

CNN Training

How to increase training accuracy?

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Ph.D. in Computer Science

Objectives

Activation and Initialization

Glorot initialization (2010)

$$W \sim \mathcal{N}\left(0, \frac{1}{n_j}\right)$$

n_j is #inputs in layer j

Assuming activation functions are linear

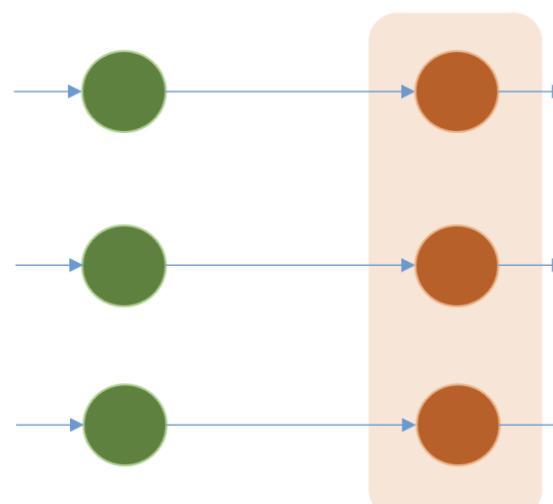
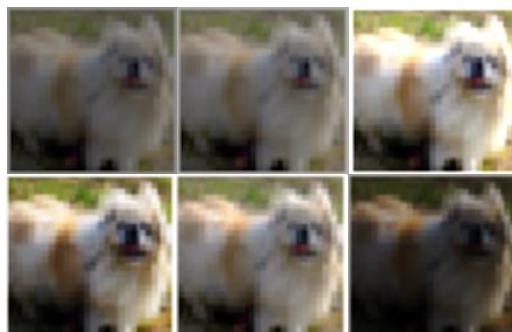
He initialization (2015)

Taking activation function into account

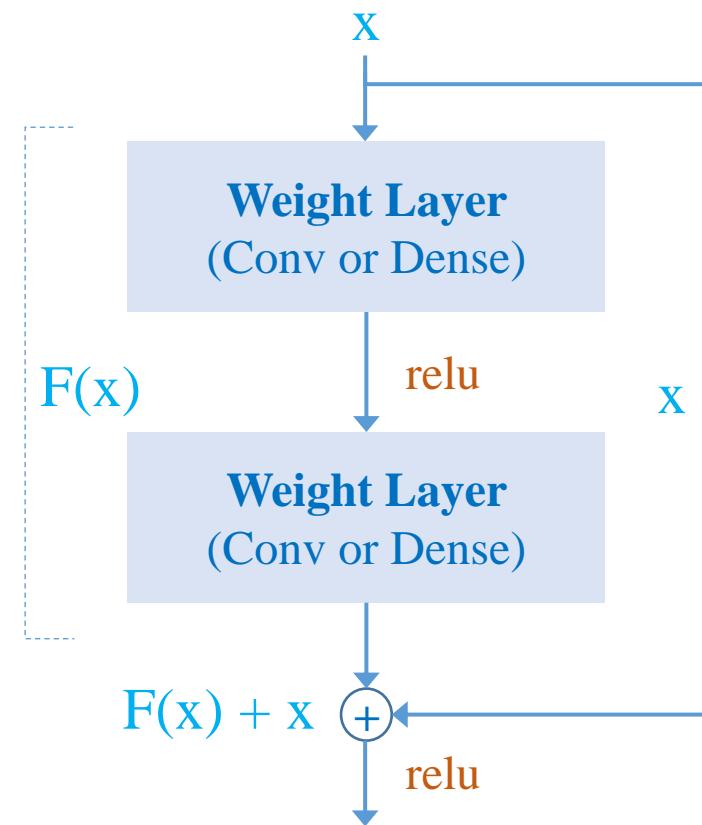
Adapt to ReLU activation

$$W \sim \mathcal{N}\left(0, \frac{2}{n_j}\right)$$

Data and Feature Normalization



Skip Connections



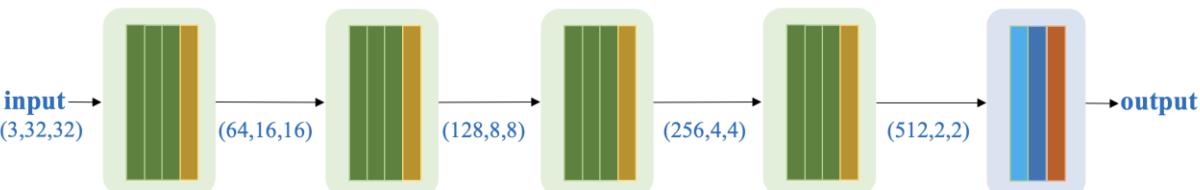
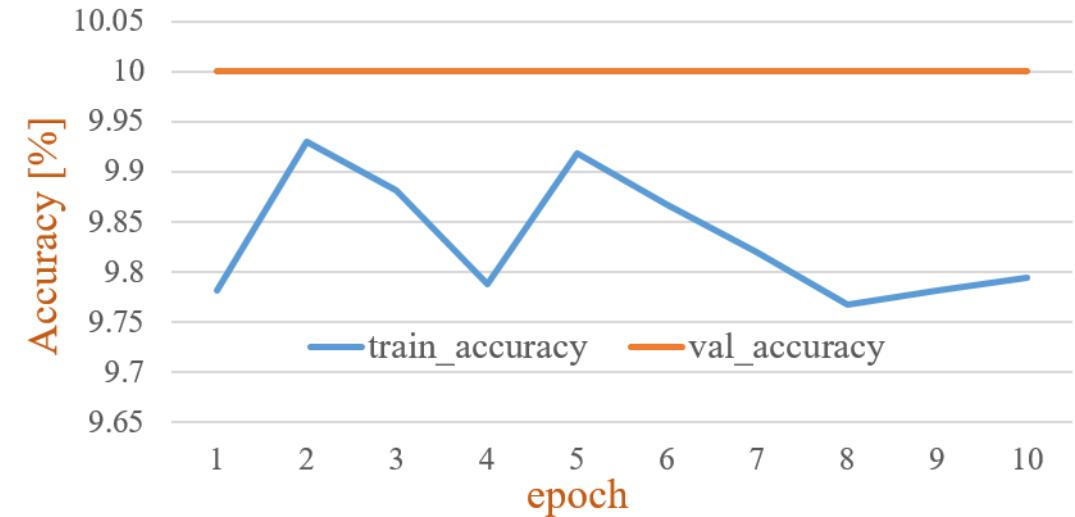
Outline

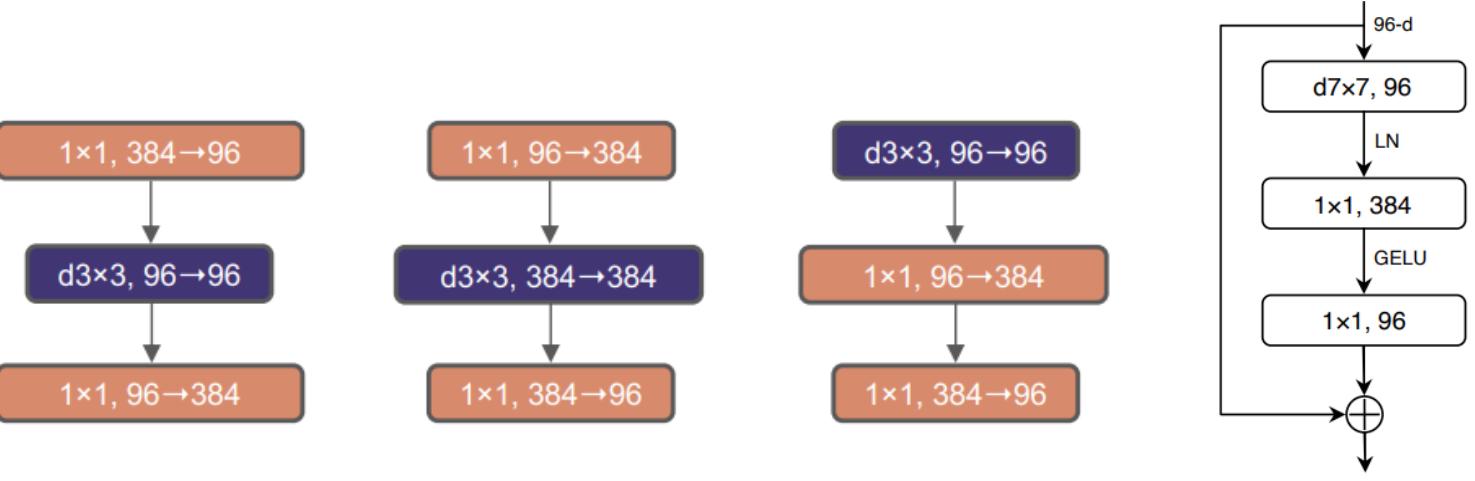
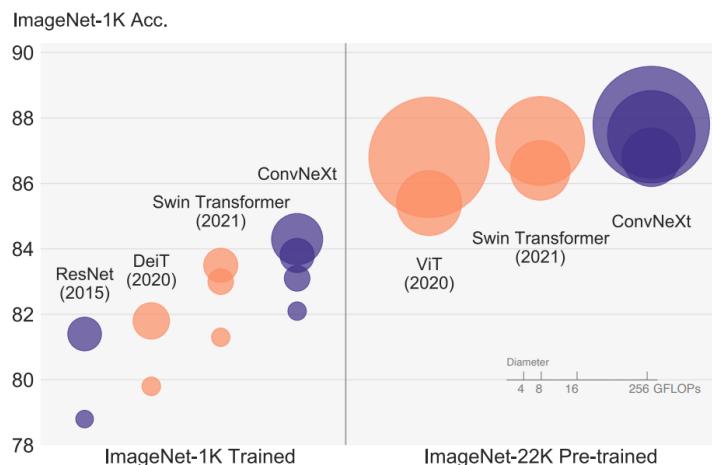
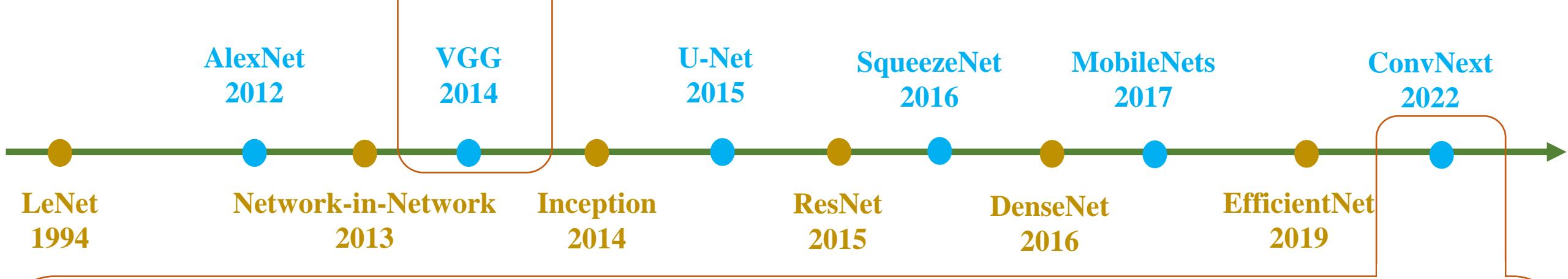
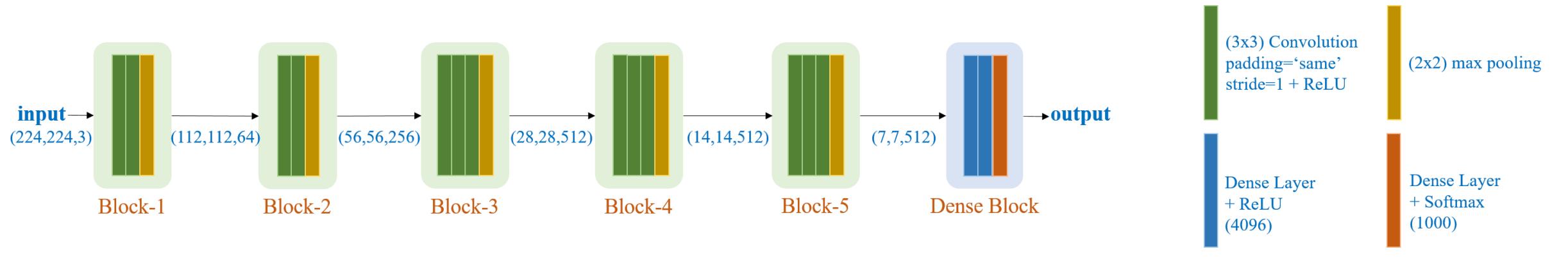
SECTION 1

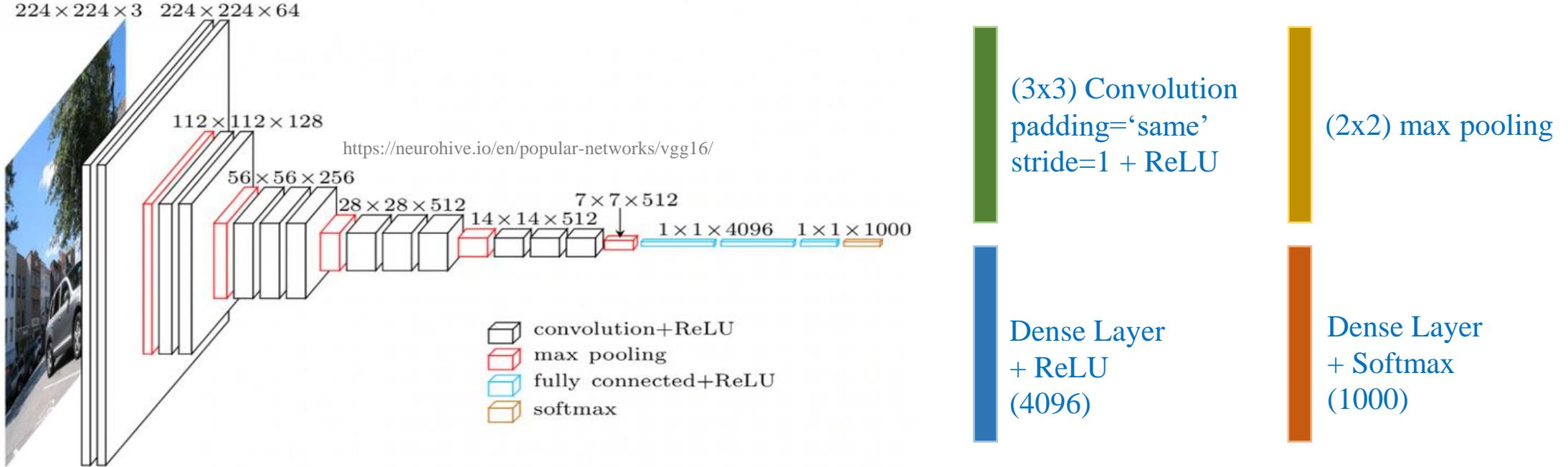
Setting-up Context

SECTION 2

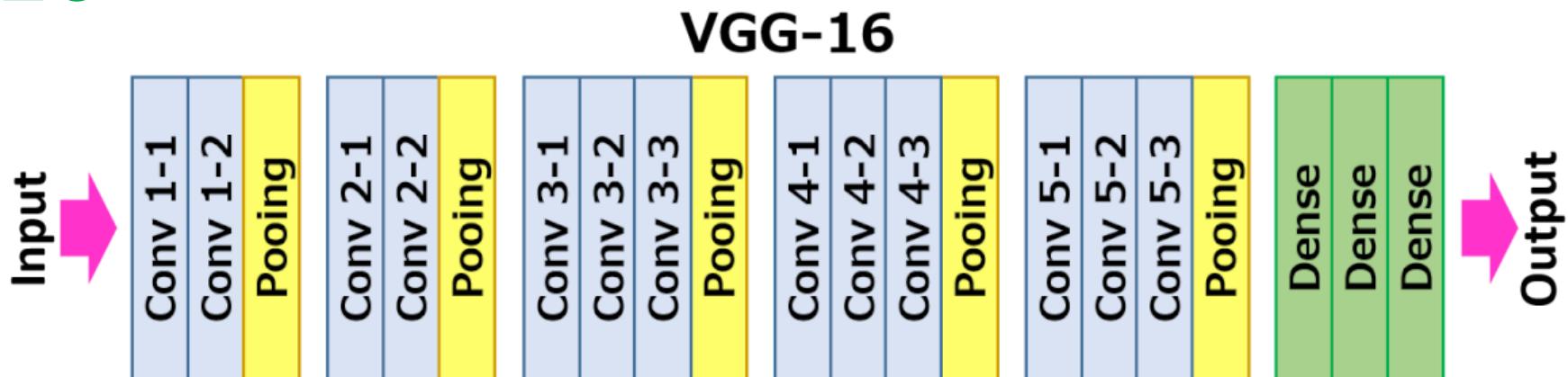
Solutions for the Context





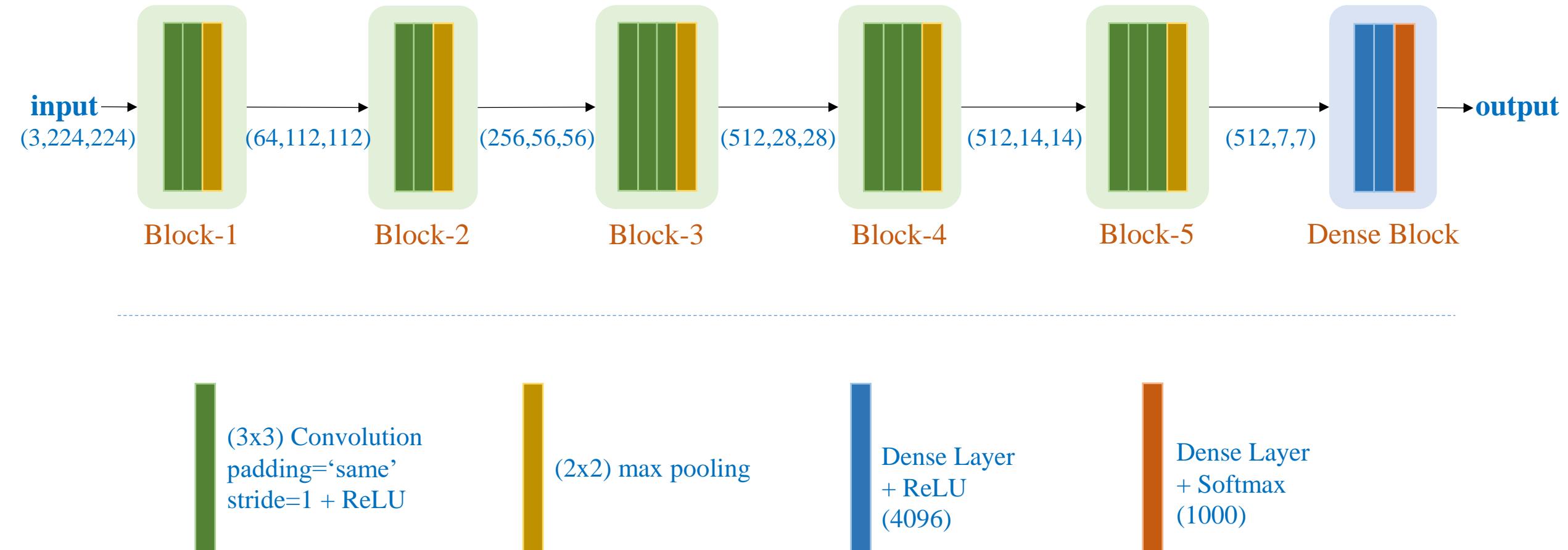


VGG16



CNN Architectures

❖ VGG16 for ImageNet



```
# Define the blocks
block1 = nn.Sequential(
    nn.Conv2d(3, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(64, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block2 = nn.Sequential(
    nn.Conv2d(64, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(128, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block3 = nn.Sequential(
    nn.Conv2d(128, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block4 = nn.Sequential(
    nn.Conv2d(256, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block5 = nn.Sequential(
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
```

```
# Classifier
classifier = nn.Sequential(
    nn.Flatten(),
    nn.Linear(512*7*7, 4096), nn.ReLU(inplace=True),
    nn.Linear(4096, 4096), nn.ReLU(inplace=True),
    nn.Linear(4096, 1000),
)

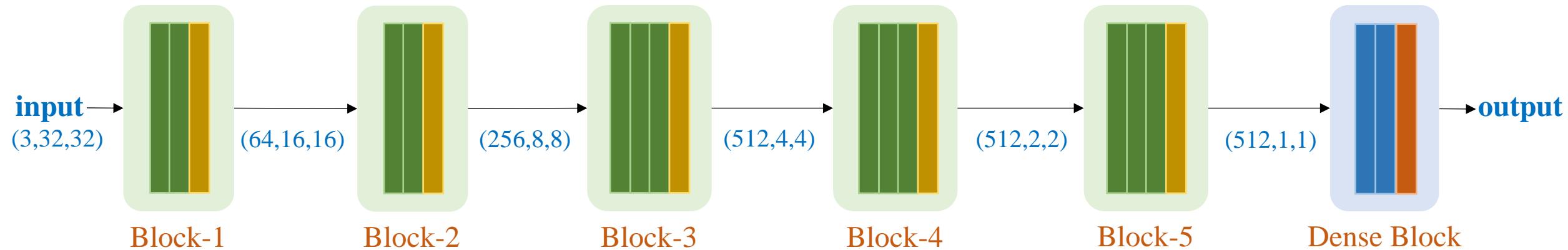
# Combine all blocks into one model
class VGG16(nn.Module):
    def __init__(self):
        super(VGG16, self).__init__()
        self.block1 = block1
        self.block2 = block2
        self.block3 = block3
        self.block4 = block4
        self.block5 = block5
        self.classifier = classifier

    def forward(self, x):
        x = self.block1(x)
        x = self.block2(x)
        x = self.block3(x)
        x = self.block4(x)
        x = self.block5(x)
        x = self.classifier(x)
        return x

# Instantiate the model
model = VGG16()
```

CNN Architectures

❖ VGG16-like for Cifar-10



(3x3) Convolution
padding='same'
stride=1 + ReLU

(2x2) max pooling

Dense Layer
+ ReLU
(256)

Dense Layer
+ Softmax
(10)

```
# Define the blocks
block1 = nn.Sequential(
    nn.Conv2d(3, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(64, 64, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block2 = nn.Sequential(
    nn.Conv2d(64, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(128, 128, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block3 = nn.Sequential(
    nn.Conv2d(128, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(256, 256, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block4 = nn.Sequential(
    nn.Conv2d(256, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
block5 = nn.Sequential(
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.Conv2d(512, 512, kernel_size=3, padding=1), nn.ReLU(inplace=True),
    nn.MaxPool2d(kernel_size=2, stride=2),
)
```

```
# Classifier
classifier = nn.Sequential(
    nn.Flatten(),
    nn.Linear(512*1*1, 256), nn.ReLU(inplace=True),
    nn.Linear(256, 256), nn.ReLU(inplace=True),
    nn.Linear(256, 10),
)

# Combine all blocks into one model
class VGG16(nn.Module):
    def __init__(self):
        super(VGG16, self).__init__()
        self.block1 = block1
        self.block2 = block2
        self.block3 = block3
        self.block4 = block4
        self.block5 = block5
        self.classifier = classifier

    def forward(self, x):
        x = self.block1(x)
        x = self.block2(x)
        x = self.block3(x)
        x = self.block4(x)
        x = self.block5(x)
        x = self.classifier(x)
        return x

# Instantiate the model
model = VGG16()
```

Image Data

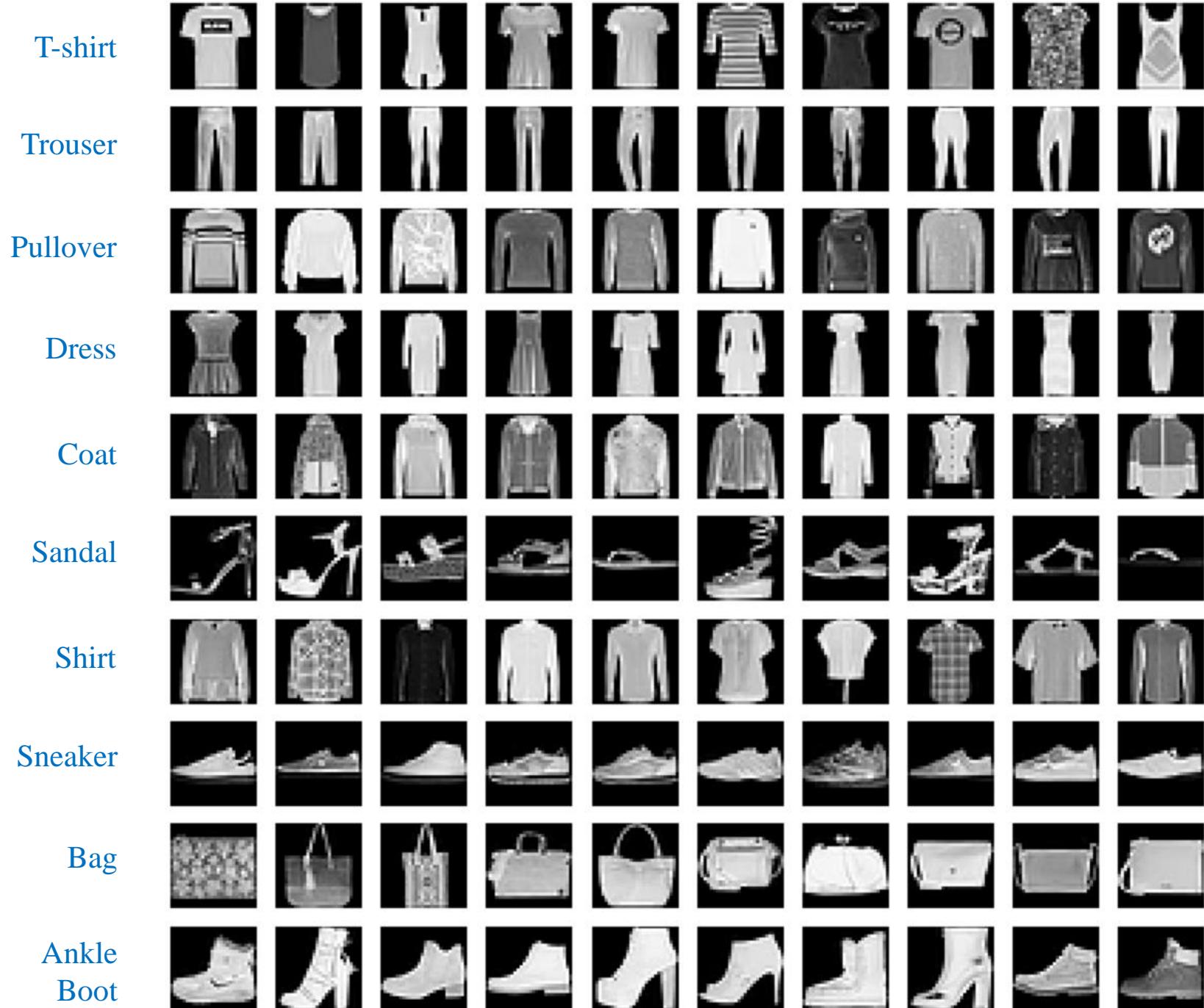
Fashion-MNIST dataset

Grayscale images

Resolution=28x28

Training set: 60000 samples

Testing set: 10000 samples



Network Training

❖ Fashion-MNIST dataset

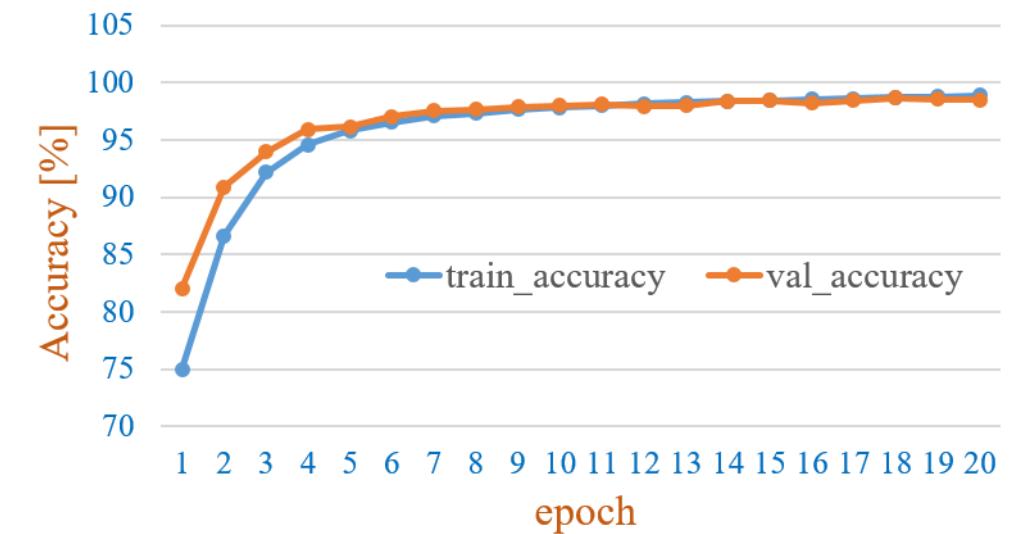
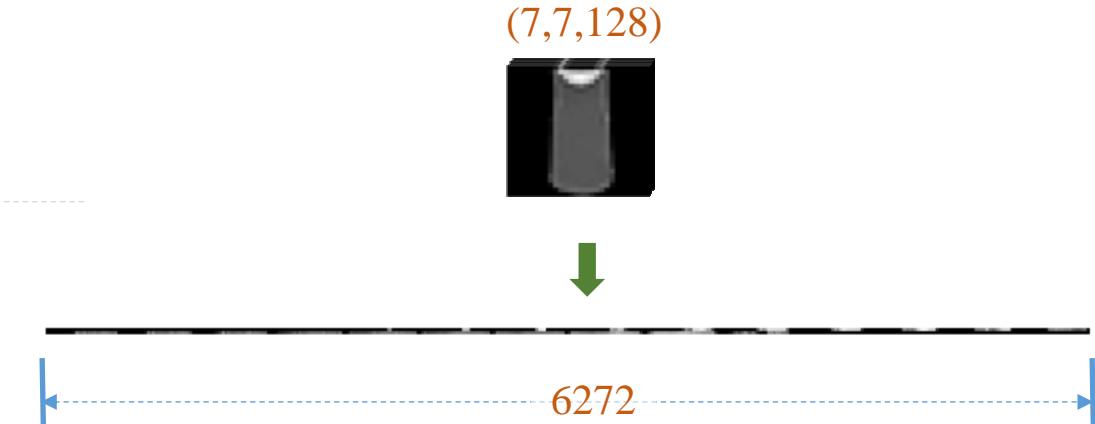


(3x3) Convolution
padding='same'
stride=1 + Sigmoid

(2x2) max pooling

Flatten

Dense Layer-10
+ Softmax



Network Training

❖ Fashion-MNIST dataset

X-data format

(batch, channel, height, width)

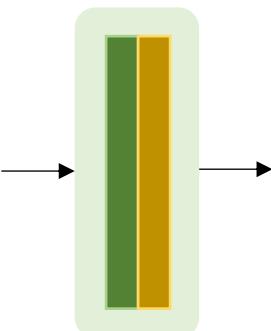
Data normalization [0,1]

(3x3) Convolution with 64 filters,
stride=1, padding='same'
+ Sigmoid activation
+ glorot_uniform initialization

Adam optimizer and Cross-entropy loss

(3x3) Convolution
padding='same'
stride=1 + Sigmoid

(2x2) max pooling



```
# Data
transform = Compose([transforms.ToTensor()])
train_set = FashionMNIST(root='data',
                           train=True,
                           download=True,
                           transform=transform)
trainloader = DataLoader(train_set,
                         batch_size=256,
                         shuffle=True,
                         num_workers=4)
```

```
import torch.nn as nn
import torch.nn.init as init

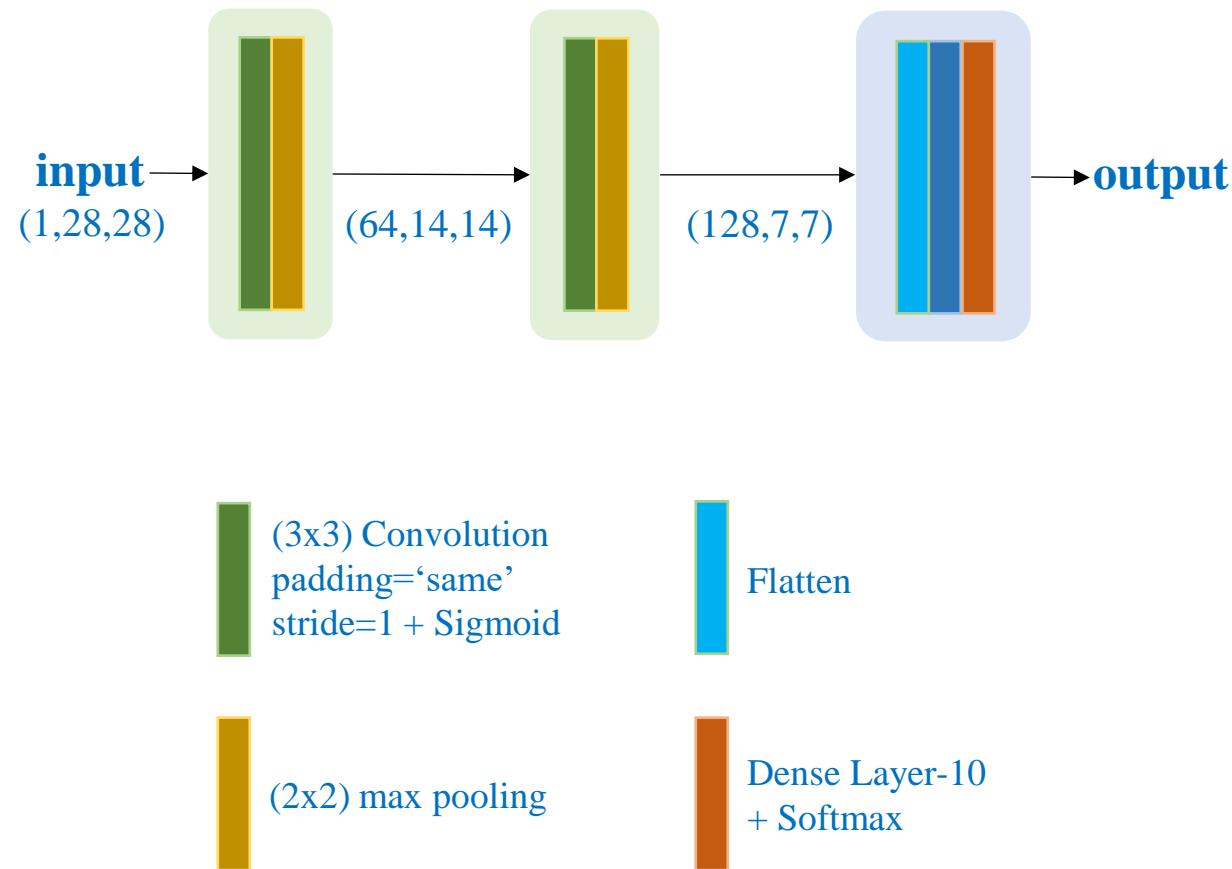
block = nn.Sequential(nn.Conv2d(1, 64, 3,
                               stride=1,
                               padding='same'),
                      nn.Sigmoid(),
                      nn.MaxPool2d(2, 2))

for m in block:
    if isinstance(m, nn.Conv2d):
        init.xavier_uniform_(m.weight)
        if m.bias is not None:
            init.zeros_(m.bias)

# Loss and optimizer
criterion = nn.CrossEntropyLoss()
optimizer = Adam(model.parameters(), lr=1e-3)
```

Network Training

❖ Fashion-MNIST dataset



```
# Declare layers
conv_layer1 = nn.Sequential(
    nn.Conv2d(1, 64, 3, stride=1, padding='same'),
    nn.Sigmoid(),
    nn.MaxPool2d(2, 2)
)
conv_layer2 = nn.Sequential(
    nn.Conv2d(64, 128, 3, stride=1, padding='same'),
    nn.Sigmoid(),
    nn.MaxPool2d(2, 2)
)

flatten = nn.Flatten()
fc_layer1 = nn.Sequential(
    nn.Linear(128*7*7, 512),
    nn.Sigmoid()
)
fc_layer2 = nn.Linear(512, 10)

# Given data x
x = conv_layer1(x)
x = conv_layer2(x)
x = flatten(x)
x = fc_layer1(x)
x = fc_layer2(x)
```

Network Training

Cifar-10 dataset
(more complex dataset)

Color images

Resolution=32x32

Training set: 50000 samples

Testing set: 10000 samples

airplane



automobile



bird



cat



deer



dog



frog



horse



ship

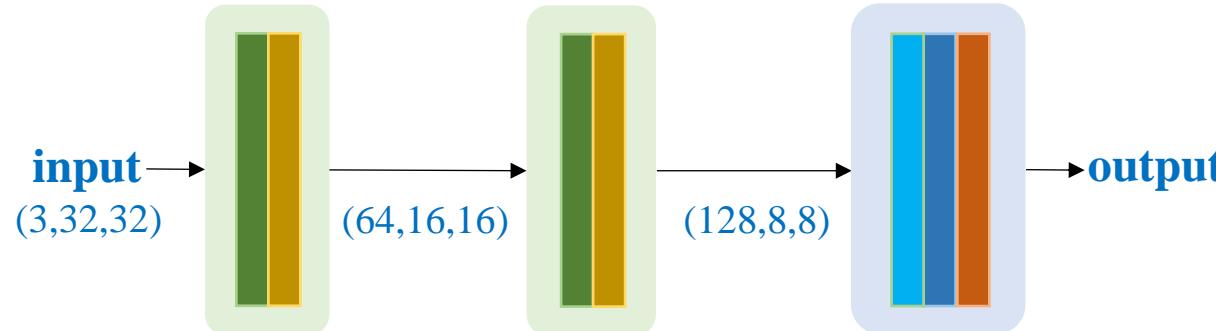


truck



Network Training

❖ Cifar-10 dataset



(3x3) Convolution
padding='same'
stride=1 + Sigmoid

(2x2) max pooling

Flatten

Dense Layer-10
+ Softmax

Data normalization [0,1]

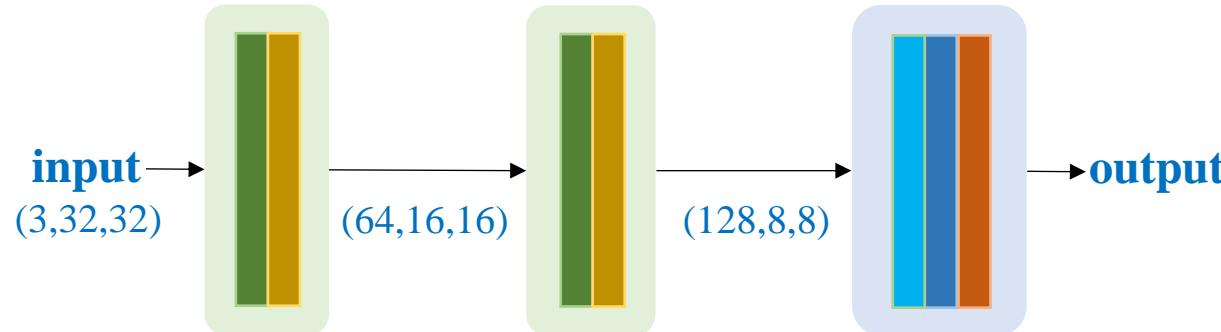
Glorot uniform initialization

Adam optimizer with lr=1e-3

```
conv_layer1 = nn.Sequential(  
    nn.Conv2d(1, 64, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
conv_layer2 = nn.Sequential(  
    nn.Conv2d(64, 128, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
  
flatten = nn.Flatten()  
fc_layer1 = nn.Sequential(  
    nn.Linear(128*8*8, 512),  
    nn.Sigmoid()  
)  
fc_layer2 = nn.Linear(512, 10)  
  
# Given data x  
x = conv_layer1(x)  
x = conv_layer2(x)  
x = flatten(x)  
x = fc_layer1(x)  
x = fc_layer2(x)
```

Network Training

❖ Cifar-10 dataset



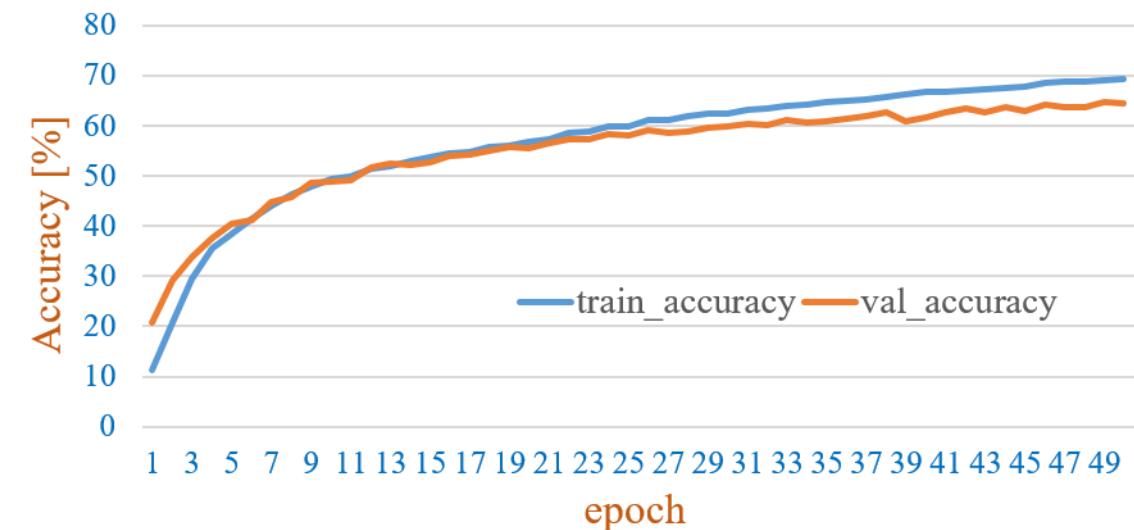
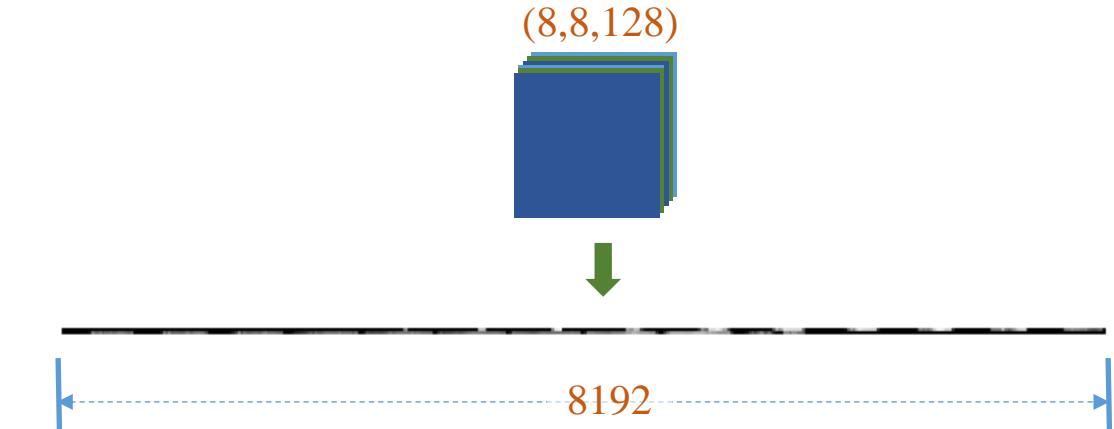
(3x3) Convolution
padding='same'
stride=1 + Sigmoid

(2x2) max pooling

Flatten

Dense Layer-10
+ Softmax

Accuracy: 69.3% - Val_accuracy: 64.5%



Network Training

❖ Cifar-10 dataset:

❖ Adding more layers

(3x3) Convolution
padding='same'
stride=1 + Sigmoid

Flatten

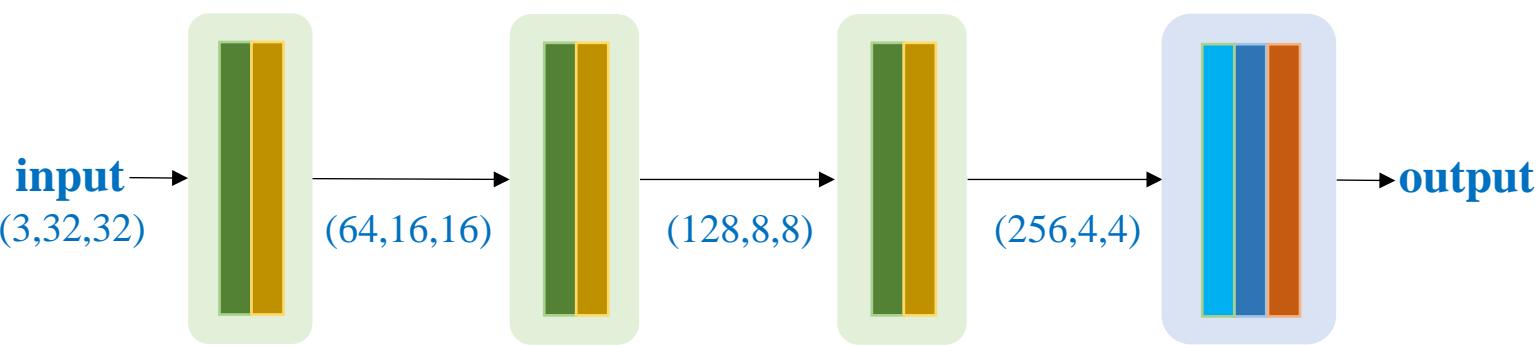
(2x2) max pooling

Dense Layer-10
+ Softmax

Data normalization [0,1]

Glorot uniform initialization

Adam optimizer with lr=1e-3



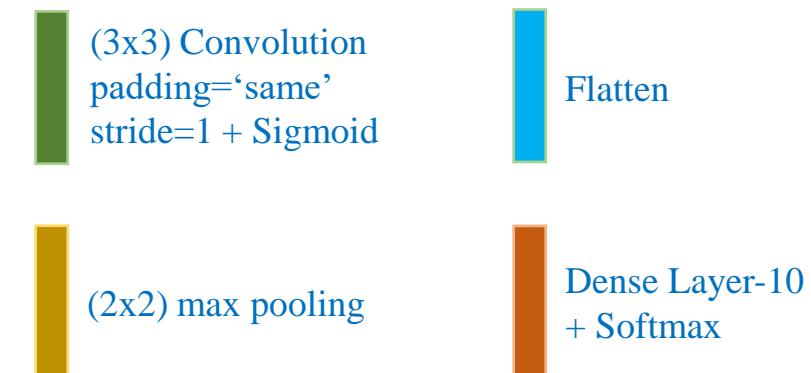
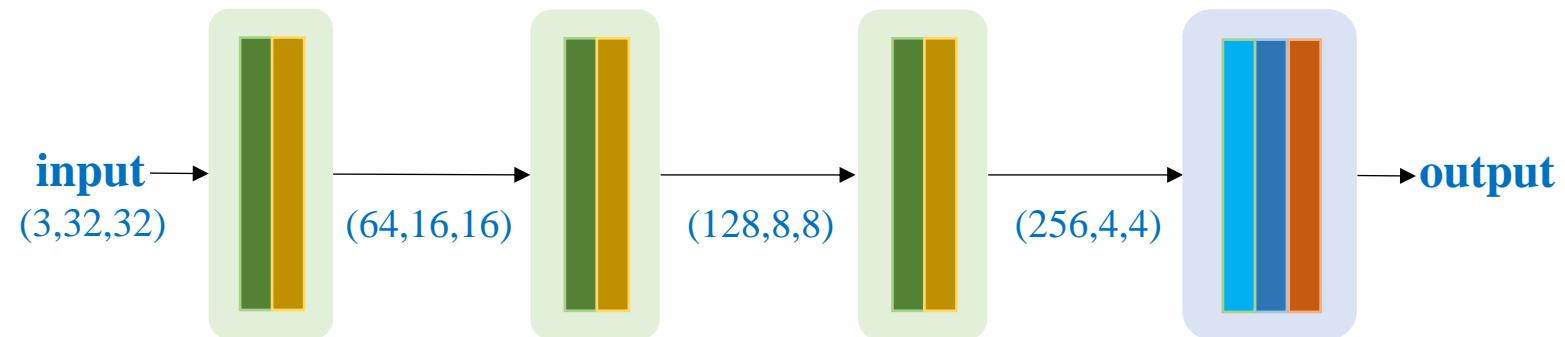
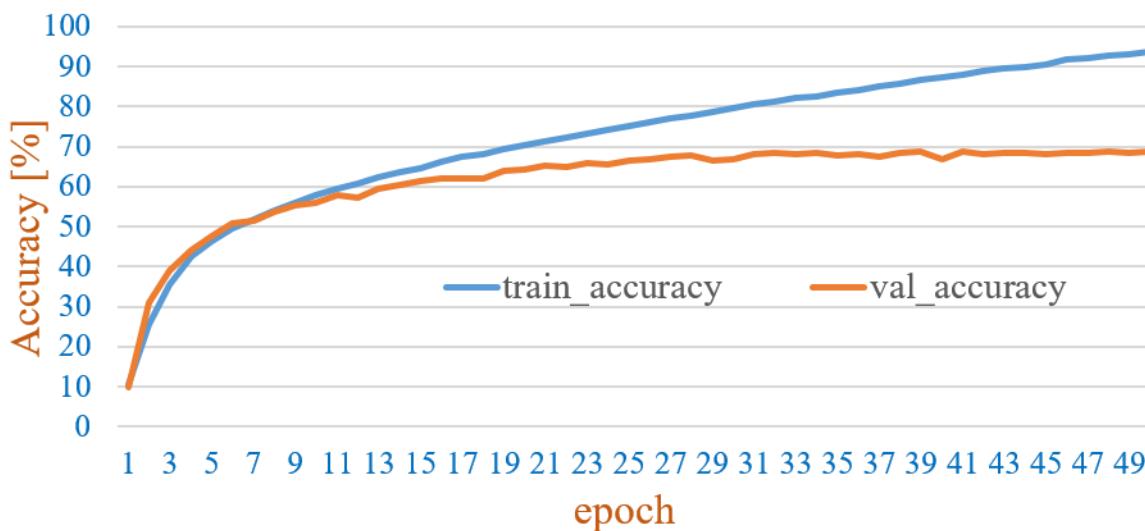
```
conv_layer1 = nn.Sequential(  
    nn.Conv2d(3, 64, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
conv_layer2 = nn.Sequential(  
    nn.Conv2d(64, 128, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
conv_layer3 = nn.Sequential(  
    nn.Conv2d(128, 256, 3, stride=1, padding='same'),  
    nn.Sigmoid(),  
    nn.MaxPool2d(2, 2)  
)  
  
flatten = nn.Flatten()  
fc_layer1 = nn.Sequential(  
    nn.Linear(256*4*4, 512),  
    nn.Sigmoid()  
)  
fc_layer2 = nn.Linear(512, n_classes)
```

Network Training

❖ Cifar-10 dataset:

❖ Adding more layers

Good news: Network accuracy increases about 25%



Accuracy: 93.8% - Val_accuracy: 68.7%

Network Training

Cifar-10 dataset:

❖ Keep adding more layers

(3x3) Convolution
padding='same'
stride=1 + Sigmoid



Flatten

(2x2) max pooling

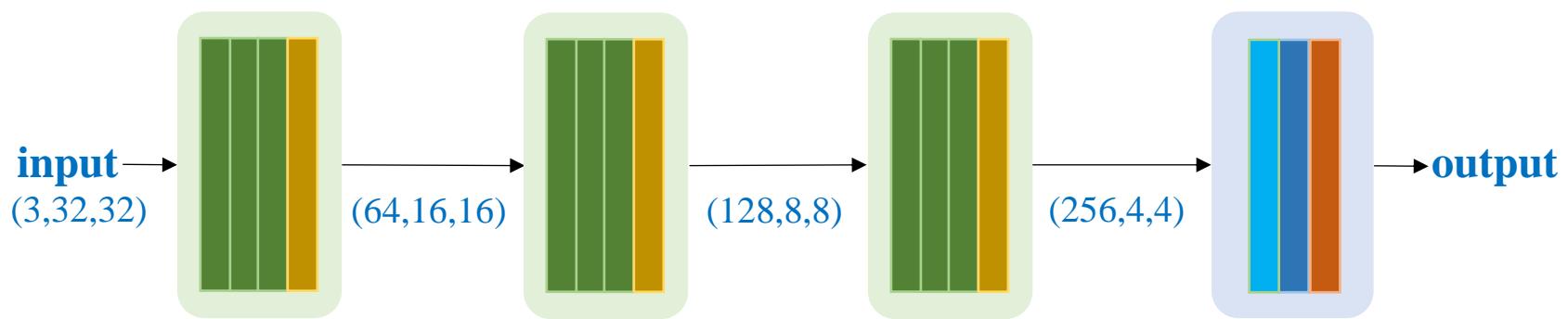


Dense Layer-10
+ Softmax

Data normalization [0,1]

Glorot uniform initialization

Adam optimizer with lr=1e-3



```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.Sigmoid(),
                           nn.MaxPool2d(2, 2))

conv_layer4 = nn.Sequential(nn.Conv2d(64, 128, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer5 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer6 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.Sigmoid(),
                           nn.MaxPool2d(2, 2))

conv_layer7 = nn.Sequential(nn.Conv2d(128, 256, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer8 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.Sigmoid())
conv_layer9 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.Sigmoid(),
                           nn.MaxPool2d(2, 2))

flatten = nn.Flatten()

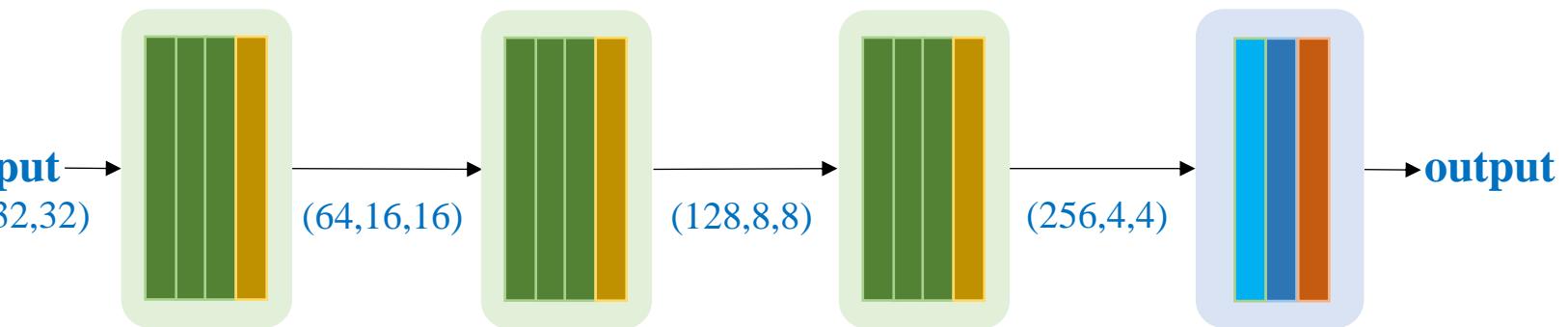
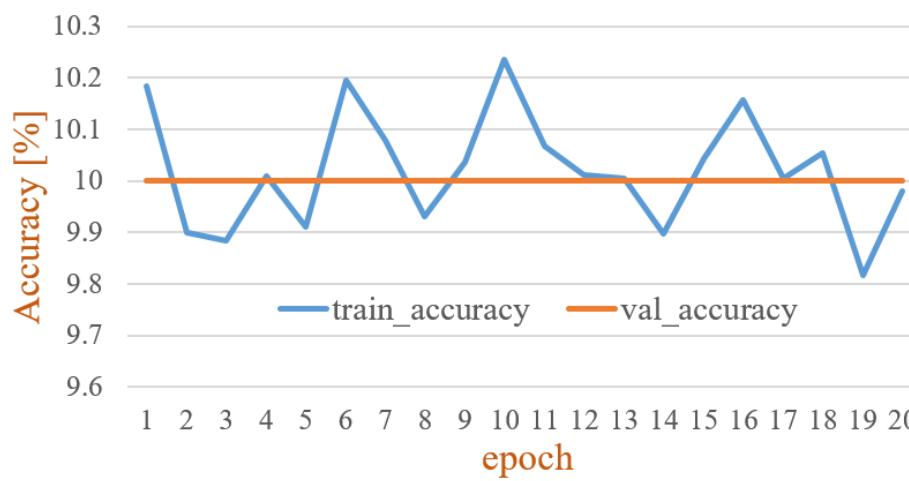
fc_layer1 = nn.Sequential(nn.Linear(256*4*4, 512), nn.Sigmoid())
fc_layer2 = nn.Linear(512, 10)
```

Network Training

❖ Cifar-10 dataset:

- ❖ Keep adding more layers

The network does not learn



(3x3) Convolution
padding='same'
stride=1 + Sigmoid

(2x2) max pooling

Flatten

Dense Layer-10
+ Softmax

Dense Layer-512
+ Sigmoid

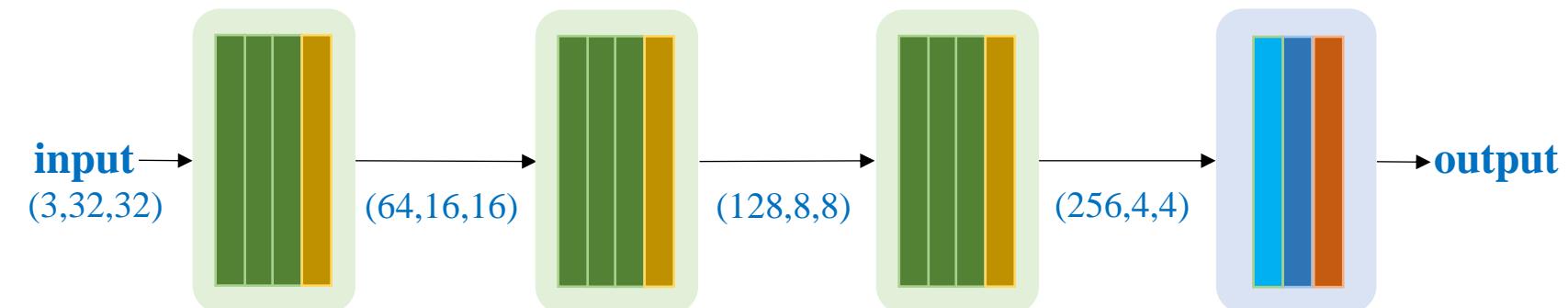
Network Training

❖ Cifar-10 dataset:

- ❖ Keep adding more layers

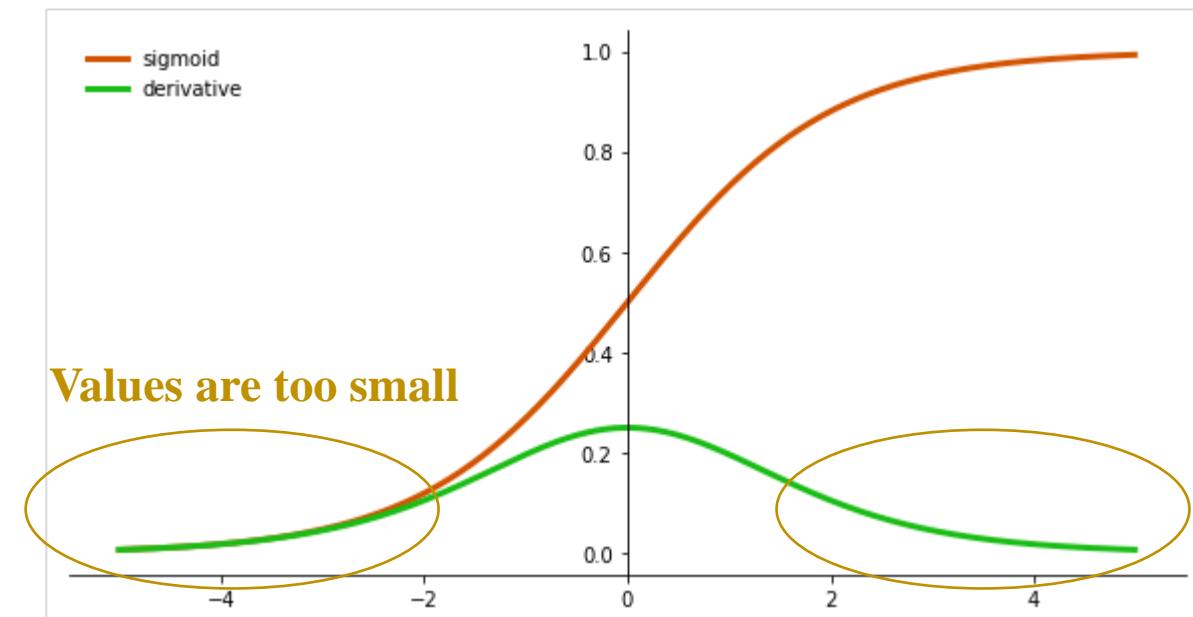
(3x3) Convolution
padding='same'
stride=1 + Sigmoid

Dense Layer-512
+ Sigmoid



$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

Vanishing Problem

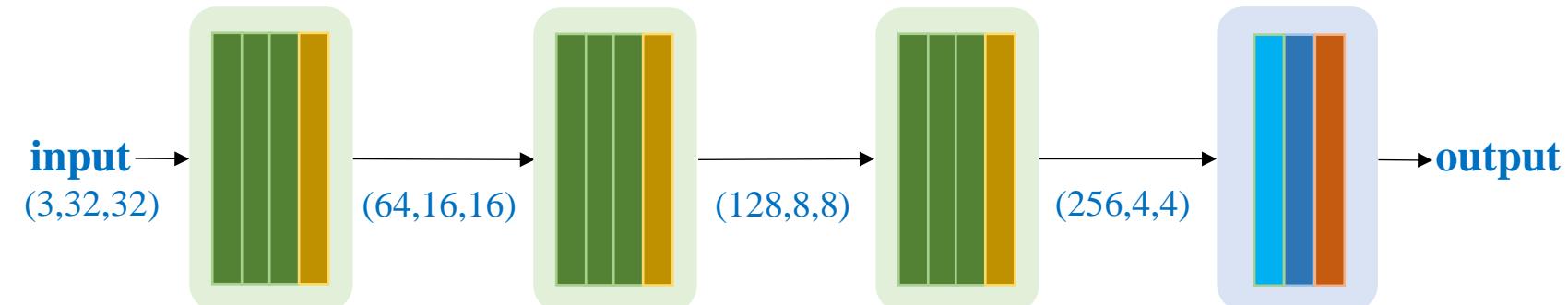


Network Training

❖ Cifar-10 dataset:

❖ Keep adding more layers

(3x3) Convolution
padding='same'
stride=1 + ReLU



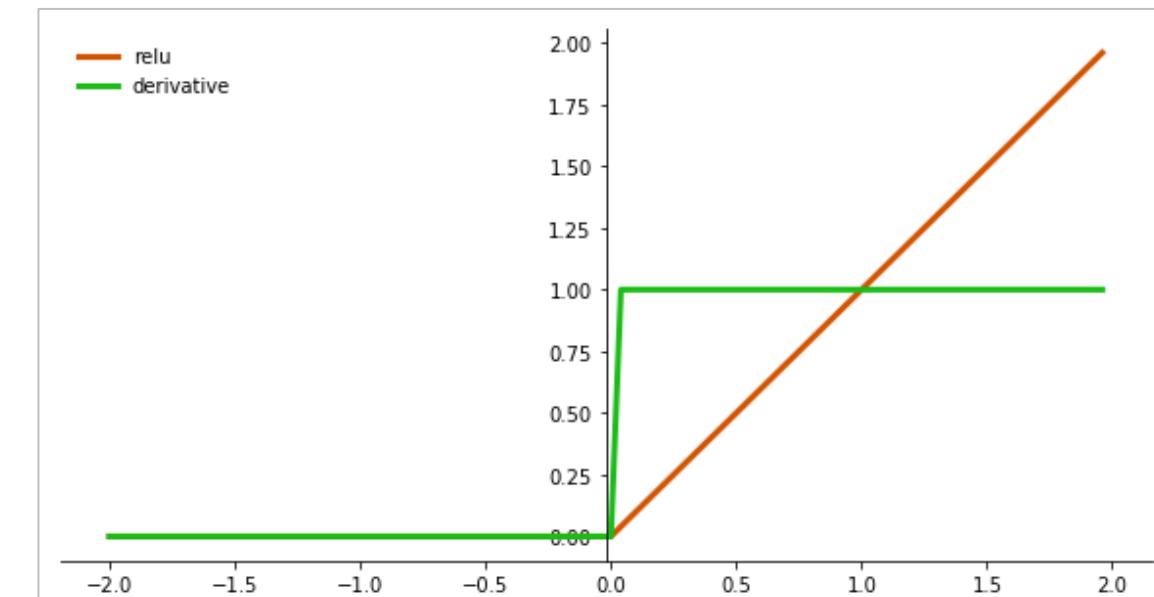
Dense Layer-512
+ ReLU

$$\text{ReLU}(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

nn.Conv2D(...), nn.Sigmoid()

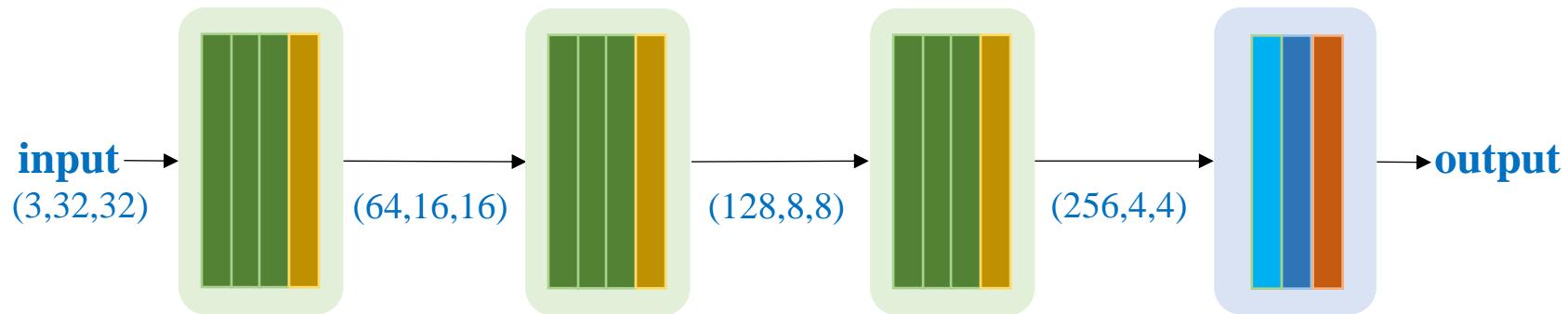


nn.Conv2D(...), nn.ReLU()



Network Training

- ❖ Cifar-10 dataset:
 - ❖ Use ReLU



```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU(),
                           nn.MaxPool2d(2, 2))

conv_layer4 = nn.Sequential(nn.Conv2d(64, 128, 3, stride=1, padding='same'), nn.ReLU())
conv_layer5 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU())
conv_layer6 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU(),
                           nn.MaxPool2d(2, 2))

conv_layer7 = nn.Sequential(nn.Conv2d(128, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer8 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer9 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU(),
                           nn.MaxPool2d(2, 2))

flatten = nn.Flatten()

fc_layer1 = nn.Sequential(nn.Linear(256*4*4, 512), nn.ReLU())
fc_layer2 = nn.Linear(512, 10)
```

(3x3) Convolution
padding='same'
stride=1 + ReLU

Flatten

(2x2) max pooling

Dense Layer-10
+ Softmax

Dense Layer-512
+ ReLU

Data normalization [0,1]

Glorot uniform initialization

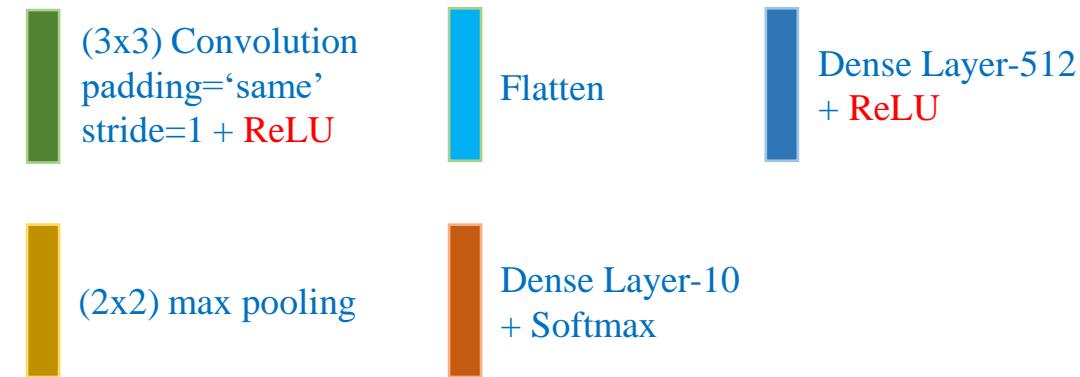
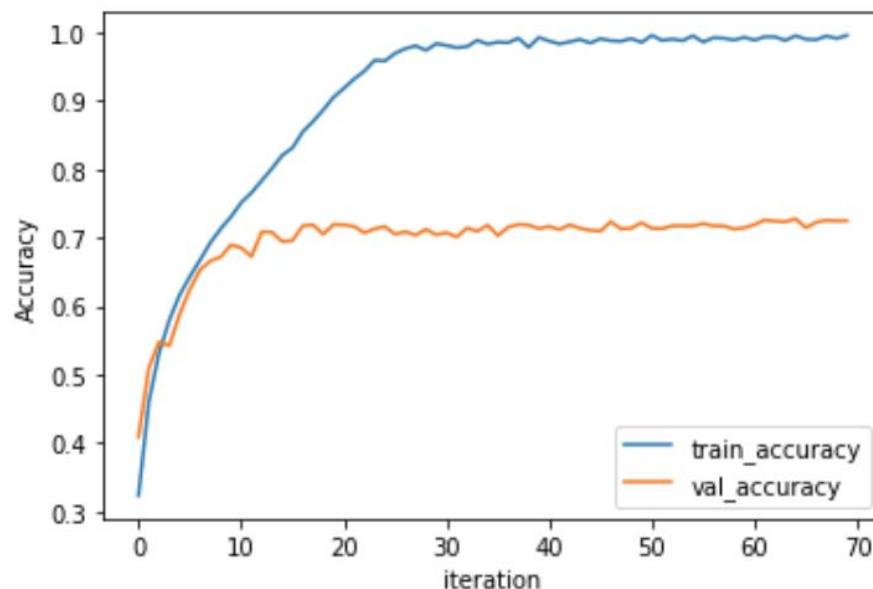
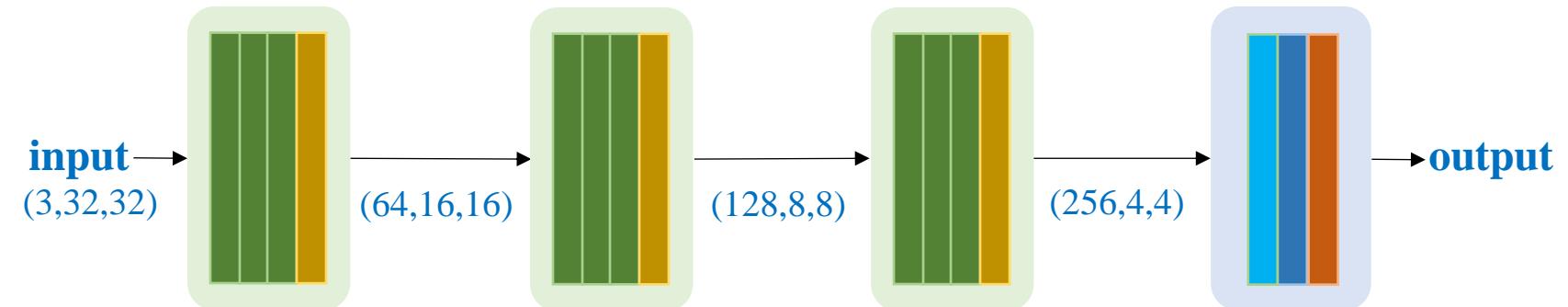
Adam optimizer with lr=1e-3

Network Training

❖ Cifar-10 dataset:

- ❖ Use ReLU

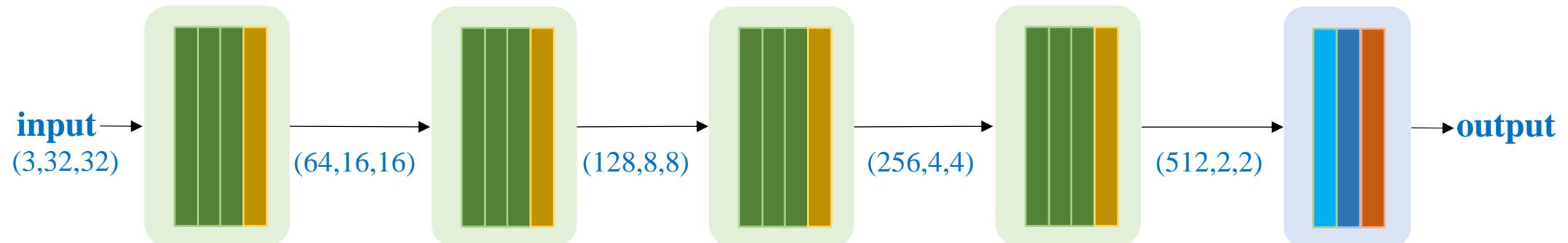
Training Accuracy reaches up to 99%



Adding more layers; Hope reach to 100%

Network Training

- ❖ Use ReLU and add more layers



Data normalization [0,1]
Glorot uniform initialization
Adam optimizer with lr=1e-3

(3x3) Convolution padding='same' stride=1 + ReLU
(2x2) max pooling
Flatten
Dense Layer-512 + ReLU
Dense Layer-10 + Softmax

Implementation

```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU(),
                           nn.MaxPool2d(2, 2))

conv_layer4 = nn.Sequential(nn.Conv2d(64, 128, 3, stride=1, padding='same'), nn.ReLU())
conv_layer5 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU(),)
conv_layer6 = nn.Sequential(nn.Conv2d(128, 128, 3, stride=1, padding='same'), nn.ReLU(),
                           nn.MaxPool2d(2, 2))

conv_layer7 = nn.Sequential(nn.Conv2d(128, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer8 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU())
conv_layer9 = nn.Sequential(nn.Conv2d(256, 256, 3, stride=1, padding='same'), nn.ReLU(),
                           nn.MaxPool2d(2, 2))

conv_layer10 = nn.Sequential(nn.Conv2d(256, 512, 3, stride=1, padding='same'), nn.ReLU())
conv_layer11 = nn.Sequential(nn.Conv2d(512, 512, 3, stride=1, padding='same'), nn.ReLU())
conv_layer12 = nn.Sequential(nn.Conv2d(512, 512, 3, stride=1, padding='same'), nn.ReLU(),
                           nn.MaxPool2d(2, 2))

flatten = nn.Flatten()

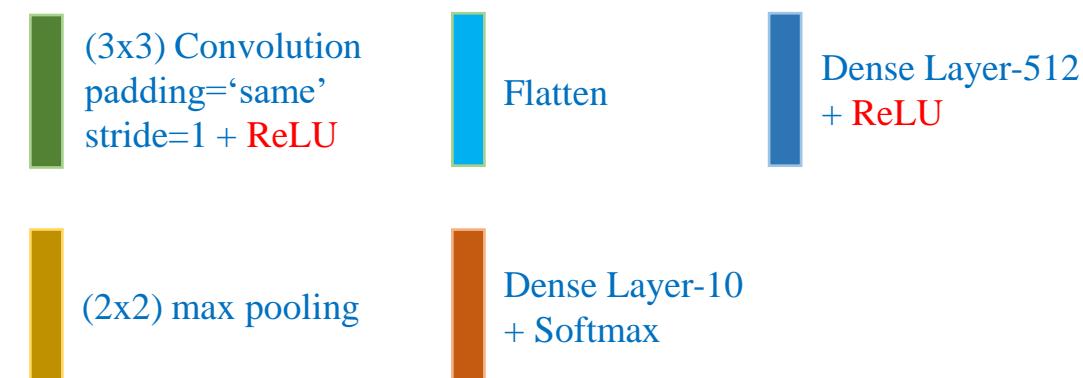
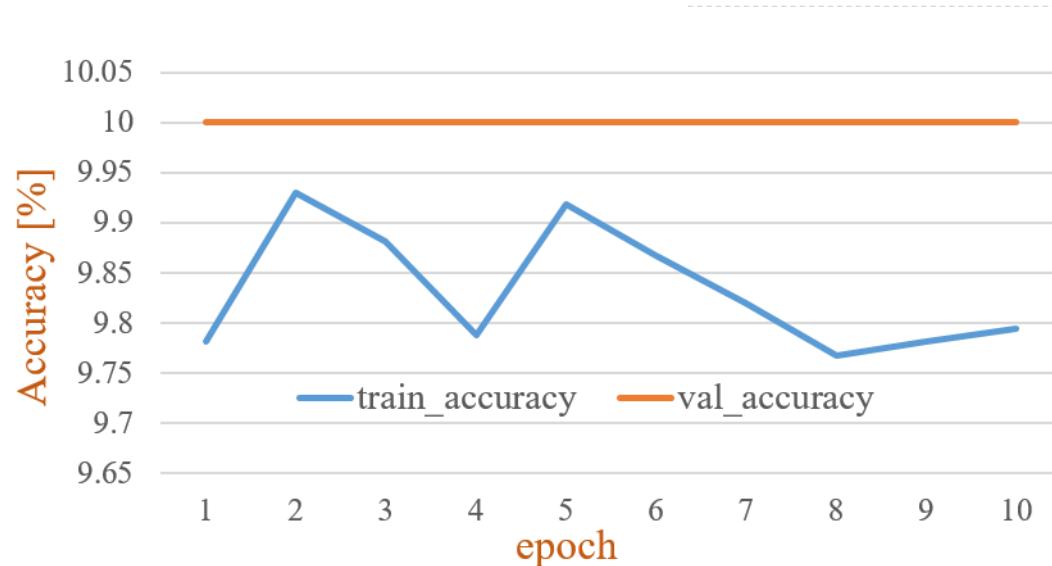
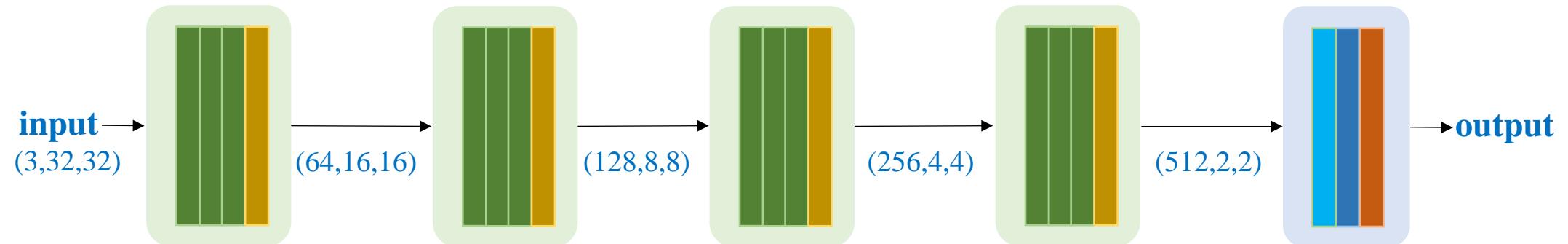
fc_layer1 = nn.Sequential(nn.Linear(512 * 2 * 2, 512), nn.ReLU())
fc_layer2 = nn.Linear(512, 10)
```

```
def initialize_weights(self):
    for m in self.modules():
        if isinstance(m, nn.Conv2d):
            init.xavier_uniform_(m.weight)
            if m.bias is not None:
                init.zeros_(m.bias)
        elif isinstance(m, nn.Linear):
            init.xavier_uniform_(m.weight)
            if m.bias is not None:
                init.zeros_(m.bias)

def forward(self, x):
    x = self.conv_layer1(x)
    x = self.conv_layer2(x)
    x = self.conv_layer3(x)
    x = self.conv_layer4(x)
    x = self.conv_layer5(x)
    x = self.conv_layer6(x)
    x = self.conv_layer7(x)
    x = self.conv_layer8(x)
    x = self.conv_layer9(x)
    x = self.conv_layer10(x)
    x = self.conv_layer11(x)
    x = self.conv_layer12(x)
    x = self.flatten(x)
    x = self.fc_layer1(x)
    out = self.fc_layer2(x)
    return out
```

Network Training

- ❖ Use ReLU and add more layers



Network does not learn again

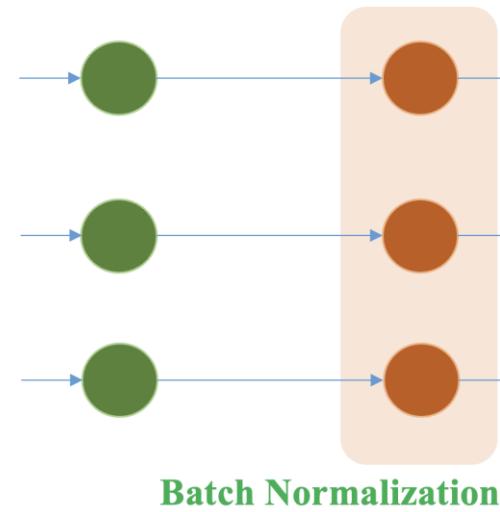
Outline

SECTION 1

Setting-up Context

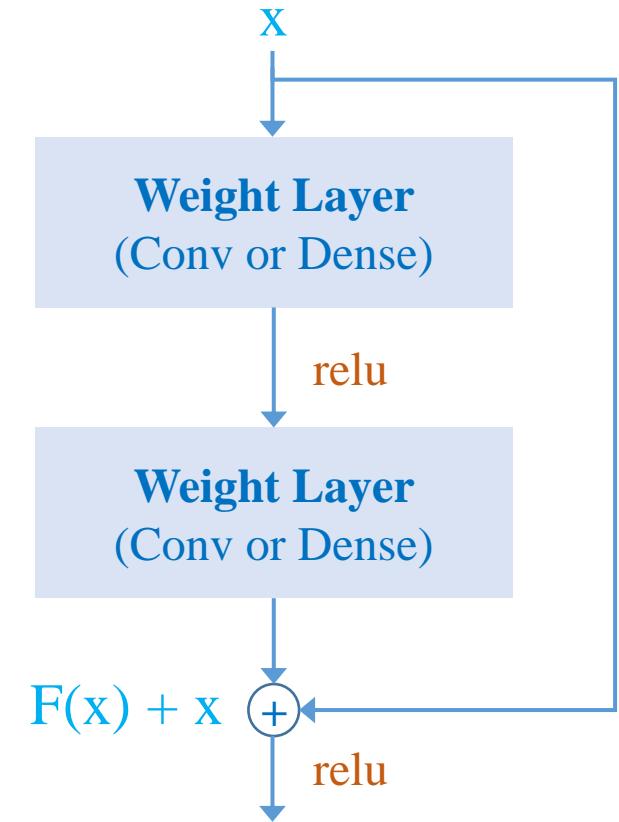
SECTION 2

Solutions for the Context



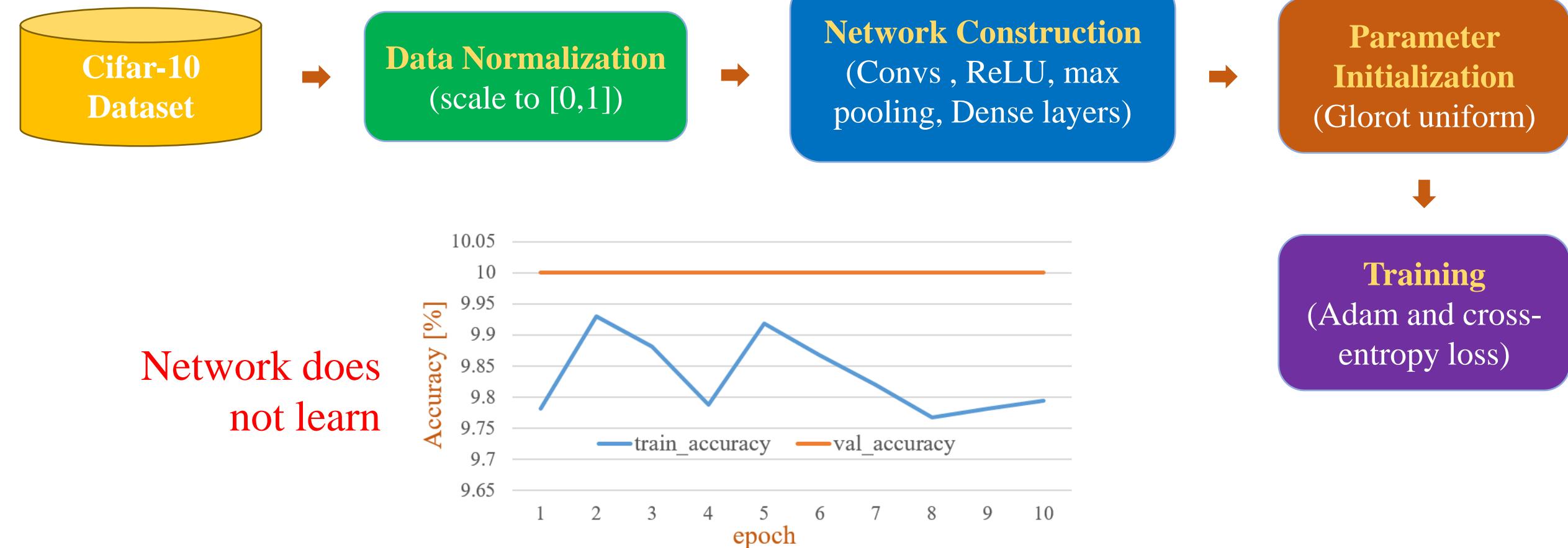
Batch Normalization

$F(x)$



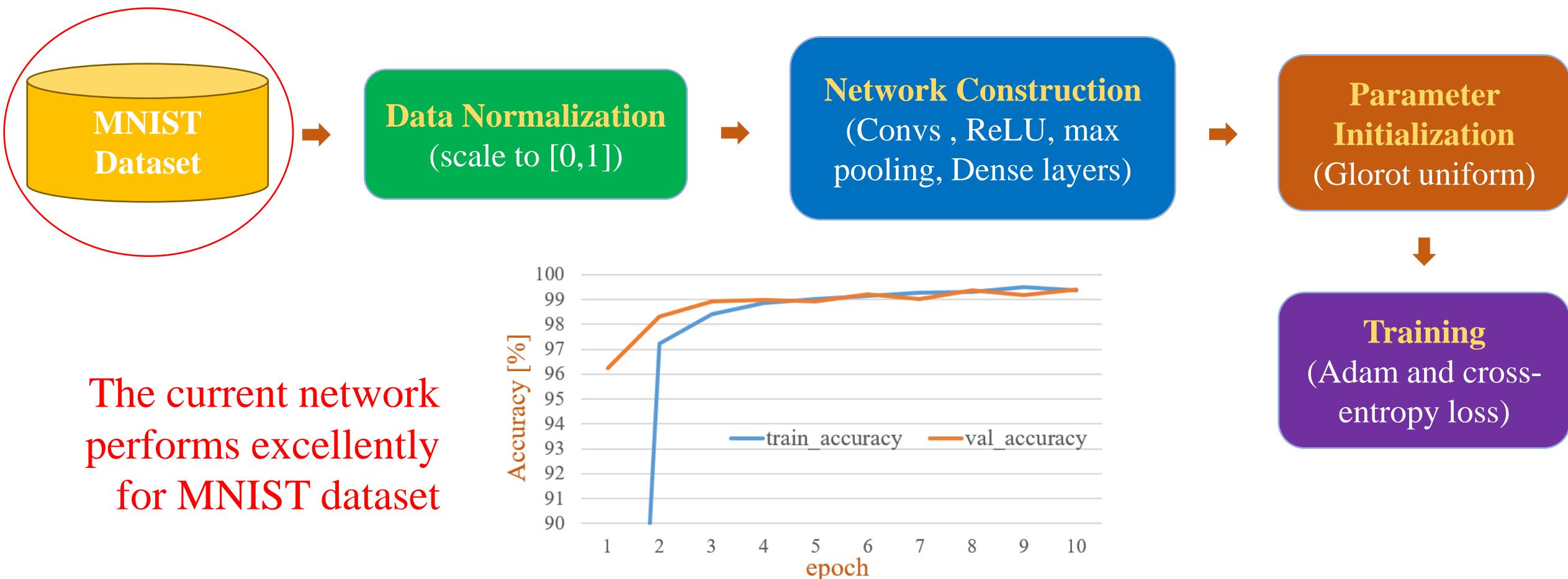
Network Training

❖ Summary of the current network



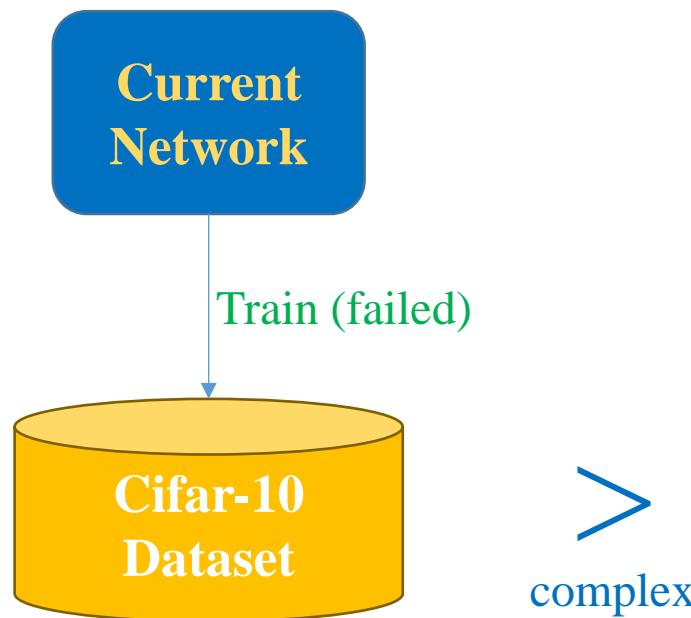
Network Training

❖ Solution 1: Observation



Network Training

❖ Solution 1: Idea

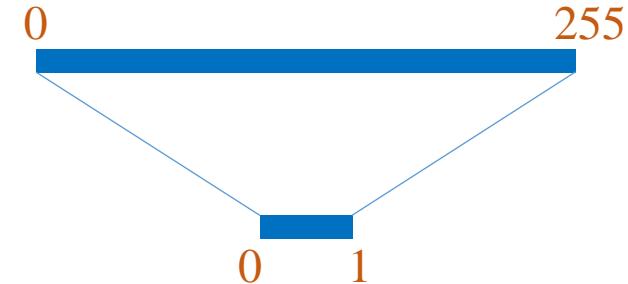


How to reduce the complexity of the Cifar-10 dataset

Data Normalization
(scale to [0,1])



Data Normalization
(convert to 0-mean and 1-deviation)



$$X = \frac{X - \mu}{\sigma}$$

$$\mu = \frac{1}{n} \sum_i X_i$$

$$\sigma = \sqrt{\frac{1}{n} \sum_i (X_i - \mu)^2}$$

Network Training

❖ Solution 1: Idea

$$\bar{X} = \frac{X - \mu}{\sigma}$$

$$\mu = \frac{1}{n} \sum_i X_i$$

$$\sigma = \sqrt{\frac{1}{n} \sum_i (X_i - \mu)^2}$$

This normalization helps network to be invariant to linear transformation

$$Y = aX + b$$

$$\bar{Y} = \frac{Y - \mu_Y}{\sigma_Y} = \bar{X}$$



$$Y = aX + b$$

$$\begin{aligned}\bar{Y} &= \frac{Y - \mu_Y}{\sigma_Y} = \frac{(aX + b) - \frac{1}{n} \sum_i (aX_i + b)}{\sqrt{\frac{1}{n} \sum_i \left((aX_i + b) - \frac{1}{n} \sum_i (aX_i + b) \right)^2}} \\ &= \frac{aX - \frac{1}{n} \sum_i aX_i}{\sqrt{\frac{1}{n} \sum_i \left(aX_i - \frac{1}{n} \sum_j aX_j \right)^2}} \\ &= \frac{X - \frac{1}{n} \sum_i X_i}{\sqrt{\frac{1}{n} \sum_i \left(X_i - \frac{1}{n} \sum_j X_j \right)^2}} = \frac{X - \mu_X}{\sqrt{\frac{1}{n} \sum_i (X_i - \mu_X)^2}} = \bar{X}\end{aligned}$$

Network Training

Solution 1: 0-mean and unit-deviation normalization

Data Normalization
(convert to 0-mean
and 1-deviation)

$$X = \frac{X - \mu_d}{\sigma_d}$$

μ_d is the mean of dataset

σ_d is the deviation for the whole dataset

```
# Load dataset with only the ToTensor transform
compute_transform = transforms.Compose([transforms.ToTensor()])
dataset = torchvision.datasets.CIFAR10(root='data', train=True,
                                         transform=compute_transform,
                                         download=True)
loader = torch.utils.data.DataLoader(dataset, batch_size=1024,
                                         shuffle=False, num_workers=4)

mean = 0.0
for images, _ in loader:
    batch_samples = images.size(0) # Batch size
    images = images.view(batch_samples, images.size(1), -1)
    mean += images.mean(2).sum(0)
mean = mean / len(loader.dataset)

variance = 0.0
for images, _ in loader:
    batch_samples = images.size(0)
    images = images.view(batch_samples, images.size(1), -1)
    variance += ((images - mean.unsqueeze(1))**2).sum([0,2])
std = torch.sqrt(variance / (len(loader.dataset)*32*32))

# Data
transform = Compose([ToTensor(),
                     Normalize(mean, std)])
train_set = CIFAR10(root='data', train=True,
                     download=True, transform=transform)
trainloader = DataLoader(train_set, batch_size=256,
                        shuffle=True, num_workers=4)
```

Network Training

❖ Solution 1: 0-mean and unit-deviation normalization

Data Normalization
(convert to 0-mean
and 1-deviation)

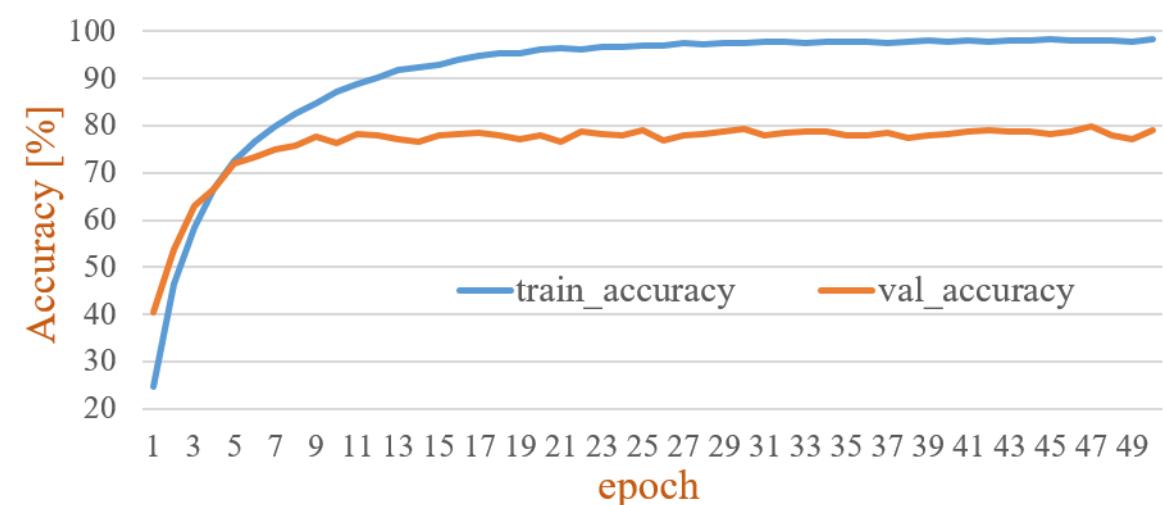
$$X = \frac{X - \mu_d}{\sigma_d}$$

μ_d is the mean of dataset

σ_d is the deviation for the whole dataset

Normalize each channel separately

```
transform = Compose([ToTensor(),
                     Normalize([0.4914, 0.4822, 0.4465],
                               [0.2470, 0.2435, 0.2616])])
train_set = CIFAR10(root='data', train=True,
                     download=True, transform=transform)
```

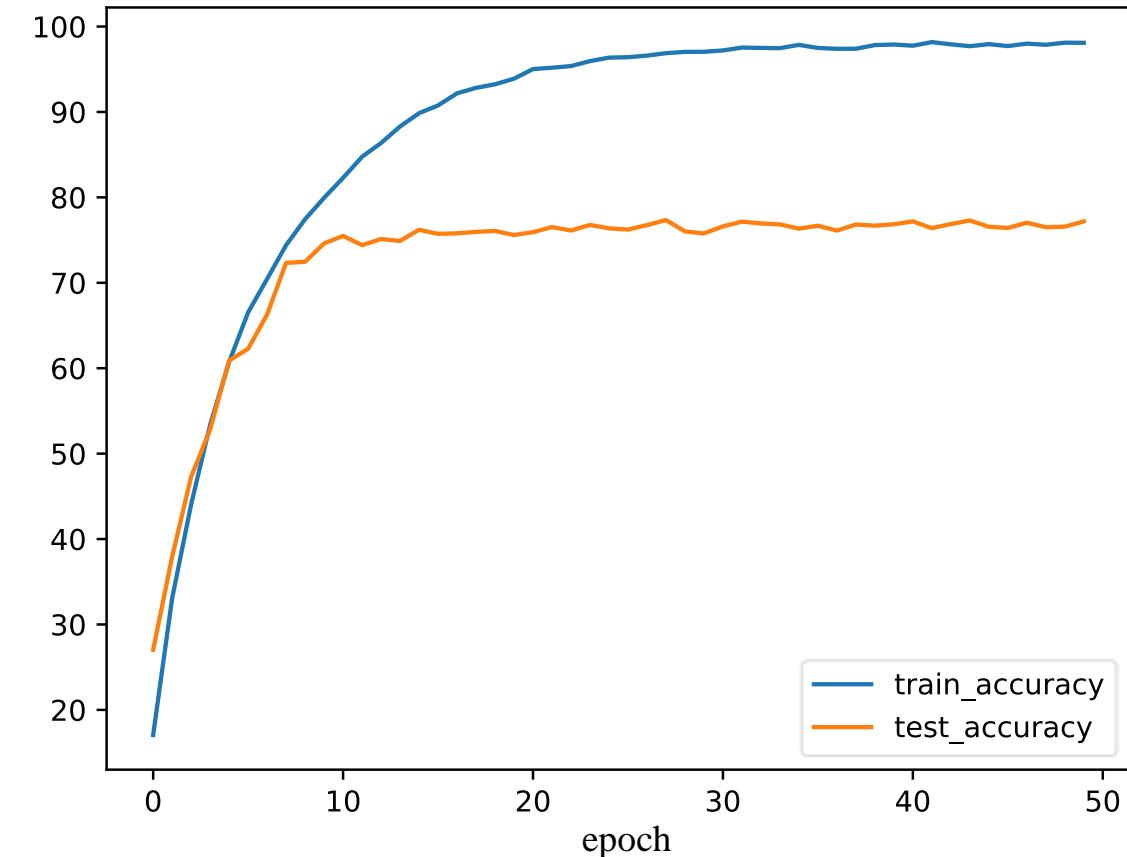
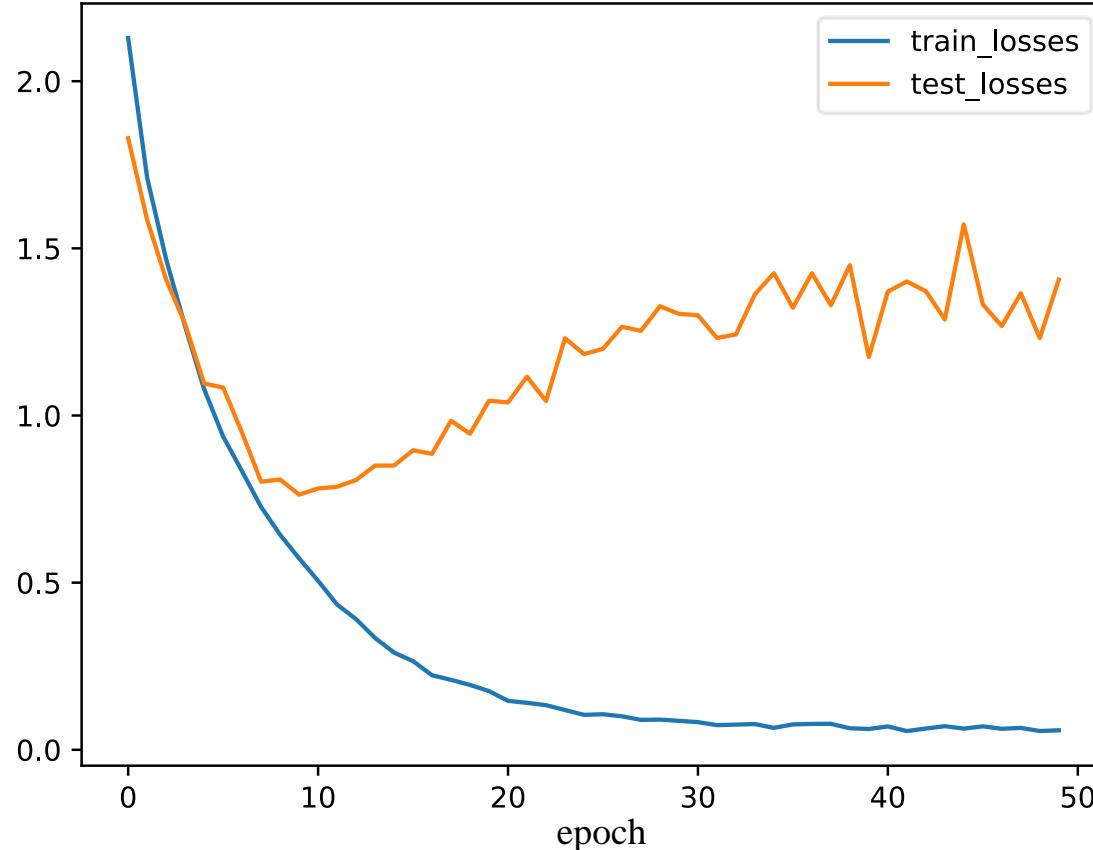


Network Training

❖ Solution 1 (extension):
Normalize to [-1, 1]

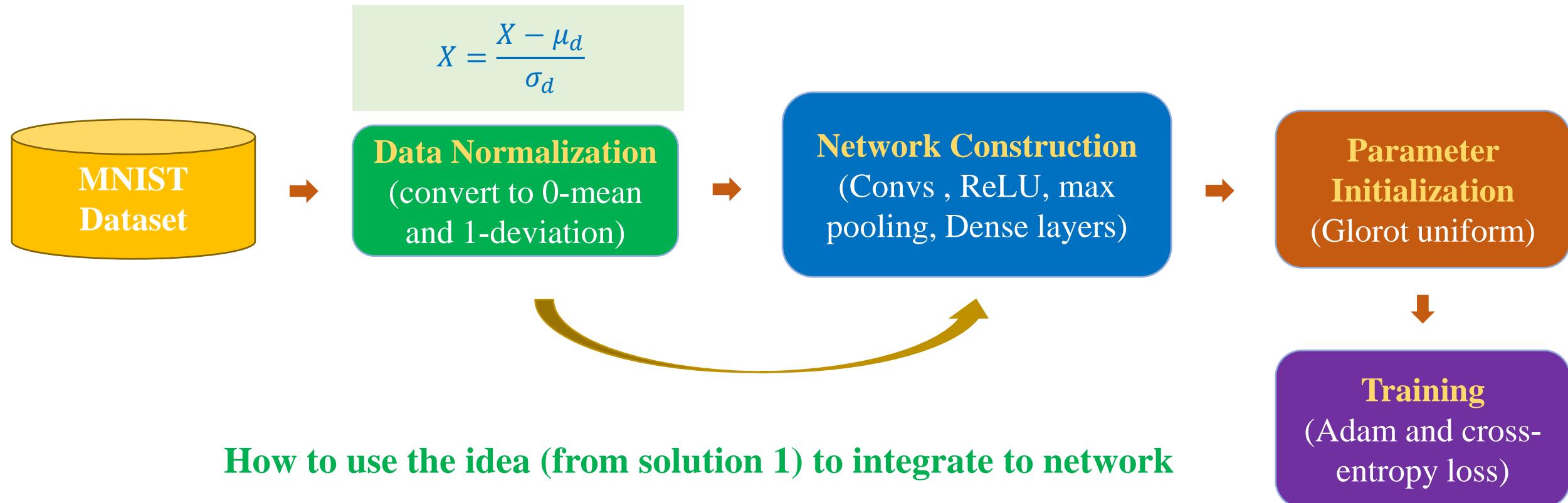
Normalize each channel separately

```
transform = Compose([ToTensor(),
                     Normalize((0.5, 0.5, 0.5),
                               (0.5, 0.5, 0.5))])
train_set = CIFAR10(root='data', train=True,
                     download=True, transform=transform)
```



Network Training

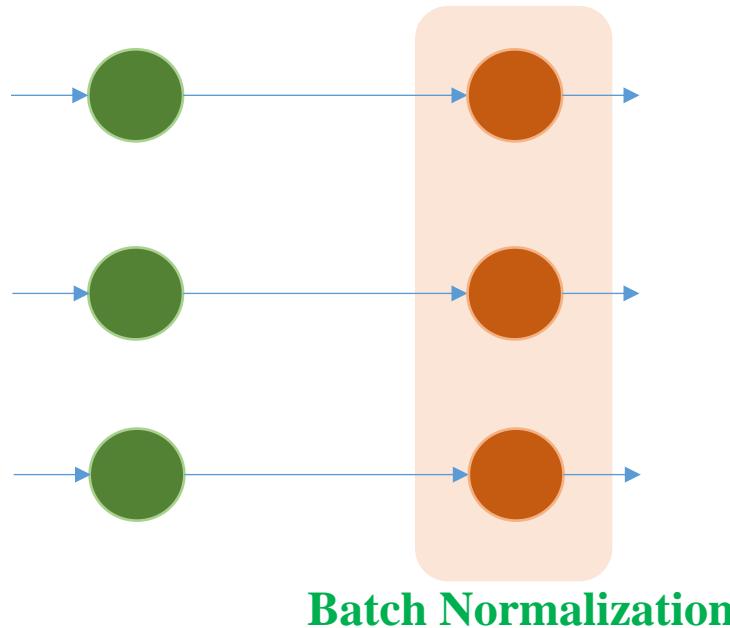
❖ Solution 2



Batch Normalization

Network Training

❖ Solution 2: Batch normalization



Do not need bias when using BN*

μ and σ are updated in forward pass
 γ and β are updated in backward pass

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

m is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize X_i

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

ϵ is a very small value

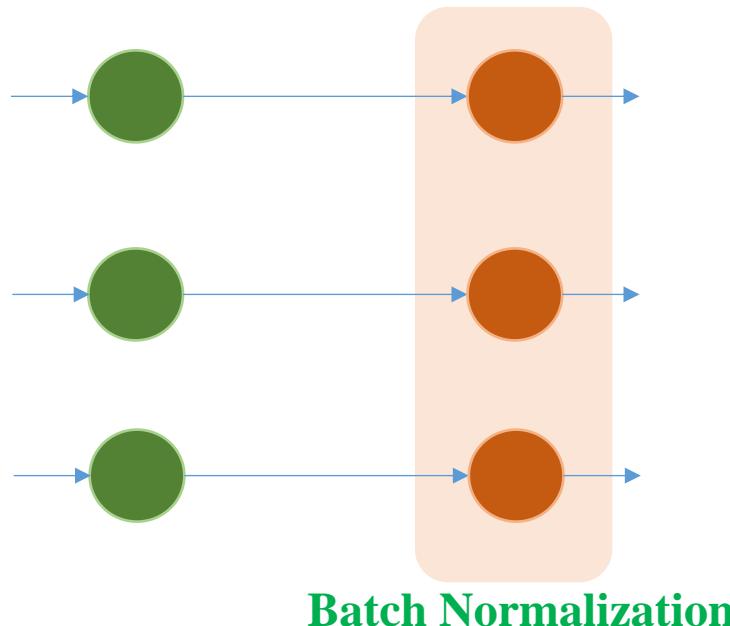
Scale and shift \hat{X}_i

$$Y_i = \gamma \hat{X}_i + \beta$$

γ and β are two learning parameters

Network Training

❖ Solution 2: Batch normalization



What if
 $\gamma = \sqrt{\sigma^2 + \epsilon}$ and $\beta = \mu$

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

m is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize X_i

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

ϵ is a very small value

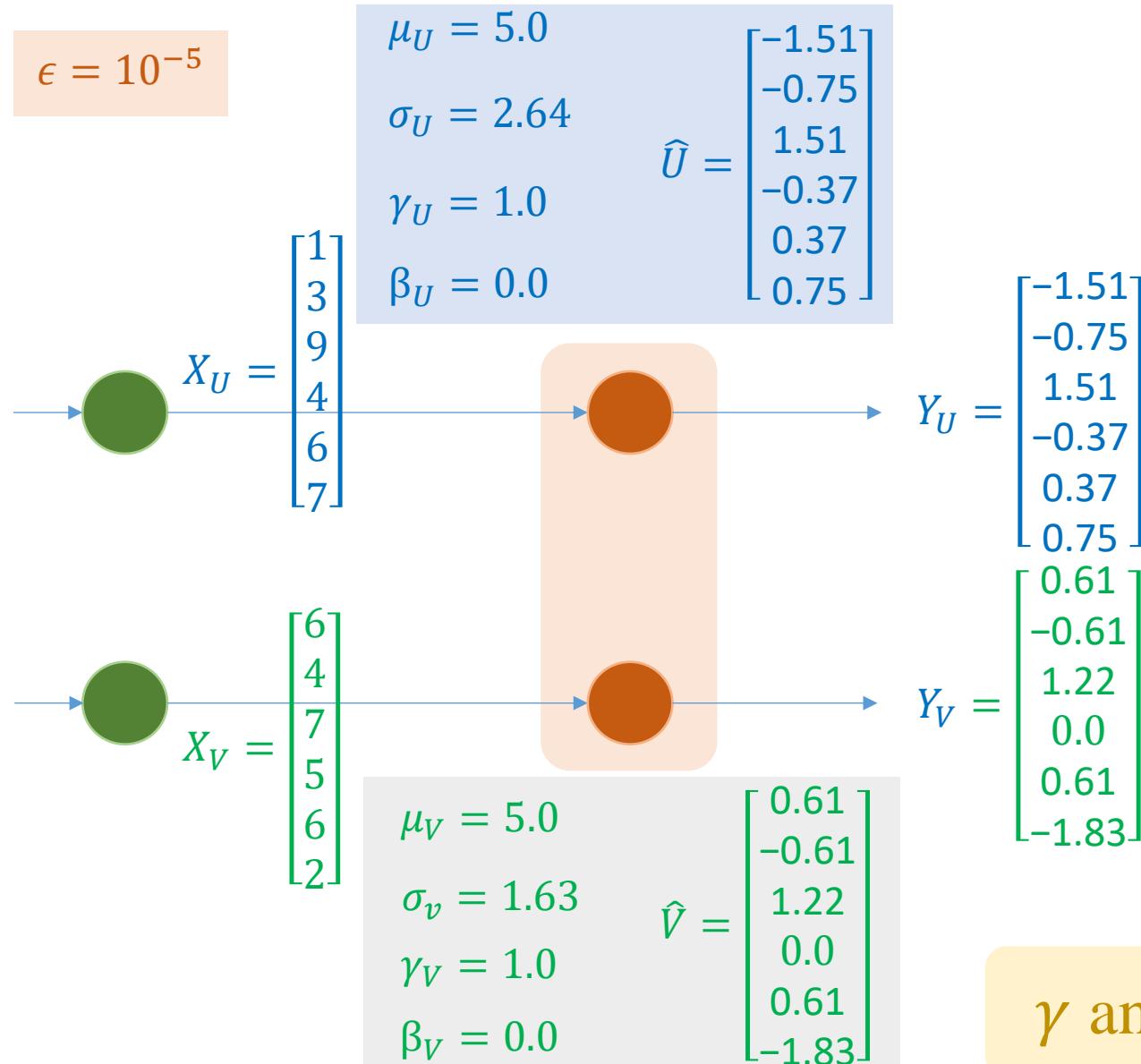
Scale and shift \hat{X}_i

$$Y_i = \gamma \hat{X}_i + \beta$$

γ and β are two learning parameters

Network Training

$$\epsilon = 10^{-5}$$



Solution 2: Batch normalization

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

m is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize X_i

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

ϵ is a very small value

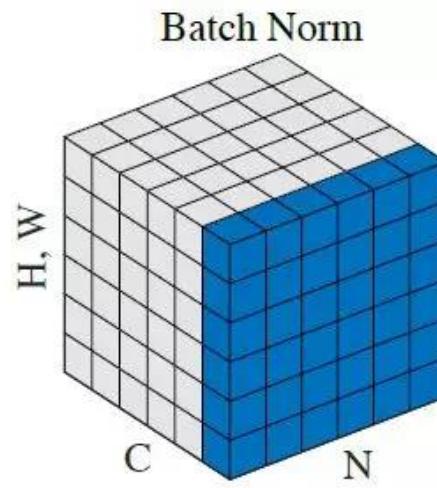
Scale and shift \hat{X}_i

$$Y_i = \gamma \hat{X}_i + \beta$$

γ and β are two learning parameters

γ and β are updated in training process

Batch Normalization



$$\epsilon = 10^{-5}$$

$$\mu_c = \frac{1}{N \times H \times W} \sum_{i=1}^N \sum_{j=1}^H \sum_{k=1}^W F_{ijk}$$

$$\sigma_c = \sqrt{\frac{1}{N \times H \times W} \sum_{i=1}^N \sum_{j=1}^H \sum_{k=1}^W (F_{ijk} - \mu_c)^2}$$

$$\mu = 2.5$$

$$\sigma^2 = 6.58$$

$$\gamma = 1.0$$

$$\beta = 0.0$$

<https://arxiv.org/pdf/1803.08494.pdf>

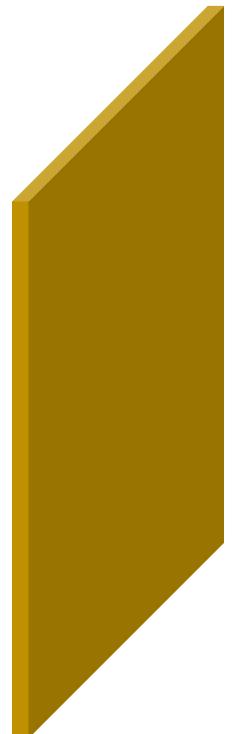
sample 1 sample 2 sample 3

$$X = \left\{ \begin{bmatrix} 7 & 5 \\ 0 & 4 \end{bmatrix}, \begin{bmatrix} 0 & 7 \\ 3 & 1 \end{bmatrix}, \begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \right\}$$



batch-size = 3

input_shape = (BS=3, C=1, H=2, W=2)



$$\hat{X} = \left\{ \begin{bmatrix} 1.75 & 0.97 \\ -0.97 & 0.58 \\ -0.97 & 1.75 \\ 0.19 & -0.58 \\ -0.19 & -0.97 \\ -0.97 & -0.58 \end{bmatrix} \right\}$$



$$\hat{Y} = \left\{ \begin{bmatrix} 1.75 & 0.97 \\ -0.97 & 0.58 \\ -0.97 & 1.75 \\ 0.19 & -0.58 \\ -0.19 & -0.97 \\ -0.97 & -0.58 \end{bmatrix} \right\}$$

Network Training

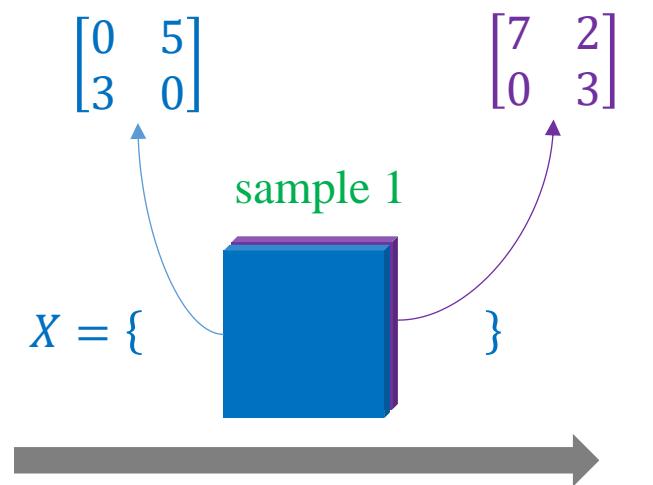
$$\epsilon = 10^{-5}$$

$$\mu = [2.0, 3.0]$$

$$\sigma^2 = [6.0, 8.67]$$

$$\gamma = 1.0$$

$$\beta = 0.0$$



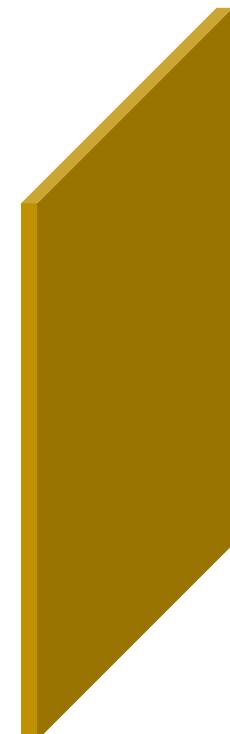
$$\hat{X} = \left\{ \begin{bmatrix} -0.94 & 1.41 \\ 0.47 & -0.94 \\ 1.56 & -0.39 \\ -1.17 & 0 \end{bmatrix} \right\}$$



$$\hat{Y} = \left\{ \begin{bmatrix} -0.94 & 1.41 \\ 0.47 & -0.94 \\ 1.56 & -0.39 \\ -1.17 & 0 \end{bmatrix} \right\}$$

batch-size = 1

sample_shape = (BS=1, C=2, H=2, W=2)

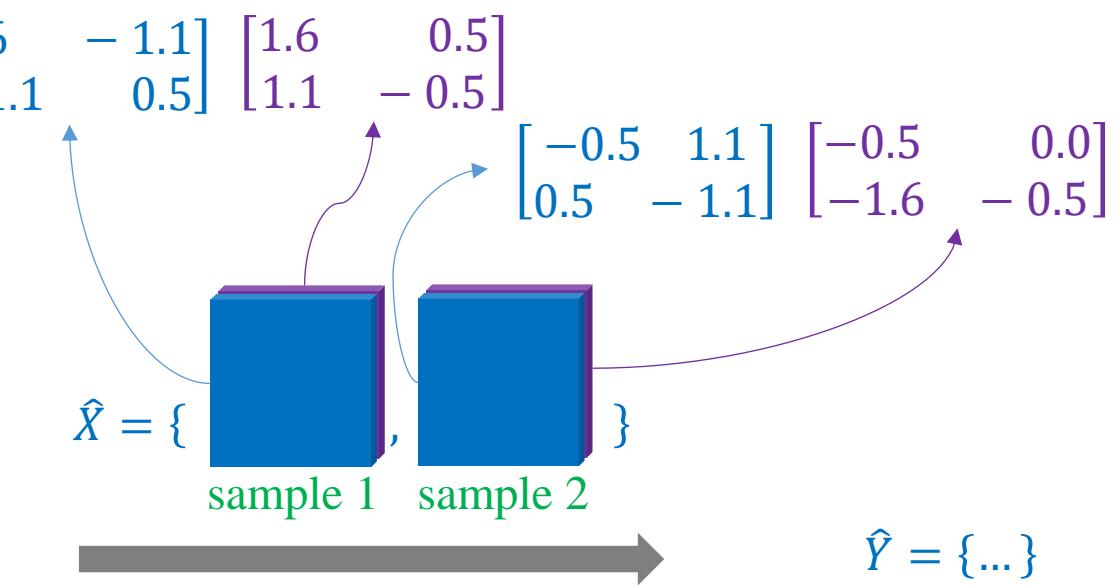
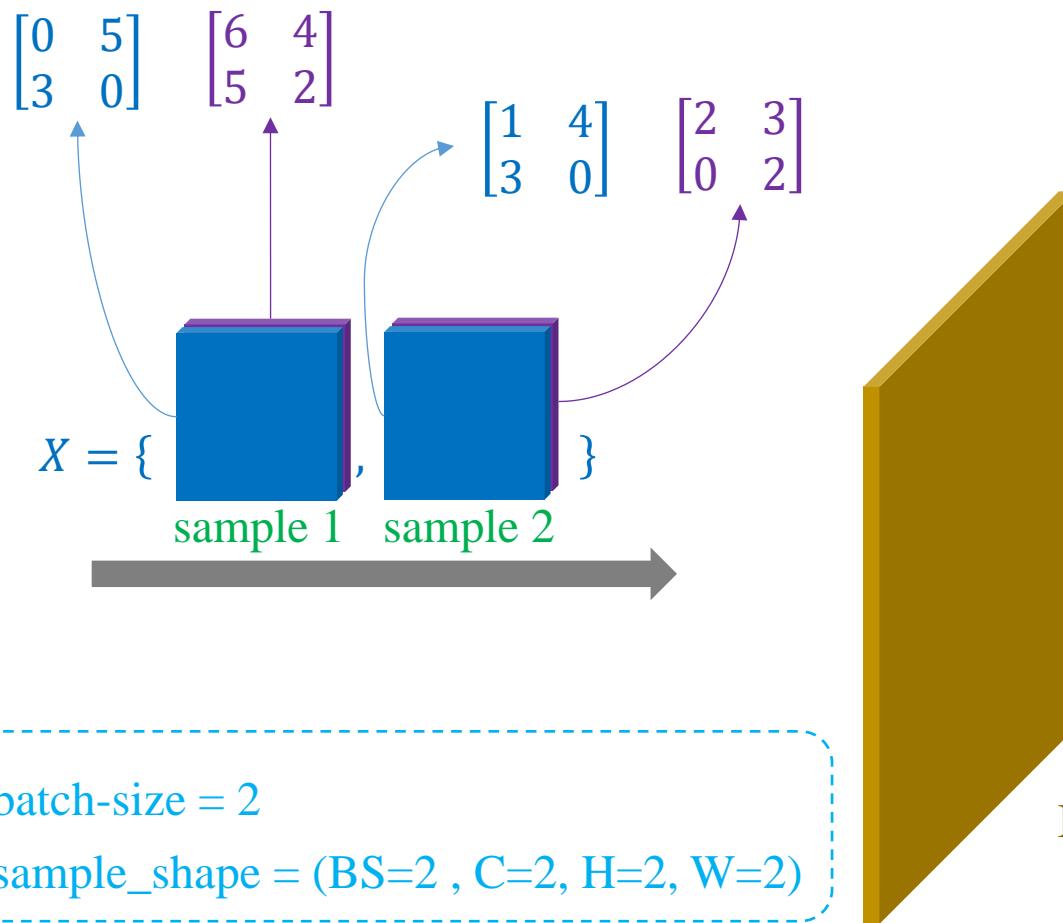


Network Training

$$\epsilon = 10^{-5}$$

$$\mu = [2.0, 3.0]$$
$$\sigma^2 = [4.0, 3.7]$$

$$\gamma = 1.0$$
$$\beta = 0.0$$



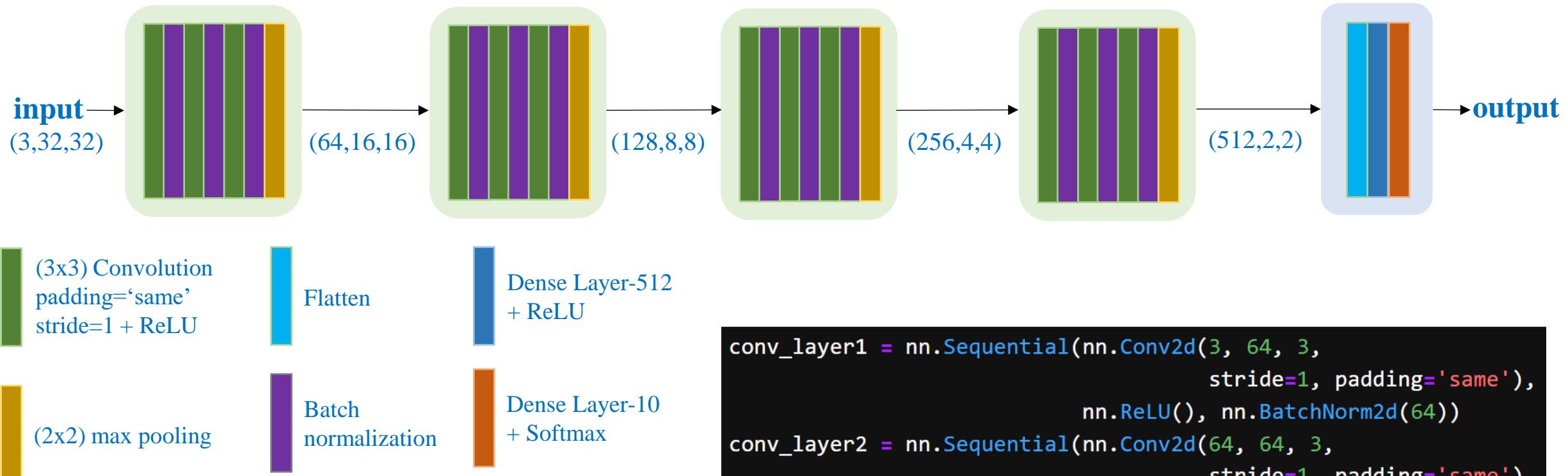
batch-size = 2

sample_shape = (BS=2 , C=2, H=2, W=2)

Batch-Norm Layer

Network Training

❖ Solution 2: Batch normalization



`torch.nn.BatchNorm2d(num_features)`
num_features (int): C from an expected input of size (N, C, H, W)

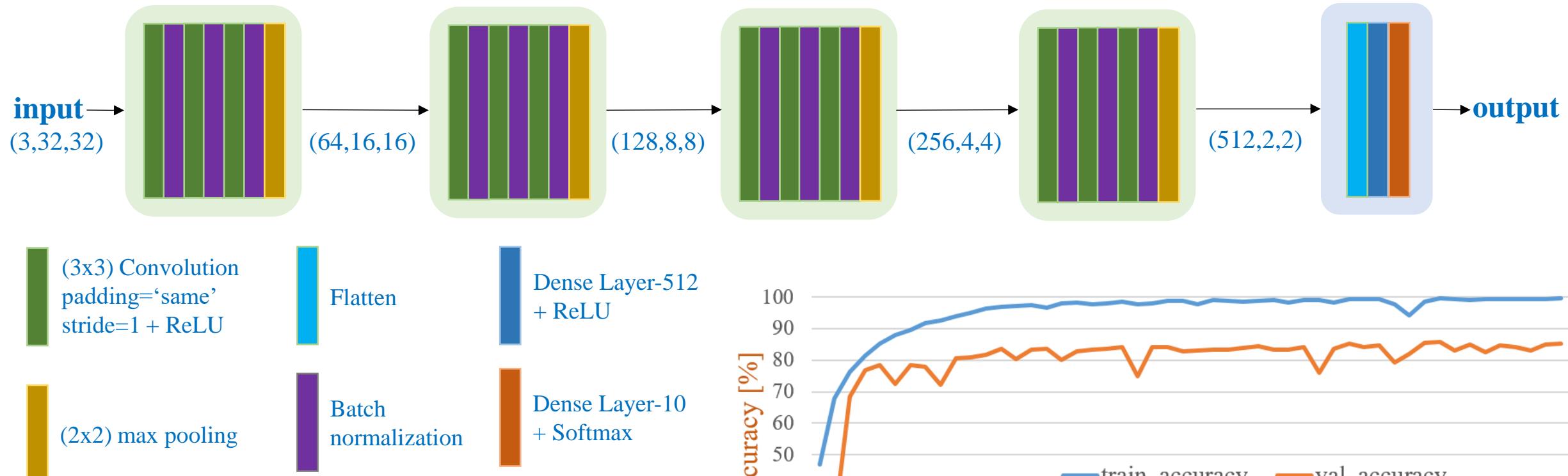
```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3,
                                    stride=1, padding='same'),
                           nn.ReLU(), nn.BatchNorm2d(64))

conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3,
                                    stride=1, padding='same'),
                           nn.ReLU(), nn.BatchNorm2d(64))

conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3,
                                    stride=1, padding='same'),
                           nn.ReLU(), nn.BatchNorm2d(64),
                           nn.MaxPool2d(2, 2))
```

Network Training

❖ Solution 2: Batch normalization



```
conv = nn.Sequential(nn.Conv2d(3, 64, 3),  
                     nn.ReLU(),  
                     nn.BatchNorm2d(64))
```

Network Training

❖ Solution 2: Batch normalization

- Speed up training
- Reduce the dependence on initial weights
- Model Generalization

Input data for a node in batch normalization layer

$$X = \{X_1, \dots, X_m\}$$

m is mini-batch size

Compute mean and variance

$$\mu = \frac{1}{m} \sum_{i=1}^m X_i \quad \sigma^2 = \frac{1}{m} \sum_{i=1}^m (X_i - \mu)^2$$

Normalize X_i

$$\hat{X}_i = \frac{X_i - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

ϵ is a very small value

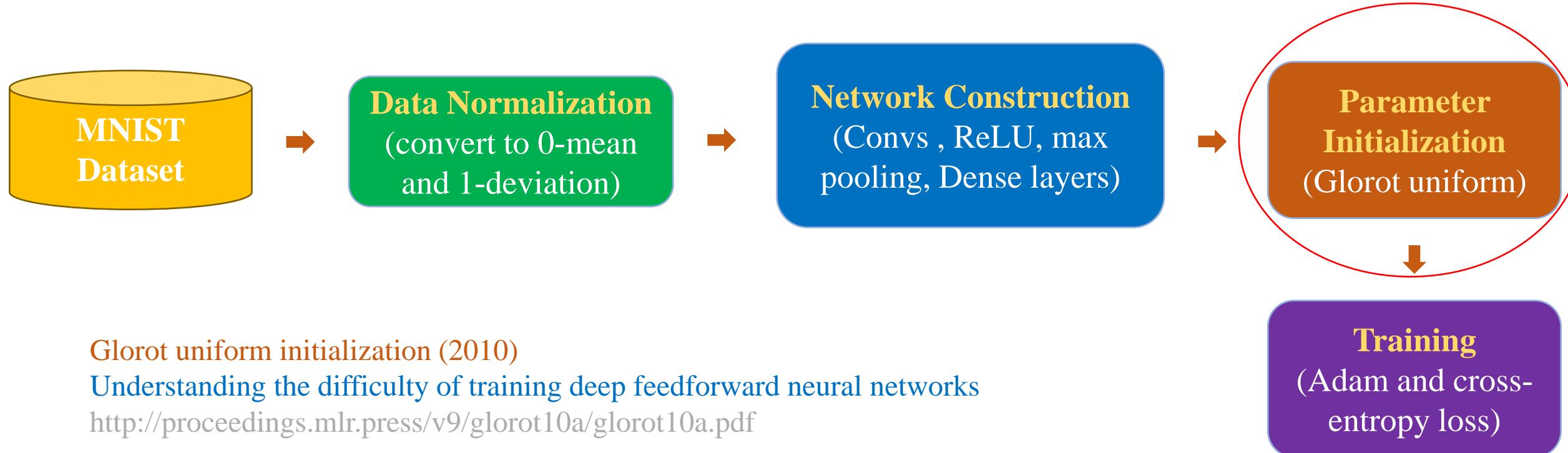
Scale and shift \hat{X}_i

$$Y_i = \gamma \hat{X}_i + \beta$$

γ and β are two learning parameters

Network Training

❖ Solution 3: Use more robust initialization



Glorot uniform initialization (2010)

Understanding the difficulty of training deep feedforward neural networks

<http://proceedings.mlr.press/v9/glorot10a/glorot10a.pdf>

He initialization (2015)

Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification

<https://arxiv.org/pdf/1502.01852.pdf>

Network Training

❖ Solution 3: He Initialization

Glorot initialization (2010)

$$W \sim \mathcal{N}\left(0, \frac{1}{n_j}\right)$$

n_j is #inputs in layer j

Assuming activation functions are linear

He initialization (2015)

Taking activation function into account

Adapt to ReLU activation

$$W \sim \mathcal{N}\left(0, \frac{2}{n_j}\right)$$

```
def initialize_weights(self):
    for m in self.modules():
        if isinstance(m, nn.Conv2d):
            init.kaiming_normal_(m.weight,
                                  nonlinearity='relu')
            if m.bias is not None:
                init.zeros_(m.bias)
        elif isinstance(m, nn.Linear):
            init.kaiming_normal_(m.weight,
                                  nonlinearity='relu')
            if m.bias is not None:
                init.zeros_(m.bias)
```

Data normalization [0,1]

He normal initialization

Adam optimizer with lr=1e-3

Network Training

❖ Solution 3: He Initialization

Glorot initialization (2010)

$$W \sim \mathcal{N} \left(0, \frac{1}{n_j} \right)$$

n_j is #inputs in layer j

Assuming activation functions are linear

He initialization (2015)

Taking activation function into account

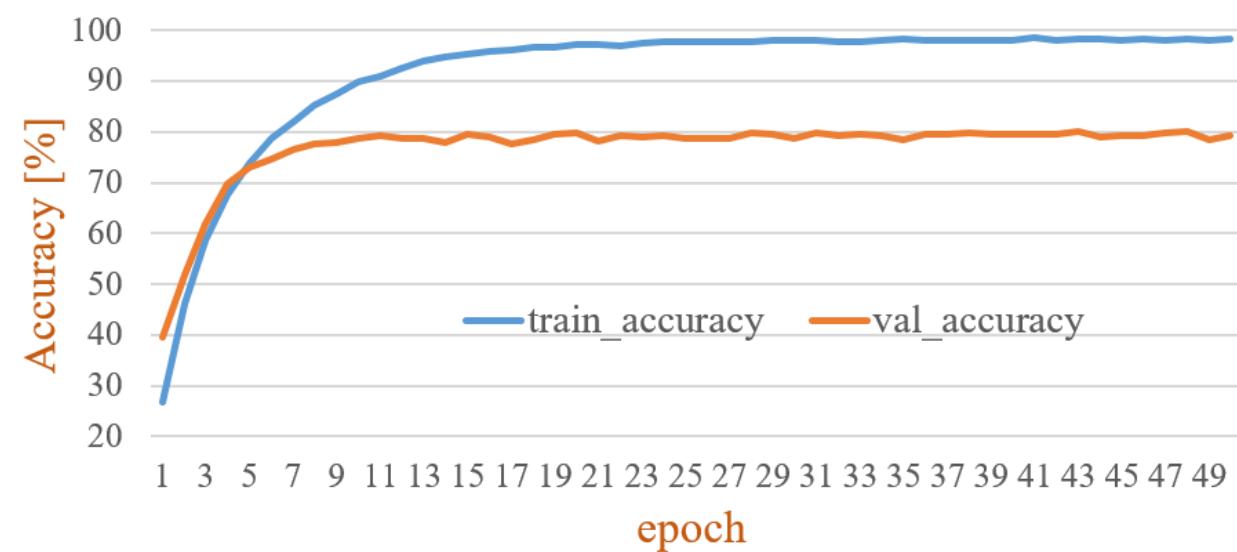
Adapt to ReLU activation

$$W \sim \mathcal{N} \left(0, \frac{2}{n_j} \right)$$

Data normalization [0,1]

He normal initialization

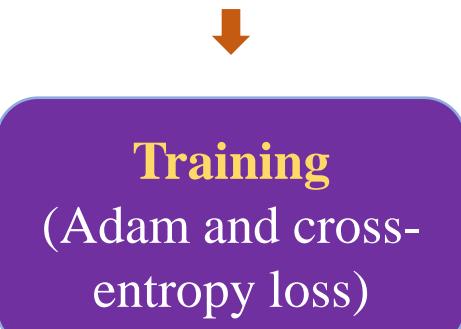
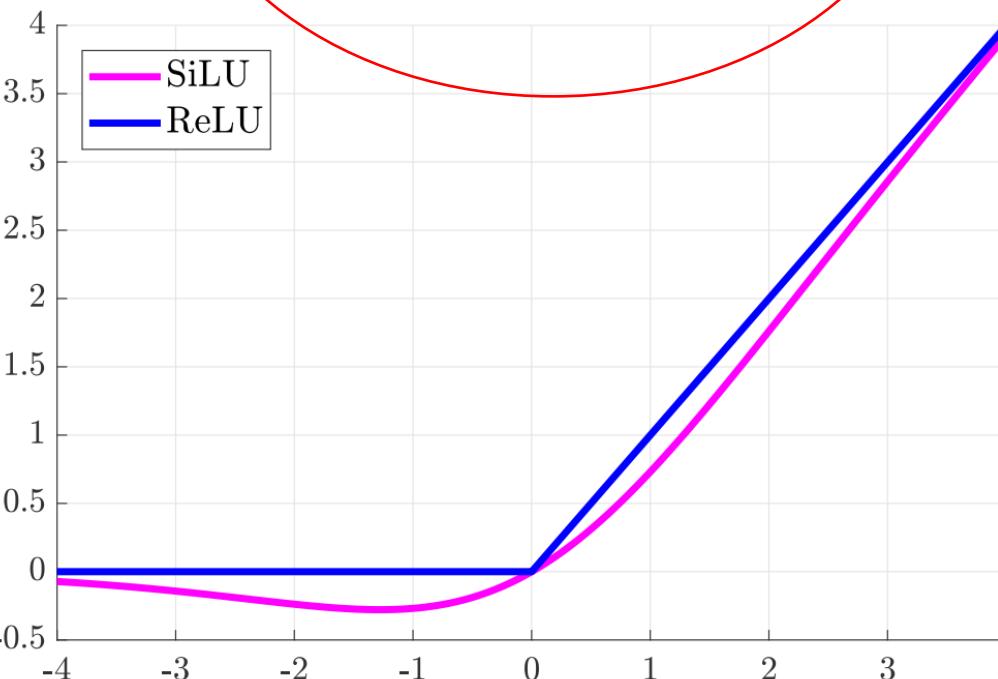
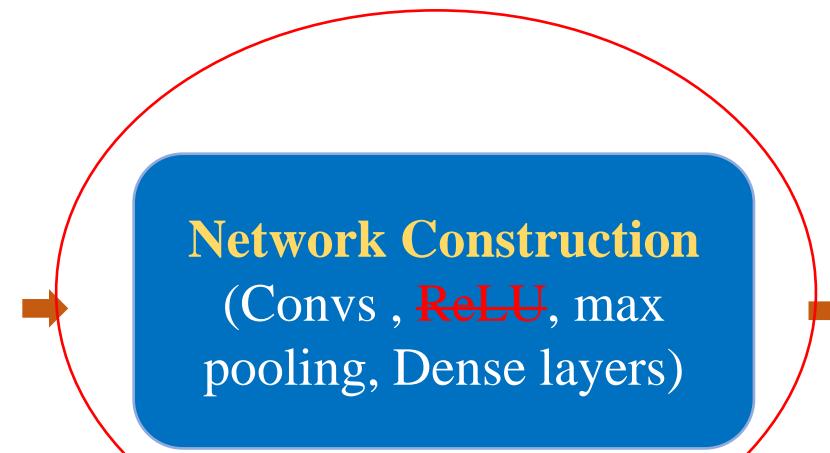
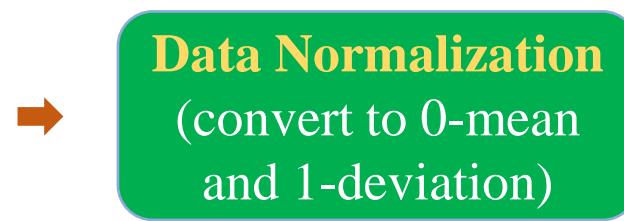
Adam optimizer with lr=1e-3



Network Training

❖ Solution 4: Using advanced activation

SwiGLU(.), 2020



2017 Sigmoid Linear Unit (SiLU)

$$\text{Swish}(x) = x * \frac{1}{1 + e^{-x}}$$

2010

$$\text{ReLU}(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

```
conv_layer1 = nn.Sequential(  
    nn.Conv2d(3, 64, 3, stride=1, padding=1),  
    nn.SiLU()  
)
```

<https://arxiv.org/pdf/1702.03118.pdf>

Network Training

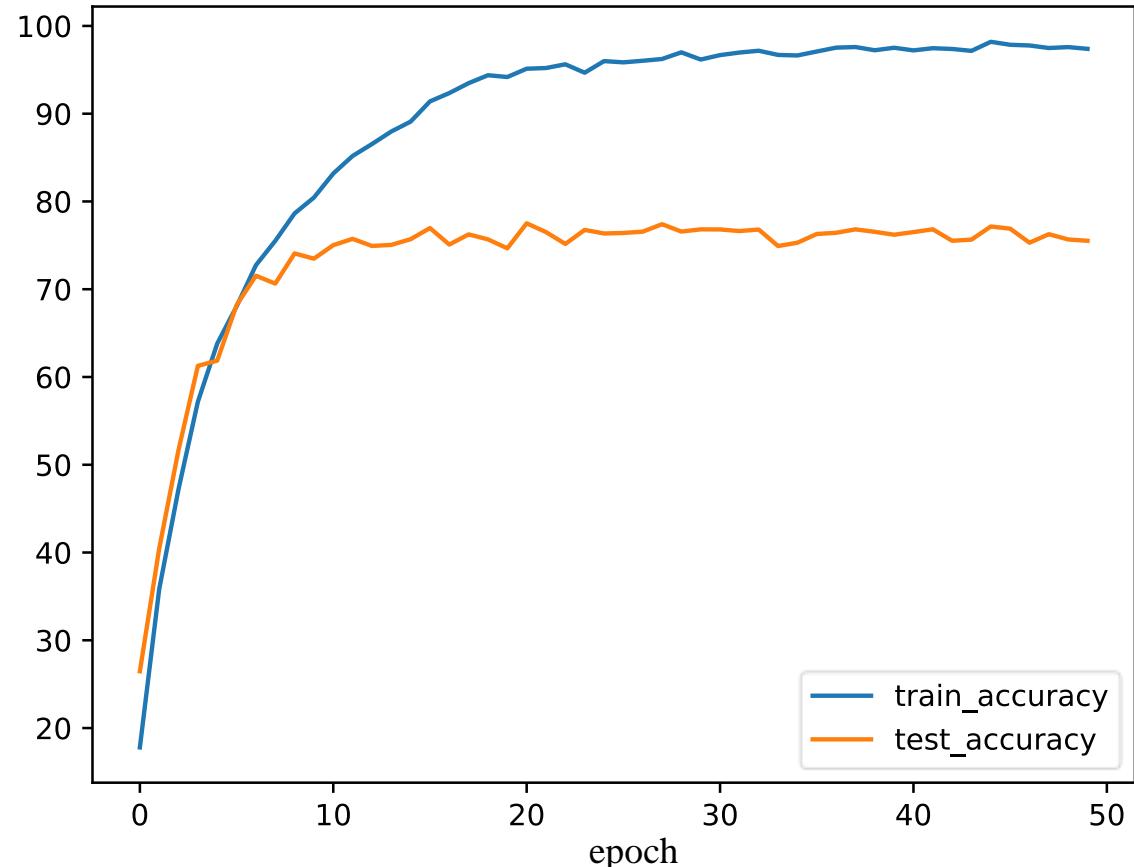
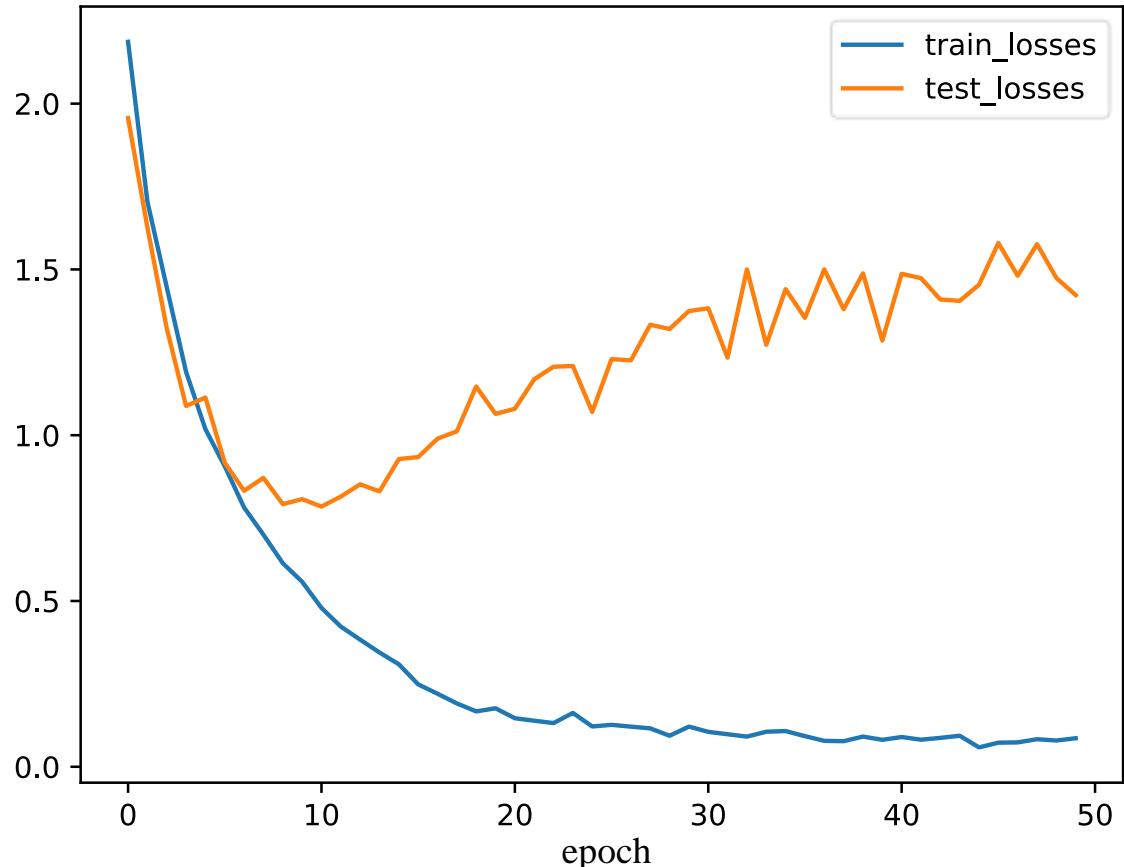
❖ Solution 4: Using advanced activation

2017 Sigmoid Linear Unit (SiLU)

$$\text{swish}(x) = x * \frac{1}{1 + e^{-x}}$$

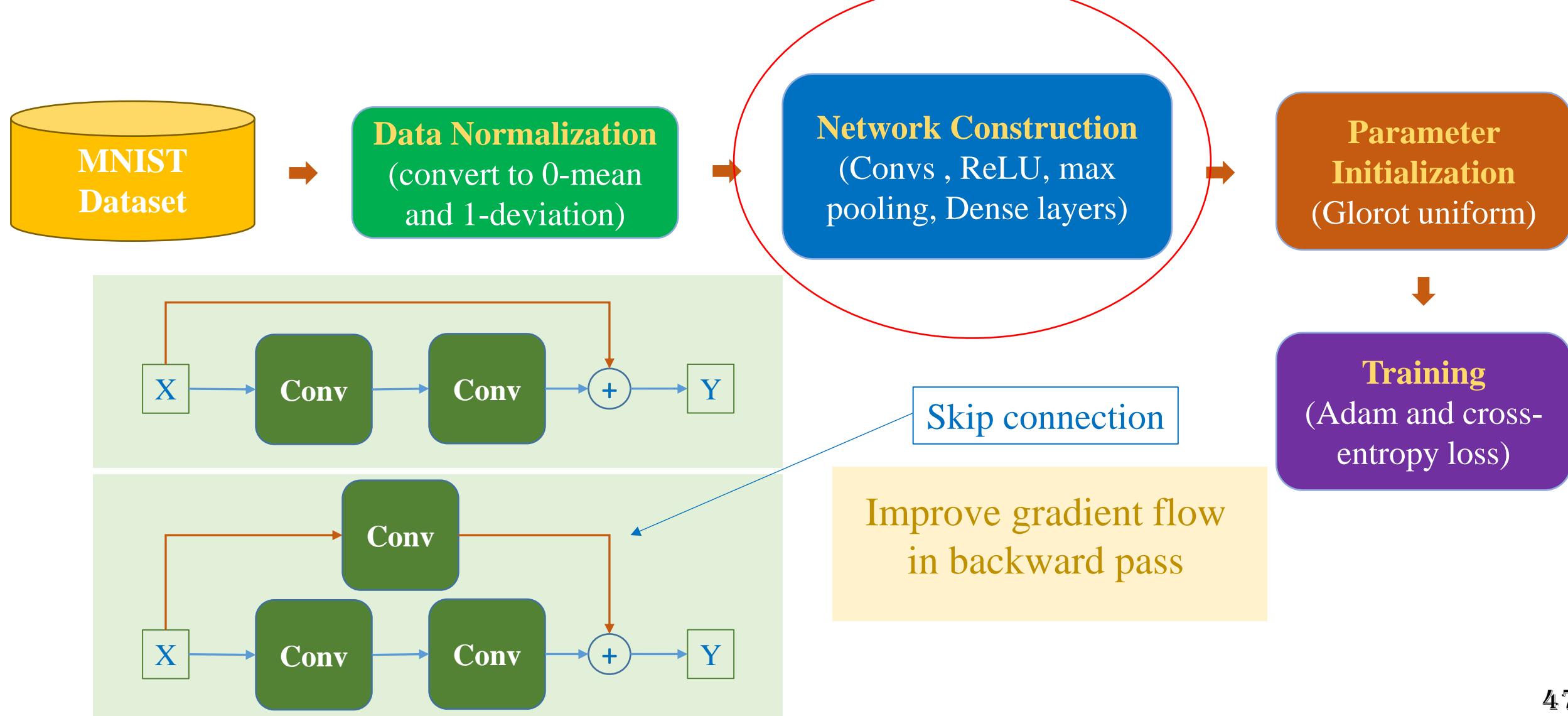
```
conv_layer1 = nn.Sequential(  
    nn.Conv2d(3, 64, 3, stride=1, padding=1),  
    nn.SiLU()  
)
```

<https://arxiv.org/pdf/1702.03118.pdf>



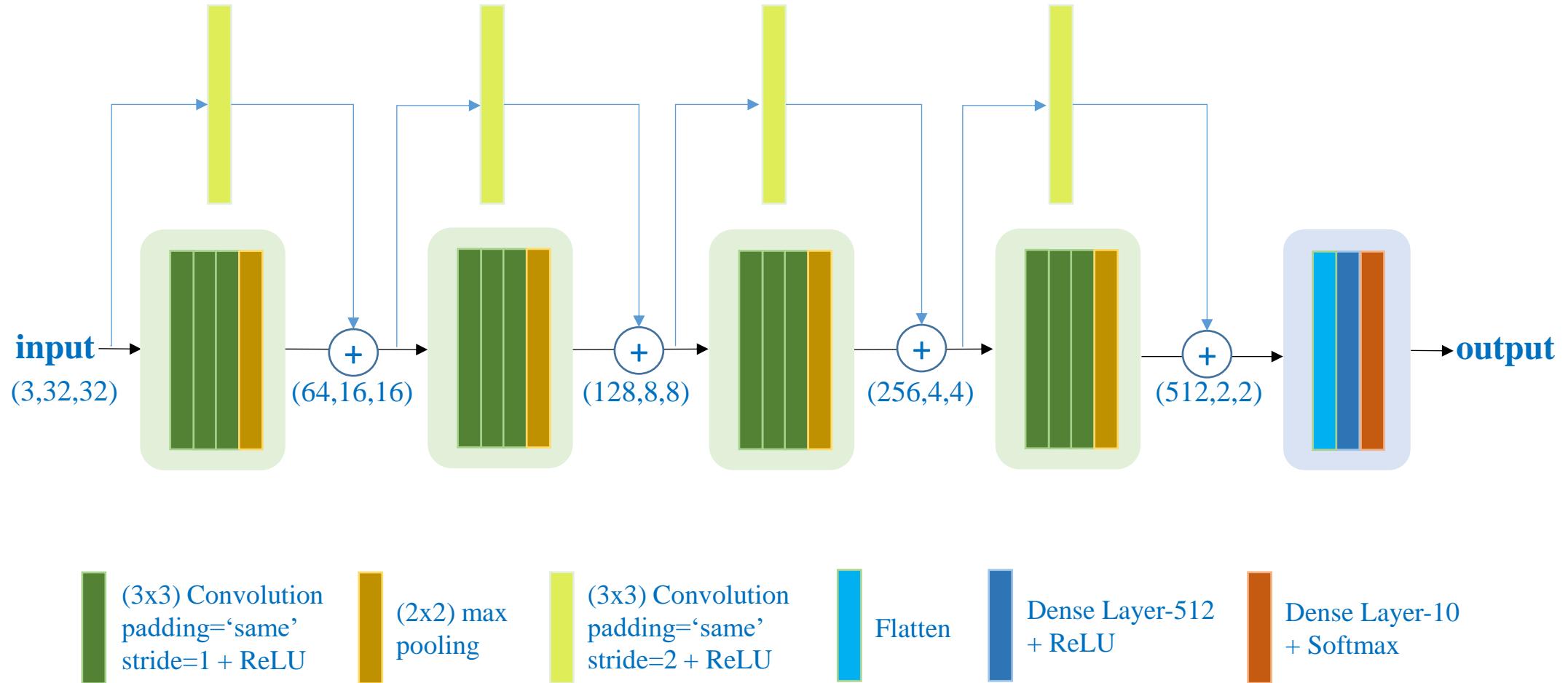
Network Training

❖ Solution 5: Skip connection



Network Training

❖ Solution 5: Skip connection

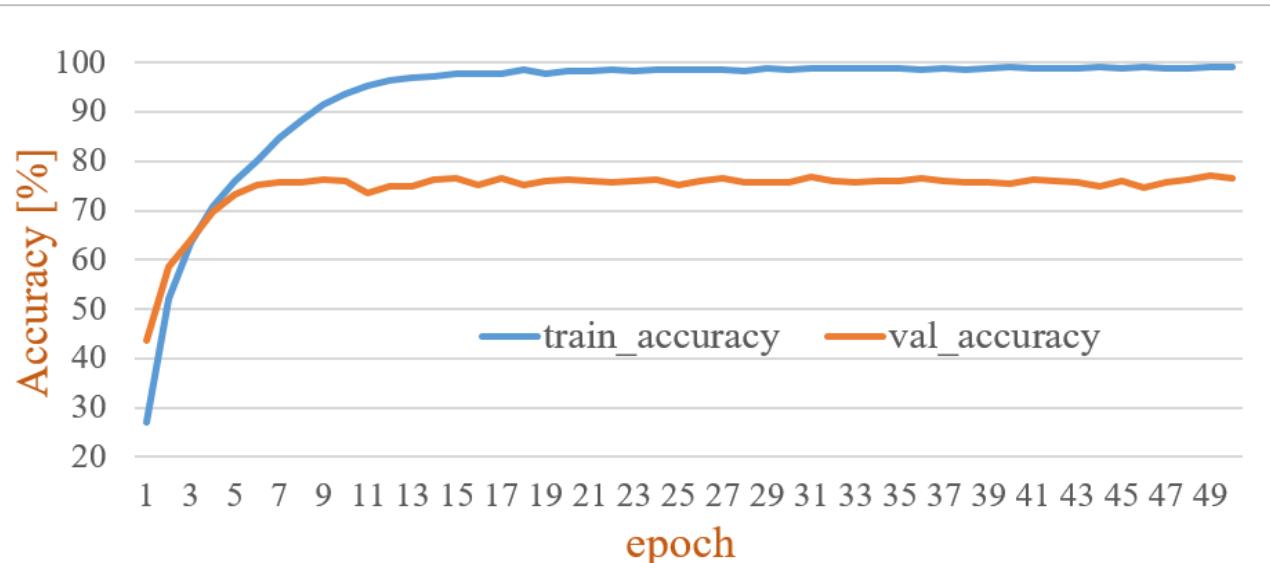
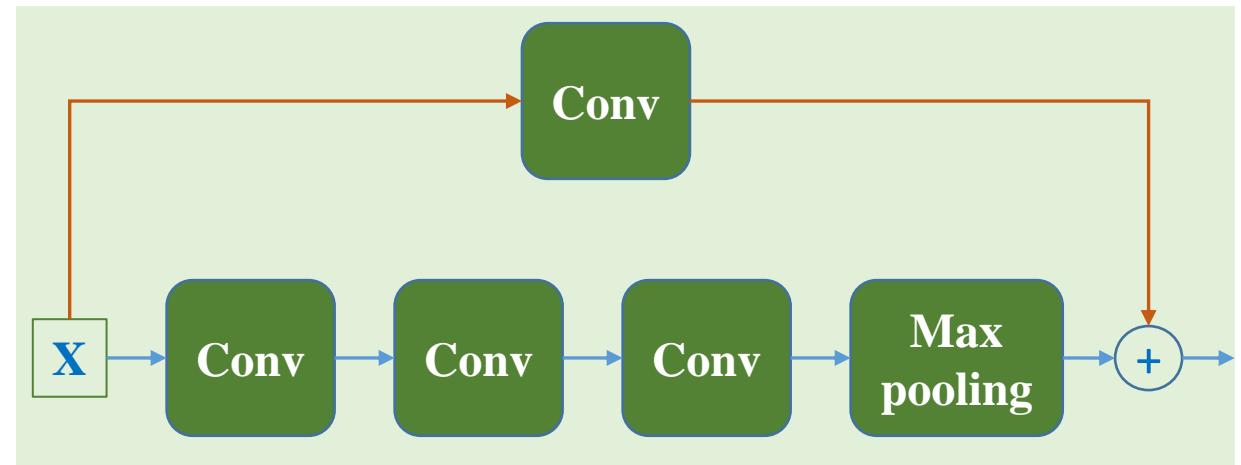


Network Training

❖ Solution 5: Skip connection

```
conv_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer2 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU())
conv_layer3 = nn.Sequential(nn.Conv2d(64, 64, 3, stride=1, padding='same'), nn.ReLU(),
                            nn.MaxPool2d(2, 2))
res_layer1 = nn.Sequential(nn.Conv2d(3, 64, 3, stride=2, padding=1), nn.ReLU())

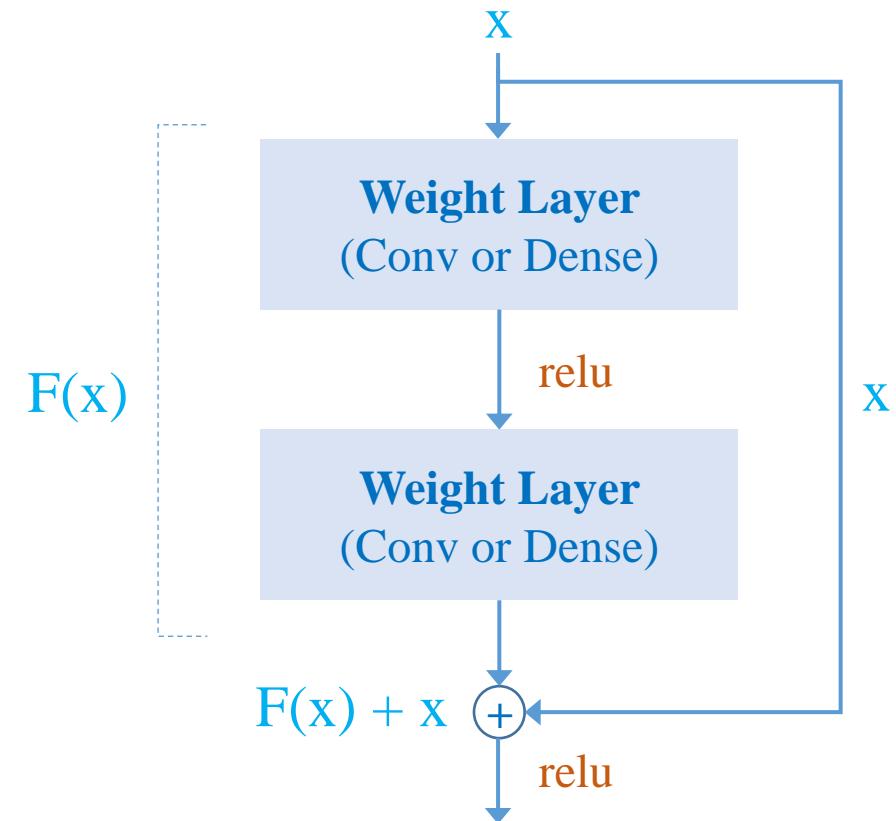
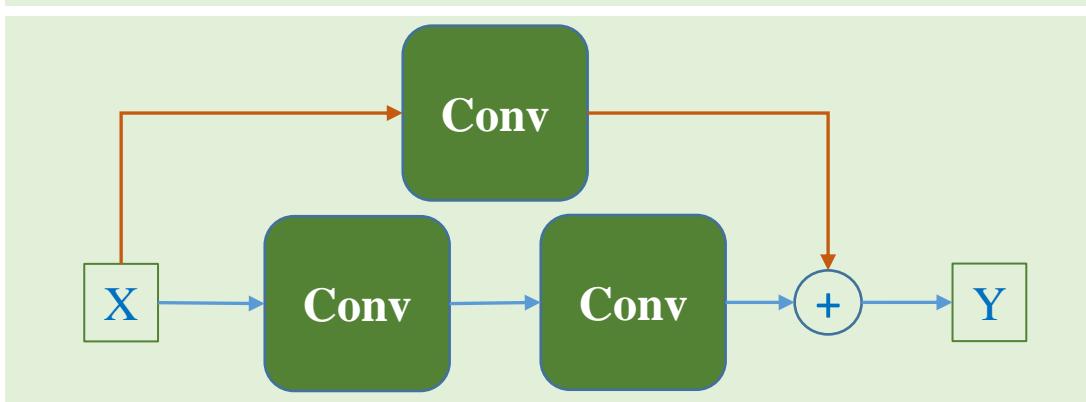
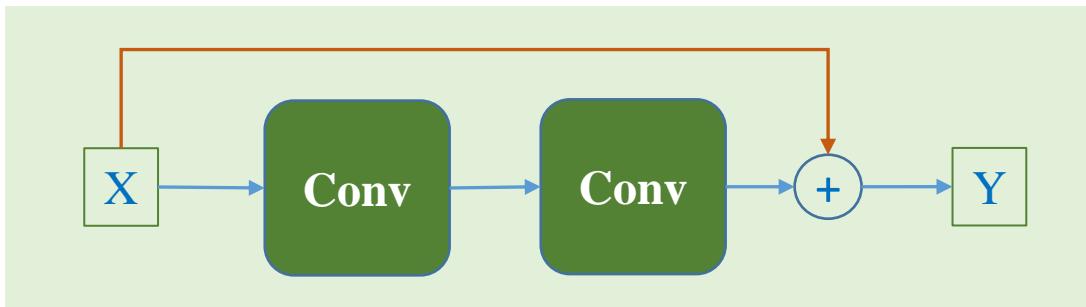
# Given x
previous_input_x = x
x = self.conv_layer1(x)
x = self.conv_layer2(x)
x = self.conv_layer3(x)
res = self.res_layer1(previous_input_x)
x = x + res
```



There are several variants that use fully skip connection, concatenation, long skip connection

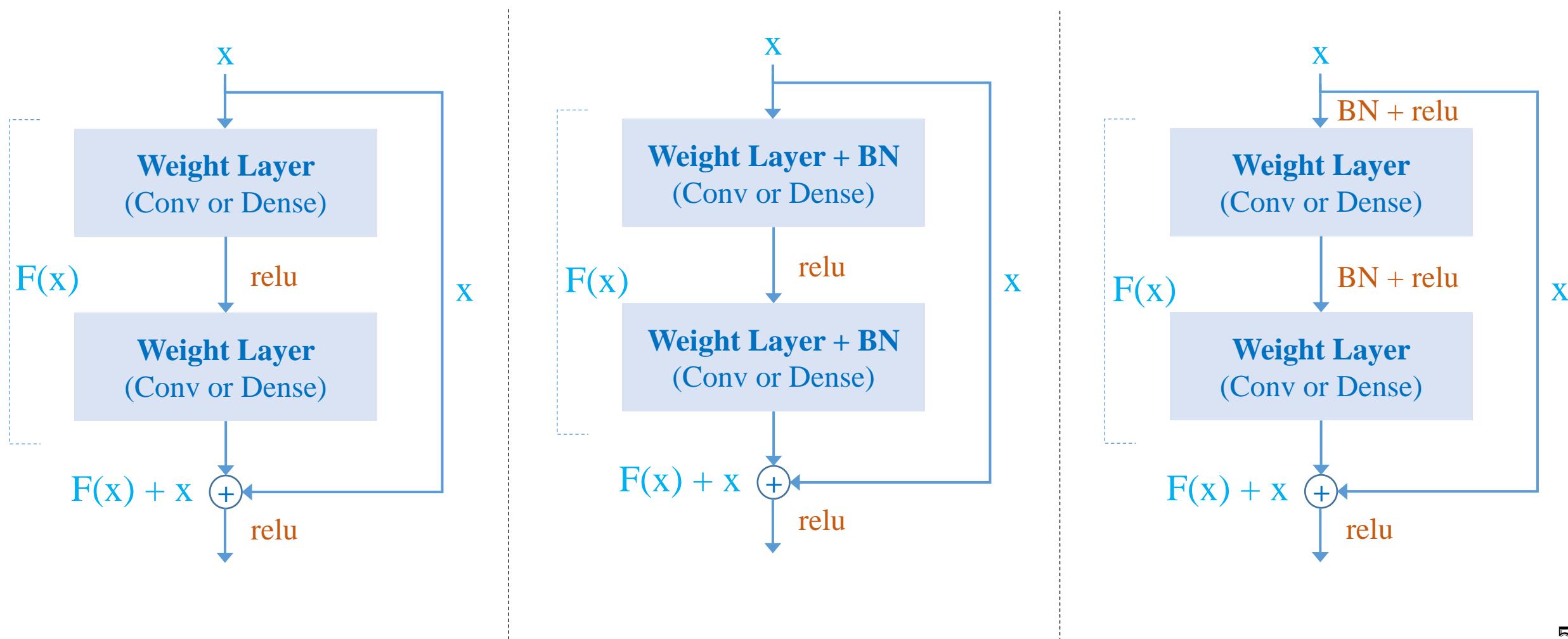
Network Training

❖ Solution 5: Skip connection



Network Training

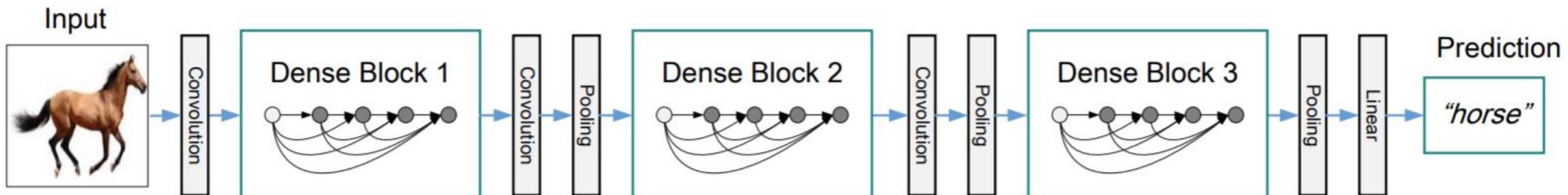
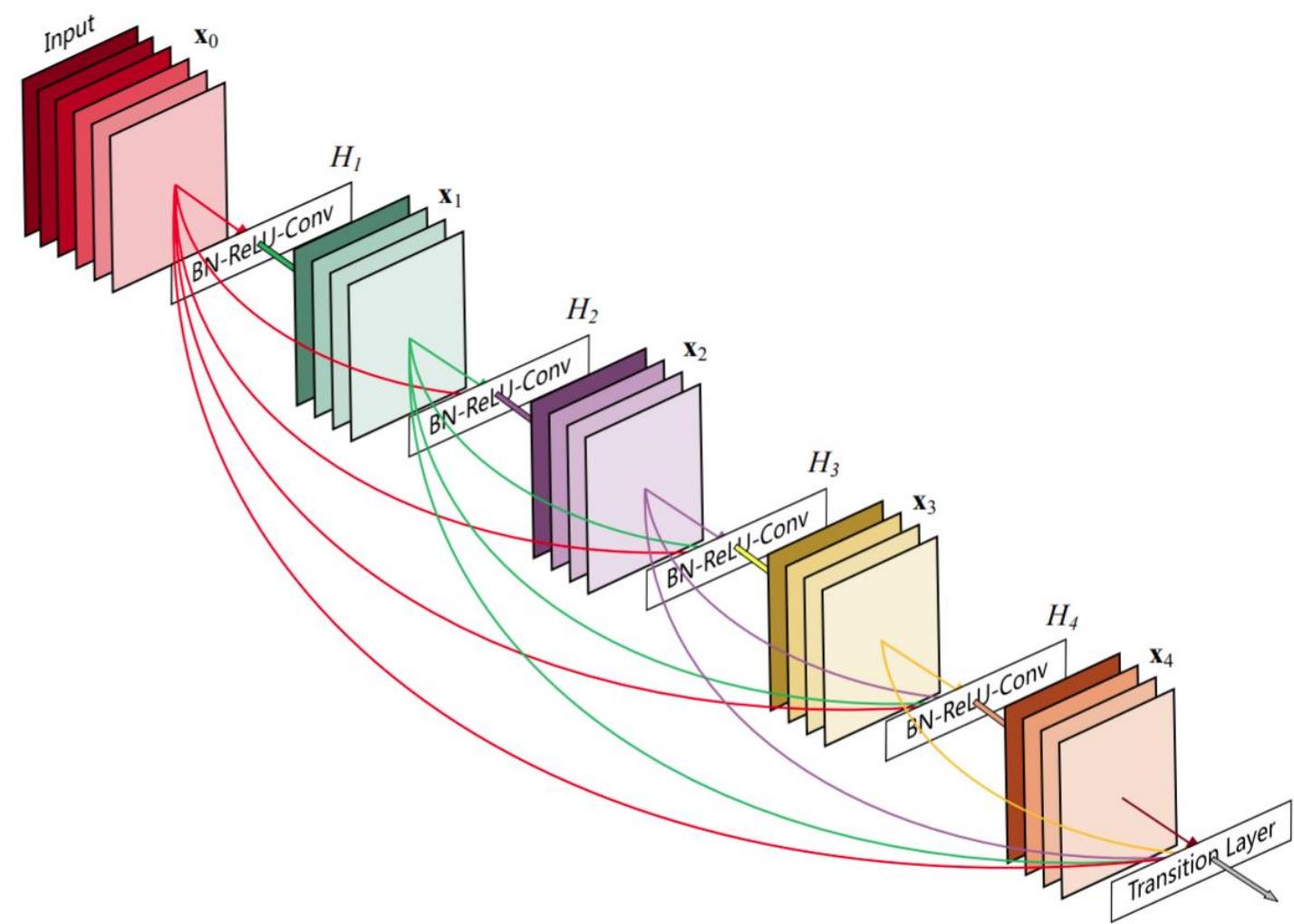
❖ Solution 5: Skip connection



Network Training

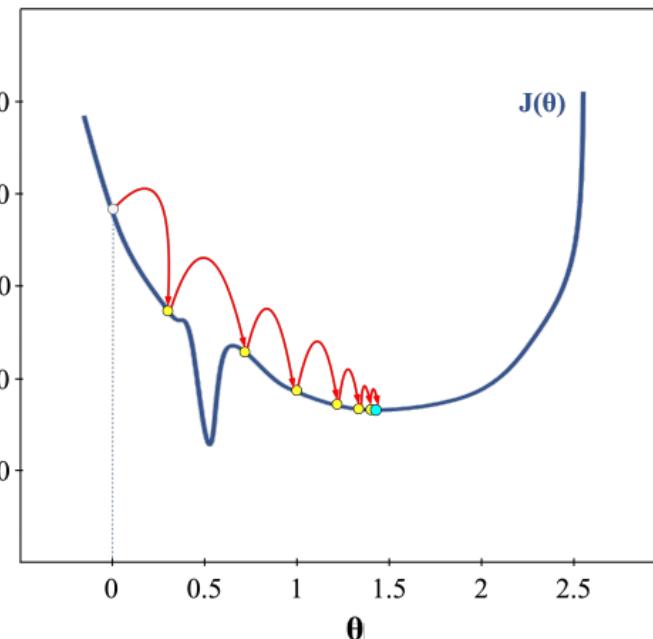
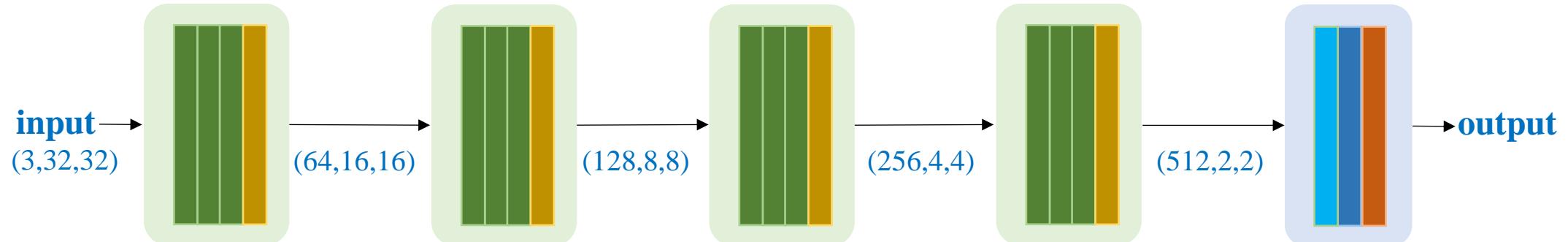
❖ Solution 5: Skip connection

<https://arxiv.org/pdf/1608.06993v5.pdf>



Network Training

❖ Solution 6: Reduce learning rate

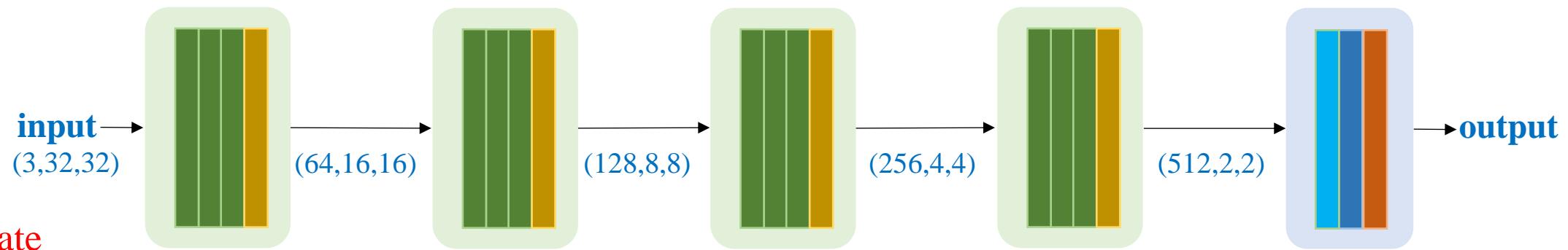


(3x3) Convolution padding='same' stride=1 + ReLU
(2x2) max pooling
Flatten
Dense Layer-512 + ReLU

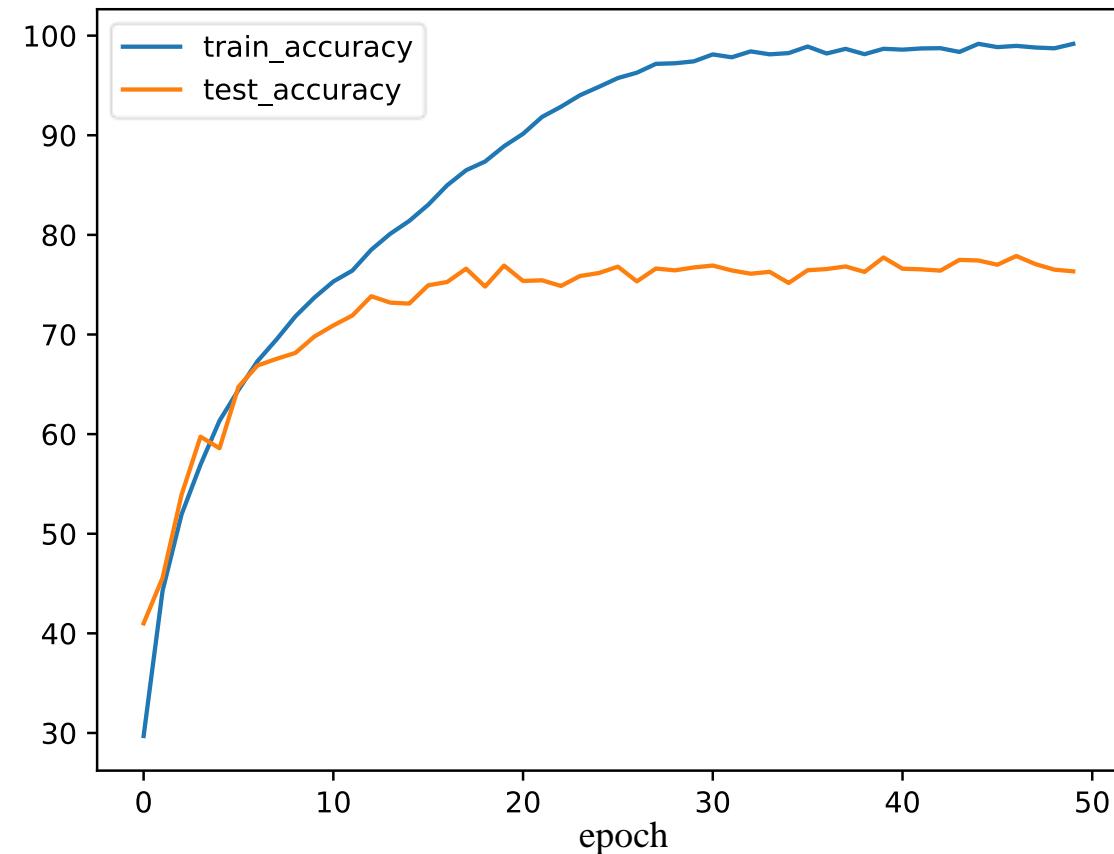
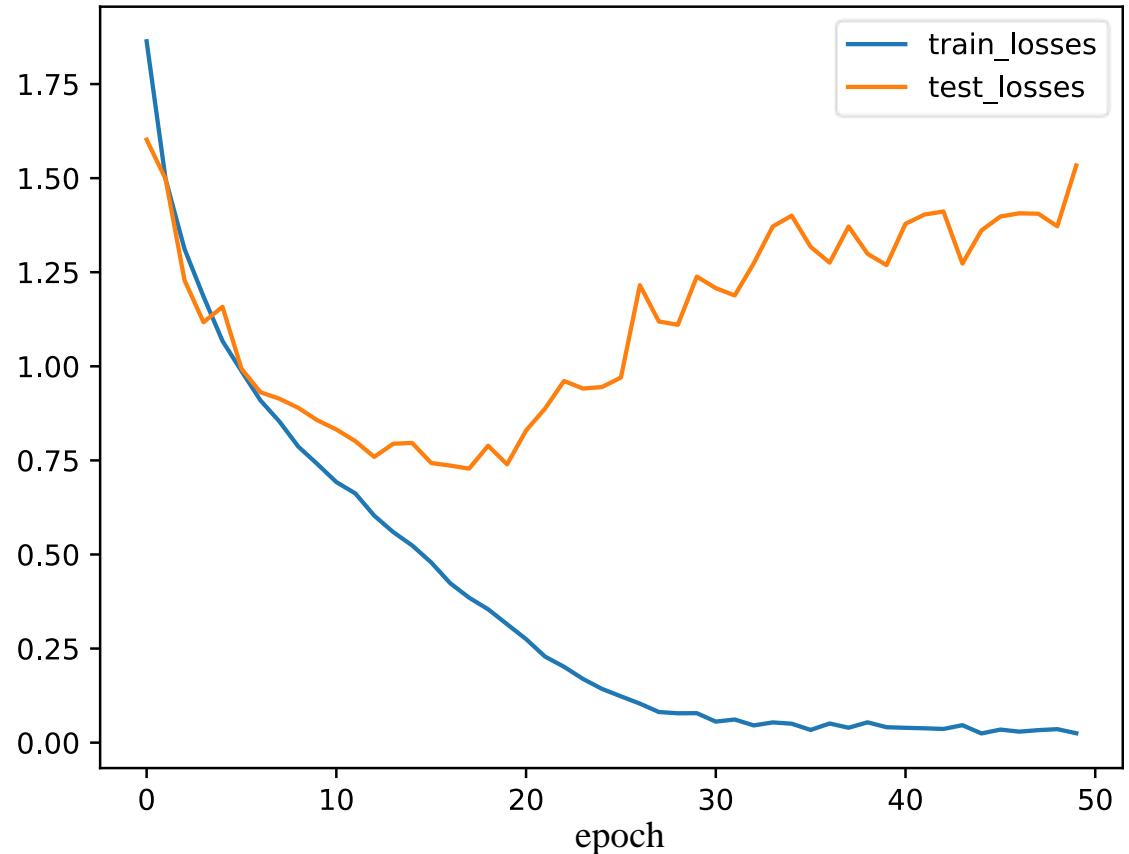
Dense Layer-10 + Softmax

```
# Loss and optimizer
criterion = nn.CrossEntropyLoss()
optimizer = Adam(model.parameters(), lr=1e-4)
```

Network Training



Reduce learning rate





Summary

Further Reading

Skip connection

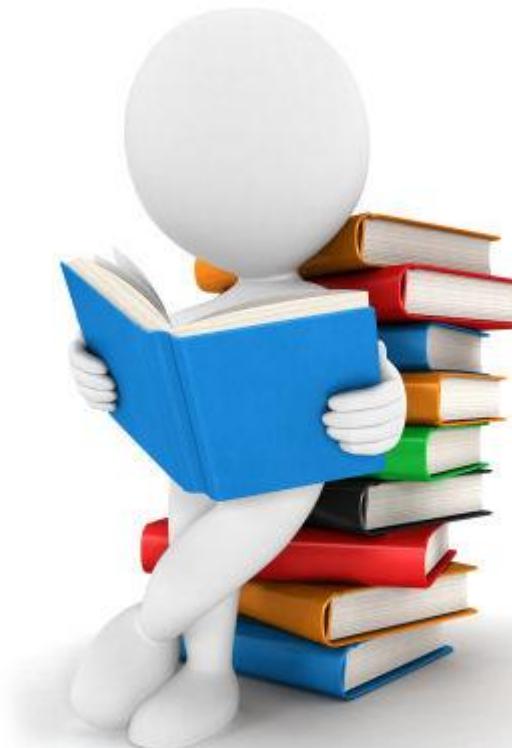
<https://theaisummer.com/skip-connections/>

Trying to overfit Data

<http://karpathy.github.io/2019/04/25/recipe/>

DenseNet

<https://arxiv.org/pdf/1608.06993v5.pdf>



Summary

- ❖ Train a CNN model
 - ❖ Try to overfit data

