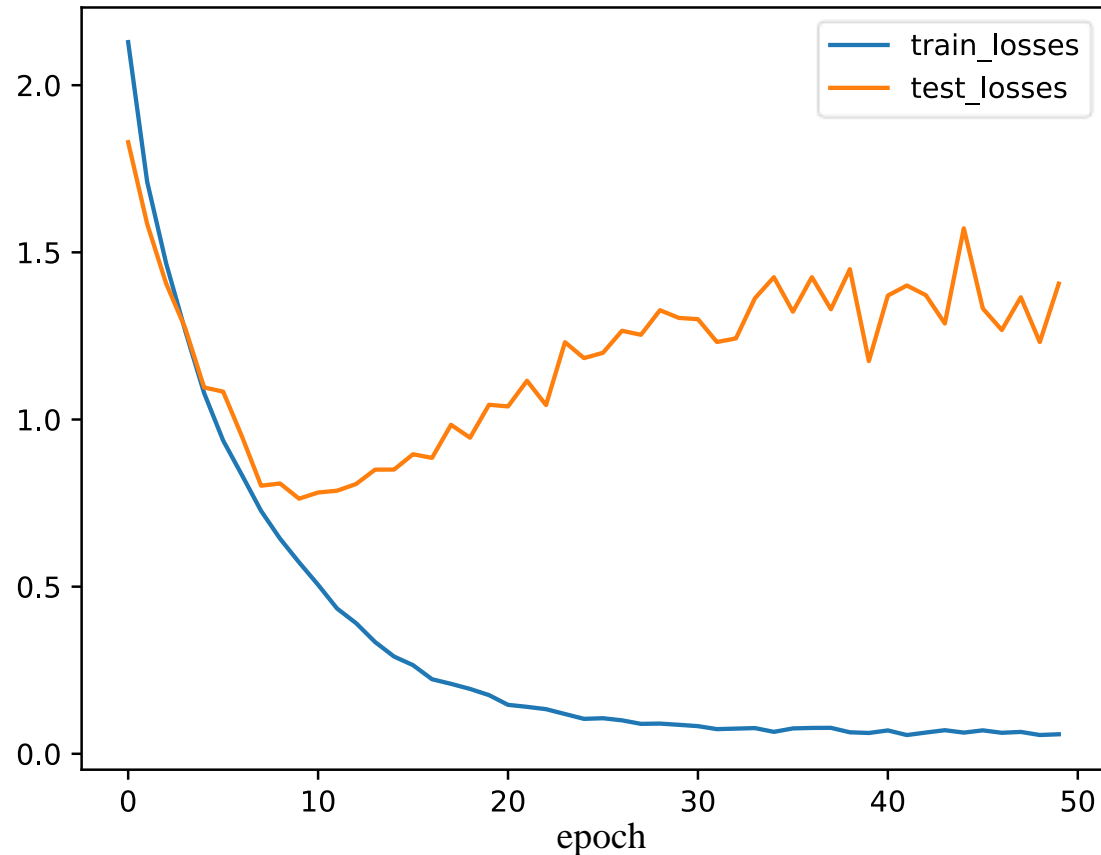


# Network Training

## ❖ Solution 1 (extension): Normalize to [-1, 1]

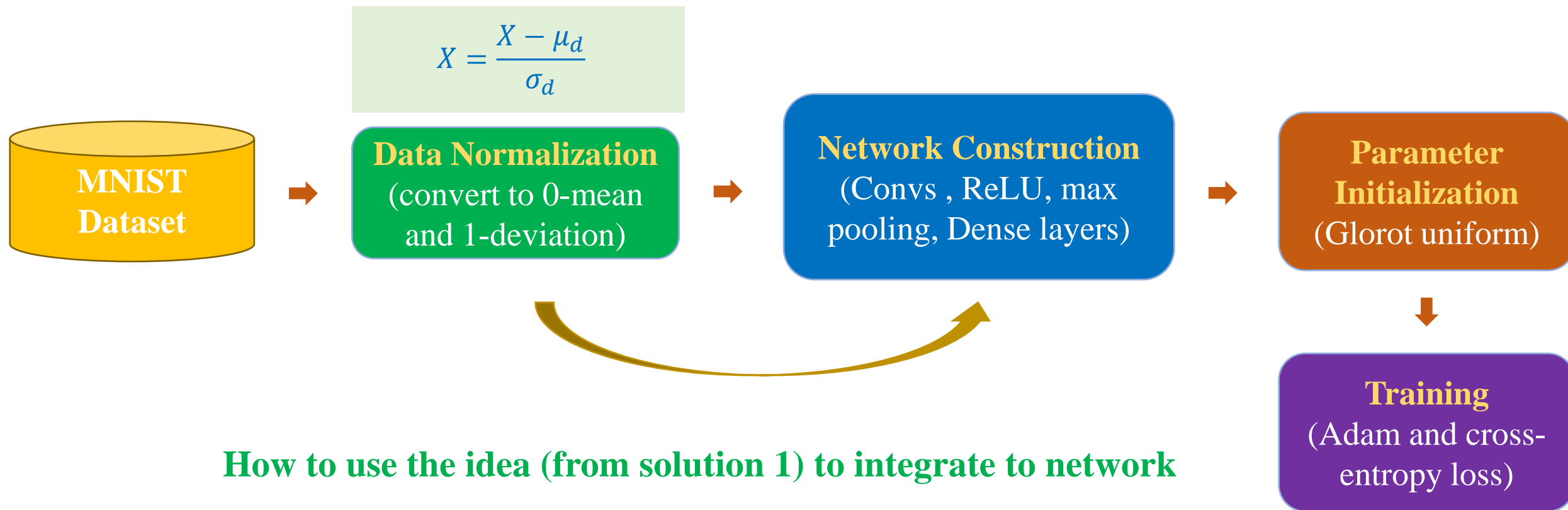
Normalize each channel separately

```
transform = Compose([ToTensor(),  
                     Normalize((0.5, 0.5, 0.5),  
                               (0.5, 0.5, 0.5))])  
train_set = CIFAR10(root='data', train=True,  
                    download=True, transform=transform)
```



# Network Training

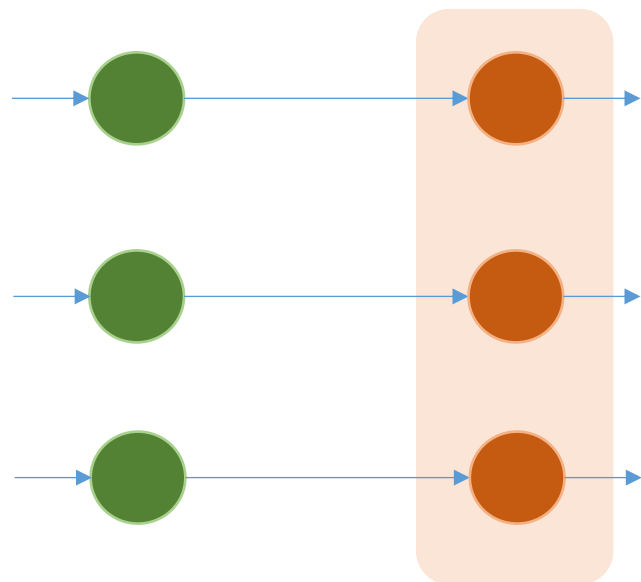
## ❖ Solution 2



How to use the idea (from solution 1) to integrate to network

**Batch Normalization**

## ❖ Solution 2: Batch normalization



Batch Normalization

Do not need bias when using BN\*

$\mu$  and  $\sigma$  are updated in forward pass  
 $\gamma$  and  $\beta$  are updated in backward pass

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

$m$  is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize  $X_i$

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

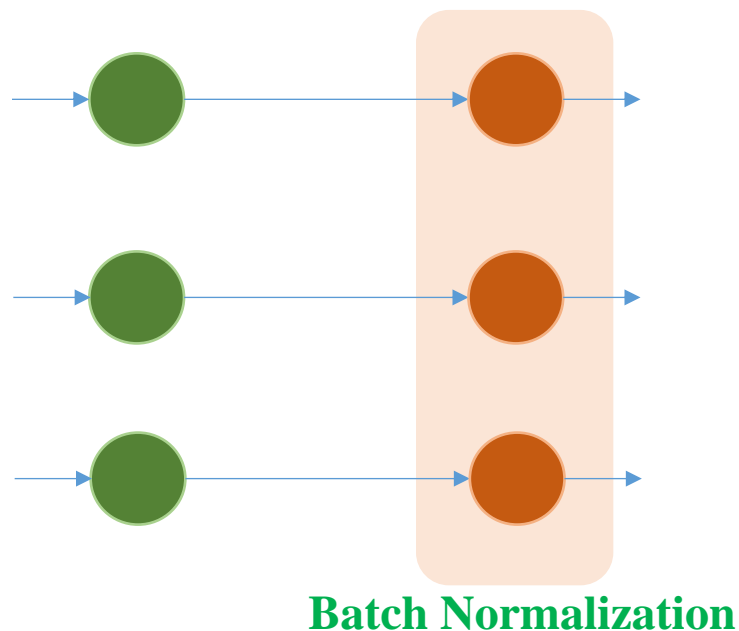
$\epsilon$  is a very small value

Scale and shift  $\hat{X}_i$

$$Y_i = \gamma \hat{X}_i + \beta$$

$\gamma$  and  $\beta$  are two learning parameters

## ❖ Solution 2: Batch normalization



What if

$$\gamma = \sqrt{\sigma^2 + \epsilon} \text{ and } \beta = \mu$$

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

$m$  is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize  $X_i$

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

$\epsilon$  is a very small value

Scale and shift  $\hat{X}_i$

$$Y_i = \gamma \hat{X}_i + \beta$$

$\gamma$  and  $\beta$  are two learning parameters

\_\_\_\_\_

Diagram illustrating the relationship between parameters and the covariance matrix  $\hat{U}$ :

- Parameters (left):
  - $\epsilon = 10^{-5}$
  - $\mu_U = 5.0$
  - $\sigma_U = 2.64$
  - $\gamma_U = 1.0$
  - $\beta_U = 0.0$
- Covariance Matrix  $\hat{U}$  (right):
 
$$\hat{U} = \begin{bmatrix} -1.51 & -0.75 & 1.51 & -0.37 & 0.37 & 0.75 \end{bmatrix}$$

$$\hat{U} = \begin{bmatrix} 1.51 \\ -0.37 \\ 0.37 \\ 0.75 \end{bmatrix}$$

$$Y_U = \begin{bmatrix} -1.51 \\ -0.75 \\ 1.51 \\ -0.37 \\ 0.37 \\ 0.75 \end{bmatrix}$$

$$Y_V = \begin{bmatrix} 0.61 \\ -0.61 \\ 1.22 \\ 0.0 \\ 0.61 \\ -1.83 \end{bmatrix}$$

$$\hat{V} = \begin{bmatrix} 0.61 \\ -0.61 \\ 1.22 \\ 0.0 \\ 0.61 \\ -1.83 \end{bmatrix}$$

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

$m$  is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize  $X_i$

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

$\epsilon$  is a very small value

Scale and shift  $\hat{X}_i$

$$Y_i = \gamma \hat{X}_i + \beta$$

$\gamma$  and  $\beta$  are two learning parameters

$$X = \{X_1, \dots, X_m\}$$

## Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

## Normalize $X_i$

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

$\epsilon$  is a very small value

## Scale and shift $\hat{X}_i$

$$Y_i = \gamma \hat{X}_i + \beta$$

$\gamma$  and  $\beta$  are two learning parameters

$\gamma$  and  $\beta$  are updated in training process

# Batch Normalization

$$\epsilon = 10^{-5}$$

$$\mu_c = \frac{1}{N \times H \times W} \sum_{i=1}^N \sum_{j=1}^H \sum_{k=1}^W F_{ijk}$$

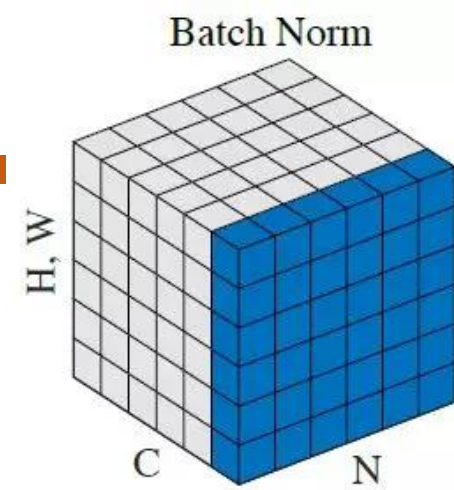
$$\sigma_c = \sqrt{\frac{1}{N \times H \times W} \sum_{i=1}^N \sum_{j=1}^H \sum_{k=1}^W (F_{ijk} - \mu_c)^2}$$

$$\mu = 2.5$$

$$\sigma^2 = 6.58$$

$$\gamma = 1.0$$

$$\beta = 0.0$$



<https://arxiv.org/pdf/1803.08494.pdf>

sample 1   sample 2   sample 3

$$X = \left\{ \begin{bmatrix} 7 & 5 \\ 0 & 4 \end{bmatrix}, \begin{bmatrix} 0 & 7 \\ 3 & 1 \end{bmatrix}, \begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \right\}$$



batch-size = 3

input\_shape = (BS=3, C=1, H=2, W=2)



$$\hat{X} = \left\{ \begin{bmatrix} 1.75 & 0.97 \\ -0.97 & 0.58 \end{bmatrix}, \begin{bmatrix} -0.97 & 1.75 \\ 0.19 & -0.58 \end{bmatrix}, \begin{bmatrix} -0.19 & -0.97 \\ -0.97 & -0.58 \end{bmatrix} \right\}$$



$$\hat{Y} = \left\{ \begin{bmatrix} 1.75 & 0.97 \\ -0.97 & 0.58 \end{bmatrix}, \begin{bmatrix} -0.97 & 1.75 \\ 0.19 & -0.58 \end{bmatrix}, \begin{bmatrix} -0.19 & -0.97 \\ -0.97 & -0.58 \end{bmatrix} \right\}$$



# Network Training

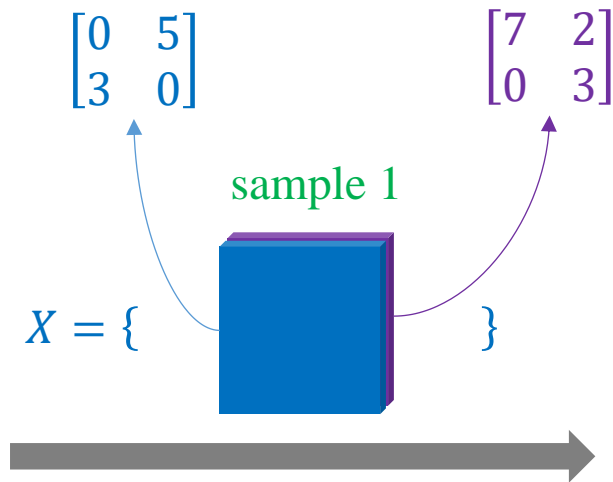
$$\epsilon = 10^{-5}$$

$$\mu = [2.0, 3.0]$$

$$\sigma^2 = [6.0, 8.67]$$

$$\gamma = 1.0$$

$$\beta = 0.0$$



$$\hat{X} = \left\{ \begin{bmatrix} -0.94 & 1.41 \\ 0.47 & -0.94 \\ 1.56 & -0.39 \\ -1.17 & 0 \end{bmatrix} \right\}$$

$$\hat{Y} = \left\{ \begin{bmatrix} -0.94 & 1.41 \\ 0.47 & -0.94 \\ 1.56 & -0.39 \\ -1.17 & 0 \end{bmatrix} \right\}$$

batch-size = 1

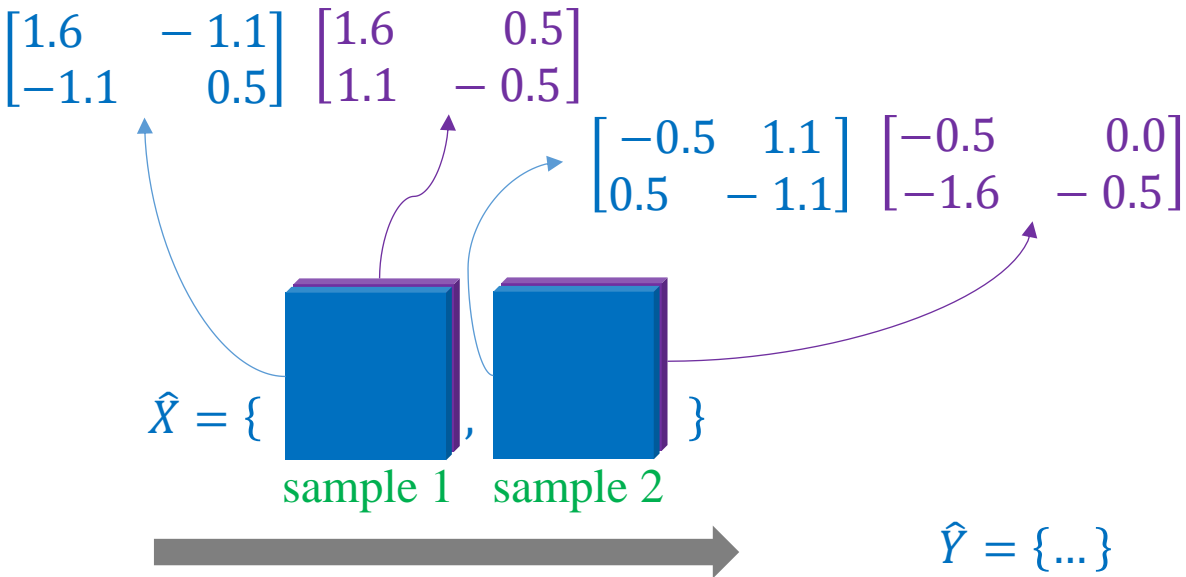
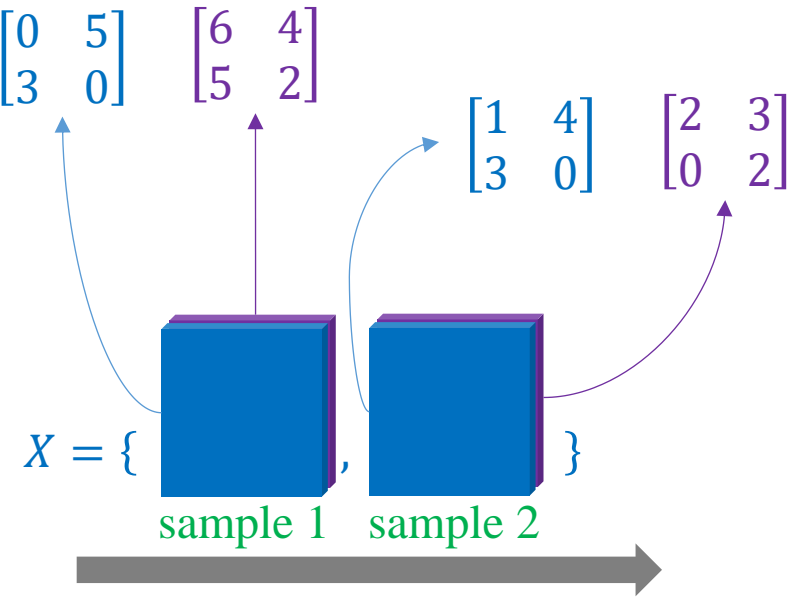
sample\_shape = (BS=1, C=2, H=2, W=2)

# Network Training

$\epsilon = 10^{-5}$

$\mu = [2.0, 3.0]$   
 $\sigma^2 = [4.0, 3.7]$

$\gamma = 1.0$   
 $\beta = 0.0$

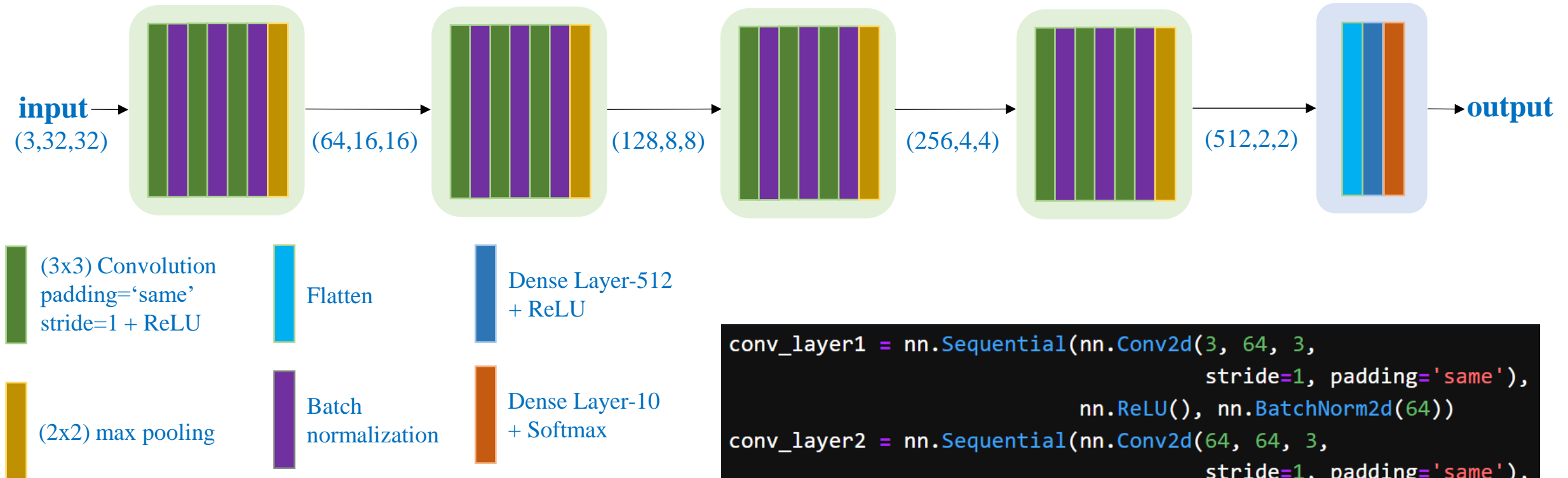


batch-size = 2  
 sample\_shape = (BS=2 , C=2, H=2, W=2)

Batch-Norm Layer

# Network Training

## ❖ Solution 2: Batch normalization

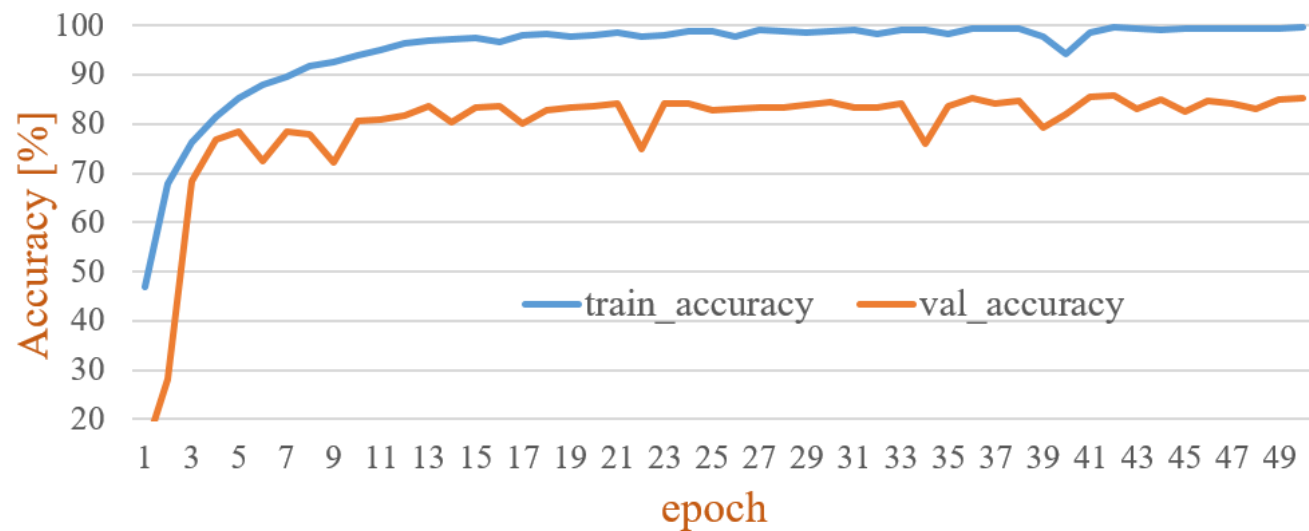
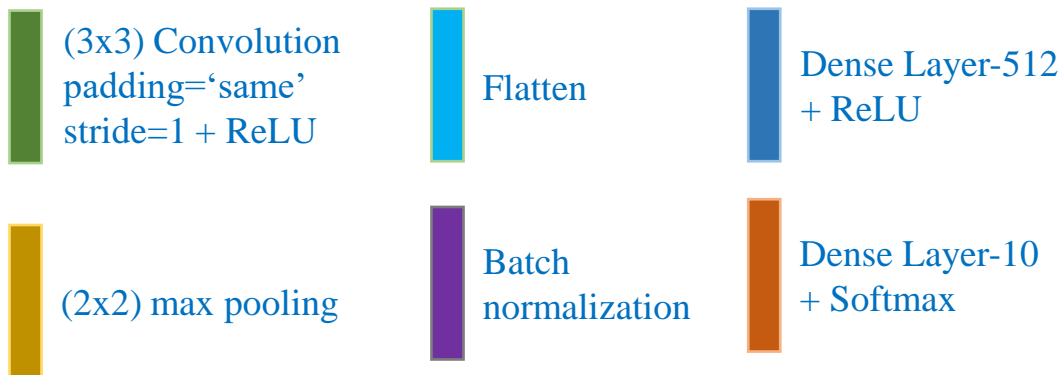
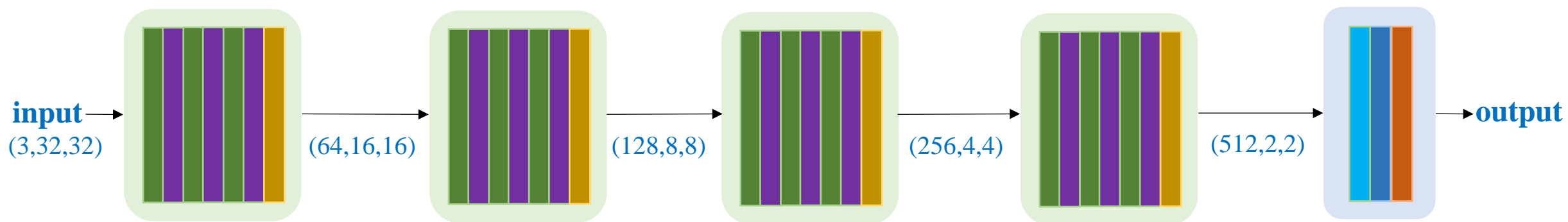


`torch.nn.BatchNorm2d(num_features)`  
`num_features (int): C from an expected input of size (N, C, H, W)`

```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3,
                                      stride=1, padding='same'),
                             nn.ReLU(), nn.BatchNorm2d(64))
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3,
                                      stride=1, padding='same'),
                             nn.ReLU(), nn.BatchNorm2d(64))
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3,
                                      stride=1, padding='same'),
                             nn.ReLU(), nn.BatchNorm2d(64),
                             nn.MaxPool2d(2, 2))
```

# Network Training

## ❖ Solution 2: Batch normalization



```
conv = nn.Sequential(nn.Conv2d(3, 64, 3),
                     nn.ReLU(),
                     nn.BatchNorm2d(64))
```

## ❖ Solution 2: Batch normalization

Speed up training

Reduce the dependence on initial weights

Model Generalization

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

$m$  is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize  $X_i$

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

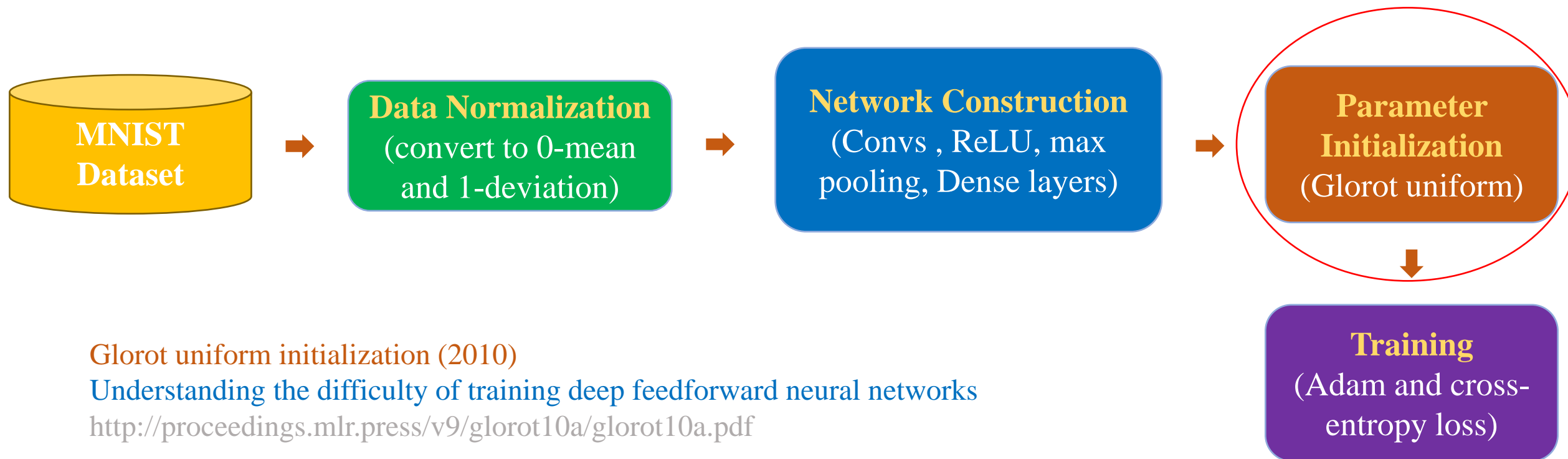
$\epsilon$  is a very small value

Scale and shift  $\hat{X}_i$

$$Y_i = \gamma \hat{X}_i + \beta$$

$\gamma$  and  $\beta$  are two learning parameters

## ❖ Solution 3: Use more robust initialization



Glorot uniform initialization (2010)

Understanding the difficulty of training deep feedforward neural networks

<http://proceedings.mlr.press/v9/glorot10a/glorot10a.pdf>

He initialization (2015)

Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification

<https://arxiv.org/pdf/1502.01852.pdf>

## ❖ Solution 3: He Initialization

Glorot initialization (2010)

$$W \sim \mathcal{N}\left(0, \frac{1}{n_j}\right)$$

$n_j$  is #inputs in layer  $j$

Assuming activation functions are linear

He initialization (2015)

Taking activation function into account

Adapt to ReLU activation

$$W \sim \mathcal{N}\left(0, \frac{2}{n_j}\right)$$

```
def initialize_weights(self):  
    for m in self.modules():  
        if isinstance(m, nn.Conv2d):  
            init.kaiming_normal_(m.weight,  
                                nonlinearity='relu')  
            if m.bias is not None:  
                init.zeros_(m.bias)  
        elif isinstance(m, nn.Linear):  
            init.kaiming_normal_(m.weight,  
                                nonlinearity='relu')  
            if m.bias is not None:  
                init.zeros_(m.bias)
```

Data normalization [0,1]

He normal initialization

Adam optimizer with lr=1e-3

## ❖ Solution 3: He Initialization

Glorot initialization (2010)

$$W \sim \mathcal{N}\left(0, \frac{1}{n_j}\right)$$

$n_j$  is #inputs in layer  $j$

Assuming activation functions are linear

He initialization (2015)

Taking activation function into account

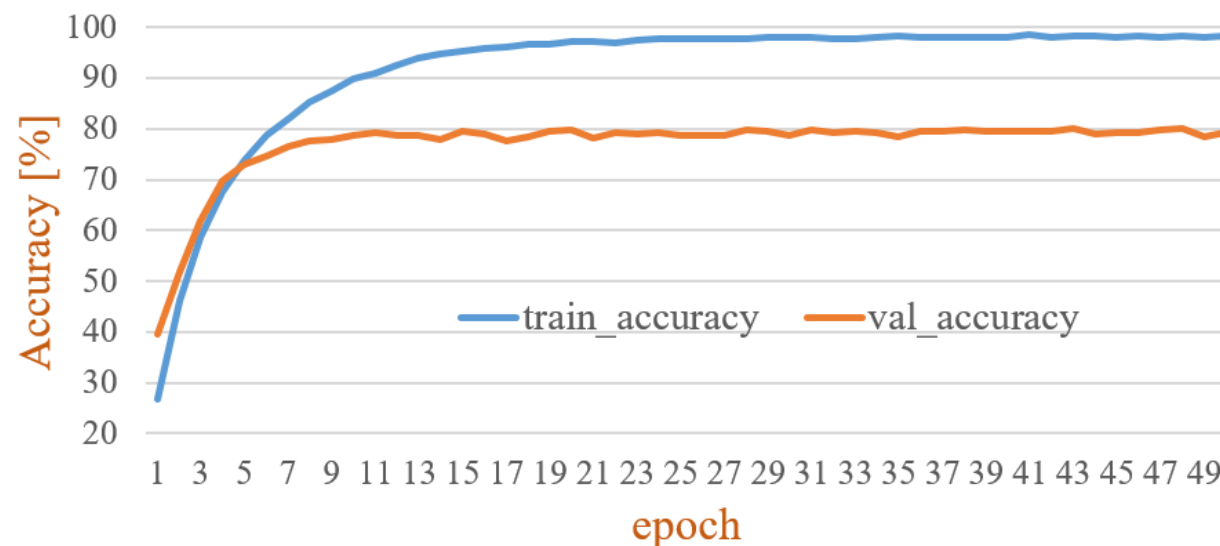
Adapt to ReLU activation

$$W \sim \mathcal{N}\left(0, \frac{2}{n_j}\right)$$

Data normalization [0,1]

He normal initialization

Adam optimizer with lr=1e-3

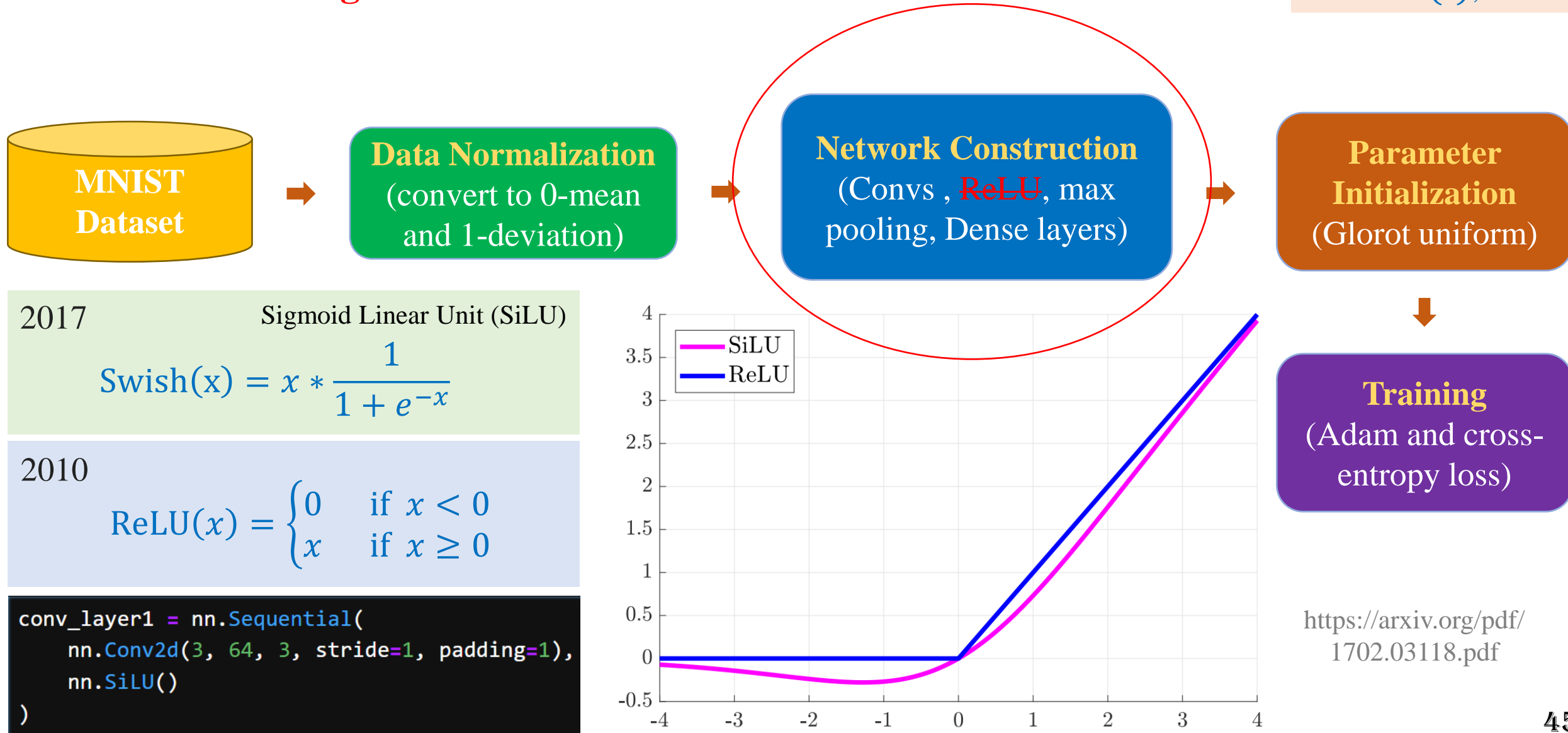




# Network Training

## ❖ Solution 4: Using advanced activation

SwiGLU(.), 2020



# Network Training

## ❖ Solution 4: Using advanced activation

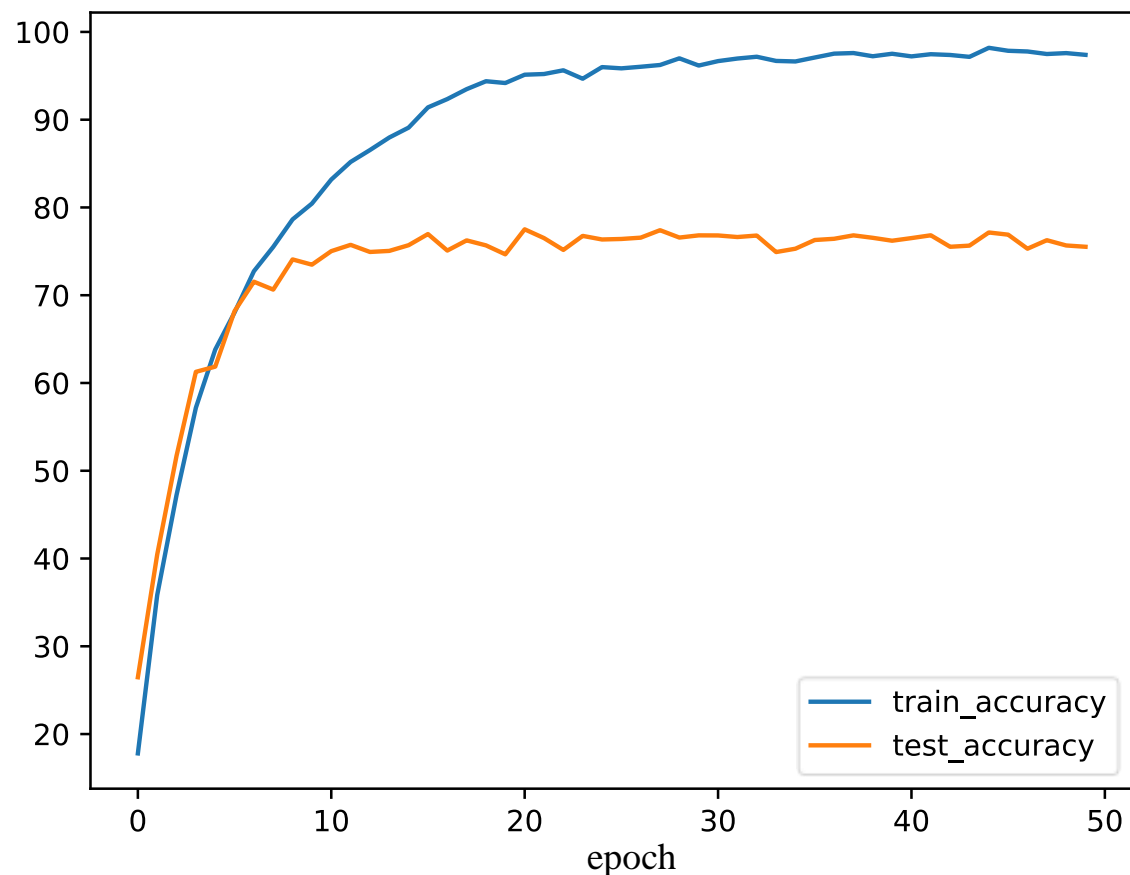
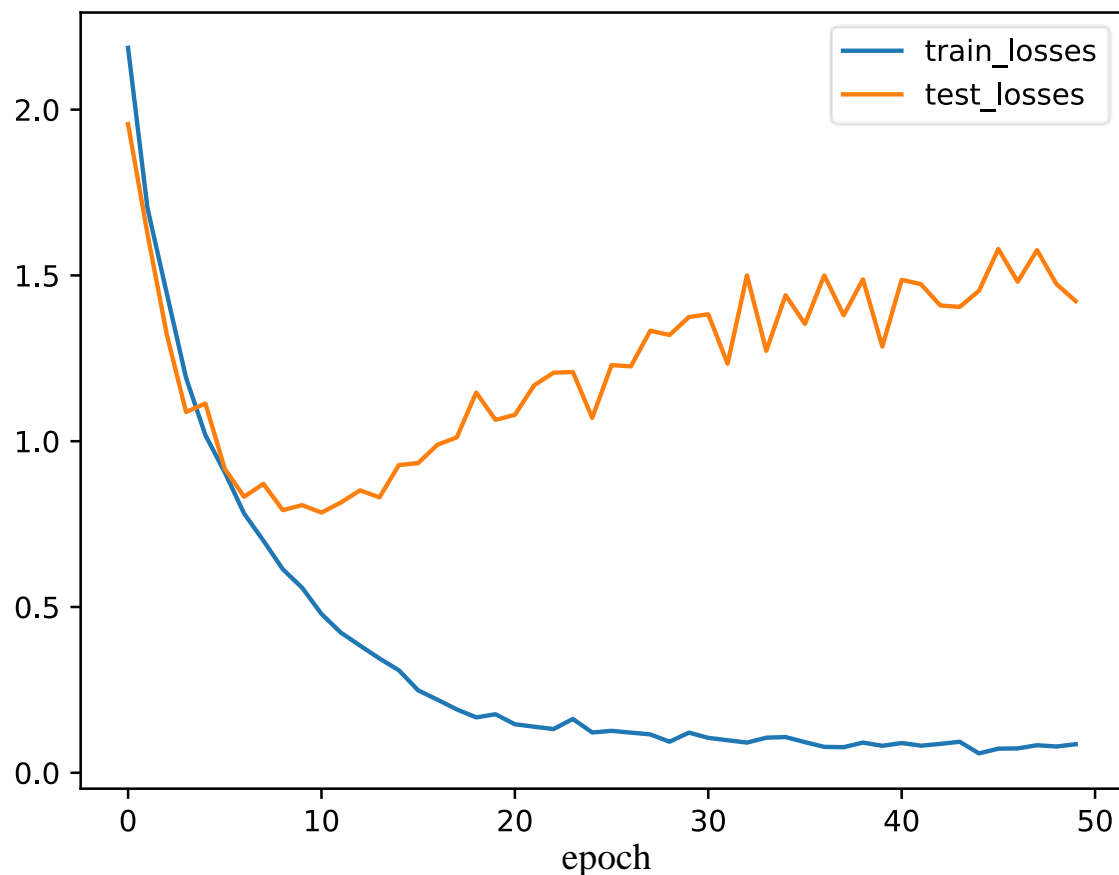
2017

Sigmoid Linear Unit (SiLU)

$$\text{swish}(x) = x * \frac{1}{1 + e^{-x}}$$

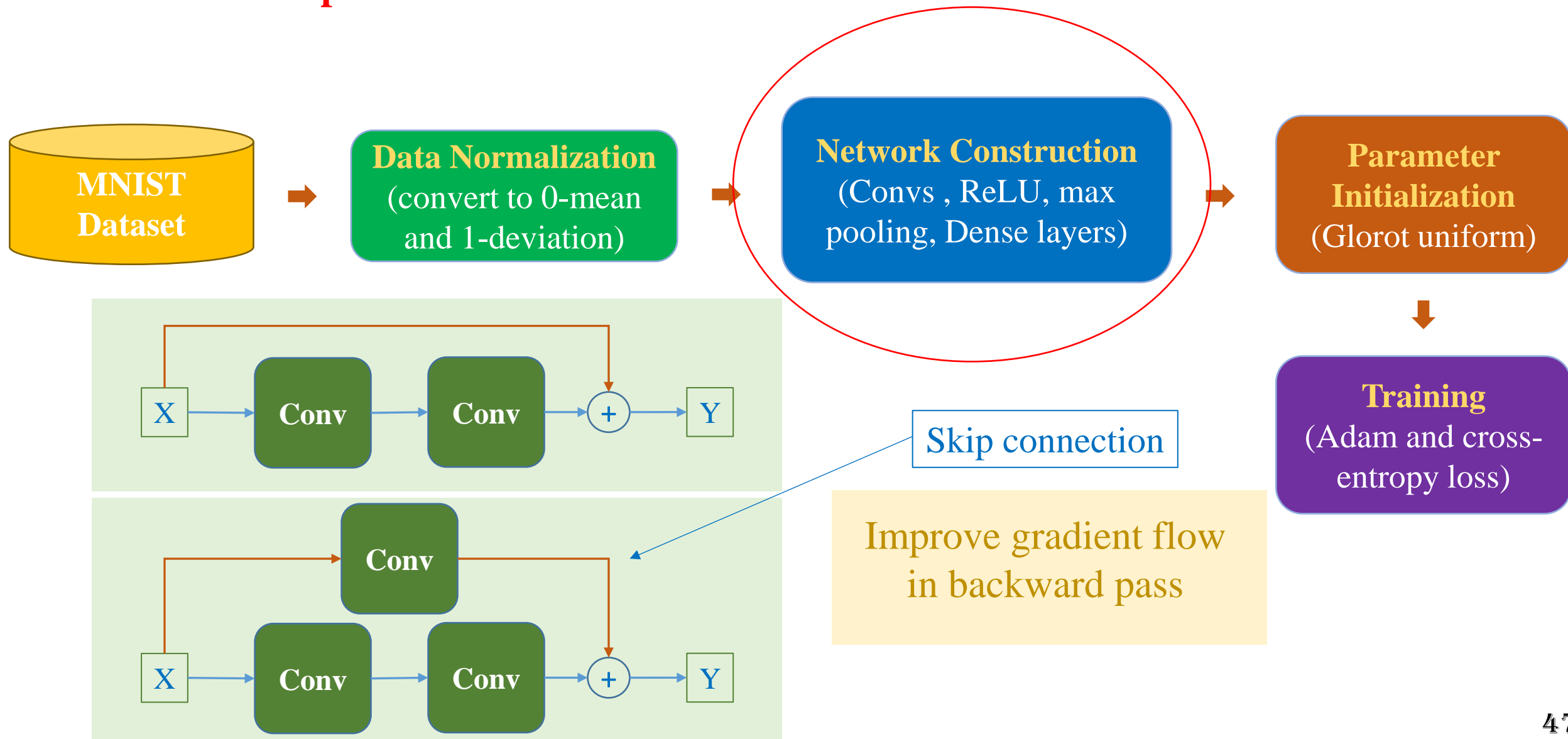
```
conv_layer1 = nn.Sequential(  
    nn.Conv2d(3, 64, 3, stride=1, padding=1),  
    nn.SiLU()  
)
```

<https://arxiv.org/pdf/1702.03118.pdf>

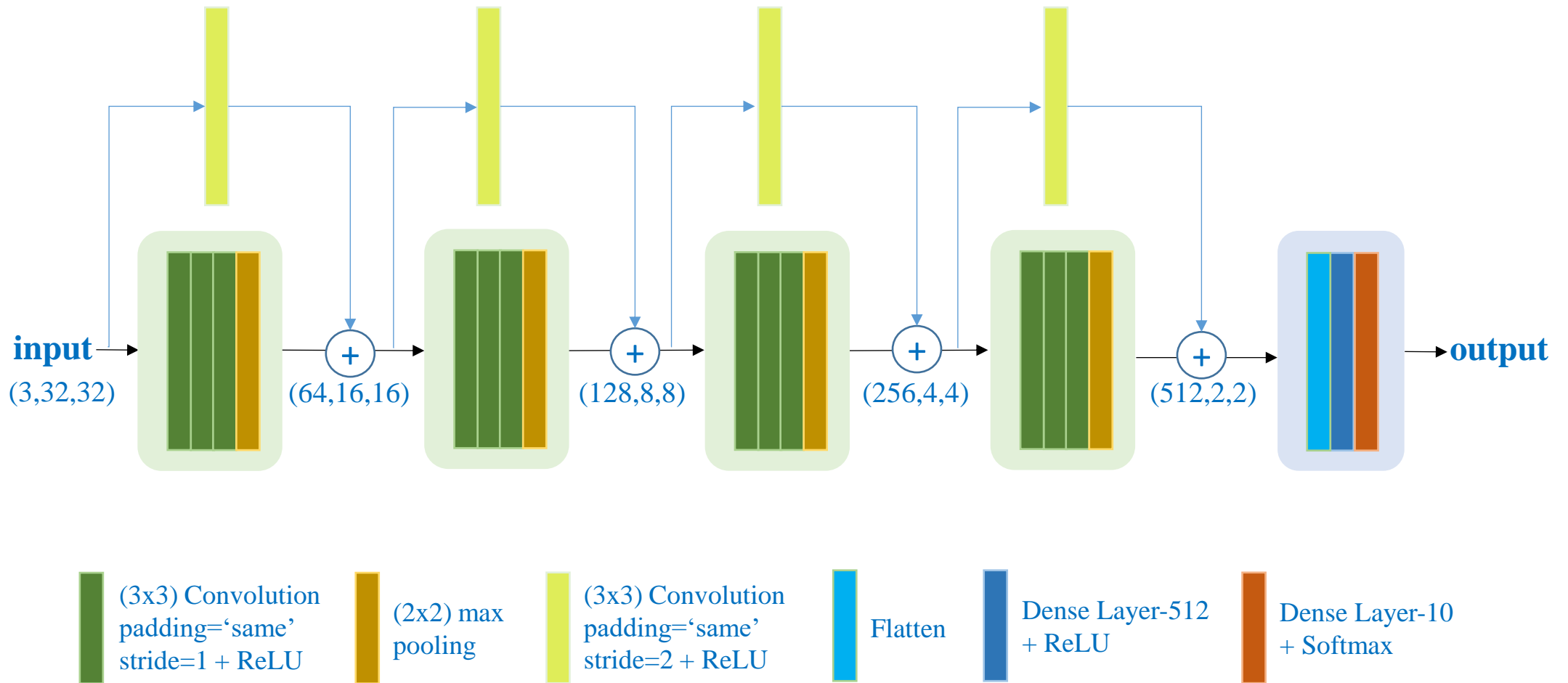


# Network Training

## ❖ Solution 5: Skip connection



## ❖ Solution 5: Skip connection

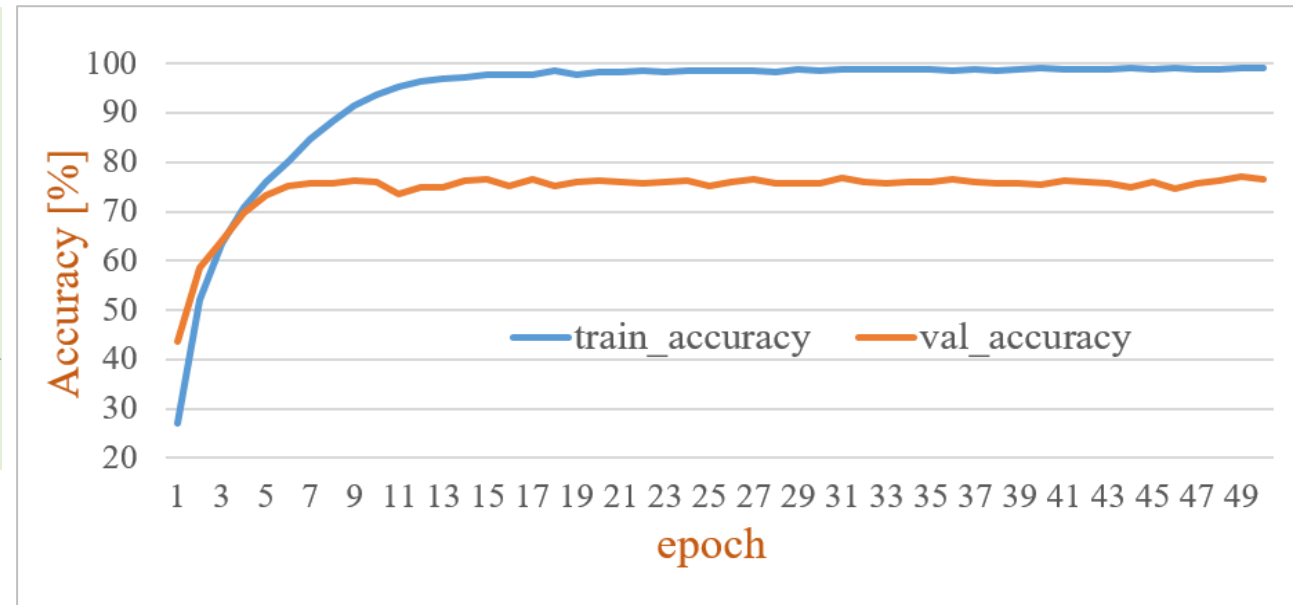
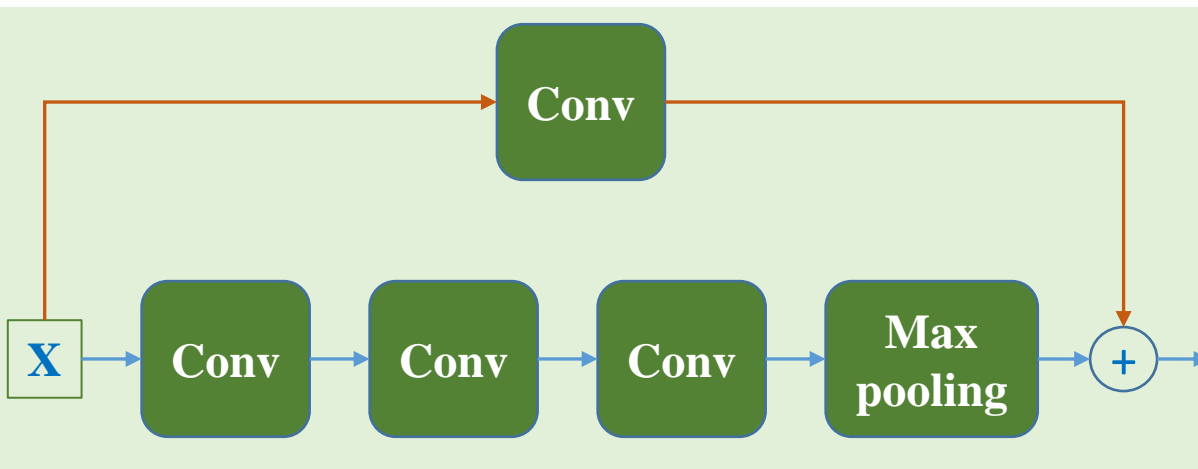


# Network Training

## ❖ Solution 5: Skip connection

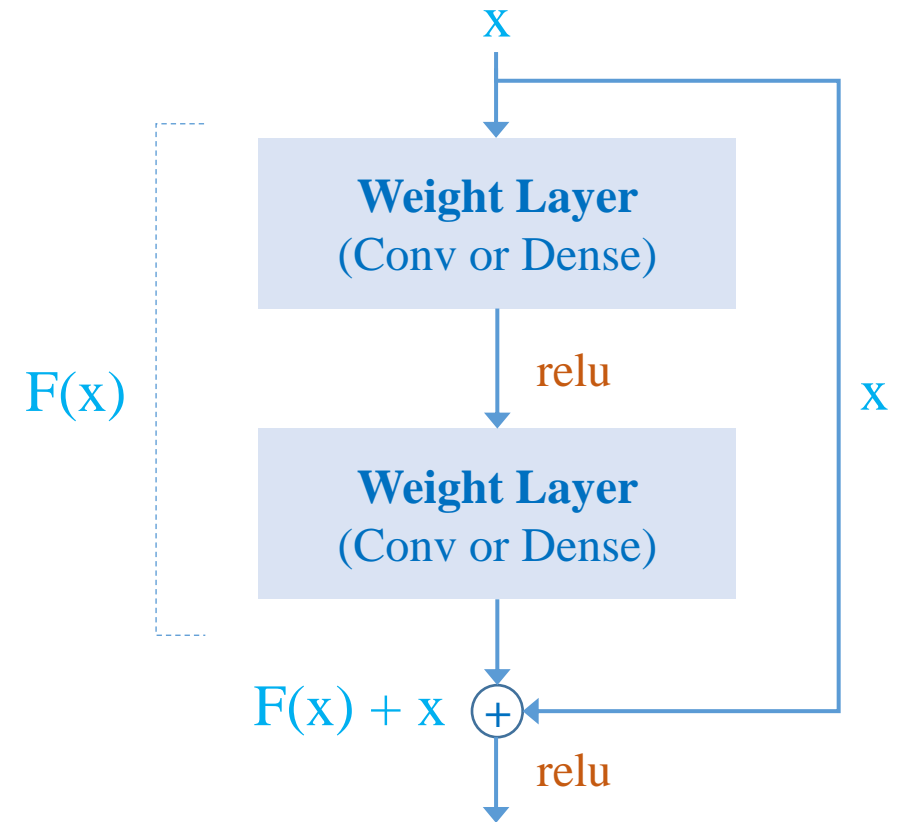
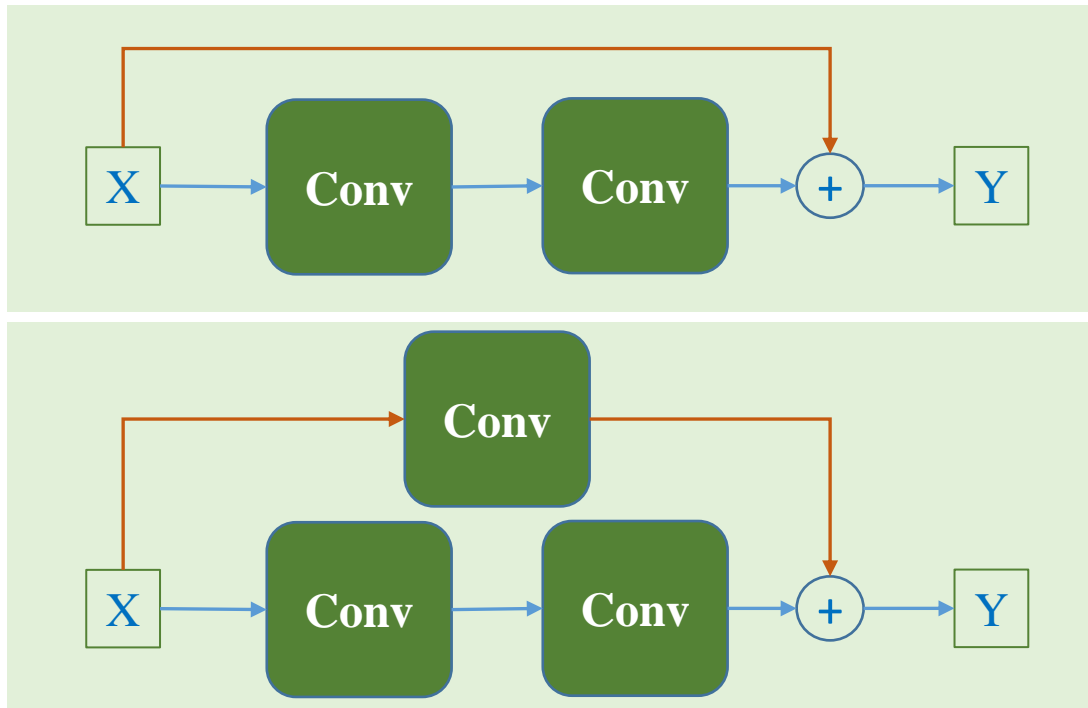
```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU(),
                             nn.MaxPool2d(2, 2))
res_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=2, padding=1), nn.ReLU())

# Given x
previous_input_x = x
x = self.conv_layer1(x)
x = self.conv_layer2(x)
x = self.conv_layer3(x)
res = self.res_layer1(previous_input_x)
x = x + res
```

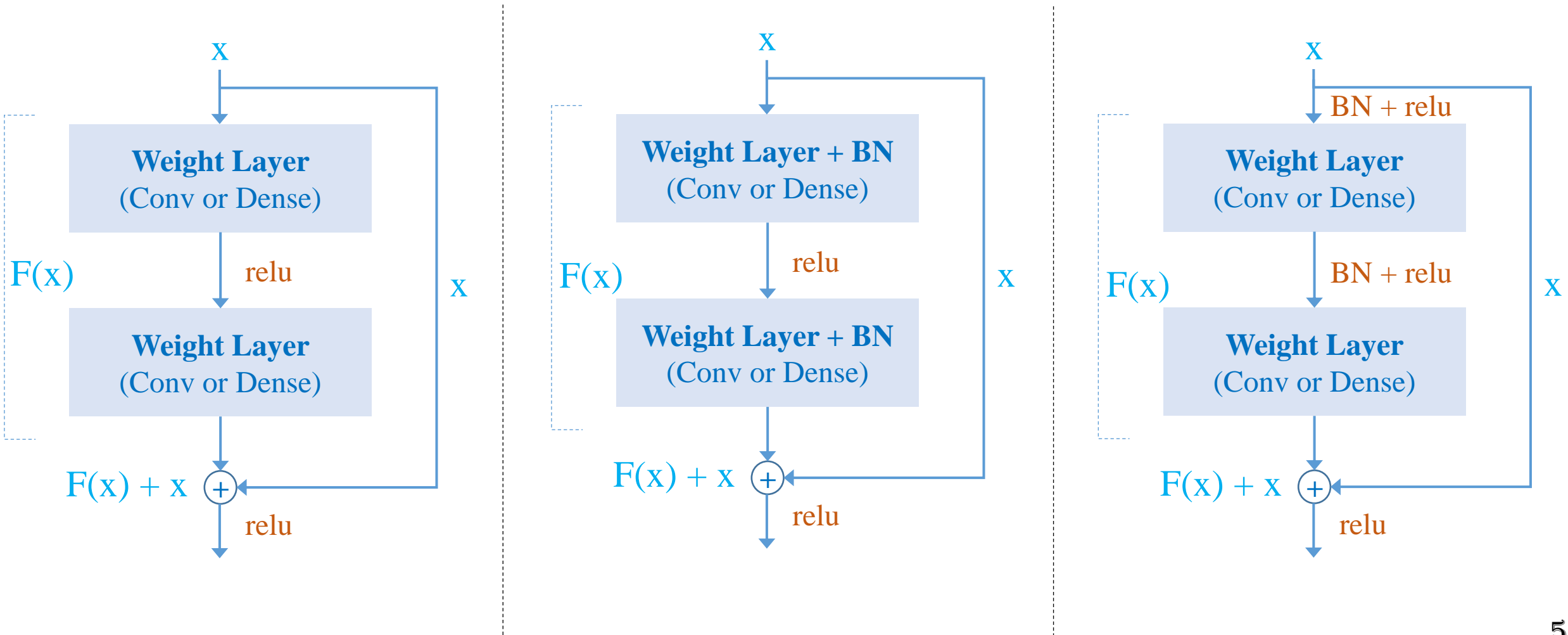


There are several variants that use fully skip connection, concatenation, long skip connection

## ❖ Solution 5: Skip connection



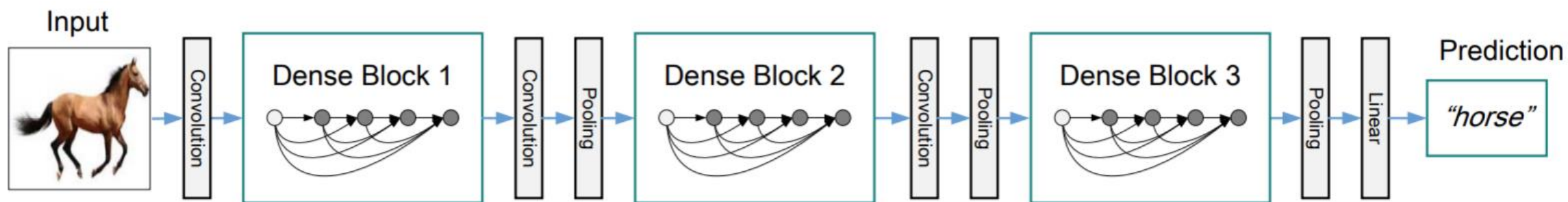
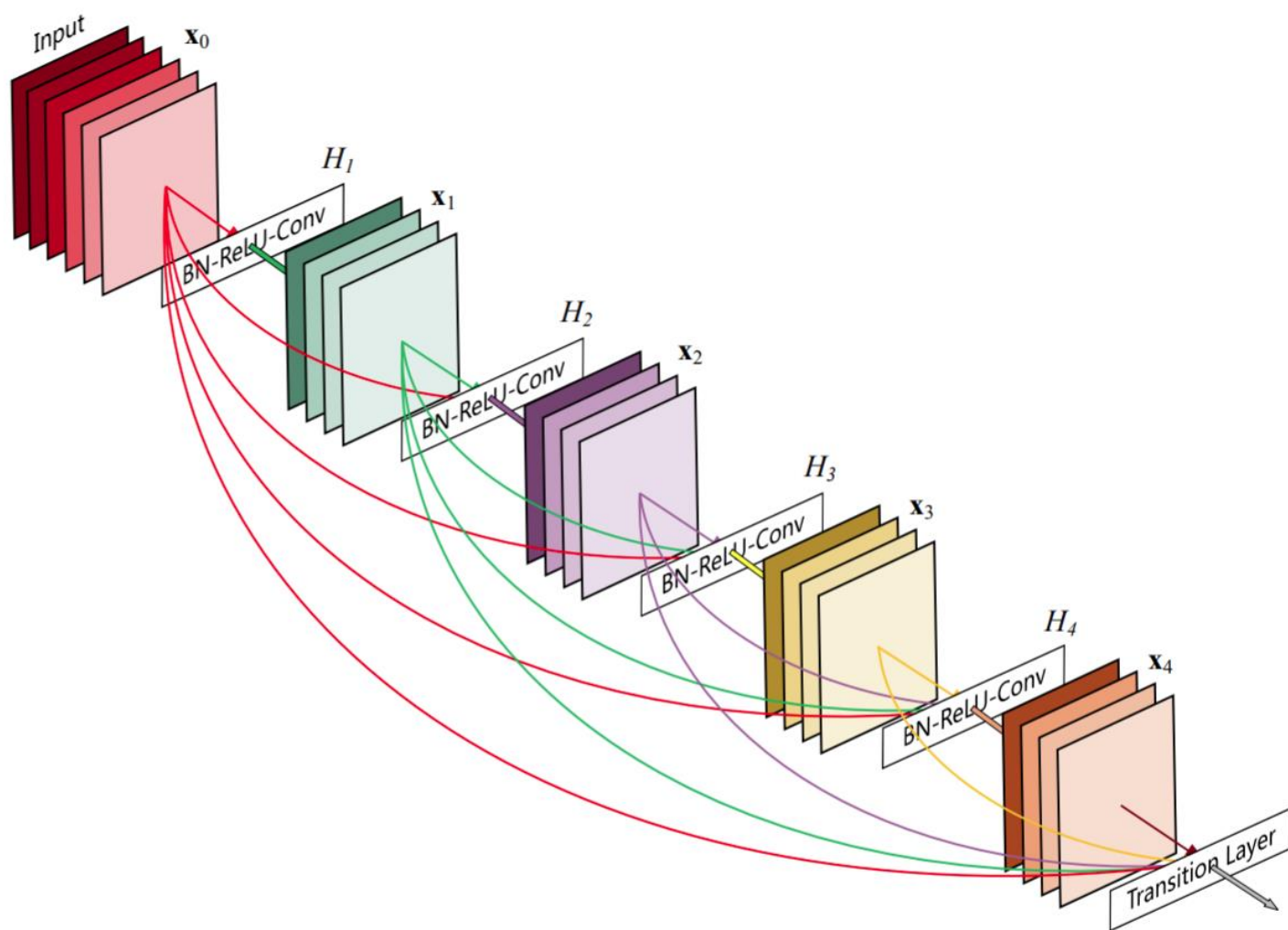
## ❖ Solution 5: Skip connection



# Network Training

## ❖ Solution 5: Skip connection

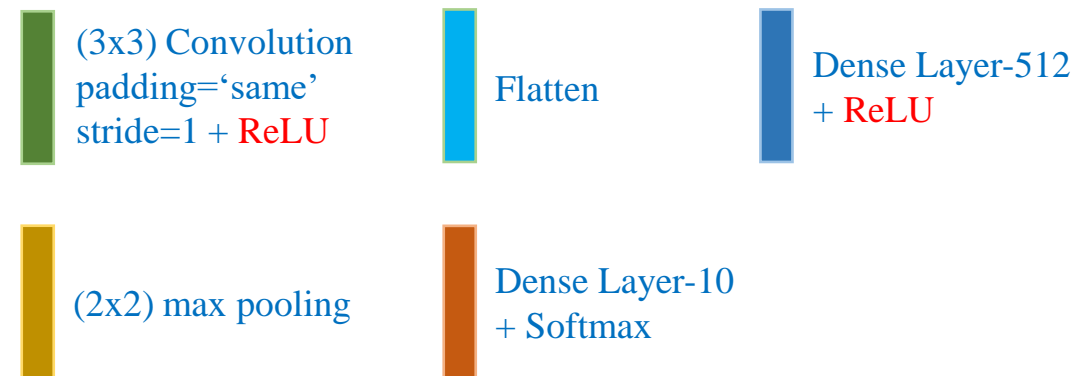
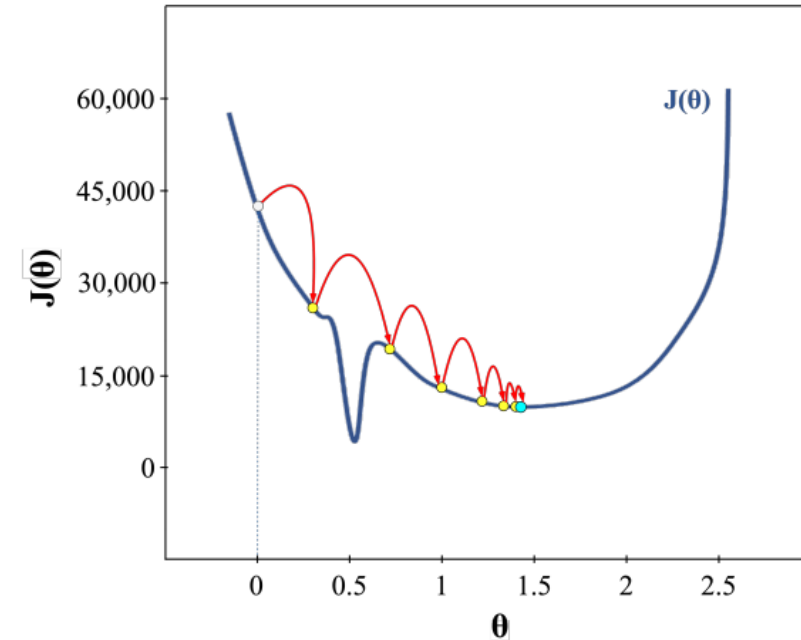
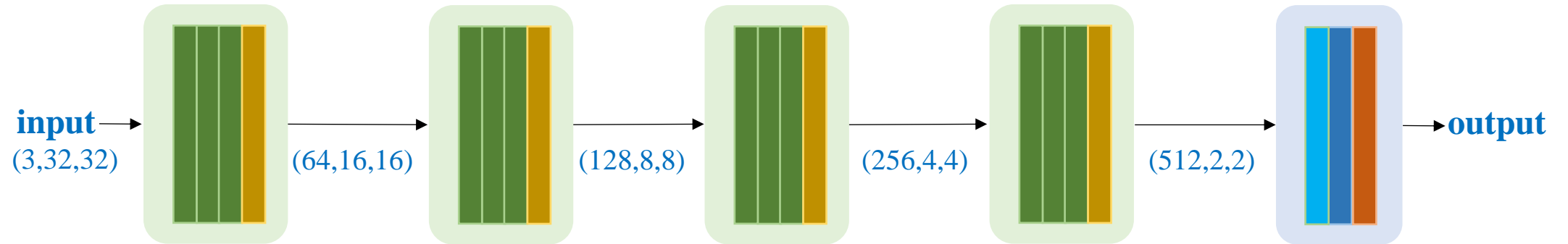
<https://arxiv.org/pdf/1608.06993v5.pdf>





# Network Training

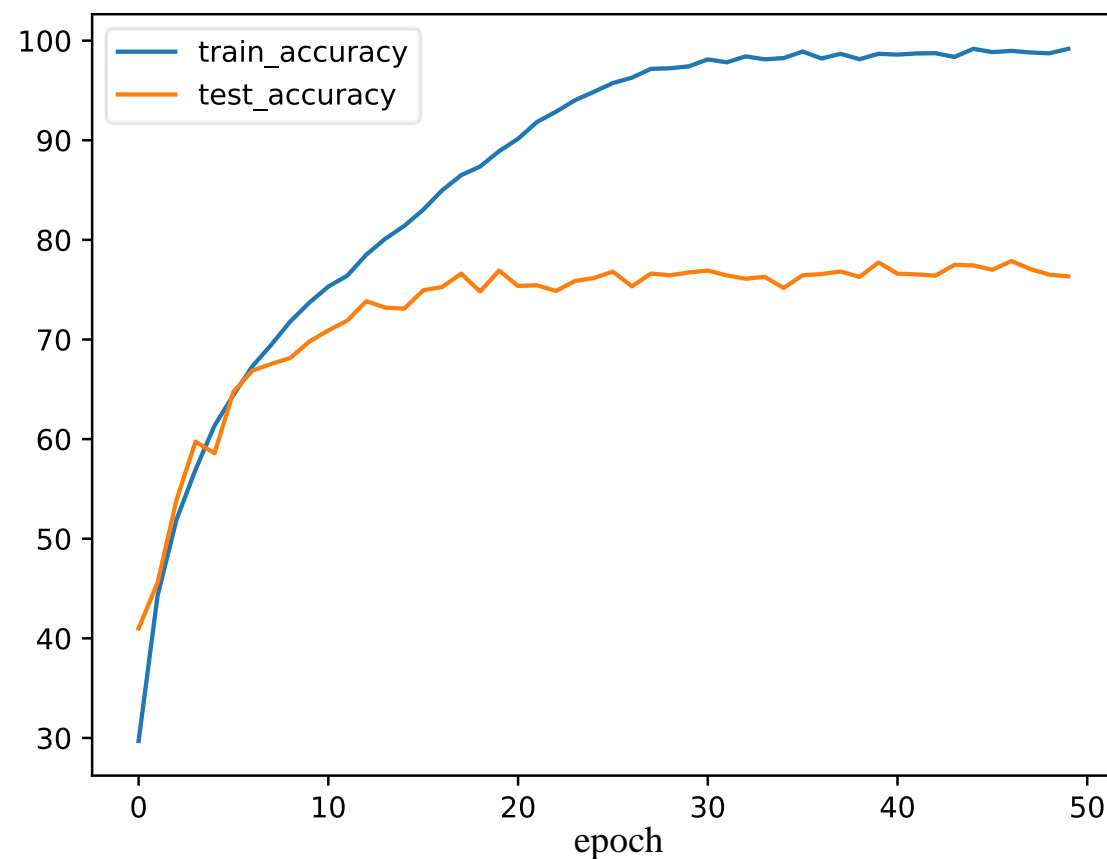
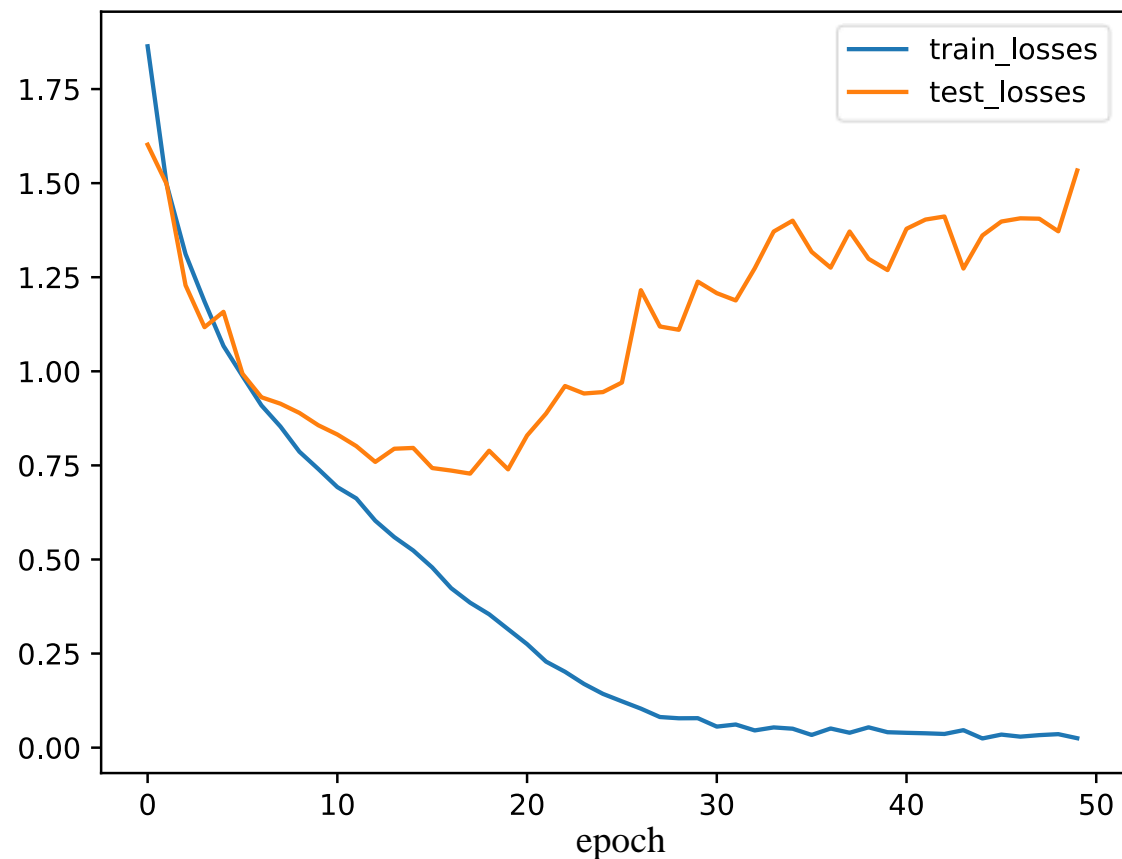
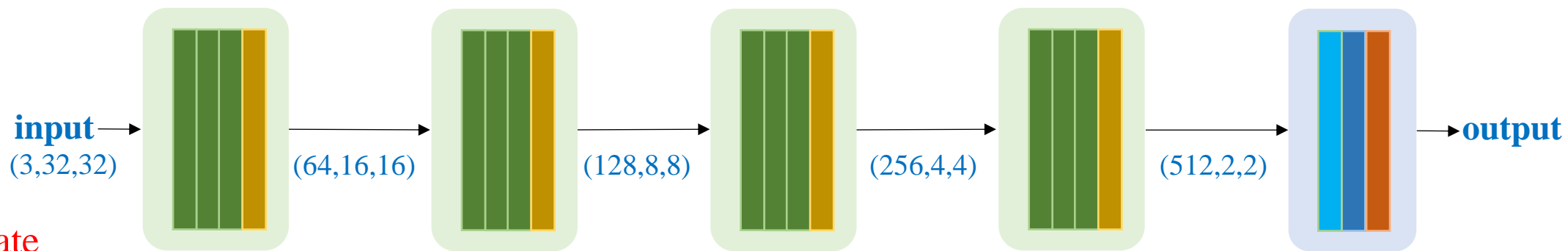
## ❖ Solution 6: Reduce learning rate

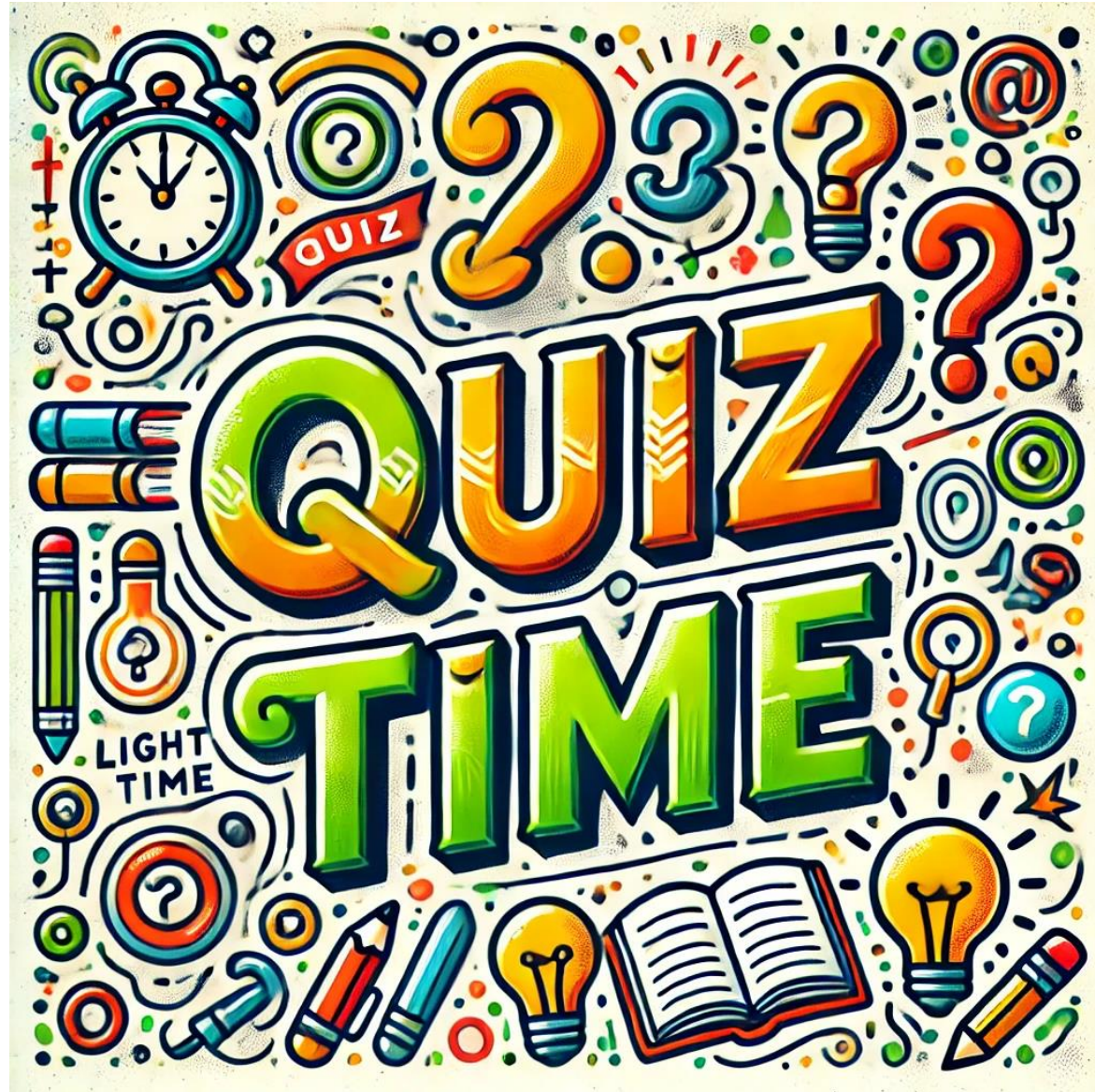


```
# loss and optimizer
criterion = nn.CrossEntropyLoss()
optimizer = Adam(model.parameters(), lr=1e-4)
```

# Network Training

Reduce learning rate





# Summary

## Skip connection

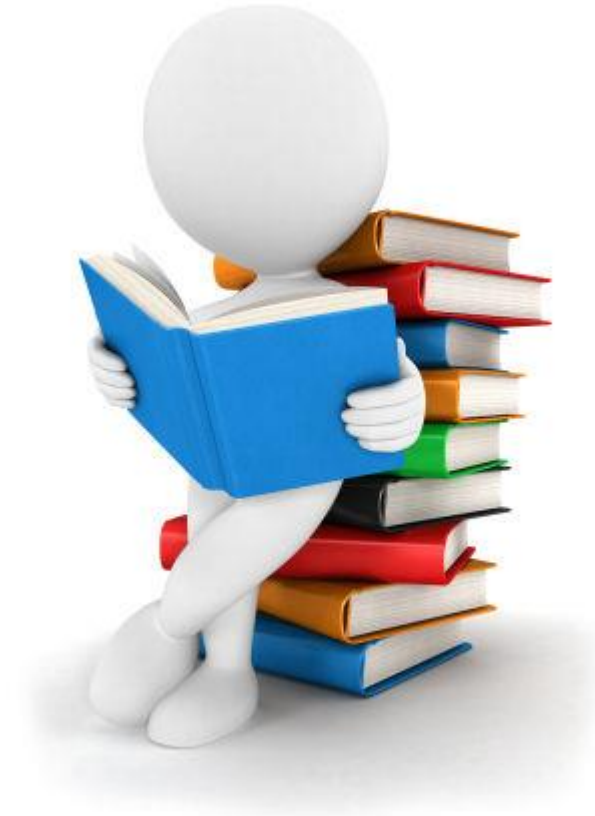
<https://theaisummer.com/skip-connections/>

## Trying to overfit Data

<http://karpathy.github.io/2019/04/25/recipe/>

## DenseNet

<https://arxiv.org/pdf/1608.06993v5.pdf>



# Summary

## ❖ Train a CNN model

### ❖ Try to overfit data

