

Some thoughts on discrete non-commutative geometry

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The main ingredient which catalyzes Connes' formulation of non-commutative geometry is Gelfand duality:

Theorem .1 (Gelfand). There is a contravariant equivalence of categories between \mathbf{Top}

This duality also has a special case particular to differential geometry

Theorem .2.

Expanding the category $\mathbf{C^*Alg}$ to $\mathbf{C^*Alg}$, the category of all possibly non-commutative C^* -algebras, and attempting to similarly expand \mathbf{Top}_c