

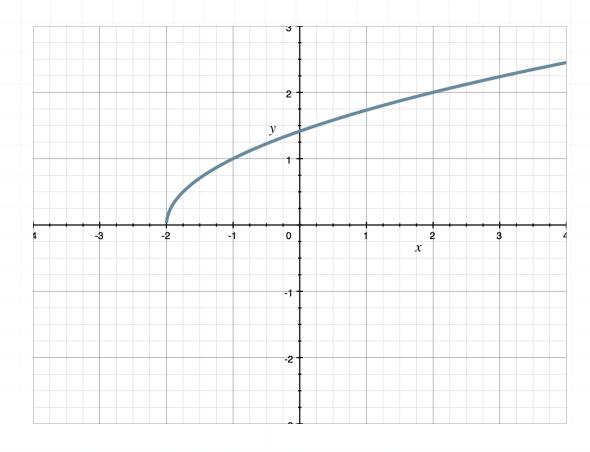
# Calculus 1 Workbook

Inverse functions and logarithms



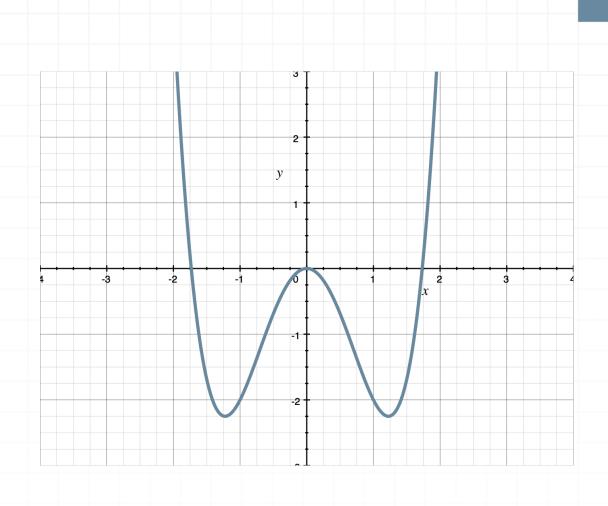
# HORIZONTAL LINE TEST

■ 1. Does the graph represent a one-to-one function?

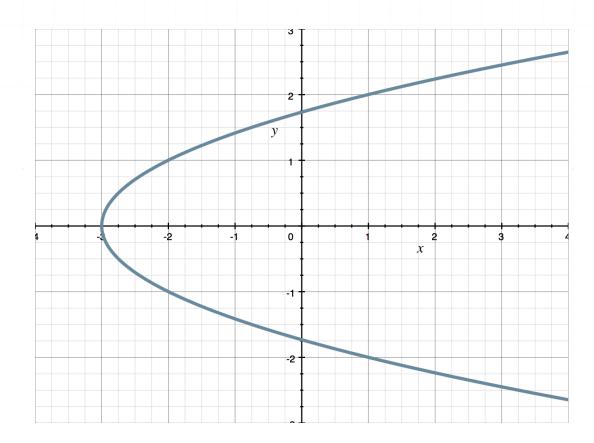


■ 2. Does the graph represent a one-to-one function?

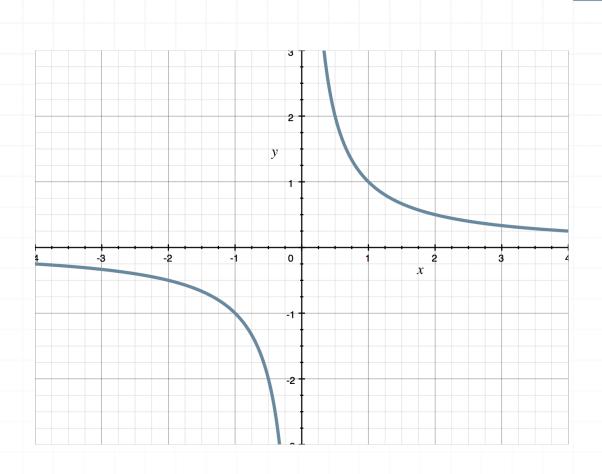




■ 3. Does the graph represent a one-to-one function?



■ 4. Does the graph represent a one-to-one function?



■ 5. Show that the function is one-to-one by showing that f(a) = f(b) leads to a = b.

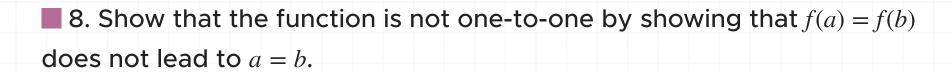
$$f(x) = 3x - 4$$

■ 6. Show that the function is one-to-one by showing that f(a) = f(b) leads to a = b.

$$f(x) = \frac{x+1}{x-5}$$

■ 7. Show that the function is not one-to-one by showing that f(a) = f(b) does not lead to a = b.

$$f(x) = x^2 - 6$$



$$f(x) = (x+3)(x-2)$$



#### **INVERSE FUNCTIONS**

■ 1. What is the inverse of the function?

$$f(x) = \frac{1}{2}x - 3$$

2. What is the inverse of the function?

$$f(x) = -4x + 5$$

■ 3. What is the inverse of the function?

$$f(x) = \frac{x}{x+2}$$

■ 4. What is the inverse of the function?

$$f(x) = \frac{2x}{x - 5}$$

■ 5. What is the inverse of the function?

$$f(x) = \frac{1}{x} + 3$$

■ 6. What is the inverse of the function?

$$f(x) = -\frac{3}{x - 2} - 4$$

■ 7. What is the inverse of the function?

$$f(x) = \frac{x-2}{x+3}$$

■ 8. What is the inverse of the function?

$$f(x) = \frac{5+x}{4-x}$$



## FINDING THE EQUATION OF A LINE FROM POINTS ON ITS INVERSE

■ 1. Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(1) = -2$$

$$f^{-1}(-3) = -1$$

**2.** Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(0) = 3$$

$$f^{-1}(-2) = 1$$

■ 3. Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(2) = 5$$

$$f^{-1}(4) = 9$$

 $\blacksquare$  4. Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(-3) = 2$$

$$f^{-1}(1) = 4$$

■ 5. Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(-4) = 7$$

$$f^{-1}(-1) = 14$$

■ 6. Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(5) = -4$$

$$f^{-1}(10) = -12$$

■ 7. Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(-3) = -4$$

$$f^{-1}(3) = 12$$

■ 8. Find f(x) if  $f^{-1}(x)$  is a linear function.

$$f^{-1}(1) = 3$$

$$f^{-1}(2) = 6$$

## LAWS OF LOGARITHMS

■ 1. Write the expression as a single logarithm. Solve if possible.

$$\log_2 2 + \log_2 4$$

■ 2. Write the expression as a single logarithm. Solve if possible.

$$\log_{3} 216 - \log_{3} 24$$

■ 3. Write the expression as a single logarithm. Solve if possible.

$$\log_4 10 - 3\log_4 2$$

■ 4. Write the expression as a single logarithm. Solve if possible.

$$2\log_7 4 + 3\log_7 5$$

■ 5. Solve the equation.

$$\log_a 2 + \log_a 4 = \log_a (x+2)$$

■ 6. Solve the equation.

$$\log_4(x+5) - \log_4(x-2) = \log_4 3$$

■ 7. Solve the equation.

$$2\log_b x = \log_b 49$$

■ 8. Solve the equation.

$$\log_{12} x = \frac{3}{2} \log_{12} 16$$



