Decision Tree Exercises - Part 1

Summary

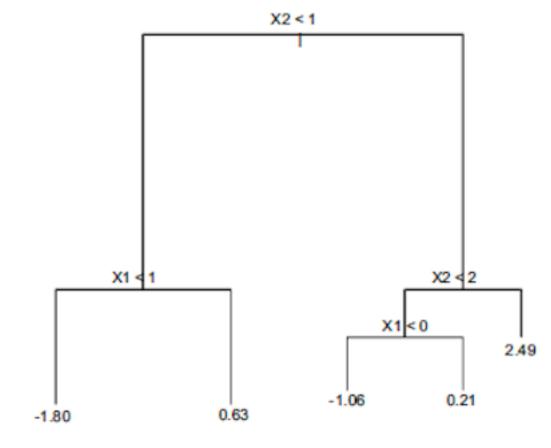
These exercises focus on understanding how a decision tree is built and interpreted.

Exercise 1

- Sketch an example of your own invention: a partition of a two dimensional feature space that could result from recursive binary splitting. Your example should contain at least six regions.
- Draw a decision tree corresponding to this partition. Label all aspects of your two figures, including the regions, the cutpoints, etc.
- Can you express your decision tree as a set of nested rules for classification: If .. (if.. else..) .. else .. (if .. else ..) ..

Exercise 2

Consider the following regression tree:



corrsponding to the above tree, and indicate the mean (output) for each region. Exercise 3

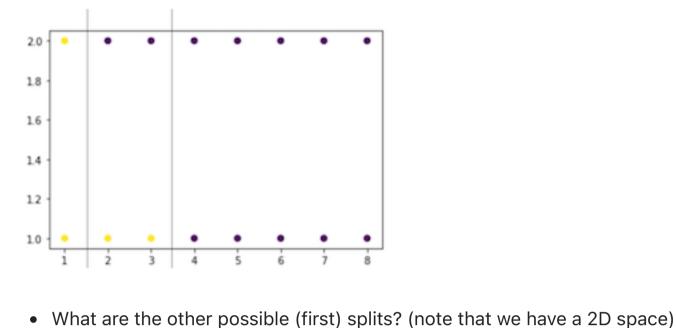
Sketch a partition [0,2]x[0,3] of a two dimensional feature space (X1 and X2) and divide it into the regions

Explain in your own words: What is a Decision Tree? How does it work? What are some similarities or differences to other algorithms you have used in this course?

S1

Exercise 4

Consider the following simple classification setting with two classes, and S1 and S2 as two out of many possible first splits of the data set.



S2

Here we want to try three different impurity functions: a) classfication error rate, b) Gini index, and c) entropy.

Use all the three impurity functions, and compute by hand the weighted average of impurities of the child nodes, if:

we split the data by S1

we split the data by S2

- Are the results differet for S1 and S2 when we use: Classfication error rate?
- Gini index?
 - Entropy?

(i.e., there is no information gain).

- One of the conditions we can use as stopping condition is to stop when further splitting does not reduce impurity

Use the above impurity functions on the whole dataset (before splitting).

 Based on each impurity function, is there any impurity reduction due to splitting the data by S1 or S2? • Which of the impurity functions do you prefer to use? why?

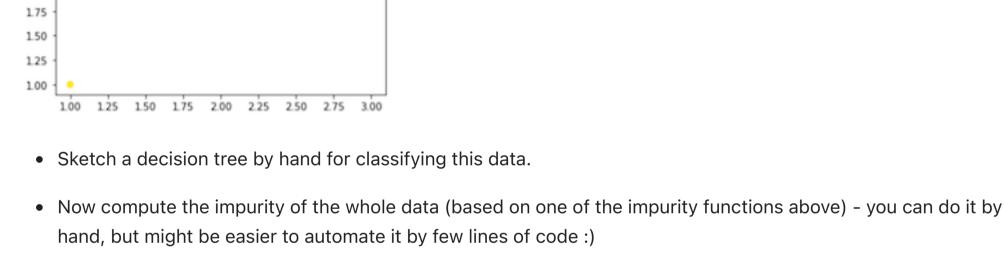
- Exercise 5 Consider the Gini index or entropy, and classification error, in the following simple classification setting with two

classes.

3.00

2.00

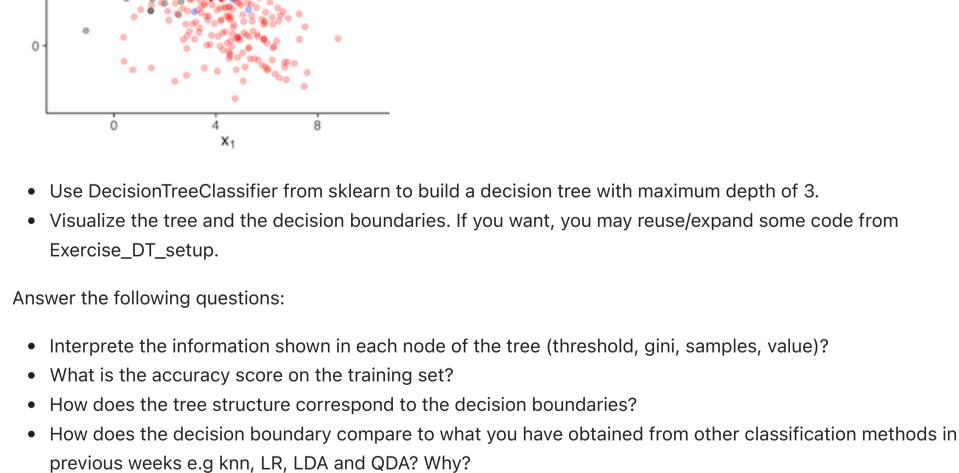
2.75 2.50 2.25



- information gain) for the split. What is the best split? Is it the same as the first split in your hand-made decision tree?
- Continue splitting based on the information gain until there is no classification error.

• Try every possible split, compute the impurity of each region and the weighted average of the children (or the

- **Exercise 6** Now use the datasets Ex1-training.csv and Ex1-test.csv



- Exercise 7
 - this case? How deep must the tree be to reach 95% accuracy on the training data? (Note: this is just to understand how the

decision tree works. For real performance measures we would of course always use a test set).

(max_depth=None) allows the tree to grow until all leaves are pure or until another stopping criterion is reached.

• Re-run the code above with no limit on max_depth. What happens? How much of a difference does it make in

Limiting the max_depth is a way of regularizing a decision tree, i.e. limit its complexity. The default setting

 How well would you expect these trees to generalize? Plot training and test error for different max_depth. Does it match your expectation?

min_samples_leaf and max_leaf_nodes are among other parameters that can be used to regularize a decision tree.

 Try varying their values on some of the trees trained above, does it affect these trees? How? Why? **Exercise 8**

Find and read the documentation for these parameters, what do they do?

In this exercise, we train a regression tree for a 1-D feature space.

def regr1D(N): """ Returns 1D regression (x,y) dataset """

global seed

In []:

```
x = np.random.uniform(low= -50, high=50, size=(N,))
    y = 0.02 * x ** 3 + x ** 2 - 70 * x - 3
    y = y + (np.random.randn(N) * 50) #add noise
    return x, y
np.random.seed(42)
X,y = regr1D(100)
X = X \cdot reshape(-1, 1)
```

- Run the code above to generate a regression dataset Then train a regression tree using DecisionTreeRegressor() with max_depth=2 and visualize it.
- How do you interprete the tree?
- Train more regression trees for the same dataset, increasing the max_depth to 3 or higher. What happens? Do you see any obvious advantages or disadvantages in using a decision tree for regression tasks?