## Idea of the limit

The **limit** of a function is the value the function approaches at a given value of x, regardless of whether the function actually reaches that value.

For an easy example, consider the function

$$f(x) = x + 1$$

To find the value of the function f(x) when x = 5, we plug x = 5 into the function, and we get

$$f(5) = 5 + 1$$

$$f(5) = 6$$

So 6 is the limit of the function at x = 5, because 6 is the value that the function approaches as the value of x gets closer and closer to 5.

It's strange to talk about the value that a function "approaches," but if we look at some of the other values around x = 5, we start to get a better idea of what we mean. For instance,

if we plug 
$$x = 4.9999$$
 into  $f(x)$ , then  $f(x) = 5.9999$ , or

if we plug 
$$x = 5.0001$$
 into  $f(x)$ , then  $f(x) = 6.0001$ .

We start to see that, as we get closer to x = 5, whether we're approaching it from the 4.9999 side or the 5.0001 side, the value of f(x) gets closer and closer to 6.

x	4.9998	4.9999	5	5.0001	5.0002
f(x)	5.9998	5.9999	6	6.0001	6.0002

In this simple example, the limit of the function is 6, because that's the actual value of the function at that point; the point is defined. In limit notation, here's how that looks:

$$\lim_{x \to 5} x + 1 = 6$$

This notation tells us that "the limit of the function x + 1, as x approaches 5, is 6."

## **Example**

Find the limit.

$$\lim_{x \to 16} \sqrt{x} + 2$$

To find the limit, substitute the value that x approaches, x = 16, into the function.

$$\sqrt{16} + 2$$

$$4 + 2$$

6

So the value of the limit is 6.

$$\lim_{x \to 16} \sqrt{x} + 2 = 6$$

