



Saturday Morning Statistics #19

April 9<sup>th</sup>, 2022



# The 10 Commandments of Forecasting

- Mnow what you are forecasting.
- Understand the purpose of forecasting.
- Acknowledge the cost of the forecast error.
- Rationalize the forecast horizon.
- Understand the choice of variables.
- Rationalize the forecasting model used.
- Mow how to present the results.
- Now how to decipher the forecast results.
- Use recursive methods.
- Understand that forecasting models evolve over time.

2/6

### Forecast Evaluation

The root mean squared error is defined as

$$RMSE = \sqrt{\frac{1}{T} \sum_{t=0}^{T} (Y_{t+1} - \hat{Y}_{t+1})^2}$$

and can be used to compare forecasts.

## **VAR Models**

Assume the following system of linear equations for output, y, inflation,  $\pi$ , and the interest rate, i.

$$y_{t} = \alpha_{y} + \dots + \beta_{j} y_{t-j} + \dots + \gamma_{j} \pi_{t-j} + \dots + \delta_{j} i_{t-j} + \mu_{t}^{y}$$

$$\pi_{t} = \alpha_{\pi} + \dots + \theta_{j} y_{t-j} + \dots + \phi_{j} \pi_{t-j} + \dots + \lambda_{j} i_{t-j} + \mu_{t}^{x}$$

$$i_{t} = \alpha_{i} + \dots + \psi_{j} y_{t-j} + \dots + \kappa_{j} \pi_{t-j} + \dots + \rho_{j} i_{t-j} + \mu_{t}^{i}$$

### VAR Model in Matrix Form

Assume a system of linear equations for output, y, inflation,  $\pi$ , and the interest rate, i,

$$y_t = \alpha_y + \dots + \beta_j y_{t-j} + \dots + \gamma_j \pi_{t-j} + \dots + \delta_j i_{t-j} + \mu_t^y$$
  

$$\pi_t = \alpha_\pi + \dots + \theta_j y_{t-j} + \dots + \phi_j \pi_{t-j} + \dots + \lambda_j i_{t-j} + \mu_t^x$$
  

$$i_t = \alpha_i + \dots + \psi_j y_{t-j} + \dots + \kappa_j \pi_{t-j} + \dots + \rho_j i_{t-j} + \mu_t^i$$

that can be written in matrix form as

$$\begin{pmatrix} y_t \\ \pi_t \\ i_t \end{pmatrix} = \begin{pmatrix} \alpha_y \\ \alpha_\pi \\ \alpha_i \end{pmatrix} + A_1 \begin{pmatrix} y_{t-1} \\ \pi_{t-1} \\ i_{t-1} \end{pmatrix} + \dots + A_j \begin{pmatrix} y_{t-j} \\ \pi_{t-j} \\ i_{t-j} \end{pmatrix} + \begin{pmatrix} \mu_t^y \\ \mu_t^\pi \\ \mu_t^i \end{pmatrix}.$$



# Insights of the Day

- Now is better than never.
- Record your predictions.
- Evaluate your predictions to make even better forecasts in the future!