



Cannabis Data Science

# Cannabis Data Science #59

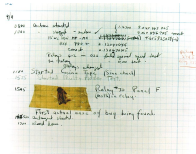
March 30<sup>th</sup>, 2022

# Looking back at the history of computing...



# The Importance of Computers

- Mathematician **Grace Hopper** ("Grandma COBOL") completes A-0, a program that allows a computer user to use English-like words instead of numbers to give the computer instructions in 1952.
- Helped the first commercial electronic computer and applications for COBOL (common-business-oriented language).
- 70 years later, Google's fourth undersea internet cable, named Grace Hopper, connecting the US, UK, Spain, and is expected to soon be operational (2022).



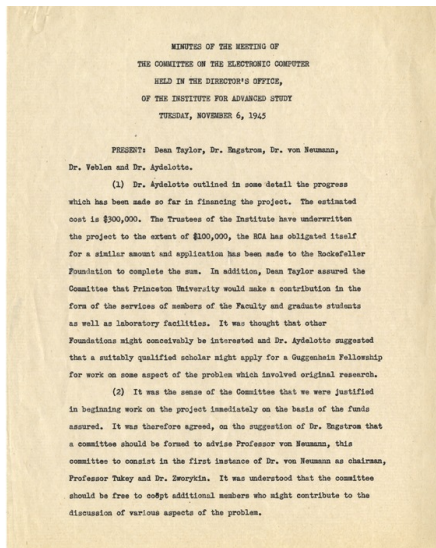
First actual case of a bug being found (1960).  
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Grace Hopper, Washington DC, 1978.

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# From Top Secret to Open Access



## The Electronic Computer Project (1945-1947)

- Led by Professor John von Neumann.
- Put into the public domain.
- 20,000,000 multiplications took 6 hours of continuous computing.

*"There are two kinds of people in the world:  
Johnny von Neumann ..."*





*"...and the rest of us."*  
- Eugene Wigner

# Searching for the origins of data science

John von Neumann founded the field of **game theory**.

- *Theory of Games and Economic Behavior*, von Neumann and Morgenstern (1944).
- von Neumann—Morgenstern utility function:

$$U(p) = \sum_{k=1}^K u(x_k)p_k$$

where  $p_k$  is the probability of outcome  $k$  that, if realized, provides payoff  $x_k$ , and function  $u$  expresses the utility of each respective payoff.

- Today, **Bayes' Theorem** is used to endogenized probability, making it subjective. Subjective probabilities are updated in light of new information, thus connecting the concepts of **rational choice** and inference.

# Jumping into Game Theory

## Repeated Games

- **Finite games:** Usually solved by backwards induction.
- **Infinite games:** Typically, difficult to solve.
- Even if the game being played in each round is identical, repeating that game a finite or an infinite number of times can, in general, lead to very different outcomes (equilibria), as well as very different optimal strategies.



# Modeling Player Preferences

Given that player  $i$ 's valuation of the game diminishes with time depending on a **discount factor**  $\delta < 1$ , then player  $i$ 's utility is

$$U_i = \sum_{t \geq 0} \delta^t u_i(x_t)$$

where

$$u_i(x_t) = \sum_{k=1}^K u_i(x_k) p_k$$

The cutting edge is repeated games with incomplete information, where players have to formulate beliefs about probabilities,  $p$ .

# Solving Games

**Nash Equilibrium** – A strategy profile for a game in which no player has a profitable unilateral deviation.

**Subgame Perfect Nash Equilibrium** – A strategy profile for a dynamic game with Nash equilibrium for every subgame.

**Bayesian Nash Equilibrium** – A strategy profile that maximizes the expected payoff for each player given their beliefs and given the strategies played by the other players.

# Congestion Model

Given

- Cannabis **producers**,  $i = 1, \dots, N$ ,
- Cannabis **products**,  $m = 1, \dots, M$ ,
- A time horizon,  $t = 1, \dots, T$ .

Under the following assumptions:

- Any **producer** can produce any **product**.
- The *cost* to produce an item of any type is  $c = 0$ .
- A **producer** can change the type of **product** it produces at a set *interval*,  $t_i$ .<sup>1</sup>

**Strategy:** Every time,  $t_i$ , a **producer** can choose it's **product** type:

- 1 The **producer** looks at the number of **producers** of each type,  $n_m$ ,
- 2 The **producer** calculates the average profits for the **producer** of each **product** type,  $E[\pi]_m$ , for  $t_i$ ,
- 3 The **producer** chooses the most profitable **product** to produce,  $m^*$ , for  $t_i$ , taking into consideration that each other **producer**,  $j = 1, \dots, J$ , will produce the product that is most profitable for them at each  $t_j$ .

# Question and Hypothesis

## Question of the day.

- What is the **Nash Equilibrium** of the congestion game?



**Thank you for coming.**

### Insight of the Day

- It's all fun and **games**, until someone makes a profit!

What would you like to talk about next week?