



Example Project 1

Group 1

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a) Algorithm Implementation - hybridSort()

```
void hybridSort(int start, int end, int arr[], int S)
{
    int mid;
    if(end-start+1 > S)
    {
        mid = (start+end)/2;

        hybridSort(start, mid, arr, S);
        hybridSort(mid+1, end, arr, S);

        // merge
        merge(arr, start, mid, end);
    }
    else //length of array smaller than S
    {
        insertionSort(start, end, arr);
    }
    return;
}
```

a) Algorithm Implementation - merge()

```
void merge(int arr[], int start, int mid, int end) {  
    int i, j, k;  
    // size of left array  
    int n1 = mid - start + 1;  
    // size of right array  
    int n2 = end - mid;  
    int *leftArr = malloc(sizeof(int) * n1);  
    int *rightArr = malloc(sizeof(int) * n2);  
  
    // copy data to 2 separate arrays so we can  
merge    for (i = 0; i < n1; i++)  
        leftArr[i] = arr[start + i];  
    for (j = 0; j < n2; j++)  
        rightArr[j] = arr[mid + 1 + j];  
  
    ....  
}
```

a) Algorithm Implementation - merge()

```
...
// merge the 2 arrays back into arr from arr[start] to arr[end]
i = 0;
j = 0;
k = start;
while (i < n1 && j < n2) {
    comp++;
    if (leftArr[i] <= rightArr[j]) {
        arr[k] = leftArr[i];
        i++;
    }
    else {
        arr[k] = rightArr[j];
        j++;
    }
    k++;
}

// if leftArr not empty, copy remaining elements
while (i < n1) {
    arr[k] = leftArr[i];
    i++;
    k++;
}

// if rightArr not empty, copy remaining elements
while (j < n2) {
    arr[k] = rightArr[j];
    j++;
    k++;
}
free(leftArr);
free(rightArr);
}
```

a) Algorithm Implementation - insertionSort()

```
void insertionSort(int start, int end, int  
arr[])  
    int i,j,temp;  
  
    for(i=start+1;i<=end;i++)  
    {  
        for(j=i;j>start;j--)  
        {  
            comp++;  
            if(arr[j]<= arr[j-1])  
            {  
                temp= arr[j];  
                arr[j]= arr[j-1];  
                arr[j-1]=temp;  
            }  
            else  
                break;  
        }  
    }  
    return;  
}
```

b) Data Generation

Generated 7 datasets in the range of [0, 10,000,000) with seed=2001



```
from numpy import random
max = 10000000
random.seed(2001)
with open("dataset.txt", 'w') as f:
    for cap in [1000, 10000, 100000, 500000,
                1000000, 5000000, 10000000]:

        arr = random.randint(max,size=(cap))
        string = ",".join(map(str, arr))
        f.write(string)
        f.write("\n")
```

c) Theoretical Analysis

Merge Sort

Let i = number of iterations of MergeSort function

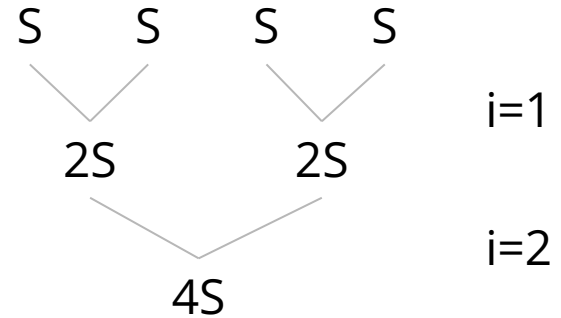
$$2^i(S) = n$$

$$2^i = \frac{n}{S}$$

$$i \log_2 2 = \log_2\left(\frac{n}{S}\right)$$

$$i = \log_2\left(\frac{n}{S}\right)$$

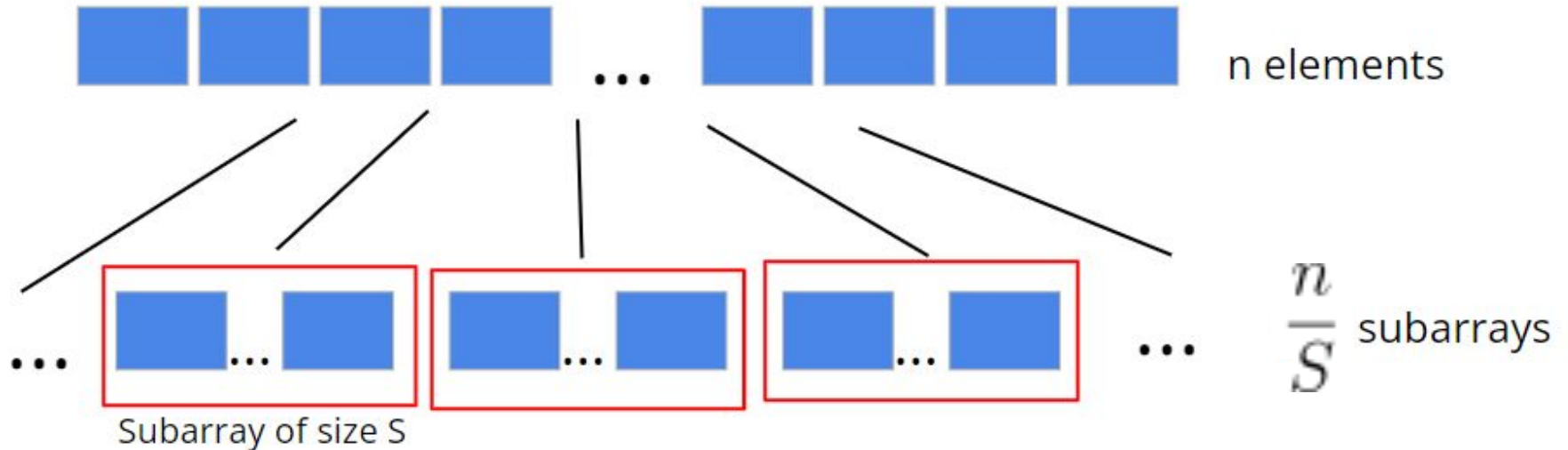
- Number of comparisons per iteration = $O(n)$
- Time complexity = $n \log_2\left(\frac{n}{S}\right) = O\left[n \log_2\left(\frac{n}{S}\right)\right]$



c) Theoretical Analysis

Insertion Sort

- Number of subarrays to sort: $\frac{n}{S}$



c) Theoretical Analysis

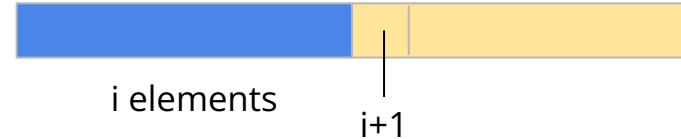
Insertion Sort

Best Case: $\frac{n(S-1)}{S}$

Worst Case: $\frac{n(S-1)}{2}$

c) Theoretical Analysis

Insertion Sort: Average Case



Number of comparisons in the i th iteration = $\frac{1}{i}(1 + 2 + \dots + i)$

If size of subarray is S , there are $(S-1)$ iterations

Number of comparisons = $1 + \frac{1}{2}(1 + 2) + \frac{1}{3}(1 + 2 + 3) + \dots + \frac{1}{S-1}(1 + \dots + S-1) = \frac{1}{4}(S-1)(S+2)$
per subarray

Number of comparisons = $\frac{n(S-1)(S+2)}{4S} = O(\frac{nS}{4})$
for $\frac{n}{S}$ subarrays

c) Theoretical Analysis

Hybrid Sort

$$\text{Worst case} = n \log_2\left(\frac{n}{S}\right) + nS$$

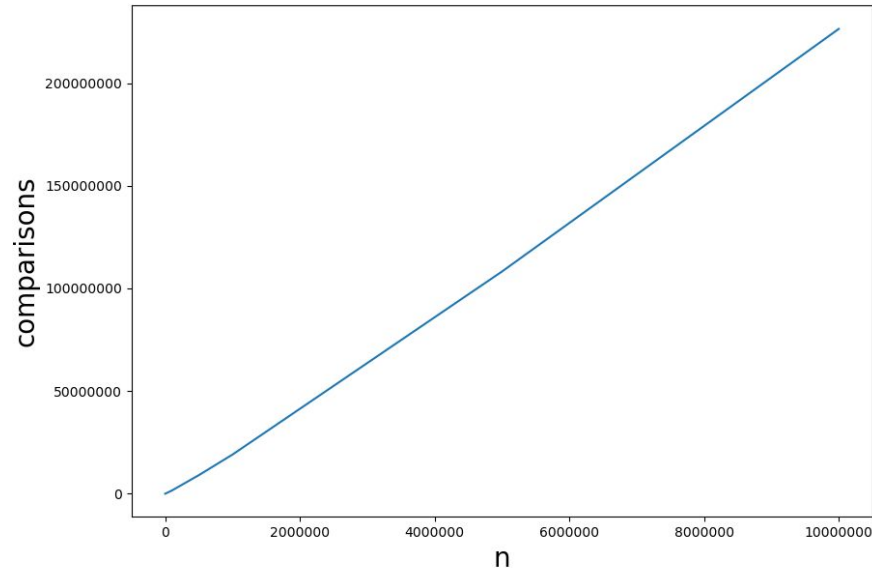
$$\text{Average case} = n \log_2\left(\frac{n}{S}\right) + \frac{nS}{4}$$

$$\text{Best case} = n \log_2\left(\frac{n}{S}\right) + \frac{n}{S}(S - 1)$$

c i) Fix S, Vary n: comps over S

For randomly chosen S=10:

n	1,000	10,000	100,000	500,000	1,000,000	5,000,000	10,000,000
comps	9,117	126,761	1,558,302	9,036,737	19,071,221	108,215,228	226,414,009

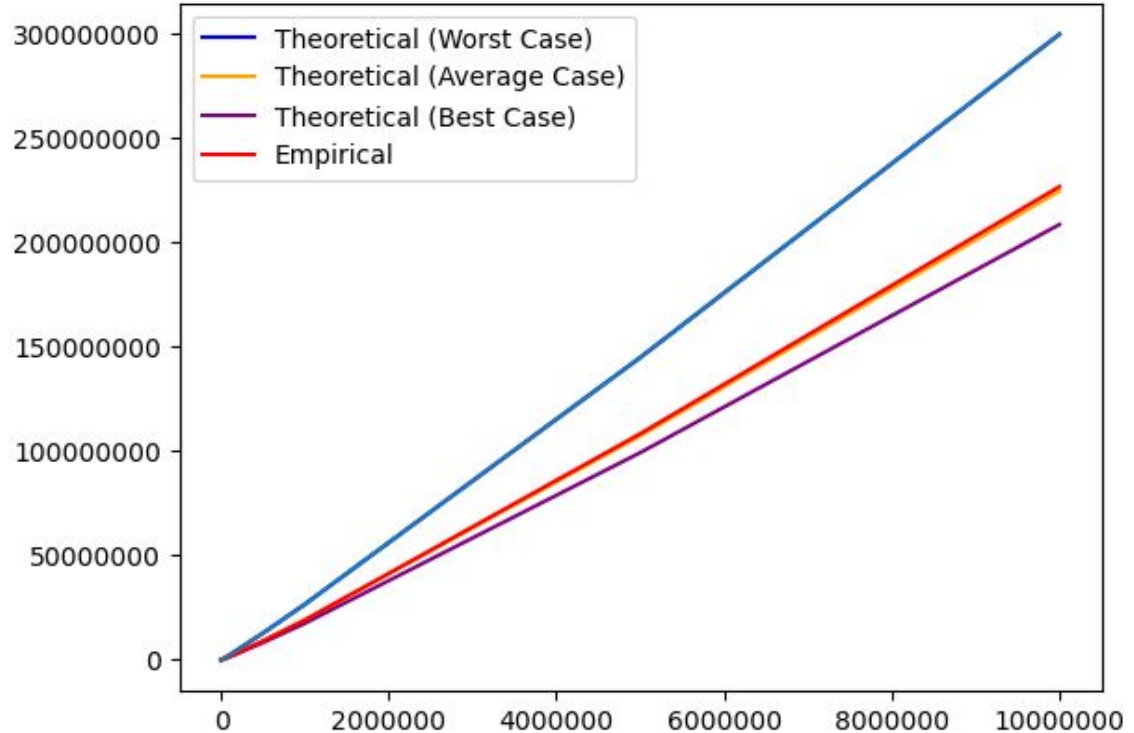


c i) Fix S, Vary n: Theoretical vs Empirical

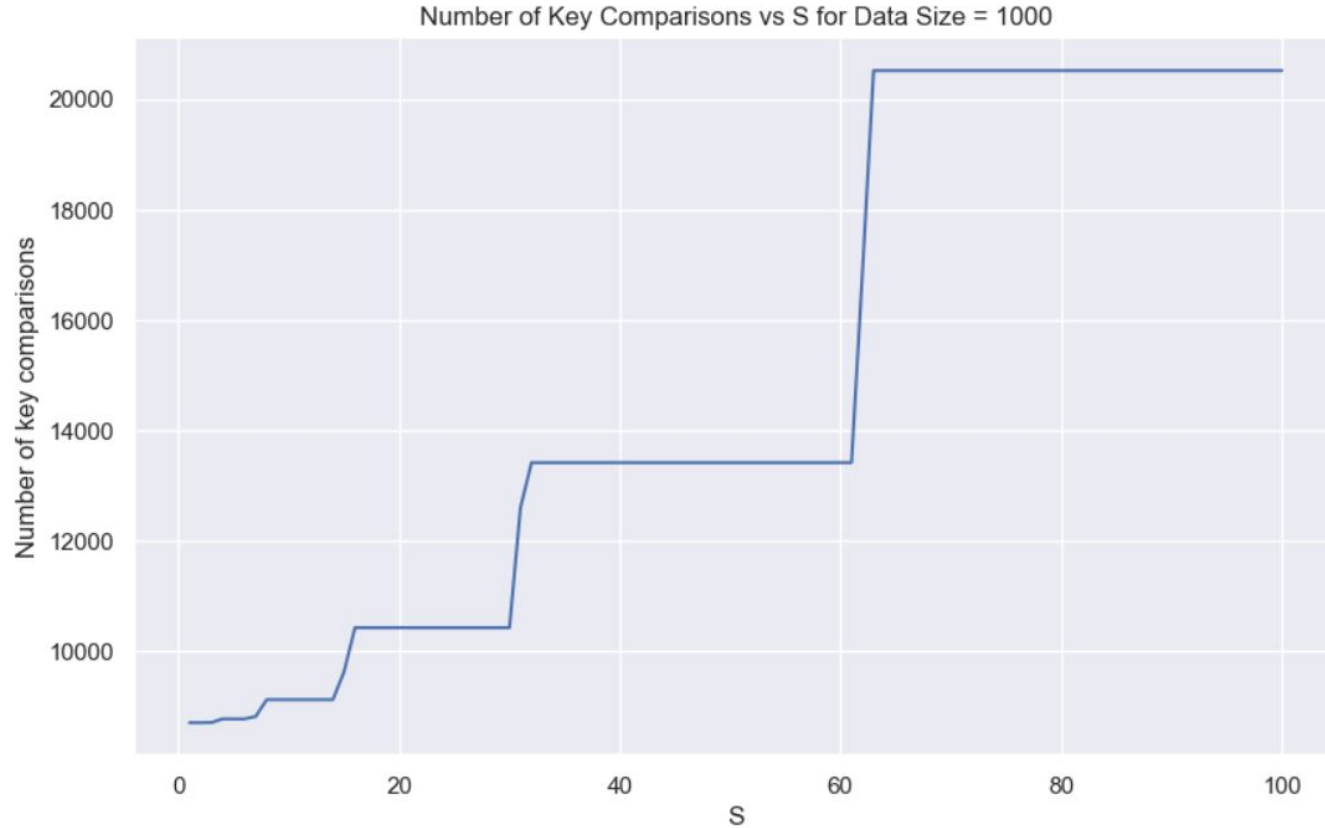
Worst Case: $n \log_2\left(\frac{n}{S}\right) + nS$

Average Case: $n \log_2\left(\frac{n}{S}\right) + \frac{nS}{4}$

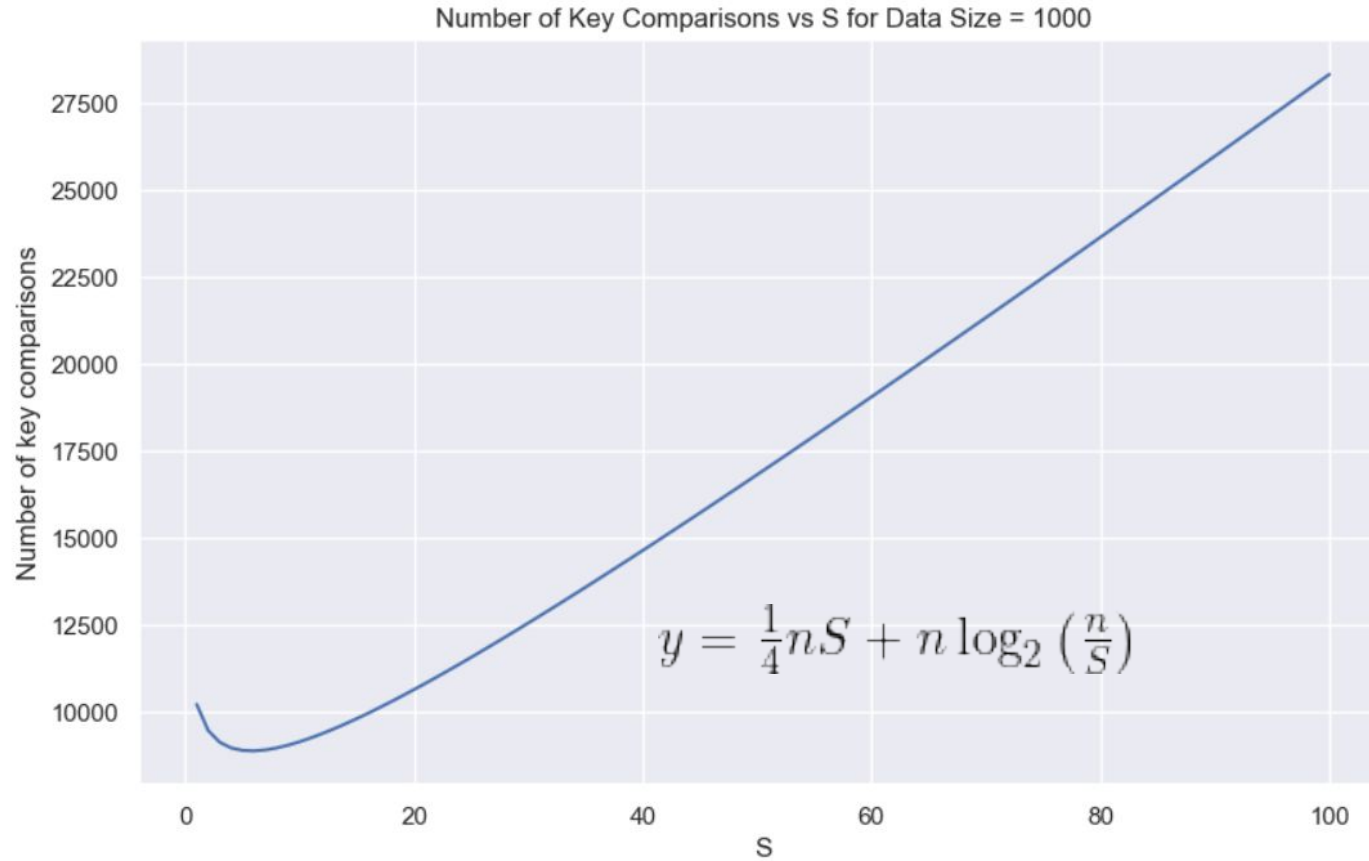
Best Case: $n \log_2\left(\frac{n}{S}\right) + \frac{n}{S}(S-1)$



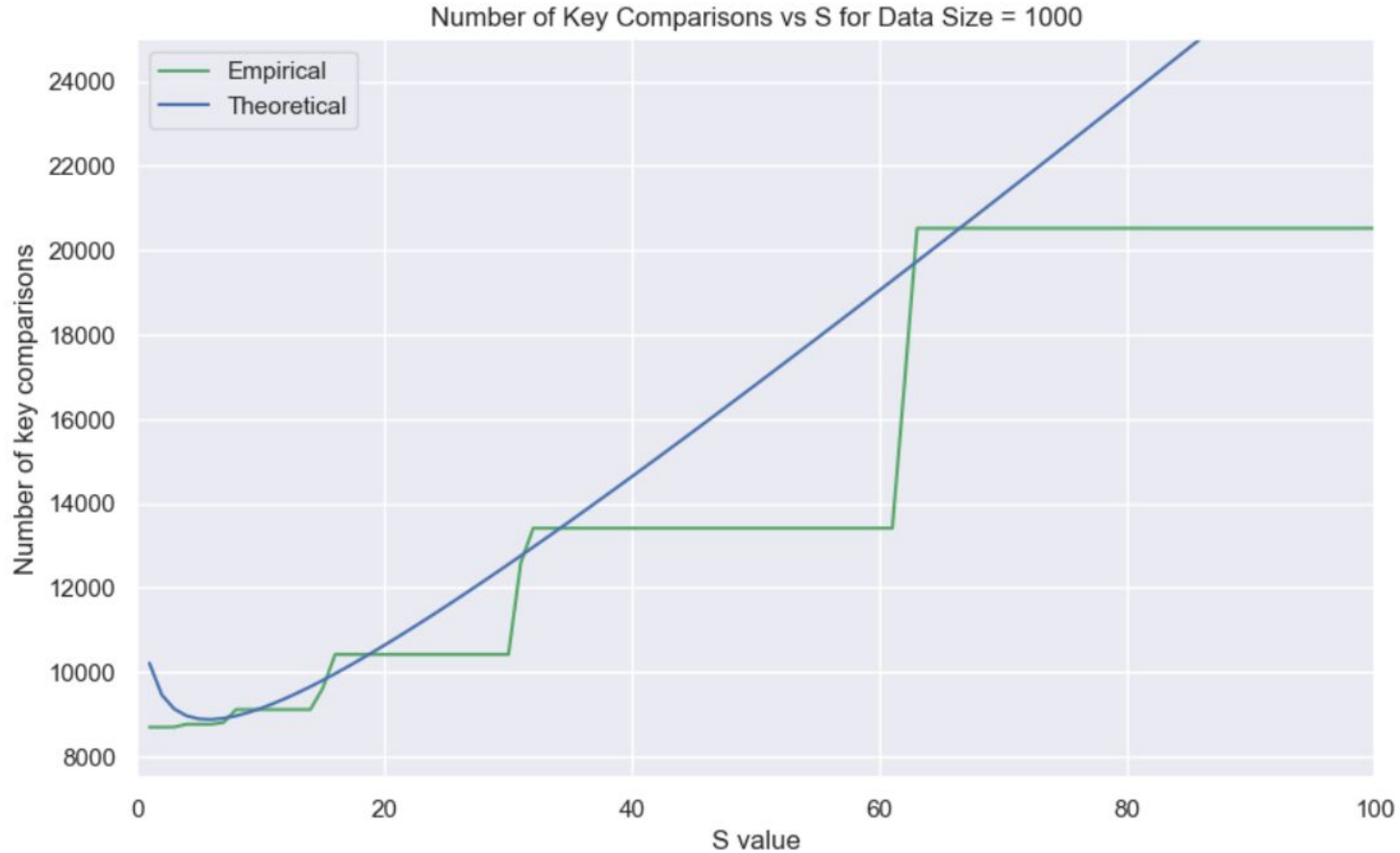
cii) Vary S, Fix n: Empirical



cii) Vary S, Fix n: Theoretical



cii) Vary S, Fix n: Theoretical vs Emp



cii) Vary S, Fix n: Theoretical vs Emp

1000



500

⋮

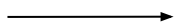
56



When $S = 56, 57, 58, \dots, 111$, subarray size is the same

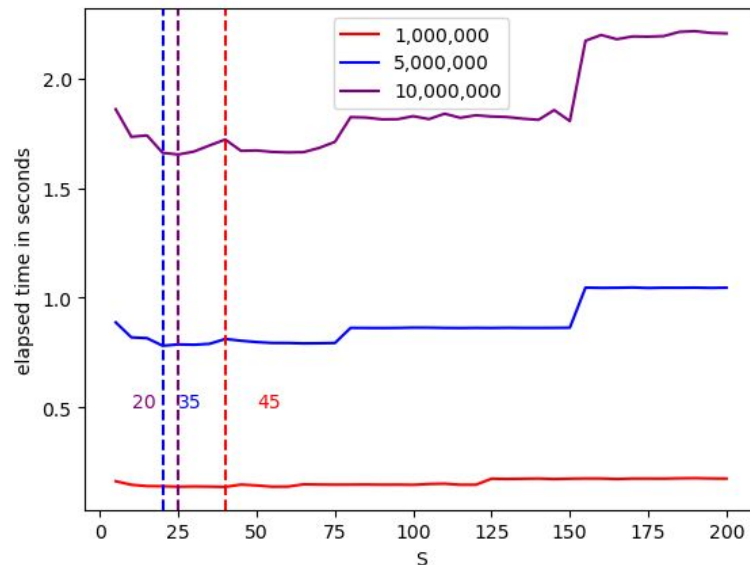
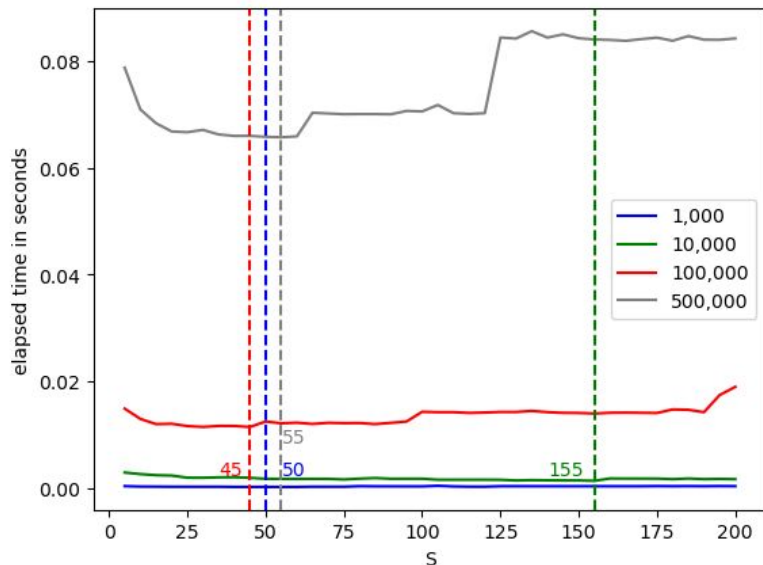


28



When $S = 28, 29, \dots, 55$, subarray size is the same

c iii) Vary S, Vary n: What is the optimal S?



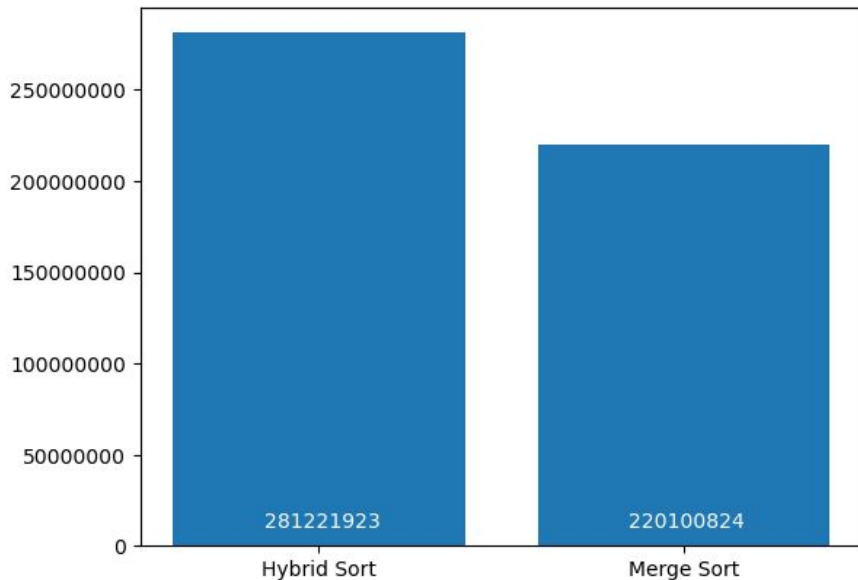
20, 35, 45, **45**, 50, 55, 155

We will use the median S value of the 7 datasets as the optimal S

d) Hybrid Sort vs Merge Sort

```
clock_t start_time = clock();  
hybridSort(0, index - 1, arr2, S);  
clock_t end_time = clock();  
double elapsed_time = (double)(end_time - start_time) /  
CLOCKS_PER_SEC;
```

Key Comparisons



CPU Time

