New Trends in Time-Series Anomaly Detection

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ABSTRACT

Anomaly detection is an important problem in data analytics with applications in many domains. In recent years, there has been an increasing interest in anomaly detection tasks applied to time series. In this tutorial, we take a holistic view on anomaly detection in time series, starting from the core definitions and taxonomies related to time series and anomaly types, to an extensive description of the anomaly detection methods proposed by different communities in the literature. Then, we discuss shortcomings in traditional evaluation measures. Finally, we present new solutions to assess the quality of anomaly detection approaches and new benchmarks capturing diverse domains and applications.

1 INTRODUCTION

A wide range of sensing, networking, storage, and processing solutions enable the collection of enormous amounts of measurements over time [45, 53, 59]. The recording of these measurements results in an ordered sequence of real-valued data points commonly referred to as *time series*. Analytical tasks over time series data are becoming increasingly important in virtually every domain [6, 20, 30, 31, 35, 46, 48–51, 54], including astronomy [28], biology [5], energy sciences [3], environmental sciences [23], medicine [55], and social sciences [18].

Anomaly detection has received ample academic and industrial attention [21, 44]. Moreover, as illustrated in Figure 1, anomaly detection applied to time series (compared to other data types) is attracting more interest lately. As commonly defined in the literature [7, 27], anomalies refer to data points (single points or group of points) that do not conform to some notion of normality or an expected behavior based on previously observed data. In practice, anomalies can correspond to [1]: (i) noise or erroneous data (e.g., broken sensors), or (ii) actual data of interest (e.g., anomalous behavior of the measured system). In both cases, detecting such cases is crucial for many applications [2, 26].

In recent years, many research works have appeared in this area of time-series anomaly detection. Multiple surveys and experimental benchmarks have been written to summarize and analyze the state-of-the-art proposed methods [8, 29, 47, 52, 57]. Such surveys and benchmarks provide a holistic view of anomaly detection methods and how they perform on benchmarks.

Therefore, based on these recent works, this tutorial provides a comprehensive view of the task of anomaly detection in time series. We start from terminology and definitions for time series, anomaly, and method types to appropriate accuracy evaluation measures. Our goal is three-fold: (i) introduce the motivations and the challenges related to the anomaly detection task in time series by describing a taxonomy of time series and anomaly type usually considered in the literature, (ii) describe the category of anomaly detection methods proposed in the literature as well as their comparisons on recently proposed benchmarks, (iii) discuss

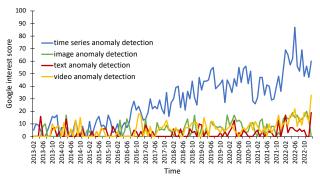


Figure 1: Evolution of the Google interest score for anomaly detection over time series, images, text, and video.

the different solutions to evaluate anomaly detection methods and assess the robustness of the evaluation measures. Finally, we discuss the open research problems and opportunities for anomaly detection in time series.

2 TIME SERIES ANOMALY DETECTION

In this tutorial, we will go through the problem of anomaly detection in time series, starting from very basic definitions of time series and anomaly to analyzing the appropriate evaluation measures to use for the specific case of anomaly detection.

2.1 Introduction, Motivation, and Foundations

We will start by discussing examples of scientific domains and industrial applications that rely on large time series collections and need to perform anomaly detection. We illustrate this variety of domains by showing concrete time series with real anomalies from multiple domains. Figure 2 displays multiple of examples of time series and anomalies from various domains. In Figure 2, ECG [41], MITDB [42], SVDB [24] are ElectroCardioGram (ECG) in which anomalies are either irregular heartbeats or arrhythmia. Moreover, SensorScope [61] is a collection of environmental data, such as temperature, humidity, and solar radiation, collected from a typical tiered sensor measurement system, and Daphnet [4] contains the annotated readings of 3 acceleration sensors at the hip and leg of Parkinson's disease patients that experience freezing of gait (FoG) during walking tasks.

While these previously described examples illustrate well the variety of domains and application in the scope of time series anomaly detection, we then introduce some foundational aspects of time series and anomaly detection. We first introduce the different types of time series. Specifically, we define a **univariate** time series as an ordered sequence of real values on a single dimension. In this case, a subsequence can be represented as a vector. Then, we define a **multivariate** time series as either a set of ordered sequences of real values (with each ordered sequence having the same length) or an ordered sequence of vectors composed of real values. In this specific case, a subsequence is a matrix in which each line corresponds to a subsequence of one single dimension. Moreover, a core characteristic of time series is their evolution with time. Therefore, we define **static** time series as sequences with a fixed length. In this case, one does

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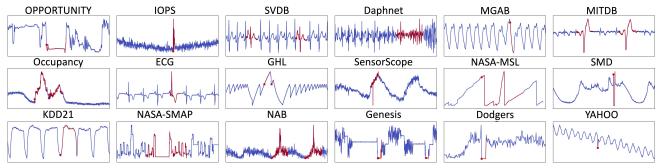


Figure 2: Example of time series from different domains with anomalies (in red) of different types [52].

not expect more values to be added and can analyze points or subsequences simultaneously. We also define **streaming** time series as sequences with an infinite length with new points or subsequences continuously arriving. In this case, models need to be updated dynamically as new points arriving. Finally, the distribution of the values of a time series might change over time. In this case, we make a distinction between **stationary** (i.e., with a constant distribution of values over time) and **non-stationary** (i.e., with a changing distribution of values over time) time series. Moreover, even though the distribution of values is constant, the normal behavior (i.e., the subsequence representing the normal and recurrent behavior, such as a normal heartbeat) might change over time. In this case, we talk about **single normality** and **multiple normalities** time series.

We then introduce the different types of anomalies. There are three types of time-series anomalies: *point*, *contextual*, and *collective* anomalies. We describe them in the following section.

- 2.1.1 **Point Anomaly**. The first category, *point* anomalies, refers to data points that deviate remarkably from the rest of the data. The IOPS dataset in Figure 2 depicts an an example of *point* anomaly and Figure 3(a.1.1) illustrates a synthetic example.
- 2.1.2 **Contextual Anomaly**. Then, *contextual* anomalies refer to data points within the expected range of the distribution (in contrast to point anomalies) but deviate from the expected data distribution, given a specific context (e.g., a window). The YAHOO dataset in Figure 2 depicts an an example of *contextual* anomaly and Figure 3(a.1.2) illustrates a synthetic example.
- 2.1.3 **Collective Anomaly**. With *collective* anomalies, we refer to sequences of points that do not repeat a typical (previously observed) pattern. The SVDB dataset in Figure 2 depicts an an example of *collective* anomaly and Figure 3(a.2) illustrates a synthetic example.

The first two categories, namely, point and contextual anomalies, are referred to as *point-based* anomalies, whereas *collective* anomalies are referred to as *subsequence* anomalies.

2.1.4 Single vs. Multiple Anomalies. Then, on top of these categories, the combination of them also matters. First, we need to differentiate time series containing *single* anomalies from time series containing *multiple* anomalies. Last, the *multiple* time series category has to be divided into two other categories, namely time series containing *multiple different* and *multiple similar* anomalies. For instance, the MITDB and Genesis time series in Figure 2 contains multiple similar anomalies. As described in the next section, some methods that are based on nearest-neighbor distance might be affected by this distinction. Figure 3 illustrates all the aforementioned anomaly types and combinations. For all these definitions and taxonomies, we will provide explicit examples.

2.2 Existing Methods and Benchmarks

We will then dive into the existing anomaly detection methods proposed in the literature. Due to the large variety of applications, domains, and anomaly types, every year, a vast number of papers appear in the literature proposing new methods for anomaly detection in time series, and it is beyond our scope to cover extensively here. In this tutorial, we will only briefly summarize popular categories of methods, and we refer the attendees to three recent survey papers for detailed coverage of methods [8, 16, 25].

We will first mention the three main categories of methods based on the external knowledge provided to them. First, **unsupervised** methods take the time series as input only and are not provided by any information relative to the normal or abnormal behavior. Then, **semi-supervised** methods take as input time series without any anomalies. In this case, the model is trained on normal data only. Finally, **supervised** methods take as input separately both normal and abnormal data. Thus, the model is trained to discriminate the anomalies from the normality.

Then, we will describe the following categories of methods (refer to Figure 4):

- 2.2.1 **Distance-based Methods**. The first family of method is distance-based appraoches. These methods focus on the analysis of subsequences for the purpose of detecting anomalies in time series, mainly by utilizing distances to a given model. For instance, discord-based approaches use the nearest neighbor distances among subsequences [19, 22, 33, 34, 37, 38, 58, 62]. As another example, recent methods in this category first cluster data to obtain the normal behavior and compute the distance to this normal behavior to detect anomalies [9–15].
- 2.2.2 **Density-based Methods**. Second, instead of measuring nearest neighbor distances, density-based methods focus on detecting globally normal or isolated behaviors. General-purpose multi-dimensional point outlier methods have been proposed in this category [17, 36, 39], with Isolation Forest [36] working particularly well when extended for subsequences [11]. The latter aims to isolate instances (or time series and subsequences in our specific case) by building random splitting trees. The longer the depth of the tree, the more splits were necessary to isolate a given instance. Thus, an anomaly score can be computed based on the depth of the trees.
- 2.2.3 **Forecasting-based Methods**. Third, forecasting-based methods, such as recurrent neural network-based [40] or convolutional network-based approach [43], have been proposed for this task. Such methods use the past values as input, predict the following one, and use the forecasting error as an anomaly score.
- 2.2.4 **Reconstruction-based Methods**. Last, reconstruction-based methods, such as the AutoEncoder-based approach [56],

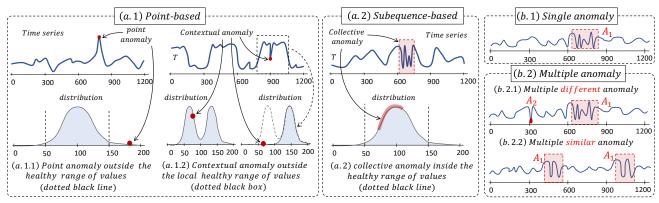


Figure 3: Synthetic examples of different types of anomalies in time series.

are trained to reconstruct the time series and use the reconstruction error as an anomaly score. As both forecasting and reconstruction-based categories detect anomalies using prediction errors (either forecasting or reconstruction error), we can group them into **prediction-based methods**.

Finally, we will discuss recent benchmarks proposed for anomaly detection in time series task [29, 32, 47, 52, 57]. Such benchmarks provide a large collection of time series from various domains and evaluate multiple methods belonging to the aforementioned categories. In this tutorial, we will discuss the results and conclusions of these recent benchmarks. Figure 2 illustrates several time series from the TSB-UAD benchmark [52] that contains 18 different datasets from different domains and applications, with a total of more than 2000 time series.

2.3 Evaluating Anomaly Detection

In the last part of this tutorial, we will focus on evaluating anomaly detection accuracy. Indeed, the choice of measure to quantify the quality of methods may also significantly bias the experimental outcome. Thus, we will start by describing the evaluation measures. Briefly, we will first discuss traditional measures, such as Precision, Recall, and F-score, that assess the methods by assuming each time-series point can be marked as an anomaly or not (e.g., by a threshold on an anomaly score). We will then discuss range-based variants [60] that aim to overcome short-comings of traditional measures when evaluating time series containing subsequence anomalies. We will discuss AUC (i.e., Area Under the Curve) measures that, contrary to previously mentioned measures, eliminate the need to define a threshold. We will finally discuss VUS [47] (i.e., Volume Under the Surface) measures that provide more robustness for time series.

We will conclude this section on the complex question of evaluating evaluation measures. We will mainly discuss the results and the methodology proposed in a recent benchmark for evaluation measures [47, 52]. This benchmark proposes an experimental evaluation of all the aforementioned measures by comparing them with regard to (i) robustness (of labeling misalignment, anomaly score noise, and normal/abnormal ratio), (ii) separability (i.e., the ability to observe a significant difference between anomaly scores of accurate and inaccurate methods), and (iii) consistency (i.e., the ability of a measure to provide similar accuracy values for a same method applied to two similar time series). In this tutorial, we will discuss the conclusion of such an experimental evaluation, but also its limitations and challenges.

2.4 Challenges and Conclusions

We will conclude this tutorial by summarizing the main insights obtained from recent benchmarks on the performances anomaly detection methods [52] and the proper evaluation measures to evaluate them [47]. We will discuss the new problems that these insights opened. Finally, we will elaborate on new ideas and research directions (such as ensembling solutions and model selection methods) that could solve the new open problems.

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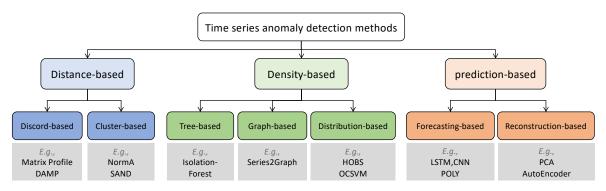


Figure 4: Taxonomy of anomaly detection methods.

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